

### INTRODUCTION

This HP-19C/HP-29C Solutions book was written to help you get the most from your calculator. The programs were chosen to provide useful calculations for many of the common problems encountered.

They will provide you with immediate capabilities in your everyday calculations and you will find them useful as guides to programming techniques for writing your own customized software. The comments on each program listing describe the approach used to reach the solution and help you follow the programmer's logic as you become an expert on your HP calculator.

You will find general information on how to key in and run programs under "A Word about Program Usage" in the Applications book you received with your calculator.

We hope that this Solutions book will be a valuable tool in your work and would appreciate your comments about it.

The program material contained herein is supplied without representation or warranty of any kind. Hewlett-Packard Company therefore assumes no responsibility and shall have no liability, consequential or otherwise, of any kind arising from the use of this program material or any part thereof.

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# DIRECT REDUCTION LOAN AMORTIZATION SCHEDULE

Loan Amt: \$45,000 APR: 9.25% Monthly Payment: \$385

Payment Number	Paid to Interest	Paid to Principal	Remaining Balance
13	343.20	41.80	44480.80
14	342.87	42.13	44438.67
15	342.55	42.45	44396.22
لمسيح			
18	341.56	43.44	44266.89
13 - 18	2054 29	255 71	44266 89
15 - 10	2034.23	233.71	77200.05

Given the periodic interest rate (i), periodic payment amount (PMT), loan amount (PV) and beginning and ending periods ( $P_1$ ,  $P_2$ ), this program will generate the values for a loan amortization schedule as pictured above, starting with the payment  $P_1$  and ending with  $P_2$ . After  $P_2$  has been reached the program calculates the accumulated interest and principle for the payments made between  $P_1$ - $P_2$ inclusively. The schedule may be started at any point in the mortgages life.

The data generated is valid for loans that have a balloon payment as well as those that are arranged to be fully amortized.

For loans with a balloon payment, the remaining balance of the last payment period is the balloon payment due in addition to the last periodic payment.

For loans scheduled to be fully amortized, the remaining balance after the last payment period may be slightly more or less than zero. This is because the program assumes that all payments are equal to the value entered for PMT. In fact for most loans the last payment is slightly more or less than the rest.

### Equations:

$$n = - \frac{\ln(-\frac{iPV}{PMT} + 1)}{\ln(1 + i)}$$

$$BAL_{P_1-1} = PMT \left[ \frac{1 - (1 + i)P_1 - 1 - N}{i} \right]$$

$$INT_{Pn} = RND (BAL_{Pn} \times \frac{1}{100})$$

$$PRIN_{Pn} = PMT - INT_{Pn}$$

$$BAL_{Pn} = BAL_{Pn-1} - PRIN_{Pn}$$

Example:

Duplicate the entries in the preceding amortization schedule.

Solution: 45000.00 STO2 mortgage amount annual percentage rate 9.25 ENT\* 12.00 ÷ payments per year periodic interest rate ST03 385.00 ST04 periodic payment amount 13.00 STO0 P1 18.00 STO1  $P_2$ GSB0 actual life of mortgage 301.14 \*\*\* remaining bal. at  $P_1-1*$ 44522.60 \*\*\* payment number 13.00 \*\*\* interest portion of pmt. 343.20 \*\*\* principle portion of pmt. 41.80 \*\*\* remaining after 13th pmt. 44480.80 \*\*\* 14.00 \*\*\* 342.87 \*\*\* 42.13 \*\*\* 44438.67 \*\*\* 15.00 \*\*\* 742.55 \*\*\* 42,45 \*\*\* 44396.22 \*\*\* 16.00 \*\*\* 342.22 \*\*\* 42.78 \*\*\* 44353.44 \*\*\* 17.00 \*\*\* 341.89 \*\*\* 43.11 \*\*\* 44310.33 \*\*\* 18.00 \*\*\* 341.55 \*\*\* 43.44 \*\*\* 44266.89 \*\*\* 2054.29 \*\*\* acc. interest periods 13-18 255.71 \*\*\* acc. principle periods 13-18 44266.35 🗰 remaining balance \*When using the HP-29C all subsequent

values are produced by pressing R/S.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in program			
2.	Enter following data in any order			
	- Original amount borrowed	PV	ST0 2	
	- Periodic interest rate	i	ST0 3	
	- Periodic payment amount	РМТ	STO 4	
3.	Key in			
	- Starting period	P1	STO 0	
	- Ending period	P2	ST0 1	
4.	Calculate life of mortgage		GSB 0	N
5.	Calculate remaining balance at Pl		R/S*	Rem. Bal.
	- Period number		R/S*	Pn N
	- Principal payment		R/S*	Pn PRIN
	- Interest payment		R/S*	Pn INT
	- Remaining balance		R/S*	Pn BAL
6.	Repeat step 5 for each period			
7.	After last period (P2)			
	Calculate accumulated totals:			
	- Accumulated interest		R/S*	Σ ΙΝΤ
	- Accumulated principal		R/S*	Σ ΡΡΙΝ
	- Remaining balance		R/S*	Rem. Bal.
8.	For a new payment period in same mortgage			
	repeat steps 3-7.			
*	If the program is run on the HP-19C, the			
	R/S is not used.			

P1 + PI 0					
02 0			51 PR/X	**	۲n
03 ST05			57 PCI9		
04 STO6			54 RCL3		
05 RCL3			55 %		
06 EEX			56 FFX		
07 2			57 7		
08 ÷			58 +		
89 STO7			59 EEX		
10 RCL2			60 7		
11 X			61 -		
12 RCL4	-	•	62 PRTX	**	Pn INT
13 ÷	+	i)	63 ST+5		
14 LHS	PV		64 +		
			65 RCL4		
10 I 17 IN			66 LSTX		
18 PCI 7	-	- 1	67 -	<b>4</b> 4	D D0.71
19 1			68 PRTX	~~	Ph PRIN
20 +		L L	69 ST+6		
21 LN			70 LSIX		
22 ÷			71 +		
23 CHS **			77 PDTV	**	Pn Rem. Bal.
24 SPC **			73 FRIA 74 CT09	~~	
25 PRTX	"New"	Ν	75 SPC	**	
26 RCL0			76 ST01		
27 1			77 <b>*</b> LBL3		
28 -			78 RCL5		
29 X≠Y			79 PRTX	**	ΣΙΝΙ
30 -			80 RCL6		
31 RCL7			81 PRTX	**	
			82 RCL9		ZININ
33 T 74 V40			83 PRTX	**	Rem. BAL P2
75 YX			84 R/S		2
36 1					
37 XIY		ᅴ			
38 -		1	** When i	isina the	HP-29C R/S must
39 RCL7		-  .	be use	d in the	place of PRTX
40 ÷			and SF	°C should	be deleted.
41 RCL4	!	Σ			
42 X		2			
43 ST09					
44 PRTX **	BAL P	1 – 1			
45 SPC **					
46 #LBL1					
47 KULI AQ DELA					
40 KOLO 49 X\Y9					
50 ESR3					
		REGI	LSTERS		L
0 P <sub>1</sub> 1	P <sub>2</sub>	2 PV	<sup>3</sup> Periodic	i <sup>4</sup> РМП	- 5 <u>Σ</u> ΤΝΤ
$6 \Sigma PRIN$ 7	i/100	8	<sup>9</sup> Rem RΔI	.0	.1
.2 .3	,	.4	.5 I	ן 16	17
18 19		20	21	22	23
24 25		26	27	28	29

### INTERNAL RATE OF RETURN UP TO 26 CASH FLOWS

The interest rate that equates the present value of all future cash flows with the original investment is known as the Internal Rate of Return (also called discounted rate of return or yield). Given the initial investment and up to 26 cash flows, this program calculates the periodic IRR.

When using this program, cash received is positive and cash outlays are negative. Zero should be keyed in for periods in which there are no cash flows.

The answer produced is the periodic rate of return. If the cash flow period is other than annual, the answer should be multiplied by the number of periods per year to determine the annual internal rate of return.

The program solves the following equation iteratively for IRR:

INV= 
$$\sum_{j=1}^{n} \frac{CF_{j}}{(1 + IRR)^{j}}$$

where: n= number of cash flows  $CF_j = j^{th}$  cash flow

Note:

Problems involving a large number of cash flows can often result in long execution times.

#### Example:

A shopping center requires a \$200,000 investment, and will be sold at the end of 3 years. If this investment results in the semi-annual net cash flows shown, what is the internal rate of return?

End of	
Six Month Perio	d Cash Flow
1	\$-50,000
2	0
3	11,000
4	11,000
5	13,000
6	280,000
	(includes net proceeds

from sale)

#### Solution:

	GSB1	
-50000.00	R∕S	
0.00	R∕S	
11000.00	<b>R∕S</b>	
	R∕S	
13000.00	R∕S	
280000.00	R∕S	
-200000.00	GSB2	Cash paid out
4.23	***	Semi-annual IRR (%)
2.00	Х	
8.46	***	Annual IRR

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in the program			
2.	Clear registers		fREG	
3.	Initialize		GSB 1	4
4.	Beginning with the first period,		R/S	CF;
	enter all cash flows in sequence:			
	inflows positive, outflows negative,			
	and O for no cash flows.			
5.	Enter initial investment using the	INV	GSB 2	I R R (%)
	cash flow sign convention.			
6.	For a new case, go to step 2			

01 +1 PI 1			48 5	1	10-6	
UI #LDLI			49 8282		10	
62 4			50 CTO5			
03 STO0			56 6103			
04 *LBL0	store	cash flows	01 K↓			
05 R/S			52 R4		1 + IF	R I
06 STO <b>i</b>			53 1			
07 ISZ			54 -			
AR CTOR			55 EEX			
00 +1010			56 2			
10 4000			57 X			
10 HES			58 R/S		***100	$\mathcal{O}(\mathscr{C})$
11 082			59 +1 R1 5		11/1	( 10 )
12 STO1	INV					
13 RCL0	n + 3		00 KV		1, 1	
14 STO3			61 K4		1 + 11	(K <sup>*</sup>
15 1	initi	al value for	62 U			
16 ENT†	1 +	IRR	63 ST02			
17 A		2	64 GTO6			
18 9702	clear	f(i)	65 *LBL7		CFi i	i∿ 1 + IRR
10 0102		• ( • )	66 ST+2			
13 %LDL0			67 X			
20 RUL0			68 +			
21 3			69 X-7Y		<b>л</b> . тг	
22 X=Y?			78 57-2		1 + 11	(K
23 GTO8			76 3172			
24 R4					∿ <b> </b> + ]	
25 3			72 RIN		+	IKK
26 -	li					
27 RCLI	CEi					
28 CSB7						
29 097						
20 DOL 70 CTOC						
30 6105						
31 *LBL8						
32 R4						
33 R↓						
34 RCL3						
35 STO0						
36 R↓						
37 RCL2	f(i)					
38 RCI 1						
79 -						
40 V+V						
41 <del>-</del>						
42 X	Δ					
43 +	1 + I	RR	*** "Drint	v" ma.	he ind	erted
44 LSTX	, .			∧ iiiay		
45 ABS						
46 EEX						
<b>4</b> 7 CHS						
	-	REGI	STERS	-		
0 i	1 INV	2 f(i)	<sup>3</sup> n + 3	4 CF <sub>1</sub>		<sup>5</sup> CF <sub>2</sub>
6	7	8	9	.0		.1
.2	.3	.4	.5	16		17
18	19	20	21	22		23
24	25	26	27	28		29 CF
						0 26

### STRAIGHT LINE DEPRECIATION SCHEDULE

Schedule - Straight-Line Method Starting Book Value: \$375,000 Salvage Value \$30,000 Estimated Useful Life: 40.25 Years

Year (End of)	Depreciation Amount (DEP)	Remaining Depreciable Value (RDV)	Remaining Book Value (RBV)	Depreciation To Date (Reserve)
1 2	8571.43 8571.43	336428.57 327857.14	366428.57 357857.14	8571.43 17142.86
41	2142.96	0.00	30000.00	345000.00

The annual depreciation allowance using this method is determined by dividing the cost or other basis of valuation (starting book value) less its estimated salvage value by its useful life expectancy. This program develops the data shown in the example schedule, given the starting book value (SBV), salvage value (SAL), life expectancy (LIFE), and first year of the schedule (YR), (The schedule may be started at any point in the useful life.)

Fractional years lives must be entered as an integer plus a fraction. Thus a life of 12 years 3 months would be keyed in as 12.25 for LIFE.

Values for the last year of an asset with fractional years life (i.e., the 21st year's values for an asset with 20.5 years life) are calculated correctly. However, all other values represent a full year's depreciation. For this reason only integer values (whole number, 1.0, 2.0, 17.0 etc.) may be entered for YR. The program makes no checks on this value and generates invalid results if other than whole numbers are entered.

EQUATIONS:

$$DEP_{k} = \frac{SBV - SAL}{LIFE}$$

$$DEP_{k}(last year) = (\frac{SBV - SAL}{LIFE}) \cdot F$$

$$RES = (K) \cdot (\frac{SBV - SAL}{LIFE})$$

$$RDV_{k} = (LIFE-K) \cdot (\frac{SBV - SAL}{LIFE})$$

$$RBV_{k} = RDV_{k} + SAL$$

where	SOLUTION:		
	40.25	ENT*	
RES = Reserve	30000.00	ENT†	
F = Decimal portion of LIFF	375000.00	ENTT	
	1.00	GSB1	
K = Value for YR		R∕S	
EXAMPLE: Complete the schedule shown	8571.43	*** P/9	DEP1
for the first two years. Then jump to the Alst year	336428.57	***	RDV <sub>1</sub>
and generate the data for		<b>R∕</b> S	
that year.	<b>366428.5</b> 7	***	RBV <sub>1</sub>
		<b>R</b> ∕S	
	8571.43	#≭# ₽./0	RES1
	0571 47	K/ 5 4-4-4-	DED.
	0371.43	### D/C	
	727057 14	5/3 ****	DDV
	3276J7.14	*** R/S	RDV <sub>2</sub>
	357857.14	***	RBV <sub>2</sub>
		R∕S	
	17142.86	***	RES <sub>2</sub>
	41.00	STOØ	YR
		R∕S	
	2142.86	***	DEPul
		<b>R</b> ∕S	
	0.00	***	RDV 4 1
		<b>R∕S</b>	
	30000.00	***	RBV <sub>41</sub> =SAL
		R∕S	
	345000.00	***	RES <sub>41</sub>
		<b>R</b> ∕S	

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in the program			
2.	Enter data			
2a.	Life of asset in years	LIFE	ENT 1	
2b.	Salvage value	SAL	ENT ↑	
2c.	Starting book value (beginning basis)	SBV	ENT ↑	
2d.	Year for which depreciation is to be			
	calculated	YR	GSB 1	
3.	RUN:			
3a.	Depreciation		R/S	DEP
3b.	Remaining depreciable value		R/S	RDV
3c.	Remaining book value		R/S	RBV
3d.	Total depreciation to date (Reserve)		R/S	RES
4.	For next year's values, go to step 3a			
5.	For another year's values, enter year and			
	go to step 3a	YR	STO O	

01 *LBL1 02 ST00 03 R↓ 04 ST01 05 R↓ 06 ST02 07 R↓ 08 ST03 09 R/S 10 *LBL5 11 1 12 + 13 X∠Y? 14 ET09		Bevond	useful life	48 R/S 49 RCL5 50 RCL6 51 - 52 ISZ 53 R/S 54 RCL0 55 RCL3 56 GT05 57 #LBL9 58 0 59 ÷ 60 #LBL8 61 0	, F	*** RBV *** RES
15 FRC 16 STO4 17 RCL3 18 RCL0 19 ÷				62 STO6 63 R/S 64 GTO7 65 R/S	*	*** RDV = 0
20 1 21 X>Y? 22 RCL4 23 1		Last y	ear?			
24 × 25 RCL3 26 ÷ 27 RCL1 28 RCL2 29 - 30 ST05		l or F				
31 × 32 R/S 33 RCL3 34 RCL0 35 V2V0		*** DE	Ρ	*** "Printx	" mav be	inserted to
35 X2Y7 36 GTO8 37 - 38 RCL3 39 ÷ 40 RCL5 41 × 42 ST06		Last y	ear?	replace	"R/S".	
43 R/S 44 *LBL7 45 RCL6 46 RCL2 47 +		*** RD'	V			
			REGI	STERS	1	
<sup>o</sup> YR	1 SI	3V	<sup>2</sup> SAL	<sup>3</sup> LIFE	4 F	<sup>5</sup> SBV-SAL
<sup>6</sup> RDV	7		8	9	.0	.1
.2	.3		.4	.5	16	17
18	19		20	21	22	23
24	25		26	27	28	29

### SUM OF THE YEARS' DIGITS

Depreciation Schedule - Sum of the Years Digits Method Starting Book Value: \$375,000 Salvage Value: \$30,000 Expected Useful Life: 40.25 Years

Year (End of)	Depreciation Amount (DEP)	Remaining Depreciable Value (RDV)	Remaining Book Value (RBV)	Depreciation To Date (Reserve)			
1	16,725.38	328,274.62	358,274.62	16,725.38			
2	16,309.85	311,964.77	341,964.77	33,035.23			
41	103.88	0.00	30,000.00	345,000.00			

The sum-of-the-years' digits method is an accelerated form of depreciation, allowing more depreciation in the early years of an asset's life than allowed under the straight line method. This program generates the data shown in the example schedule, given the starting book value (SBV), the salvage value (SAL), expected useful life in years (LIFE), and beginning year (YR) for the schedule. (The schedule may be started at any point in the useful life.)

Fractional years asset life must be entered as an integer plus a fraction. Thus a life of 12 years 3 months would be keyed in as 12.25 for LIFE.

Values for the last year of an asset with fractional years life (i.e., the 21st year's values for an asset with 20.5 years life) are calculated correctly. However, all other values represent a full year's depreciation. For this reason only integer values (whole numbers, 1.0, 2.0, 17.0, etc.) may be entered for YR. The program makes no checks on this value and generates invalid results if other than whole numbers are entered.

EQUATIONS:

$$SOYD = \frac{(W + 1)(W + 2F)}{2}$$

$$DEP_{k} = \left(\frac{LIFE + 1 - K}{SOYD}\right) \cdot (SBV-SAL)$$

$$RES_{k} = \left[1 - \frac{(W-K+1)x(W-K+2F)}{2x(SOYD)}\right] \cdot (SBV-SAL)$$

$$RDV_{k} = \left[\frac{(W-K+1)x(W-K+2F)}{2x(SOYD)}\right] \cdot (SBV-SAL)$$

 $RBV_{k} = RDV_{k} + SAL$ 

### Where

### SOLUTION:

K = va	lue for YR			
RFS. = Re	serve at period k	40.25	ENT†	
K K		30000.00	ENT†	
W = In	teger portion of LIFE	375000.00	ENT↑	
E - Do	cimal portion of LIFE	1.00	GSB1	
r - De			R∕S	
EXAMPLE:	Complete the schedule shown	16725.38	***	DEP <sub>1</sub>
	for the first two years.		<b>R</b> ∕S	עסס
	Then jump to the 4lst year	328274.62	***	RDV1
	and generate the data for		R∕S	
	that year.	358274.62	***	RBV <sub>1</sub>
			R∕S	
		16725.38	***	RES1
			R∕S	
		1 <i>6309</i> .85	***	DEP <sub>2</sub>
			<b>R∕S</b>	עסס
		311964.77	***	RDV <sub>2</sub>
			R∕S	$RBV_2$
		341964.77	***	
			R∕S	DEC
		3 <b>3035.</b> 23	<b>東京市</b>	RES <sub>2</sub>
		41.00	STOØ	
			R∕S	DFP
		103.88	***	
			R∕S	עסס
		0.00	***	KUV <sub>41</sub>
			R/S	RRV
		30000.00	***	NDV41
			R/S	DEC
		345000.00	<b>東東市</b>	$RES_{41}$

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in the program			
2.	Enter data			
2a.	Life of asset in year	LIFE	ENT ↑	
2b.	Salvage value	SAL	ENT ↑	
2c.	Starting book value (beginning basis)	SBV	ENT ↑	
2d.	Year for which depreciation is to be			
	calculated	YR	GSB 1	
3.	RUN:			
3a.	Depreciation		R/S	DEP
3b.	Remaining depreciable value		R/S	RDV
3c.	Remaining book value		R/S	RBV
3d.	Total depreciation to date (Reserve)		R/S	RES
4.	For next year's values, go to step 3a			
5.	For another year's values, enter year and			
	go to step 3a	YR	STO O	

01 *LBL1			48 RCL5 49 197	*** RI	3V
02 STO0 03 R↓ 04 STO1 05 X‡Y 06 -			50 R/S 51 GTO5 52 *LBL9 53 ENT†	*** R Next yea	ES year or new r
07 ST08 08 R4 09 ST03 10 GSB9 11 ST07	SOVD		54 FRL 55 ENT↑ 56 + 57 X≠Y 58 INT	2F	
12 R/S 13 *LBL5 14 RCL0 15 RCL3 16 1	5010		59 + 60 LSTX 61 1 62 + 63 ×	Wor	√- k
17 + 18 XZY? 19 GT08 20 XZY 21 -	Beyond u	seful life	64 2 65 ÷ 66 RTN 67 *LBL8 68 0		
21 – 22 RCL7 23 ÷ 24 RCL8 25 ×			69 ÷ 70 *LBL7 71 0 72 ST05 73 R/S	Error	DV = 0
26 R/S 27 RCL3 28 RCL0 29 - 30 X<0?	*** DEP		74 GT06		
31 GT07 32 GSB9 33 RCL7 34 ÷					
35 RCL8 36 × 37 ST05 38 R∕S 39 *LBL6	*** RDV				
40 RCL8 41 RCL5 42 - 43 ST05	RES				
44 RCL1 45 X≠Y 46 - 47 R∕S			*** "PRIN replac	TX" may be in ce "R/S".	serted to
		REGIS	STERS		
0 YR 1	SBV 2		<sup>3</sup> LIFE	4	<sup>5</sup> RDV/RES
6 7 cm	/D 8	SBV SAL	9	.0	.1
		JDV-JAL	5	16	17
18 19	20	)	21	22	23
24 25	26	6	27	28	29

### VARIABLE RATE DECLINING BALANCE DEPRECIATION SCHEDULE

Depreciation Schedule - Declining Balance Method Starting Book Value: \$375,000 Salvage Value \$30,000 Expected Useful Life: 40 Years Rate: 1.5

Year (End of)	Depreciation Amount (DEP)	Remaining Depreciable Value (RDV)	Remaining Book Value (RBV)	Depreciation To Date (Reserve)
1	14,062.50	330,937.50	360,937.50	14,062.50
2	13,535.16	317,402.34	347,402.34	27,597.66
15	8,235.18	181,369.51	211,369.51	163,630.49

The variable rate declining balance method is another form of accelerated depreciation; as such it provides for more depreciation in earlier years and decreasing depreciation in later years. This program generates the data shown in the example schedule given the starting book value (SBV), salvage value (SAL), useful life expectancy (LIFE), the declining rate factor (FACT), and the first year of the desired schedule (YR). The schedule may be started at any point in the useful life.

The "variable rate" is indicated as either a factor or percent with equal frequency in the business community. Thus, "1.5 declining balance factor" and "150% declining balance" have the same meaning. The number to be keyed in for FACT in this program, should be in factor form, that is 1.25, 1.5, 2, and not 125, 150 or 200.

This method of depreciation is unique in that it may generate depreciation greater than the depreciable value for some assets, while it may not generate sufficient depreciation for others.

This program will not allow an asset to be depreciated below its salvage value. That is when the generated depreciation for a year, usually the last, is greater than the remaining depreciable value, the latter is displayed as the depreciation amount. Program 6 is provided to assist in determining the best time to switch to straight line depreciation (tax laws permitting) so that an asset may be fully depreciated.

Fractional years lives must be entered as an integer plus a fraction however. Thus, a life of 12 years 3 months would be keyed in as 12.25.

Values for the last year of an asset with fractional years life (i.e., the 21st year's values of an asset with 20.5 years life) are calculated correctly. However, all other values represent a full year's depreciation. For this reason only integer values (whole

### EQUATIONS:

<sup>DEP</sup> k	= SBV • $(1 - \frac{FACT}{LIFE})^{k-1} \cdot (\frac{FACT}{LIFE})$
res <sub>k</sub>	$= SBV \cdot \left[1 - (1 - \frac{FACT}{LIFE})^{k}\right]$
rdv <sub>k</sub>	= (SBV - SAL) - RES <sub>k</sub>
RBVk	= $RDV_k$ + $SAL$ = $SBV_k$ - $RES_k$

Where

k =	Va	lue	for	Y	R		
RES	k =	Res	serve	9	at	year	k

- <u>EXAMPLE</u>: Duplicate the schedule shown. Also calculate the remaining depreciable value in the last year.
- NOTE: Note that in the last year of the asset's life there would still be a total of \$51,294.43 of remaining depreciable value on the books if this schedule were used throughout the asset's life. (See program 6)

Solution:

40.00	ENT†	
30000.00	ENT†	
375000.00	ENT↑	
1.50	GSB1	
1.00	GSB2	
	R/S	
14062.50	***	DEP1
	R∕S	
<b>330</b> 937.50	<b>東京市</b>	RDV 1
	R∕S	
360937.50	東東東	$RBV_1$
	R/S	
14062.50	***	RES <sub>1</sub>
17575 10	K/5 444	DFP.
13333.15	*** D/C	DLI 2
717402 74	₹/3 ★***	RDV <sub>2</sub>
011702.07	*** ₽∕S	
347402.34	***	<b>BBV</b> 2
UN ICLICI	R/S	ND V2
27597.66	***	DES
15.00	STOØ	KLJ <sub>2</sub>
	R∕S	
8235.18	***	DEP <sub>15</sub>
	R∕S	
181369.51	***	RDV 1 5
	R∕S	
211369.51	<b>東東東</b>	RBV15
	R∕S	550
163630.49	*** *	RES <sub>15</sub>
40.00	STOP	
7167 70	<b>₹</b> ∕\$	DFP
3167.32	*** 7.20	02.40
51004 47	₹<3 ****	עחס
J1224.43	不不不	KDV40

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in the program			
2.	Enter data			
2a.	Life of asset in years	LIFE	ENT 1	
2b.	Salvage value	SAL	ENT 1	
2c.	Starting book value (beginning basis)	SBV	ENT ↑	
2d.	Declining rate factor (1 <fac<2)< td=""><td>FACT</td><td>GSB 1</td><td></td></fac<2)<>	FACT	GSB 1	
3.	Enter year for which depreciation is to be	YR	GSB 2	
	calculated			
4.	RUN:			
4a.	Depreciation		R/S	DEP
4b.	Remaining depreciable value		R/S	RDV
4c.	Remaining book value		R/S	RBV
4d.	Total depreciation to date (Reserve)		R/S	RES
5.	For next years values, go to step 4a			
6.	For another year's values, enter year and	YR		
	go to step 4a			
	· · ·			

01 *LBL1 02 STC5			48 RCL2		Donnoc	ishle value
03 R4			50 X>Y?		behrec	Table value
04 STU1 05 R4			51 GT08			
06 ST02			52 SIU7 57 -		Deprec	iable value
07 R4			54 RCL8			
08 ST03			55 -			
09 R/S			56 CHS		DEP + (	depreciable
10 ALDLZ 11 STOR			57 0		value ·	- RES
12 R/S			58 X>Y?			
13 *LBL5			59 6108 68 XZY			
14 RCL0			61 R/S		*** DEF	
15 RCL3			62 #LBL7			
			63 RCL1			
18 XZY2			64 RCL2			
19 GT09			60 - 55 PCL7			
20 1	Beyond	useful life	67 -			
21 RCL5			68 R/S		*** RD	/
22 RCL3			69 RCL1		N.B	
23 ÷			70 RCL7			
24 5705 25 -			71 -		*** DD1	,
26 ST07			72 R/S			
27 RCL0			73 182 74 PC17		Next ye	ear
28 1			75 R/S			
29 -			76 GT05		*** RES	
30 YX			77 *LBL9			
31 RCL6			78 0		Ennon	
32 × 77 Pri 1			79 ÷		Errer	
34 X			80 *LBL8			,
35 ST08	DEP		81 KLL8 92 P/C		*** DEF	
36 RCL6			83 GT07			
37 RCL1			84 *LBL6			
38 ×			85 R/S		*** DFI	P = 0
39 1 AD DCL7			86 GT07		DLI	- 0
41 RCLO			87 R/S			
42 Y×						
43 -			*** "Printx"	may be	insert	ced to
44 RCL1	DEC		replace '	'R/S"		
45 X						
40 3107 47 PCI1						
TI KULI						
		REGIS	STERS	4		5 5407
∪ YK	· SBV	rest SAL	° LIFE	<sup>4</sup>		FACI
° FACT/LIFE	1-FACT/LIFE	DEPK		.0		17
.2	KES	.4	.5	16		17
18	19	20	21	22		23
24	25	26	27	28		29

### CROSSOVER POINT-DECLINING BALANCE TO STRAIGHT LINE

As indicated in the description and example for program 5, the declining balance method of depreciation may not fully depreciate an asset in the asset's lifetime. In these circumstances there is an optimum point in the useful life where a switch from the declining balance method to the straight line method should be made. This is the "crossover point", the first year in which the depreciation by the straight line method is greater than if depreciation were continued using declining balance method. (In accordance with Internal Revenue Service publication 534, the straight line depreciation is determined by dividing the remaining depreciable value by the remaining useful life.)

Given the starting book value (SBV), salvage value (SAL), useful life expectancy (LIFE), and declining balance factor (FACT), this program calculates the last year that the declining balance method should be used, and the remaining life and remaining book value after this "last year" so that a switch to straight line depreciation can be made. Should there be no optimum crossover point, a zero is displayed. This implies that the declining balance method is "best" for the entire depreciable life.

Thus, this program, the declining balance depreciation program (5) and the straight line depreciation program (3) may be used as follows:

- A. This program is used to determine the "crossover point" and associated values.
- B. Program 5 is entered and a declining balance depreciation schedule is generated for the early years up to and including the year indicated as being the "last year".

Note that since the depreciation programs use the same storage register conventions, only a value for YR need be keyed in for program 5.

C. Finally, program 3 is entered. The remaining book value at the end of the last "declining balance year" is keyed in for starting book value and the remaining life is keyed in for the asset's life. A straight line depreciation schedule may now be generated for the remaining years.

Note that for this portion of the depreciation schedule the value for "total depreciation to date" (reserve) will be in error by an amount equal to the amount depreciated during the declining balance calculations.

As in program 5 the declining balance factor (FACT) should be entered in factor form (1.25, 1.5, 2.0), not as a percent (125, 150, 200).

Equations:

SBV(1 - 
$$\frac{FACT}{LIFE}$$
)<sup>k-1</sup> · ( $\frac{FACT}{LIFE}$ ) $> \frac{BV}{LIFE + 1-k}$ 

$$BV_{k} = SBV - SAL - RES_{k}$$
  
RES<sub>k</sub> = SBV  $\left[1 - (1 - \frac{FACT}{LIFE})^{K}\right]$ 

K = the value for YR

The largest integer value for K which maintains the above inequality is the "last year" to use the Declining Balance depreciation method.

#### Example:

An asset has a starting book value of \$375,000, a 40 year life expectancy, and a projected salvage value of \$30,000. Using a 1.5 declining balance factor:

- Determine the crossover point and the associated remaining life and remaining book value.
- Generate the depreciation data for the declining balance "last year" with program 5 (Normally the user would generate a full schedule beginning with the lst year).
- Switching to the straight line method (program 3), generate the depreciation data for the year following the declining balance "last year".

Solution:

1 60	ENTA		
1.00	Enti		
40.00	ENTŤ		
30000.00	ENT†		
375000.00	GSB1		
18.00	***	last ye	ar
	R/S		
22.00	***	remaini	ng life
	R/S		0
188471.01	***	RBV	
Key in pr	rograi	n 5	
18.00	GSB2		
	R∕S		
7343.03	***	DEP <sub>18</sub>	
	<b>R</b> ∕9	10	
158471.01	***	RDV <sub>18</sub>	
	₽7S	/	
188471.01	***	RBV 18	Note agreemer
	<u>R/S</u>	°° W	ICH KEV ADOVE
:86528.99	***	$RES_{18}$	

t )

```
Key in program 3
      22.00 ENT*
                       (the first year of
   30000.00 ENT†
                       straight line depre-
  188471.01 ENT†
                   YR ciation)
       1.00 GSB1
             R/S
                   DEP<sub>19</sub>
    7203.23 ***
             R/S
                   RDV 19
  151267.78 ***
             R∕S
                   RBV<sub>19</sub>
  181267.78 ***
```

etc.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Enter data:			
2a	• Declining rate factor (1 <fact<u>&lt;2)</fact<u>	FACT	ENT ↑	
2b	· Life of asset in years	LIFE	ENT 1	
2c	· Salvage value	SAL	ENT 1	
2d	• Starting book value (beginning basis)	SBV		
3	Calculate last year to use declining		GSB 1	last year
	balance method			
4	Calculate remaining life		R/S	rem. life
5	Calculate remaining book value		R/S	RBV
6	For a new case go to step 2			

	T		40 V\V0			
01 *LBL1 02 STO1			49 GT00		iterat	e
03 R4 04 Sto2			51 R/S		***las	t year
05 R4 06 ST03			52 RCL0			
07 R↓ 08 STO5 09 1			55 R/S 56 RCL6		***rem	. life
10 STO0 11 RCL5 12 RCL3	start	with K = 3	57 RCL2 58 + 59 R/S		***RBV	
13 ÷ 14 STO7 15 -			60 #LBL9 61 0 62 R/S		displa	y "O"
16 STO8 17 *LBL0 10 107						
18 152 19 RCL0 20 RCL3	К – 1					
21 1 22 + 23 X2Y2						
24 GT09 25 RCL8	no cro	ossover point				
26 RCL0 27 YX						
28 1 29 - 78 PCL1						
31 X 32 RCL1						
33 + 34 RCL2						
35 - 36 STO6 37 DCL2	BV					
37 RCL3 38 RCL0 39 -						
40 ÷ 41 RCL8	right inec	side of quality				
42 RCL0 43 yx 44 RCL7			***"Pr	int x"	may be	inserted to
44 ROL7 45 X 46 RCL1			re re	place	"к∕Ѕ".	
47 X	left s	side of inequa	lity			
		nEGI				5
<u>К – I I S</u> 6 ву <sup>7</sup> ғаст	3V /LIFF	<sup>∠</sup> SAL <sup>8</sup> 1- FACT/LIFF	° LIFE 9	4 .0		<sup>o</sup> FACT .1
.2 .3		.4	.5	16		17
18 19		20	21	22		23
24 25		26	27	28		29

### NOMINAL TO EFFECTIVE/EFFECTIVE TO NOMINAL RATE CONVERSION

An annual effective interest rate demonstrates the effect of compounding for a full year of compounding periods at a particular periodic interest rate. The periodic interest rate to be used is determined by dividing the number of compounding periods in a year into the stated annual nominal interest rate. The effect is such that if the nominal rate is held constant, as the number of compounding periods per year is increased ihe annual effective interest rate will increase. The ultimate or upper limit in this process is to have an infinite number of compounding periods in a year, commonly called continuous compounding.

The first part of the program addresses finite compounding, that is quarterly compounding, monthly compounding, etc. Given the number of compounding periods in a year and one of the rates (nominal or effective) the other rate can be calculated. If for example, you require the periodic interest rate for a calculation, given the effective rate, use this program to determine the annual nominal rate first. Dividing the nominal rate by the number of compounding periods in a year will give the required periodic interest rate.

The latter part of the program is for contininuous compounding. Given either rate, the other can be calculated.

The most common and straightforward definition of effective interest rate has been implemented. Occasionally other definitions will be used and the results will not compare exactly with those calculated by these programs. For example, since the maximum annual nominal rate that savings institutions can offer is regulated by law, they may modify the process (also regulated) so that the effective rate is even higher (e.g., for daily compounding, the periodic rate may be divided by 360 and then compounding accomplished for 365 periods). It is important then, when attempting to match results, to understand the process employed.

#### EQUATIONS:

finite compounding

$$\mathsf{EFF} = (1 + \frac{\mathsf{NOM}}{\mathsf{C}})^{\mathsf{C}} - 1$$

continuous compounding

$$EFF = (e^{NOM} - 1)$$

#### EXAMPLES:

1. An investment with monthly cash flows (implying monthly compounding) is said to have an annual effective yield (interest rate) of 21%. What annual (nominal) yield and periodic yield does this represent?

2. A bank offers a savings plan with a 5% annual nominal interest rate. What is the annual effective rate if compounding is continuous?

SOLUTIONS:

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in the program			
2.	Enter constant and go to either step 3a	100	STO O	
	for finite compounding or step 3b for			
	continuous compounding			
3a.	Enter			
	- The number of compounding periods/year	c/yr	STO 1	
	and one of the following:			
	- Annual nominal rate	Nom %	ST0 2	
	or			
	- Annual effective rate	Eff %	STO 3	
4a.	Calculate the remaining rate			
	- Annual nominal rate		GSB 1	Nom %
	or			
	- Annual effective rate		GSB 2	Eff %
3b.	Enter one of the following:			
	- Annual nominal rate	Nom %	STO 4	
	or			
	- Annual effective rate for continuous	Effcont <sup>%</sup>	STO 5	
	compounding			
4b.	Calculate the remaining rate			
	- Annual nominal rate		GSB 3	Nom %
	or			
	- Annual effective rate for continuous		GSB 4	$Eff_{cont}$ %
	compounding			

			T		1	
01 *LBL1			48	-		
02 PC13			49	RCLØ		
07 DCI0			50	Х		
00 KCE0 04 ÷			51	R/S	*** Ef	ff
04 ÷						cont
00 1						
05 +						
07 RCLI						
<b>0</b> 8 1/X						
09 YX						
10 1						
11 -						
12 RCL1						
13 X						
14 RCL0						
15 x						
16 R/S	*** N	m				
17 #1 R1 2		5111				
10 PC1 2						
10 ROLL 10 PCI 1						
19 ROLI						
20 KLL0						
21 ×						
22 ÷						
23 1						
24 +						
25 RCL1						
26 YX						
27 1						
28 -						
29 RCL0						
30 X	+++ F	c.c				
31 R/S		T T				
32 *LBL3						
33 RCL5						
34 PCLA						
75 ±						
76 1						
77 1						
70 14						
30 LN 70 PCL0						
37 RULU 40 -						
40 ×						
41 R/S	*** N	om				
42 *LBL4						
43 RCL4						
44 RCL0						
45 ÷						
46 e <sup>x</sup>						
47 1						
	I	RFGI	I STERS			
0 100	1 C/1	2 Nom	3	4		5 Fff
6	<u> </u>				011]	
-		-	-			
.2	3	.4	.5	16		17
18 1	9	20	21	22		23
-						
24 2	25	26	27	28		29

### LEASE VERSUS PURCHASE

This program calculates the present value of the cost of purchasing, CP, the present value of the cost of leasing, CL, and the net difference using the following equations:

$$CP = P + \frac{M(1 + i)^{n} - 1}{i(1 + i)^{n}} - \frac{SV}{(1 + i)^{n}}$$

$$CL = L \frac{(1 + i)^{n} - 1}{i(1 + i)^{n}}$$

Net Difference = CP - CL

#### where

- P = purchase price
- M = maintenance costs, per period
- i = the opportunity interest rate, per period
- n = the number of periods (useful life)
- SV = salvage value
- L = lease payments

It also calculates the cost of purchasing after leasing for n periods.

$$OP = \frac{P - Credits}{(1 + i)^{n}} + (L - M)\frac{(1 + i)^{n}}{i(1 + i)^{n}}$$

where Credits = rental credits applied toward purchase

This program is adapted from HP-65 Users' Library program #01093A by Robert Dudugjian.

#### Example:

Suppose a purchase price of \$14,972, maintenance of \$15/month, a salvage value at the end of 84 months of \$1,000 and lease payments of \$325/mo. Suppose further an opportunity rate of interest of .00757543 per month.

Suppose further that the equipment is leased for 12 months and then purchased with \$900 rental credits. What is the cost of doing this above the cost of outright purchasing? Suppose it is leased for 24 months with \$2000 rental credits.

#### Solution:

14972.00	ST01	
325.00	ST04	
0.00757543	ST05	
15.00	ST06	
1000.00	ST07	
84.00	GSB1	
15371.15	***	СР
	<b>R∕S</b>	
-4771.33	***	Net (since the answer is less than 0, it implies
988.88	ENTT	it is cheaper to pur-
12.00	GSB2	chase rather than to lease by \$4771.33)
1424.73	***	OP <sub>1</sub>
2000.00	ENT↑	
24.00	GSB2	
2630.41	***	OP <sub>2</sub> Cost of leasing for 24 months before purchasing

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Store data:			
2a	Purchase price	Р	ST0 1	
2b	Lease payments	L	STO 4	
2c	Opportunity rate of interest	i, per period	ST0 5	
2d	Maintenance cost	m, per period	ST0 6	
2e	Salvage value	SV	ST0 7	
3	Enter useful life	n, periods		
4	Calculate net cost of purchasing		GSB 1	СР
5	Calculate net difference		R/S	CP - CL
6	For a new case, go to step 2			
7	(Optional) Enter:			
7a	Rental credits applied to purchase price	Credits	ENT 1	
7b	Periods of interim lease	m, periods		
8	Calculate cost of leasing for m periods,		GSB 2	OP
	before purchasing			
9	For another case, go to step 7			

D4							
01 #LELI				48 ST03			
02 GSB0				49 RTN			
03 RCL1							
04 RCL7							
AS POLO							
05 V							
100 A							
67 -							
08 RCL6							
09 RCL3							
10 X							
11 +							
12 R/S		*** CF	)				
17 PC14							
14 PCL7							
IT KOLO							
13 ^							
16 -		or					
17 R/S		*** CF	' - CL				
18 *LBL2							
19 GSB0							
20 RCL4							
21 RCL6							
22 -							
22 -							
23 X		Credit					
24 X7Y		creati	.5				
25 RCL1							
26 -							
27 RCL2							
28 ×							
29 -							
ZA RCII							
71 -							
70 P/C		*** 00	)				
		UF					
33 ¥LEL0							
34 RUL5							
35 1							
36 +							
37 X≠Y		n					
38 YX							
39 1/X							
40 ST02							
41   STX		(1 + 4	n				
42 ENTA		(1 + 1	1	*** "Print	x" may	be ins	erted.
A7 (					5		
40 1							
44 -							
45 X							
46 RCL5							
47 ÷							
			REGIS	STERS			
0	1 P		$\frac{2}{1}/(1 + i)^{n}$	$(1 + i)^{n}$ -	1 4 L		<sup>5</sup> i
6 M	7 SV		8	$i(1 + i)^{n}$	.0		.1
.2	.3		.4	5	16		17
18	19		20	21	22		23
24	25		26	27	28		29

### REAL ESTATE RENTAL INVESTMENT ANALYSIS

Using the equations below, this program solves for monthly rent or cash flow, gross return on investment, and taxable income.

Cash flow %=  $\frac{\text{Rent/month} - \text{Cost/month}}{\text{Investment/12}}$ 

Gross growth return = Cash flow % +

(P x Inflation rate) + Equity build-up Investment

Depreciation/yr = <u>P - Value of land</u> (book value) depreciable life

 $\approx \frac{.7 P}{20}$ 

Taxable gain = Actual cash flow depreciation

This program is adapted from HP-65 Users' Library program #01216A by John Feemster Example:

A house is for sale for \$30,000 with an assumable 6 3/4% FHA Loan paid down to \$23,500. Payments of principle, interest, taxes, and insurance are \$239.17 per month. The place will rent for \$275.00/month. The investor is in the 30% tax bracket. The inflation rate is 7%. Determine the cash flow %, gross growth return, and taxable income from the investment.

Solution:

30000.00 ST01 23500.00 -6500.00 \*\*\* ST02 239.17 ST03 275.00 ST04 GSB3 6.61 \*\*\* Cash flow (%) 23500.00 ENT† 6.75 ENT† 7.00 GSB4 26.37 \*\*\* Return (%) 30.00 R/S 199.13 \*\*\* Taxable income (\$)

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Store data:			
2a	Purchase price	P,\$	STO 1	
2b	Investment	Ι,\$	ST0 2	
2c	Payment/month	Pmt, \$	STO 3	
2d	Either Rent/month	Rent, \$	STO 4	
	or Cash flow (% of Investment)	Cash F, %	STO 5	
3	Initialize		GSB 1	
4	Calculate either Rent		GSB 2	Rent/mo, \$
	or Cash flow		GSB 3	Cash flow,%
5	Calculate gross return on investment			
5a	Loan amount	Loan, \$	ENT ↑	
5b	Interest rate	i,%	ENT ↑	
5c	Inflation factor	INF, %	GSB 4	Gross return, %
6	Calculate			
	Taxable income			
6a	Tax Bracket	TB, %	R/S	<pre>\$ taxable/ vr</pre>
				J.

	· · · · · · · · · · · · · · · · · · ·						
01 *LBL1	initia	lize	48	ST+6			
02 I			47	RULZ			
<b>0</b> 3 2			30	÷			
04 ST×3	annual	payments	51	RCL5			
05 EEX			52	÷			
RE 2			53	RCLØ			
97 STN9			54	х			
00 CT-F			55	R/S		***gro	ss return
			56	RCIR			
09 R/S			57	÷			
10 *LBL2	calcul	ate rent	50	- 			
11 RCL5			38	5106			
12 RCL2			59	RULI			
13 ×			60	•		approx	. bldg. value
14 RCL3			61	7		~~~~~~	
15 +			62	Х			
15 1			63	2			
17 2			64	0		deprec	iation, 20
17 2			65	÷		vear	basis
18 -			66	CHC		<b>J</b> =	
19 STO4			57	PCIE			
20 R/S	*** re	ent/month	67	ROLD			
21 *LBL3	calcul	ate cash flow	68	KULZ			
22 RCL4			69	X			
23 1			70	+			
24 2			71	RCL7			
25 X			72	÷			
25 PCI 7			73	RCL8			
20 KCES			74	Х			
			75	R/S		*** ta	xable \$
28 KULZ							
29 ÷							
30 STO5							
31 RCL0							
32 ×							
33 R/S	<b>***</b> Ca	ish flow					
34 *LBL4	calcul	ate gross					
35 RCI A	retur	n on invest-					
76 -	ment						
77 PCI 1							
70 V	anowth	due to					
	infl-	tion					
39 5105							
40 R4		• • • • •					
41 X	appro>	. interest/yr					
42 RCL0							
43 ÷							
44 CHS			<b></b>				
45 RCL3				Print	x" may	De ins	sertea.
46 +							
47 ST07							
	I	REGI	L				
<sup>0</sup> 100 <sup>1</sup> Purcl	n. price	<sup>2</sup> Investment	<sup>3</sup> Ann	pmts.	4 Rent	/mo.	<sup>5</sup> Cash flow
6 used 7		8	9		.0		.1
used Equi	.y gain	lax pracket	5		16		17
.2 .3		.4	.0		0		17
18 19		20	21		22		23
24 25		26	27		28		29

### BREAK-EVEN ANALYSIS

This program solves the following equations for Break-Even point in units  $(BEP_u)$ , Break-even point in dollars  $(BEP_D)$ , Margin of Safety Ratio (M), and Profit or Loss:

Computation Based on Units

- 1)  $BEP_u = \frac{F}{S-V}$ 2)  $M = \frac{u-BEP_u}{u}$
- 3) Profit or Loss = u(S-V)-F

Computation Based on Dollars

1) 
$$BEP_D = \frac{F}{R}$$
  
2)  $M = \frac{D - BEP_D}{D}$ 

where

- F = Total fixed costs
- V = Variable cost per unit
- S = Sales price per unit
- u = Expected sales in units
- D = Expected sales in dollars
- R = Marginal income ratio = (S-V)/S
- <u>NOTE</u>: The margin of safety will generally have no meaning if expected sales are less than sales at the break-even point.

This program is adapted from HP-65 Users' Library program #01275A by Louis Martinez.

#### EXAMPLE:

The Delux Publishing Company publishes a magazine with variable costs of \$0.40 and a sales price of \$0.50. The company has annual fixed cost of \$1,000,000.

Compute the following:

- Break-even point in (a) units and (b) dollars.
- (a) Profit or loss and (b) Margin of safety ratio for expected sales of 12,500,000 magazines.
- (a) Profit or loss and (b) Margin of safety ratio for expected sales of \$20,000,000.
- Sales volume in (a) units and (b) dollars needed to generate a profit of \$5,000,000.

### SOLUTION:

0.40	ENTT	
0.50	ENTT	
1000000.00	GSB1	
10000008.00	***	BEP.
	R∕S	u
5000000.00	***	BEPn
12500000.00	GSB2	D
250000.00	***	Profit
	R∕S	
0.20	***	Μ
20000000.00	GSB3	
3000000.00	***	Profit
	R∕S	
0.75	***	М
5000000.00	ST+1	
	GSB4	
60000000.00	***	BEP
	R/S	- u
30000000.00	***	BEP

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Key in the program			
2.	Enter data:			
2a.	Variable cost per unit	v	ENT↑	
2b.	Sales price per unit	S	ENT↑	
2c.	Fixed costs	F		
3.	Compute break-even point in units		GSB 1	BEPu
4.	Compute break-even point in dollars		R/S	BEPD
5.	ENTER:			
5a.	Expected sales in units	u		<b>D</b>
5b.	Compute profit (or loss if negative)		GSB 2	or Loss
5c.	Compute margin of safety ratio		R/S	м
6a.	Expected sales in dollars	D		<b>D</b>
6b.	Compute profit (or loss if negative)		GSB 3	Profit or Loss
6c.	Compute margin of safety ratio		R/S	м
7.	(Optional) To compute sales volume			
	necessary to provide a desired profit:			
7a.	Add the desired profit to fixed costs	DES. Profit	ST0 +1	
7b.	Compute break-even point in units		GSB 4	BEPu
7c.	Go to step 4			
8.	For a new case, go to step 2			

01 *LBL1 02 sto1 03 R4				***	Μ	
04 STO2 05 X≠Y 06 STO3 07 -	S-V					
08 ST04 09 RCL2 10 ÷ 11 ST05	P					
12 *LBL4 13 RCL1 14 RCL5	K					
15 ÷ 16 STO7 17 RCL1 18 RCL4	BEPD					
19 ÷ 20 STO6 21 R∕S 22 X≭Y	*** BE	Pu				
23 R/S 24 *LBL2 25 ST08 26 FCL4	*** BE	P <sub>D</sub>				
27 × 28 RCL1 29 -	*** D	ofit on loss				
30 R/S 31 RCL8 32 RCL6 33 - 74 RCL8		UTTE OF LOSS				
34 KCL0 35 ÷ 36 R/S 37 *LBL3 20 ST09	*** M					
39 RCL5 40 x 41 RCL1			*** "Printx"	may be inse	erted to replace	"R/S".
43 R/S 44 RCL8 45 RCL7 46 -	*** Pı	rofit or Loss				
47 RCL8						
		REGI	STERS			
0		2 5	3 V	4 S-V	° R	
<sup>6 BEP</sup> u	/ BEPD	<sup>8</sup> u or D	9	.0	.1	
.2	.3	.4	.5	16	17	
18	19	20	21	22	23	
24	25	26	27	28	29	1

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In the Hewlett-Packard tradition of supporting HP programmable calculators with quality software, the following titles have been carefully selected to offer useful solutions to many of the most often encountered problems in your field of interest. These ready-made programs are provided with convenient instructions that will allow flexibility of use and efficient operation. We hope that these Solutions books will save your valuable time. They provide you with a tool that will multiply the power of your HP-19C or HP-29C many times over in the months or years ahead.

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