## HEWLETT-PACKARD

Step-by-Step Solutions For Your HP Calculator Engineering Applications


HP-32S

## Help Us Help You!

Please take a moment to complete this postage-paid card, tear it out and put it in the mail. Your responses and comments will help us better understand your needs and will provide you with the best procedures to solve your problems. Thank you!

## HELP US HELP YOU!

Book: Engineering Applications Date acquired: $\qquad$
Name $\qquad$
Street $\qquad$
City, State, Zip
Phone $\qquad$ ) $\qquad$ Business $\qquad$ or Home $\qquad$

1. What calculator will you use this book with? 008 $\square$ HP-32S 006 Other $\qquad$
2. How many other HP solution books have you bought for this calculator? $\qquad$
3. What is your OCCUPATION?
$101 \square$ Student $103 \square$ Professional $109 \square$ Other $\qquad$
4. Where did you purchase this book?
$403 \square$ Bookstore $404 \square$ Discount or Catalog Store 407 Mail Order 410 HP Direct

411 Other $\qquad$
5. How did you first hear about this book?
$501 \square$ HP Owner $503 \square$ Advertising $506 \square$ Salesperson $507 \square$ Brochure $508 \square$ Other
6. To what degree did this book influence your calculator purchase decision? $601 \square$ Major Influence $602 \square$ Minor Influence $603 \square$ No Influence
7. How well does this book cover the material you expected?
$701 \square$ Good $702 \square$ Moderate $703 \square$ Low
8. What level of knowledge is required to make use of the topics in this book? $801 \square$ High 802 $\qquad$ Medium 803 $\qquad$ Low
9. How clearly was the material in this book presented?

901 Good 902Moderate 903 $\square$ Low
10. How would you rate the value of this book for your money? $111 \square$ High 112 Medium 113 $\qquad$ Low

Comments: (Please comment on improvements and additional applications or subjects you would like HP to cover in this or another solution book.) $\qquad$
$\qquad$
$\qquad$
$\qquad$


## $\|\|\|$

BUSINESS REPLY MAIL
postage will be paid by addressee



## Engineering Applications

Step-by-Step Solutions for Your HP-32S Calculator

Edition 1 June 1988
Reorder Number 00032-90057

## Notice

This manual and any keystroke programs contained herein are provided " as is" and are subject to change without notice. Hewlett-Packard Company makes no warranty of any kind with regard to this manual or the keystroke programs contained herein, including, but not limited to, the implied warranties of merchantability and fitness for a particular purpose. Hewlett-Packard Co. shall not be liable for any errors or for incidental or consequential damages in connection with the furnishing, performance, or use of this manual or the keystroke programs contained herein.

- Hewlett-Packard Co. 1988. All rights reserved. Reproduction, adaptation, or translation of this manual, including any programs, is prohibited without prior written permission of Hewlett-Packard Company, except as allowed under the copyright laws. Hewlett-Packard Company grants you the right to use any program contained in this manual in this Hewlett-Packard calculator.

The programs that control your calculator are copyrighted and all rights are reserved. Reproduction, adaptation, or translation of those programs without prior written permission of Hewlett-Packard Co. is also prohibited.

Corvallis Division 1000 N.E. Circle Blvd. Corvallis, OR 97330, U.S.A.

## Printing History

## Contents

## 5 How to Use This Book

17 Electrical Engineering8 Reactance Chart
11 Impedance of a Ladder Network
15 Smith Chart Conversions
21 Transistor Amplifier Performance
226 Mechanical Engineering
27 Black Body Thermal Radiation
32 Ideal Gas Equation
35 Conduit Flow
40 Static Equivalent at a Point
45 Composite Section Properties
52 Soderberg's Equation for Fatigue
35 Civil Engineering
56 Mohr's Circle for Stress
63 Field Angle Traverse
469 Statistics
70 t Statistics
$70 \quad$ Paired t Statistics
71 t Statistic for Two Means
76 Chi-Square Evaluation
80 F Distribution
84 Analysis of Variance (One Way)
88 Binomial Distribution
92 Poisson Distribution
$5 \quad 95$ Mathematics
96 Triangle Solutions
102 Derivative of a Function
104 Linear Interpolation
106 Circle Determined by Three Points

## How to Use This Book

The Engineering Applications solutions book provides sets of keystrokes and routines to help you solve a variety of engineering, statistics, and mathematics problems. The routines have been written to provide for easy use and minimum memory space. This book is to be used with the HP-32S calculator.

Before you use the solutions in this book, you should be familiar with the following concepts from the owner's manual:

- The basics of your calculator - how to perform arithmetic operations, move from menu to menu, and use the menu keys to do calculations.
- How to use the SOLVE function to solve for a variable.
- How to enter numbers for statistics.
- How to key in and run a program. You may wish to refer to the Function Index in your HP-32S Owner's Manual for information on how to key a particular function into a program.
- How to determine the number of bytes in a program and how to display the checksum.

Keys and Menu Selection. A key on the calculator keyboard is represented like this: STO. A shifted function is preceded by a shift key, like this: ASIN . A menu label is represented like this: $\{\mathrm{DEE}\}$. It is often necessary to go through several menus to obtain the desired


Display Formats. The examples in this book show numbers displayed to four decimal places. You may change the number of decimal places your calculator displays by pressing DISP $\{\mathrm{F} \times\}$ and the number of decimal places desired. If you wish to see the full 12-digit precision of a number regardless of the display format, press $\square$ SHOW ; the full precision number is displayed as long as you hold down the SHOW key.

Programs. The HP-32S calculator uses single letters to denote program labels; you have up to 26 labels in program memory. When keying in the program listings in this book, your calculator will display a DUFLICAT. LEL error if you use a letter for a label that is already used in program memory. To avoid this problem, simply choose a different letter to designate the label. Be sure to change any XEQ or GTO statements that correspond to the newly-assigned label and make note of the changes so that when you execute the routine, you specify the proper label.

When you key in a number having more than three digits in its mantissa, the HP-32S automatically inserts appropriate commas into the number in both data-entry and programming modes.

Changing the label name of a program affects its checksum.

Checksum. A checksum is provided for each program listing as a verification that the program has been keyed in correctly. To view the checksum, press MEM $\left\{\mathrm{FFG}^{\prime} \mid 1\right\}$ and scroll through the listing to the program label you want to check. Press and hold [SHOW to display the checksum.

Our thanks to Tony Vogt of Oregon State University for developing the problems and equations in this book.

## Electrical Engineering

## Reactance Chart

This program calculates the resonant frequency, the inductance, or the capacitance of an LC circuit at resonance given the other two variables. It also calculates the capacitive and inductive reactances at resonance, which are equal.

$$
\begin{gathered}
f=\frac{1}{2 \pi \sqrt{L C}} \\
X=\frac{1}{2 \pi f C}
\end{gathered}
$$

where:
$L$ = inductance in henrys.
$C=$ capacitance in microfarads.
$f=$ resonant frequency in hertz.
$X=$ reactance in ohms.

## Program Listing.

When keying in steps R12 and R13, press 6 ENTER $\square$ and $+/-$. These steps require less memory than keying in -6.

| F61 LEL R | F 12 E |
| :---: | :---: |
| F62 IHFUT F | $\mathrm{F} 13+$ |
| F6S IHFUT L | F 1416 |
| RE4 IHFIIT E | F15 $\times$ |
| R65 2 | F1G FLLX E |
| F06 $\pi$ | F17 FCLX $W$ |
| $\mathrm{RG7} \times$ | R18 1 |
| F68 FCL $\times$ F | R19 - |
| F09 ST0 | Fig RTH |
| F1E FCLX L | Che日ksum = 6CDE |
| F11 STO $\%$ |  |

Flags Used. None.
Memory Required. 30 bytes.
Remarks. The value of $C$ is in microfarads to increase the precision of the SOLVE function.

## Program Instructions.

1. Key in program listing; press $C$ when finished.
2. Press SOLVE/S \{FH\} R.
3. Specify the unknown variable by pressing

SOLVE/S \{GOLVE $\}$ variable.
4. Key in the variable value at each prompt and press $R / S$.
5. See the variable for which the program is solving.
6. Press VIEW $X$ to see the reactance.
7. For a new case, go to step 3.

## Variables Used.

$L=$ inductance in henrys.
$C=$ capacitance in microfarads.
$F=$ resonant frequency in hertz.
$X=$ reactance in ohms.
$W=2 \pi f$ (angular velocity $\omega$ in radians per second).

## Example. Resonant Frequency and Reactance.

Calculate $F$ and $X$, when $L=1.0 \mathrm{mh}$ and $C=0.25 \mu$.
Keys:

| -SOLVE/S $\{\mathrm{FH}\}$ | $\mathrm{FN}=$ - | Prompts for program label. |
| :---: | :---: | :---: |
| R | value | Specifies program R. |
| $\underbrace{}_{\{S O L V E\}} \text { SOLVE/S }$ | SOLVE _ | Prompts for the unknown variable. |
| F | L?value | Starts program R; prompts for variables except $F$. |
| 因 3 +/- $\mathrm{R} / \mathrm{S}$ | C?value | $C$ must be in microfarads. |
| . 25 R/S | $\mathrm{F}=10,065.8424$ | Displays the resonant frequency. |
| - VIEW X | $\mathrm{X}=63.2456$ | Displays the reactance. |

## Impedance of a Ladder Network

This program computes the input impedance of a ladder network. Elements are added one at a time from right to left. The first element must be parallel. The input impedance may be viewed at any point in the ladder as the elements are added.

Given an input impedance of $Y_{i n}$, adding a shunt (parallel) $R, L$, or $C$ results in a new input impedance of:

$$
Y_{\text {new }}=\left\{\begin{array}{l}
Y_{\text {in }}+\left(\frac{1}{R_{p}}+j 0\right) \\
Y_{\text {in }}+\left(0-j \frac{1}{\omega L_{p}}\right) \\
Y_{\text {in }}+\left(0+j \omega C_{p}\right)
\end{array}\right.
$$

Adding a series $R, L$, or $C$, we have:

$$
Y_{\text {new }}=\left\{\begin{array}{l}
\left(\frac{1}{Y_{\text {in }}}+\left(R_{s}+j 0\right)\right)^{-1} \\
\left(\frac{1}{Y_{\text {in }}}+\left(0+j \omega L_{s}\right)\right)^{-1} \\
\left(\frac{1}{Y_{\text {in }}}+\left(0-j \frac{1}{\omega C_{s}}\right)\right)^{-1}
\end{array}\right.
$$

where $Z=\frac{1}{Y}$ and $\omega=2 \pi f$.

## Program Listing．

HE1 LEL H
HEL IHFUT F
H03 2
$\mathrm{H} 04 \times$
H05 $\pi$
H06 $\times$
Nat STO W
Has a
Hag EHTER
H16 RTH
Checksum＝日ece
901 LEL 5
502 CHFLK1\％
603 R
S04 R4
$505 \mathrm{CHFLX} 1 \%$
S66 CMFLX＋
sal CMFLK1～x
Gas RTH
Checksum＝9EAS
FQ1 LEL P
FGE CMFLX＋
FGS RTH
Checksum＝ 9583
C01 LEL C
CaE IHFUT C
cas RCLX $W$
C04 1
0.5 RTH

Cherksum＝190H
L61 LEL L
Lee IfFUT L
Las RCLX $W$
LG4 $1 \times$
L6．5＋－
L6E 日
LG7 RTH
Chものksuri $=517 \mathrm{E}$
FQ1 LEL R
FQE
FGG IHFIIT R
F04 1／x
F0． 5 RTH
Checkeuri＝FBET
201 LEL 2
2日2 CMFLK1×
20G $1, x \rightarrow$ 日，r
204 STO 2
20.5 ※》

2日G STO A
207 VIEN A
206 ソIEN Z
269 ※》
21日 日，トゥ
211 CHFLK1\％
212 RTH
Cherksum $=5450$

Flags Used．None．
Memory Required． 75 bytes．

## Remarks.

- The program performs calculations using the admittance in cartesian coordinates but displays the result as an impedance in polar coordinates.
- Angles must be consistent with the angular mode currently set in the calculator.


## Program Instructions.

1. Key in the program listing and press $C$ when finished.
2. Press XEQ N.
3. Key in the frequency and press R/S .
4. Select the appropriate element to add:

- Press XEQ R to add a resistor.
- Press XEQ $L$ to add an inductor.
- Press XEQ C to add a capacitor.

5. Key in the value at the prompt and press R/S.
6. Select the appropriate means of adding the element:

- Press XEQ $P$ to add the element in parallel.
- Press XEQ $S$ to add the element in series.

7. To add another element, go to step 4.
8. Press $X E Q Z$ to see the angle of the input impedance.
9. Press $R / \mathrm{S}$ to see the magnitude of the input impedance.
10. Optional: press $R / S$ to continue adding elements to the ladder.

## Variables Used.

$R=$ resistance in ohms.
$L=$ inductance in henrys.
$C=$ capacitance in farads.
$Z=$ magnitude of the input impedance in ohms.
$A=$ input impedance angle.
$F=$ frequency in hertz.
$W=2 \pi f$ (angular velocity $\omega$ in radians per second).

Example: RLC Ladder Network. Find the input impedance of the following circuit at a frequency of 1 MHz :


Keys:

- MODES \{DIG

XEQ N
( 6 R/S
XEQ R
100 R/S
XEQ $P$
XEQ C
650 [国 12 +/- $R / \mathrm{S}$ XEQ S

XEQP
XEQ R
1000 R/S
XEQ $P$
XEQ $Z$
$R / S$

Display:

F?value
0.0000

R?value
0.0100
0.0100

C?value
0.0000
0.0014

L?value
0.0000
0.0014

R? 100.0000
0.0010
0.0024
$A=-41.8224$
$Z=306.7333$

## Description:

Sets degrees mode.
Inputs frequency.
Adds resistor in parallel
(first element must be in parallel).
Adds capacitor in series.

Adds inductor in parallel.

Adds resistor in parallel.

Displays the input impedance angle.
Displays the input impedance.

## Smith Chart Conversions

The distance between a point on a Smith Chart and its center may be measured using a number of parameters. This program performs conversions between several of the most commonly used parameters: standing wave ratio, reflection coefficient, and return loss. It may also be used to convert between impedance and reflection coefficient.

$$
\sigma=\text { voltage standing wave ratio }=\frac{1+\rho}{1-\rho} .
$$

$S W R=$ standing wave ratio expressed in decibels.
$\rho=$ reflection coefficient.
R.L. = return loss.

These parameters are related as follows:
$S W R=20 \log \sigma$
R.L. $=20 \log \frac{1}{\rho}$
$\sigma=\frac{1+\rho}{1-\rho}$


These relationships are perhaps more clearly seen in this sketch:


For a system having characteristic impedance $Z_{0}$, the impedance and reflection coefficient are related by

$$
\Gamma=\rho \measuredangle \phi=\frac{\frac{\mathrm{Z}}{Z_{0}}-1}{\frac{\mathrm{Z}}{Z_{0}}+1}
$$

and

$$
\mathbf{Z}=Z \quad \Varangle \theta=Z_{0} \frac{1+\Gamma}{1-\Gamma}
$$

where:

$$
\begin{aligned}
& \Gamma=\text { complex reflection coefficient. } \\
& \rho=|\Gamma| \\
& \phi=\measuredangle \Gamma \\
& \mathbf{Z}=\text { impedance. } \\
& Z=|\mathbf{Z}| \\
& \theta=\not \mathbf{Z} .
\end{aligned}
$$

## Program Listing．

| H＠1 LEL A | HES 1 |
| :---: | :---: |
| $\mathrm{FQ2}+\cdots$ | H0S STO K |
| Chににksum＝130E | H04 IHFUT M |
| DE1 LEL D | HES IHFUT F |
| DG2 20 | HEG IHFITT D |
| DG3－ | HET IHFIIT E |
| ［04 1020 | HES FCL M |
| ［095 RTH | HE9 FEL F |
| Cherksum $=$ E6ES | H1® $\mathrm{B}, \mathrm{r}^{+\prime \mathrm{tag}}$ |
| E＠1 LEL E | H11 $\mathrm{FCL}+\mathrm{K}$ |
| E＠こ STOK | H12 FCL M |
| E63 1 | H13 FEL F |
| $\mathrm{EQ4}+$ | H14＋ |
| E65 1 | H15 日，r＋y， |
| $\mathrm{EOG} \mathrm{FCL}-\mathrm{K}$ | H1G FCL +K |
| BQ 7 － | H17 EMFL $\%$ |
| EQ8 RTH | H1S FEL D |
| Cherksum $=6802$ | H19 FEL E |
| EQ1 LEL E | Heg E，ringe |
| EQ2 STOK | H21 CMFL\％ |
| E日S 1 | Hza morerar |
| E64－ | H2S STO 2 |
| E05 1 |  |
| EQG FCL +K | H2S ST0 T |
| E 07 － | H2G UIEN T |
| E08 R RTH | H27 YIEN Z |
| Eheにksum＝170E | H2S FTH |
| FQ1 LEL F | Ch＠にkEum $=$ E610 |
| F62 1／x | GQ1 LEL G |
| Cheにksum $=7789$ | G02 IHFUT T |
| C01 LEL E | Les IHFUT 2 |
| 0.02 LOL | T04 IHFIIT D |
| ［日S 20 | LE5 IHFUT E |
| ［04 $\times$ | G06 FCL T |
| C05 RTH | GQ7 FEL 2 |
| Cheにksum＝5C10 | C08 $\mathrm{B}, \mathrm{r+rys}$ |
| H01 LEL H | GEG FCL |

G16 FCL C

G12 CMFL:
G13 STO A
G14 \ll >
$G 15 \mathrm{STO} \mathrm{E}$
G16 < >
G17 1
G18-
G19 RCL E
G20 1

Ge1 $\mathrm{FCL}+\mathrm{A}$
Gee CIFLK:
G23 $1, x+8, r^{-}$
G 24 STO F
G25 <>y
Ge6 STO M
GET YIEN M
Ge8 UIEN F
529 RTH
Checksuri $=6425$

Flags Used. None.
Memory Required. 130.5 bytes.

## Remarks.

- Each routine is independent of the others. Therefore, key in only those routines that will be used.
- Angles must be consistent with the angular mode currently set in the calculator.


## Program Instructions.

1. Key in the program listings of the routines to be used; press $C$ when finished.
2. For conversions involving real number parameters (routines $A$ thru $F$ ):

- Key in the variable and select the appropriate routine:
- Press XEQ A to convert R.L. to $\rho$.
- Press XEQ B to convert $\rho$ to $\sigma$.
- Press XEQ C to convert $\sigma$ to $S W R$.
- Press XEQ D to convert $S W R$ to $\sigma$.
- Press XEQ E to convert $\sigma$ to $\rho$.
- Press XEQ F to convert $\rho$ to R.L.
- Optional: continue converting by executing the next routine in the sequence.

3. To convert from $\mathbf{Z}$ to $\Gamma$ :

- Press XEQ G.
- Key in the values at each prompt and press R/S.
- See $M$; press R/S ; see $P$.

4. To convert from $\Gamma$ to $Z$ :

- Press XEQ $H$.
- Key in the variables at each prompt and press R/S.
- See $T$; press $\mathrm{R} / \mathrm{s}$; see $Z$.

5. For a new case, go to step 2,3 , or 4 .

## Variables Used.

$Z=$ magnitude of the impedance.
$T=$ angle of the impedance.
$P=$ magnitude of the complex reflection coefficient.
$M=$ angle of the complex reflection coefficient.
$C=$ magnitude of the characteristic impedance.
$D=$ angle of the characteristic impedance.
$A, K, B=$ variables used for intermediate results.

Example 1. Convert a $10 \mathrm{~dB} S W R$ to $\sigma$.
Keys:
Display:
Description:

10 XEQ D
3.1623

Displays $\sigma$.

Example 2. Convert a 5 dB return loss to $S W R$.

| Keys: | Display: | Description: |
| :--- | :--- | :--- |
| 5 XEQ A | 0.5623 |  |
| XEQ B | 3.5698 | Displays $\rho$. |
| XEQ C | 11.0528 | Displays $\sigma$. |

Example 3. A $75 \Omega$ system is terminated with an impedance of 53 at an angle of $41^{\circ}$. Find the reflection coefficient.

| Keys: | Display: | Descriptio |
| :---: | :---: | :---: |
| - MODES $\{\mathrm{DL}$ \} |  | Sets degrees |
| XEQ G | T? value | Inputs value |
| $41 \mathrm{R} / \mathrm{S}$ | Z?value |  |
| 53 R/S | D?value |  |
| 0 R/S | C ? value |  |
| 75 R/S | $\mathrm{M}=118.3651$ | Displays $\Gamma$. |
| R/S | $\mathrm{P}=0.4107$ | Displays $\rho$. |

Example 4. A reflection coefficient of 0.35 at an angle of $11^{\circ}$ is observed in a $100 \Omega$ system. Find the impedance.

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| XEQ H | M?value | Inputs values. |
| $11 \mathrm{R} / \mathrm{S}$ | P ? value |  |
| . 35 R/S | D?value |  |
| $0 \mathrm{R} / \mathrm{S}$ | C?value |  |
| 100 R/S | $\mathrm{T}=8.6547$ | Displays angle. |
| R/S | $\mathrm{Z}=203.8784$ | Displays magnitude of the impedance, Z . |

## Transistor Amplifier Performance

This program calculates several small-signal properties of a transistor amplifier given the $h$-parameter matrix and the source and load impedances. The properties computed are the current and voltage gains and the input and output impedances.


Definition of h-parameter matrix:

$$
\left[\begin{array}{l}
v_{1} \\
i_{2}
\end{array}\right]=\left[\begin{array}{ll}
h_{i} & h_{r} \\
h_{f} & h_{o}
\end{array}\right]\left[\begin{array}{l}
i_{1} \\
v_{2}
\end{array}\right]
$$

Current gain:

$$
A_{i}=\frac{i_{2}}{i_{1}}=\frac{-h_{f}}{1+h_{o} Z_{L}}
$$

Voltage gain:

$$
A_{v}=\frac{v_{2}}{v_{1}}=\frac{A_{i} Z_{L}}{Z_{\text {in }}}
$$

Voltage gain with source resistor：

$$
A_{v v}=\frac{v_{2}}{v_{S}}=\frac{A_{i} Z_{L}}{Z_{i n}+Z_{S}}
$$

Input impedance：

$$
Z_{\text {in }}=h_{i}+h_{r} Z_{L} A_{i}
$$

Output impedance：

$$
Z_{\text {out }}=\frac{h_{i}+Z_{S}}{h_{o} h_{i}+h_{o} Z_{S}-h_{f} h_{r}}
$$

## Program Listing．

Tg1 LEL T
TGE CLVARS
T0S 1.012
T04 STO i
Checksum＝7FE4
X01 LEL X
xGE IHFIUT（i）
XGS ISGi
804 GTO X
805 RCL I
XGE RCL
XQ
X0S ETO．
809 x》ッ
810 STO I
X11 FCL G
K12 RCL $+K$
$813 \mathrm{FCL} H$
X14 FCLX L
815 日，r－ウリ，
8161
$817+$
K1E CMFLK1／s
819 FCL E
xeg RCL F

```
k21 +--
x2e 日,r+!,%
x23 CHFL%%
824 STO H
<25 <<>>
<2E STOM
x27 <<>>
<2S RED V
<E9 RCL C
8SG FCL+K
8B1 FCL D
see RCLX L
8SS 日,r`!日,*
XS4 EMFLS%
85 FCL F
NSE FCL E
<E7 日,r`!,%
4SE DMFLS+
89 STO F
846 <<>
841 STO O
X42 <<>y
843 CMFLX1/x
844 FCL M
845 RCL H
```

x2e $6, r-+4, x$
S2S CHFLS
Xe 4 STOH
x25 x》ы
xes sTo M
xe7 《＞＞
xes RED U
8 Cg RCL C
KOU FCL＋K
SB1 FCL
see RCLX L
XSE 日， $\mathrm{r}^{-+1.2 \%}$
8 S 4 DAFLX
855 ECL H
xGE FCL E
XS7 日，r－
8Se CMFLS＋
xeg STO F
846 \ll
841 ST0
X42 ※》！
K43 CMFLX1／s
844 FCL M
845 FOLH

K4E DMFL\％
$847 \mathrm{FCL} K$
$848 \mathrm{RCL} L$
$849 \mathrm{E}, \mathrm{r}^{-+13, \%}$
$85 \mathrm{CMFL} \times$
851 XEQ V
85 ECL O
853 FCL F
854 CMFLS
X55 RCL 0
85G RCL＋I
857 RCL F
X58 RCL＋J
859 CMFLK：
XG日 REQ $V$
XE1 FCL 0
8ee RCL F
863 REQ 4
864 FCL G
$865 \mathrm{RCL} H$
XGG 日，rチリンス
867 RCL I
XGE RCL
869 CHFLS×
X 76 ECL G
X71 RCL＋ H
$872 \mathrm{RCL} H$
X73 RCLX E


```
875 DMFLK+
87G RCL E
K77 FCL+ C
X7S RCL F
879 ECLx D
```



```
NS1 DHFLX-
SE2 EmFLX1/x
8SS FCL A
8E4 RCL E
485 日,\mp@code{Hy,*}
<EG RCL+ 」
8E7 <<>y
8GS FCL+ I
899 <<>
890 CMFL%%
Checksumi = 7200
V01 LEL v
VGE n,x+6,r
VGS STO R
VG4 x<\
V05 ETO T
VबE <<>
V07 日, r->y,*
UGE YIEN T
YGG VIEN R
W10 RTH
ChEcksuri = EFFE
```

Flags Used．None．
Memory Required． 164 bytes．

## Remarks．

－This program clears all variables stored in Continuous Memory．
－Angles must be consistent with the angular mode currently set in the calculator．
－To limit the number of variables，the program uses variable $T$ for the angle and $R$ for the magnitude of all of the output results．

## Program Instructions.

1. Key in the program listings; press $C$ when finished.
2. Press XEQ $T$.
3. Key in the variables at each prompt and press $R / S$.
4. See the angle of $A_{i}$ and press R/S.
5. See the magnitude of $A_{i}$ and press R/S.
6. See the angle of $A_{v}$ and press $\mathrm{R} / \mathrm{S}$.
7. See the magnitude of $A_{v}$ and press $R / S$.
8. See the angle of $A_{v g}$ and press $\mathrm{R} / \mathrm{S}$.
9. See the magnitude of $A_{v g}$ and press R/S.
10. See the angle of $Z_{\text {in }}$ and press $R / S$.
11. See the magnitude of $Z_{i n}$ and press R/S.
12. See the angle of $Z_{\text {out }}$ and press R/S.
13. See the magnitude of $Z_{\text {out }}$.
14. For a new case, go to step 2 .

## Variables Used.

$A=$ angle of $h_{i}$.
$B=$ magnitude of $h_{i}$.
$C=$ angle of $h_{r}$.
$D=$ magnitude of $h_{r}$.
$E=$ angle of $h_{f}$.
$F=$ magnitude of $h_{f}$.
$G=$ angle of $h_{o}$.
$H=$ magnitude of $h_{o}$.
$I=$ angle of $Z_{\text {in }}$.
$J=$ magnitude of $Z_{i n}$.
$K=$ angle of $Z_{\text {out }}$.
$L=$ magnitude of $Z_{\text {out }}$.
$T=$ angle of $A_{i}, A_{v}, A_{v s}, Z_{\text {in }}, Z_{\text {out }}$.
$R=$ magnitude of $A_{i}, A_{v}, A_{v s}, Z_{\text {in }}, Z_{\text {out }}$.
$N, M, O, P, i=$ variables used for intermediate results.

Example. Find the small-signal properties of a transistor that has the following h-parameter matrix with source and load impedances of 1000 and 5000 ohms, respectively.

$$
h=\left[\begin{array}{rr}
1000 & 150 \mathrm{E}-6 \\
75 & 50 \mathrm{E}-6
\end{array}\right]
$$

## Keys:

- MODES \{DG\}

| XEQ T | A?0.0000 |
| :---: | :---: |
| R/S | B? 0.0000 |
| 1000 R/S | C? 0.0000 |
| R/S | D? 0.0000 |
| 150 因 6 +/- R/S | E? 0.0000 |
| R/S | F? 0.0000 |
| 75 R/S | G? 0.0000 |
| R/S | H? 0.0000 |
| 50 因 6 +/- R/S | I? 0.0000 |
| R/S | J? 0.0000 |
| 1000 R/S | K? 0.0000 |
| R/S | L? 0.0000 |
| 5000 R/S | $\mathrm{T}=180.0000$ |
| R/S | $\mathrm{R}=60.0000$ |
| R/S | $\mathrm{T}=180.0000$ |
| R/S | $\mathrm{R}=314.1361$ |
| R/S | $\mathrm{T}=180.0000$ |
| R/S | $\mathrm{R}=153.4527$ |
| R/S | $\mathrm{T}=0.0000$ |
| R/S | $\mathrm{R}=955.0000$ |
| R/S | $\mathrm{T}=0.0000$ |
| R/S | $\mathrm{R}=22,535.2113$ |

## Description:

Sets degrees mode.

Inputs values.

Displays angle of $A_{i}$.
Displays magnitude of $A_{i}$.
Displays angle of $A_{v}$.
Displays magnitude of $A_{v}$.
Displays angle of $A_{v s}$.
Displays magnitude of $A_{v g}$.
Displays angle of $Z_{\text {in }}$. Displays magnitude of $Z_{\text {in }}$.
Displays angle of $Z_{\text {out }}$. Displays magnitude of $Z_{\text {out }}$.

## 2

## Mechanical Engineering

## Black Body Thermal Radiation

All bodies emit thermal radiation according to their temperature. The higher the temperature, the more thermal radiation emitted. A black body is one that emits the maximum possible amount of energy at every wavelength for a specified temperature. The figure below represents the black body thermal emission as a function of wavelength.

This program can be used to calculate:

- The wavelength of maximum emissive power for a given temperature.
- The temperature corresponding to a particular wavelength of maximum emissive power.
- The total emissive power for all wavelengths.
- The emissive power at a particular wavelength and temperature.


$$
\begin{gathered}
\lambda_{\max } \mathrm{T}=c_{3} \\
E_{b(0-\chi)}=\sigma \mathrm{T}^{4} \\
E_{b \lambda}=\frac{2 \pi c_{1}}{\lambda^{5}\left(e^{c_{2} / \lambda \mathrm{T}}-1\right)}
\end{gathered}
$$

where:
$\lambda_{\text {max }}=$ wavelength of maximum emissivity in microns.
$\mathrm{T}=$ absolute temperature in ${ }^{\circ} \mathrm{R}$ or K .
$E_{b(0-x)}=$ total emissive power in $\mathrm{Btu} / \mathrm{hr}-\mathrm{ft}^{2}$ or watts $/ \mathrm{cm}^{2}$.
$E_{b \lambda}=$ emissive power at $\lambda$ in $\mathrm{Btu} / \mathrm{hr}-\mathrm{ft}^{2}-\mu \mathrm{m}$ or watts $/ \mathrm{cm}^{2}-\mu \mathrm{m}$.
$c_{1}=1.8887982 \times 10^{7} \mathrm{Btu}-\mu \mathrm{m}^{4} / \mathrm{hr}-\mathrm{ft}^{2}=5.9544 \times 10^{3} \mathrm{~W} \mu \mathrm{~m}^{4} / \mathrm{cm}^{2}$.
$c_{2}=2.58984 \times 10^{4} \mu \mathrm{~m}-{ }^{\circ} \mathrm{R}=1.4388 \times 10^{4} \mu \mathrm{~m}-\mathrm{K}$.
$c_{3}=5.216 \times 10^{3} \mu \mathrm{~m}-{ }^{\circ} \mathrm{R}=2.8978 \times 10^{3} \mu \mathrm{~m}-\mathrm{K}$.
$\sigma=1.713 \times 10^{-9} \mathrm{Btu} / \mathrm{hr}-\mathrm{ft}^{2}{ }^{\circ} \mathrm{R}^{4}=5.6693 \times 10^{-12} \mathrm{~W} / \mathrm{cm}^{2}-\mathrm{K}^{4}$.
$\sigma_{\text {exp }}=1.731 \times 10^{-9} \mathrm{Btu} / \mathrm{hr}-\mathrm{ft}^{2}-{ }^{\circ} \mathrm{R}^{4}=5.729 \times 10^{-12} \mathrm{~W} / \mathrm{cm}^{2}-\mathrm{K}^{4}$.

## Program Listing.

E日1 LEL E
BGE IHFIIT W
EGS IHFUT T
EO4 RCL W
B6.5 1/x
E06 RCLX E
E067 RCL $\div$
E098 $\mathrm{e}^{*}$
E09 1
E10 -
E11 1/x
E1E RCL 4
E13 5
E14 ${ }^{2}$
E15 -

E1G 2
E17 \%
E18 $\pi$
E19 \%
E2G FCLX A
EE 1 STO F
E2e vIEN F
E23 RTH
Checksum = 52E5
EQ1 LEL E
EG2 IHFUT T
E63 4
E64 붕
E0.5 RCLX S
EGE STO E

| E07 UIEN E | WET FETH |
| :---: | :---: |
| EQS RTH | Chロロトこum＝F204 |
| Eh心にkこum＝1506 | TE1 LEL T |
| WQ1 LEL H | TEG IHFIIT 4 |
| WEE IHFUT T | TEG FCL E |
| WGS FEL E | T04 FCL $\div$ ， |
| W64 FCL $\div$ T | TES STOT |
| W日S ETO | TEG YIEN T |
| WEE YIEN い | TET ETH |
|  |  |

Flags Used．None．
Memory Required． 67.5 bytes．
Remarks．The values of the constants differ between sources．

## Program Instructions．

1．Key in the program listing；press $C$ when finished．
2．Store the constants $A, B, C$ ，and $S$ in the appropriate storage registers．

3．Select the appropriate routine：
－Press XEQ W to calculate the wavelength of maximum power for a given temperature．
$■$ Press XEQ $T$ to calculate the temperature corresponding to a particular wavelength of maximum power．
－Press XEQ E to calculate the total emissive power．
－Press XEQ $B$ to calculate the emissive power at a particular wavelength．
－Key in the variables at each prompt and press R／S．
－See the variable for which the program is solving．
4．For a new case，go to step 3.

## Variables Used．

$$
\begin{aligned}
& T=\text { temperature. } \\
& W=\text { wavelength. } \\
& E=\text { total emissive power. } \\
& P=\text { emissive power at a given wavelength. } \\
& A=\operatorname{constant} c_{1} . \\
& B=\operatorname{constant} c_{2} . \\
& C=\operatorname{constant} c_{3} . \\
& S=\operatorname{constant} \sigma .
\end{aligned}
$$

Example．If sunlight has a maximum wavelength of $.550 \mu \mathrm{~m}$ ，what is the sun＇s temperature in $K$ ？Assume the sun is a black body．What is the total emissive power and the emissive power at $\lambda_{\max }$ ？What is the emissive power at $\lambda=0.400 \mu \mathrm{~m}$（ultraviolet limit）and $0.700 \mu \mathrm{~m}$（infrared limit）？

| Keys： | Display： | Description： |
| :---: | :---: | :---: |
| 5.9544 罭 3 STO A |  | Stores constants． |
| 1.4388 国 4 STO B |  |  |
| 2.8978 因 3 STO C |  |  |
| 5.6693 因 12 ＋／－ |  |  |
| STO S |  |  |
| XEQ T | W？value |  |
| ． 55 R／S | $\mathrm{T}=5,268.7273$ | Displays temperature． |
| XEQ E | T？5，268．7273 |  |
| R／S | $\mathrm{E}=4,368.7009$ | Displays the total emissive power． |
| XEQ B | W？0．5500 | Correct value already stored in $W$ ． |

Displays the emissive power.
XEQ $B$
W?0.5500
. 4 R/S
T?5,268.7273
R/S
$\mathrm{P}=3,964.8581$
Displays the emissive power.
XEQ $B$
W? 0.4000
. 7 R/S
T?5,268.7273
R/S
$\mathrm{P}=4,593.4033$
Displays the emissive
power. power.

## Ideal Gas Equation

Many gases obey the ideal gas law at high temperatures and low pressures. This program calculates any one of the four variables of the ideal gas equation when the other three are known.

$$
P V=n R T
$$

where:
$P=$ pressure.
$V=$ volume.
$n=$ number of moles.
$R=$ Universal Gas Constant.
$T=$ absolute temperature.

Table 2-1. Values of the Universal Gas Constant

| Value of $R$ | Units of $R$ | Units of $P$ | Units of $V$ | Units of $T$ |
| :---: | :---: | :---: | :---: | :---: |
| 8.314 | $\mathrm{N}-\mathrm{m} / \mathrm{g}$ mole-K | N/M ${ }^{2}$ | $\mathrm{m}^{3} / \mathrm{g}$ mole | K |
| 83.14 | $\mathrm{cm}^{3}$-bar/g mole-K | bar | $\mathrm{cm}^{3} / \mathrm{g}$ mole | K |
| 82.05 | $\mathrm{cm}^{3}-\mathrm{atm} / \mathrm{g}$ mole-K | atm | $\mathrm{cm}^{3} / \mathrm{g}$ mole | K |
| 0.08205 | liter-atm/g mole-K | atm | liter/g mole | K |
| 0.7302 | atm- $\mathrm{ft}^{3} / \mathrm{lbm}$ mole- ${ }^{\circ} \mathrm{R}$ | atm | $\mathrm{ft}^{3} / \mathrm{lbm}$ mole | ${ }^{\circ} \mathrm{R}$ |
| 10.73 | psi-ft ${ }^{3} / \mathrm{lbm}$ mole- ${ }^{-} \mathrm{R}$ | psi | $\mathrm{ft}^{3} / \mathrm{lbm}$ mole | ${ }^{\circ} \mathrm{R}$ |
| 1545 | psf-ft ${ }^{3} / \mathrm{lbm}$ mole- ${ }^{\circ} \mathrm{R}$ | psf | $\mathrm{ft}^{3} / \mathrm{lbm}$ mole | ${ }^{\circ} \mathrm{R}$ |

## Program Listing.



Flags Used. None.
Memory Required. 19.5 bytes.
Remarks. Value of $R$ must be compatible with units of $P, V$, and $T$.

## Program Instructions.

1. Key in program listing; press $C$ when finished.
2. Press SOLVE/S \{FH\} G, then specify the unknown variable by pressing SOLVE/S \{GOL'VE variable.
3. Key in the variables at each prompt and press R/S.
4. See the variable for which the program is solving.
5. For a new case, go to step 2.

## Variables Used.

$P=$ absolute pressure.
$V=$ volume.
$N=$ number of moles present.
$R=$ Universal Gas Constant.
$T=$ absolute temperature.

Example 1: Pressure. If 1.2 moles of air are enclosed in $40,000 \mathrm{~cm}^{3}$ at 1500 K , what is the pressure in atmospheres?

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| -SOLVE/S \{FH\} | $\mathrm{FN}=$ | Prompts for program label. |
| G |  | Specifies program G. |
| $\begin{aligned} & \text { SOLVE/S } \\ & \{S O L V E\} \end{aligned}$ | SOLVE | Prompts for the unknown variable. |
| P | V?value | Starts program G; |
| 40000 R/S | N ? value | prompts for variables |
| 1.2 R/S | R ? value | except $P$. |
| 82.05 R/S | T? value |  |
| 1500 R/S | $\mathrm{P}=3.6923$ | Displays the pressure. |

Example 2: Specific Volume. What is the specific volume ( $\mathrm{ft}^{3} / \mathrm{lbm}$ ) of a gas at a pressure of 3 atmospheres and a temperature of $540^{\circ} \mathrm{R}$ ? The molecular weight is $32 \mathrm{lbm} / \mathrm{lbm}$-mole.

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { SOLVE/S } \\ & \left\{\operatorname{SOL} \mathrm{V}^{\prime} \mathrm{E}\right\} \end{aligned}$ | SOLVE | Prompts for the unknown variable. (It is not necessary to redefine the program label being executed since it was defined in the last example. |
| V | P ? value | Starts program G; |
| $3 \mathrm{R} / \mathrm{S}$ | N ? value | prompts for the variables |
| 32 1/x R/S | R ? value | except $V$. |
| . 7302 R/S | T?value |  |
| 540 R/S | $\mathrm{V}=4.1074$ | Displays specific volume. |

## Conduit Flow

This program solves for either the average velocity or the pressure drop for viscous, incompressible flow in conduits.

For laminar flow ( $R e<2300$ ):

$$
f=16 / R e
$$

For turbulent flow ( $R e>2300$ ):

$$
\begin{gathered}
V^{2}=\frac{\Delta P / \rho}{2\left(f \frac{L}{D}+\frac{K_{T}}{4}\right)} \\
f=\frac{0.0772}{\left\{\log \left[\frac{6.9}{\operatorname{Re}}+\left(\frac{\varepsilon}{3.7 D}\right)^{1.111}\right]\right\}^{2}}
\end{gathered}
$$

where:
$V=$ average velocity.
$\Delta P=$ pressure drop.
$L=$ conduit length.
$D=$ conduit diameter. If the conduit is not circular, use an equivalent diameter defined by:

$$
D_{e q}=4 \times \frac{\text { Cross Sectional Area }}{\text { Wetted Perimeter }}
$$

$\varepsilon=$ surface irregularity.
$R e=$ Reynolds number; $R e=D V / \nu$.
$\nu=$ fluid kinematic viscosity.
$\rho=$ fluid density
$f=$ Fanning friction factor.
$K_{T}=$ sum of fitting factors.

Table 2-2. Fitting Coefficients

| Fitting | K |
| :--- | :---: |
| Globe valve, wide open | $7.5-10$ |
| Angle valve, wide open | 3.8 |
| Gate valve, wide open | $0.15-0.19$ |
| Gate valve, $3 / 4$ open | 0.85 |
| Gate valve, $1 / 2$ open | 4.4 |
| Gate valve, $1 / 4$ open | 20 |
| $90^{\circ}$ elbow | $0.4-0.9$ |
| Standard $45^{\circ}$ elbow | $0.35-0.42$ |
| Tee, through side outlet | 1.5 |
| Tee, straight through | 0.4 |
| $180^{\circ}$ bend | 1.6 |
| Entrance to circular pipe | $0.25-0.50$ |
| Sudden expansion | $\left(1-A_{u p} / A_{d n}\right)^{2 *}$ |
| Acceleration from $V=0$ to $V=V_{\text {entrance }}$ | 1.0 |
| $* A_{u p}$ is the upstream area and $A_{d n}$ is the downstream area. |  |

Table 2-3. Surface Irregularities

| Material | $\boldsymbol{\varepsilon}$ (Feet) | $\boldsymbol{\varepsilon}$ (Meters) |
| :--- | :--- | :--- |
| Drawn or smooth tubing | $5.0 \times 10^{6}$ | $1.5 \times 10^{6}$ |
| Commercial steel or wrought iron | $1.5 \times 10^{4}$ | $4.6 \times 10^{5}$ |
| Asphalted cast iron | $4.0 \times 10^{4}$ | $1.2 \times 10^{4}$ |
| Galvanized iron | $5.0 \times 10^{4}$ | $1.5 \times 10^{4}$ |
| Cast iron | $8.3 \times 10^{4}$ | $2.5 \times 10^{4}$ |
| Wood stave | $6.0 \times 10^{4}$ to | $1.8 \times 10^{4}$ to |
|  | $3.0 \times 10^{3}$ | $9.1 \times 10^{4}$ |
| Concrete | $1.0 \times 10^{3}$ to | $3.0 \times 10^{4}$ to |
|  | $1.0 \times 10^{2}$ | $3.0 \times 10^{3}$ |
| Riveted steel | $3.0 \times 10^{3}$ to | $9.1 \times 10^{4}$ to |
|  | $3.0 \times 10^{2}$ | $9.1 \times 10^{3}$ |

## Program Listing.



Flags Used. None.
Memory Required. 121 bytes.

## Program Instructions.

1. Key in program listing; press $\square$ when finished.
2. Press SOLVE/d $\{F H\} C$, then specify the unknown variable by pressing SOLVE/S \{GOL'VE variable.
3. Key in the variables at each prompt and press $R / S$.
4. See the variable for which the program is solving.
5. Optional: Press VIEW R to see the Reynolds number.
6. Optional: Press VIEW $F$ to see the Fanning friction factor.
7. For a new case, go to step 2.

## Variables Used.

$V=$ average velocity.
$P=$ pressure drop.
$L=$ conduit length.
$D=$ conduit diameter.
$E=$ surface irregularity.
$R=$ Reynolds number.
$B=$ fluid kinematic viscosity.
$S=$ fluid density.
$F=$ Fanning friction factor.
$K=$ fitting coefficient.

Example：Pressure Drop．A 60－meter pipe has three 180 degree bends（ $K_{T}=3 \times 1.6$ ）．The fluid is water $\left(\nu=9.3 \times 10^{-7} \mathrm{~m}^{2} / \mathrm{s}, \rho=1000\right.$ $\mathrm{kg} / \mathrm{m}^{3}$ ）．The pipe diameter is 0.030 m and the surface roughness is $3 \times$ $10^{-4} \mathrm{~m}$ ．If the average velocity is $3.20 \mathrm{~m} / \mathrm{s}$ ，what is the pressure drop in Pascals？What is the Reynolds number？What is the Fanning friction factor？

| Keys： | Display： |
| :---: | :---: |
| SOLVE／S $\{\mathrm{FH}\}$ | FN＝ |
| C | value |
| SOLVE／S | SOLVE＿ |
| \｛SOLVE\} |  |
| P | E？value |
| 3 因 4 ＋／－R／S | D？value |
| ． 03 R／S | V ？value |
| 3.2 R／S | B ？value |
| 9.3 因 7 ＋／－R／S | L？value |
| 60 R／S | K ？value |
| 4.8 R／S | S？value |
| ［国3 3 ／S | $\mathrm{P}=418,351.2590$ |
| －VIEW R | $R=103,225.8065$ |
| VIEW F | $F=0.0096$ |

## Description：

Prompts for program label．

Specifies program C．
Prompts for the unknown variable．

Starts program C；
prompts for variables except $P$ ．

Displays the pressure drop．
Displays the Reynolds number．

Displays the friction factor．

## Static Equivalent at a Point

This program calculates the two reaction forces necessary to balance any given two-dimensional force vectors, provided the vectors act through the same point. The direction of the reaction forces must be specified as an angle relative to an arbitrary axis.


Equations:

$$
\begin{aligned}
R_{1} \cos \theta_{1}+R_{2} \cos \theta_{2} & =\sum F \cos \phi \\
R_{1} \sin \theta_{1}+R_{2} \sin \theta_{2} & =\sum F \sin \phi
\end{aligned}
$$

where:

$$
\begin{aligned}
& F=\text { magnitude of each known force. } \\
& \phi=\text { direction of each known force. } \\
& R_{1}=\text { first reaction force. } \\
& \theta_{1}=\text { direction of } R_{1} . \\
& R_{2}=\text { second reaction force. } \\
& \theta_{2}=\text { direction of } R_{2} .
\end{aligned}
$$

## Program Listing.

| S01 LEL 5 | Fis IHFIUT E |
| :---: | :---: |
| 5 SGE CLVARS | H19 Sill |
| S日S IHFUT H | Heg sto m |
| Checksum $=0090$ | Hel LFETe |
| H61 LEL A | H2e dos |
| Hag IHFUT T | Hes sto d |
| H0] INFIUT F | He4 FCL ${ }^{\text {P }}$ |
| H64 FCL T | H25 RCL\% E |
| H06. FCL F | HEG ROL D |
|  | HET RCLX Y |
| H6] STO+ X | H2e |
| H6S x》y | Heg mil h |
| H69 STO+ Y | H30 RCLX |
| F16 DEE H | H31 REL C |
| H11 GTO A | HSE RCL\% E |
| H12 IHFIUT H | H3E |
| H1S SIH | H34 |
| H14 STO A | H35 ST0 R |
| H15 LAST\% | HEG VIEN R |
| H16 006 | her Lfete |
| A17 STO C | HES FCL C |


| H39 | FELX＇$~$＇ |
| :---: | :---: |
| F41 | FLLX H |
| H 42 | － |
| H 43 | ＜ |

```
H44 %
H45 STO F:
H4G YIEN R
H47 RTH
ミトににkこコM = EGSに:
```

Flags Used．None．
Memory Required． 75 bytes．

## Remarks．

－This program clears all variables stored in Continuous Memory．
－A positive value of force（tension）points away from the origin；a negative value（compression）points toward the origin．
－Angles must be consistent with the angular mode currently set in the calculator．

## Program Instructions．

1．Key in the program listing；press $C$ when finished．
2．Press XEQ S．
3．Key in the variables at each prompt and press R／S ．
4．See the first reaction force，then press $R / S$ ．
5．See the second reaction force．
6．For a new case，go to step 2 ．

## Variables Used．

$N=$ number of known forces．
$T=$ angle of each known force．
$F=$ value of each known force．
$A=$ direction of the first reaction force．
$B=$ direction of the second reaction force．
$R=$ value of the unknown forces $R_{1}$ and $R_{2}$ ．
$D, X, Y, C=$ variables used for intermediate results．

Example 1: Balancing a Single Vector. Find the reaction forces in the following diagram:


Keys:
XEQ S
1 R/S
135 R/S
75 R/S
30 R/S
270 R/S

R/S

Display:
N?0.0000
T? 0.0000
F? 0.0000
A? 0.0000
B? 0.0000
$\mathrm{R}=61.2372$
$R=83.6516$

Description:

Example 2: Forces in a Bridge Truss. Find the reaction forces in structural members AE and CE. Assume pin connections at the joint.


Keys:
XEQ S
2 R/S
45 R/S
100 R/S
180 R/S
120 R/S
R/S
135 R/S
R/S

Display:
N?0.0000
T? 0.0000
F? 0.0000
T? 45.0000
F? 100.0000
A? 0.0000
B? 0.0000
$R=-21.4214$
$R=-100.0000$

Description:

Inputs known values.

Displays the first reaction force.
Displays the second reaction force.

## Composite Section Properties

The mechanical properties of a constant cross section member composed of a finite number of rectangular elements can be computed by adding the contribution of each rectangular region individually. This program uses this principle to calculate the area of a section, the moments of inertia about the specified set of axes, the moments of inertia about an axis translated to the centroid, the moments of inertia of the principal axes, and the angle of rotation between the translated axes and the principal axes.

$$
\begin{gathered}
A_{s i}=\Delta x_{i} \Delta y_{i} \\
A=A_{s 1}+A_{s 2}+A_{s 3}+\cdots+A_{s n} \\
\bar{x}=\frac{\sum_{i=1}^{n} x_{0 i} A_{s i}}{A} \\
\bar{y}=\frac{\sum_{i=1}^{n} y_{0 i} A_{s i}}{A} \\
I_{x y}=\sum_{i=1}^{n} x_{0 i} y_{0 i} A_{s i} \quad \sum_{\bar{x} \bar{y}}^{n}=I_{x y}-A \bar{x} \bar{y} \\
\left.I_{y}=\sum_{i=1}^{n}\left(y_{0 i}^{2}+\frac{\Delta y_{i}^{2}}{12}\right) A_{s i}=I_{x}-A \bar{y}^{2}+\frac{\Delta x_{i}^{2}}{12}\right) A_{s i} \\
J=I_{x}+I_{y} \\
I_{\bar{y}}=I_{y}-A \bar{x}^{2} \\
\phi=\frac{1}{2} \tan ^{-1}\left(\frac{2 I_{\bar{x} \bar{y}}}{I_{\bar{x}}-I_{\bar{y}}}\right) \\
I_{\bar{x} \phi}=I_{\bar{x}} \cos ^{2} \phi+I_{\bar{y}} \sin ^{2} \phi+I_{\bar{x} \bar{y}} \sin 2 \phi \\
I_{\bar{y} \phi}=I_{\bar{y}} \cos ^{2} \phi+I_{\bar{x}} \sin ^{2} \phi+I_{\bar{x} \bar{y}} \sin 2 \phi \\
J_{\phi}=I_{\bar{x} \phi}+I_{\bar{y} \phi}
\end{gathered}
$$

where:
$\Delta x_{i}=$ width of a rectangular element.
$\Delta y_{i}=$ height of a rectangular element.
$A_{s i}=$ area of an element.
$A=$ total area of the section.
$\bar{x}=x$-coordinate of the centroid.
$\bar{y}=y$-coordinate of the centroid.
$x_{0 i}=x$-coordinate of the centroid.
$y_{0 i}=y$-coordinate of the centroid.
$I_{x}=$ moment of inertia about the x-axis.
$I_{y}=$ moment of inertia about the y -axis.
$J=$ polar moment of inertia about the origin.
$I_{x y}=$ product of inertia about the origin.
$I_{\bar{x}}=$ moment of inertia about the x-axis translated to the centroid.
$I_{\bar{y}}=$ moment of inertia about the y -axis translated to the centroid.
$I_{\overline{x y}}=$ product of inertia about the translated axis.
$\phi=$ angle between the translated axis and the principal axis.
$I_{\bar{x} \phi}=$ moment of inertia about the principal x -axis.
$I_{\bar{y} \phi}=$ moment of inertia about the principal y -axis.
$J_{\phi}=$ polar moment of inertia about the principal axis.

## Program Listing．

| SQ1 LEL S | 134 FLL $\%$ |
| :---: | :---: |
| SES ELWHFS | 13S FOL \％Y |
| S63 IHFIIT H | UBE FLL E |
|  | U37 ST0＋F |
| UQ1 LEL II | USE［SE H |
| 162 IHFUT $\%$ | 139 GTO |
| U⿴囗 IFIFITT $Y$ | 140 FiL F |
| 104 IHFIIT 3 | 1141 FCL C |
| 1105 IHFIIT T | U4E FELX 0 |
| 10G FCLX | 1143 FCL $\div \mathrm{F}$ |
| 1107 STO E | 1144－ |
| 109 STI＋ A | $11459 T 0$ |
| 169 FCL $<1$ | 146 ECL C |
| U1E ETO＋ | U47 FEL $\div \mathrm{F}$ |
| U11 FEL $X$ | U4G UIEN H |
| U12 FEL E | 1149 STO |
| U13 STO＋区 | 15G 9 IEN 8 |
| U14 FEL＇$Y$ | $151>2$ |
| 115 2 | 15 FLL |
| U1E FLL T | $15 \mathrm{FCL} \div \mathrm{F}$ |
| U17 | 154 STO $\because$ |
| 111812 | 155 UIEM $\gamma$ |
| $119 \div$ | U56 |
| 120＋ | $157 \mathrm{FLCL} \times \mathrm{H}$ |
| Uこ1 FCL E | $158+$ |
| いこと STO＋H | $159 \mathrm{ELL} H$ |
| Uご FOL $\%$ | UEG YIEN H |
| 124 $\times 2$ | 161＋ |
| UES FCL 3 | UE2 STOH |
| ШЕ6 2 | 163 F |
| いご 12 | UE4 FEL H |
| 128 $\div$ | 1165＋－ |
| $129+$ | DEG FIL I |
| U36 FCL\％E | BGT UIEN I |
| U31 ETI＋I | DES UIEN－ |
| 132＋ | 169 WIEN F |
| U3S STO＋． | 118＋ |


| 1171 STOI | WG1 LEL $\psi$ |
| :---: | :---: |
| UFE FOL H | WGこ STO |
| リア3 ST0－ | WG3 YIEN G |
| 1174 UIEN H | W64 2 |
| UP5－－¢ | W65 $\times$ |
| \TE UIEH I | WGE SIH |
| $1177 \quad$ ETOT | WG7 FCLC F |
| 178－ | W6E＋－ |
| 179 STD D | WEG FEL G |
| 1EG FEL 0 | Y10 SIH |
| UE1 STO F | V11 |
| UB2 UIEN $F$ | V12 FCLX ${ }^{\text {d }}$ |
| 188 － 10 | V13－ |
| UE4 LTO 4 | V14 FCL +H |
| $185 \div$ | W15 STOH |
| U86 1\％ | V1G WIENH |
| 1187 | W17 FOL－－ |
| $188 \times$ | V18＋－ |
| 1189 HTAH | U19 STOI |
| 1962 | W2Q UIEN I |
| $1191 \div$ | W21 UIEサ－ |
| 192＋－ | W2e RTH |
| EREにkEum $=$ F4E6 | Chににくこum $=68 \mathrm{ET}$ |

Flags Used．None．
Memory Required． 175.5 bytes．

## Remarks．

－This program clears all variables stored in Continuous Memory．
－For a given origin，the polar moment of inertia is constant regardless of the angular rotation．Therefore，$J_{\overline{x y}}$ is equal to $J_{\phi}$ ．
－It is possible to obtain a negative value for the product of inertia．

## Program Instructions.

1. Key in the program listing; press $C$ when done.
2. Press XEQ S.
3. Key in the variables at each prompt and press $R / S$.
4. See the results as they are displayed and press $R / S$.
5. For a new case, go to step 2 .

## Variables Used.

$X=x_{0 i}$ and $\bar{x}$.
$Y=y_{0 i}$ and $\bar{y}$.
$S=\Delta x_{i}$.
$T=\Delta y_{i}$.
$H=I_{x}, I_{\bar{x}}$, and $I_{\bar{x} \phi}$.
$I=I_{y}, I_{\bar{y}}$, and $I_{\bar{y} \phi}$.
$J=J$ and $J_{\phi}$.
$P=I_{x y}, I_{\overline{x y}}$.
$A=$ total area of the entire section.
$G=$ angle between the translated axis and the principal axis.
$N=$ number of sections.
$D, C, B, Q=$ variables used for intermediate results.
Example 1: Rectangular Section. Calculate the section properties of the following cross section:


## Table of Inputs

| x | y | $\Delta \mathrm{x}$ | $\Delta \mathrm{y}$ |
| :---: | :---: | :---: | :---: |
| 2 | 1.5 | 4 | 3 |

## Keys:

XEQ S
1 R/S
2 R/S
$1.5 \mathrm{R} / \mathrm{S}$
4 R/S
3 R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S

Display:
N?0.0000
X?0.0000
Y?0.0000
S?0.0000
T? 0.0000
$A=12.0000$
$X=2.0000$
$Y=1.5000$
$H=36.0000$
$\mathrm{I}=64.0000$
$J=100.0000$
$\mathrm{P}=36.0000$
$\mathrm{H}=9.0000$
$\mathrm{I}=16.0000$
$\mathrm{P}=0.0000$
$\mathrm{G}=0.0000$
$H=9.0000$
$I=16.0000$
$J=25.0000$

## Description:

Inputs known values.

Displays area.
Displays $\bar{x}$.
Displays $\bar{y}$.
Displays $I_{x}$.
Displays $I_{y}$.
Displays $J$.
Displays $I_{x y}$.
Displays $I_{\bar{x}}$.
Displays $I_{\bar{y}}$.
Displays $I_{\overline{x y}}$.
Displays $\phi$.
Displays $I_{\bar{x} \phi}$.
Displays $I_{\bar{x} \phi}$.
Displays $J_{\phi}$.

Example 2: Composite Section. Calculate the section properties of the following section:


## Table of Inputs

|  | x | y | $\Delta \mathrm{x}$ | $\Delta \mathrm{y}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 5 | 11.5 | 6 | 1 |
| 2 | 1 | 6 | 2 | 12 |
| 3 | 7 | 1 | 10 | 2 |

## Keys:

XEQ S
3 R/S
5 R/S
11.5 R/S

6 R/S
1 R/S
1 R/S
6 R/S
2 R/S
12 R/S
7 R/S
1 R/S
10 R/S
2 R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
R/S
$R / S$
R/S

Display:
N?0.0000
X? 0.0000
Y? 0.0000
S? 0.0000
T?0.0000
X?5.0000
Y?11.5000
S? 6.0000
T? 1.0000
X? 1.0000
Y? 6.0000
S?2.0000
T? 12.0000
$A=50.0000$
$X=3.8800$
$Y=4.6600$
$\mathrm{H}=1,972.6667$
$\mathrm{I}=1,346.6667$
$\mathrm{J}=3,319.3333$
$\mathrm{P}=629.0000$
$\mathrm{H}=886.8867$
I=593.9467
$\mathrm{P}=-275.0400$
$\mathrm{G}=30.9814$
$H=1,052.0261$
I = 428.8072
$\mathrm{J}=1,480.8333$

Inputs known values.
Description:

Displays area.
Displays $\bar{x}$.
Displays $\bar{y}$.
Displays $I_{x}$.
Displays $I_{y}$.
Displays $J$.
Displays $I_{x y}$.
Displays $I_{\bar{x}}$.
Displays $I_{\bar{y}}$.
Displays $I_{\overline{x y}}$.
Displays $\phi$.
Displays $I_{\bar{x} \phi}$.
Displays $I_{\bar{x} \phi}$.
Displays $J_{\phi}$.

## Soderberg's Equation for Fatigue

This program calculates any one of the six variables in Soderberg's equation for fatigue when the other five are known. Soderberg's equation is shown graphically in the figure below.


Equation:

$$
\frac{s_{y p}}{F S}=\frac{s_{\max }+s_{\min }}{2}+K\left(\frac{s_{y p}}{s_{e}}\right)\left(\frac{s_{\max }-s_{\min }}{2}\right)
$$

where:
$s_{y p}=$ yield point stress.
$s_{e}=$ endurance stress from reversed bending tests.
$s_{\text {max }}=$ maximum applied stress.
$s_{\text {min }}=$ minimum applied stress.
$K=$ stress concentration factor ．
$F S=$ factor of safety．

## Program Listing．

501 LEL 5
S02 IHFIIT Y
503 IHFIIT E
604 IHFUT $A$
505 IHFUT E
SEG IHFUT K
S07 IHFIIT F
SGS FEL＇$'$
$569 \mathrm{FCL} \div \mathrm{F}$
S1E FEL A
$511 \mathrm{FCL}+\mathrm{E}$
5122
$513 \div$
514－
515 FCL A
S16 FCL－E
$S 172$
S18 $\div$
319 FCLX $\gamma$
E2G FCL $\div$ E
521 FCLX K
S22－
523 FTH
Chににkシum＝ C 95 D

Flags Used．None．
Memory Required． 34.5 bytes．

## Remarks．

－Soderberg＇s equation is valid for ductile materials only．
－Fatigue effects are magnified in corrosive environments．

## Program Instructions．

1．Key in the program listing，pressing $C$ when finished．
2．Press SOLVE／S \｛FH\} S, then specify the unknown variable by pressing SOLVE／S \｛GOLVE $\}$ variable．
3．Key in the variables at each prompt and press $R / S$ ．
4．See the variable for which the program is solving．
5．For a new case，go to step 2.

## Variables Used.

$Y=$ yield point stress.
$E=$ endurance stress.
$A=$ maximum applied stress.
$B=$ minimum applied stress.
$K=$ stress concentration factor.
$F=$ factor of safety.

Example. What is the maximum allowable applied stress if the minimum applied stress is 15,000 psi?

$$
\begin{aligned}
& s_{y p}=80,000 \mathrm{psi} . \\
& s_{e}=30,000 \mathrm{psi} . \\
& K=1.5 . \\
& F S=2.0 .
\end{aligned}
$$

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| - SOLVE/S \{FH\} | $\mathrm{FN}=$ | Prompts for program label. |
| S | value | Specifies program S. |
| $\begin{aligned} & \text { SOLVE/S } \\ & \{S O L V E\} \end{aligned}$ | SOLVE | Prompts for the unknown variable. |
| A | Y?value | Starts program S; |
| 80000 R/S | E?value | prompts for variables |
| 30000 R/S | B?value | except $A$. |
| 15000 R/S | K ? value |  |
| 1.5 R/S | F?value |  |
| $2 \mathrm{R} / \mathrm{S}$ | $\mathrm{A}=25,000.0000$ | Displays the maximum applied stress. |

3

## Civil Engineering

## Mohr's Circle for Stress

This program calculates the 2-D Mohr's circle for stress from equiangular or rectangular strain gage data or directly from known stresses.

| Configuration <br> Code | Rectangular | 2 |
| :--- | :---: | :---: |
| Type of Rosette | Delta (Equiangular) |  |
|  |  |  |



$$
\begin{gathered}
\tau_{\max }=\left[\left(\frac{S_{x}-S_{y}}{2}\right)^{2}+\tau_{x y}^{2}\right]^{\frac{1}{2}} \\
S_{1}=\frac{S_{x}+S_{y}}{2}+\tau_{\max } \\
S_{2}=\frac{S_{x}+S_{y}}{2}-\tau_{\max } \\
\theta=\frac{1}{2} \tan ^{-1}\left(\frac{2 \tau_{x y}}{S_{x}-S_{y}}\right) \\
S=\frac{S_{1}+S_{2}}{2}+\tau_{\max } \cos 2 \theta^{\prime} \\
\tau=\tau_{\max } \sin 2 \theta^{\prime}
\end{gathered}
$$

## Program Listing．

IG1 LEL I
IGE IHFUT E
I $6=$ IHFUTT $G$
IE4 IHFIIT A
I65 IHFUT E
IGE IHFUT E：
IG7 FEL E
IGG 1
IG9 FCL－
I1日 $\div$
I11 STG ，
I12 EL L E
I 131
I14 $\mathrm{FCL}+\mathrm{Q}$
I15 $\div$
I16 STO
I17 FEL H
I1s FEL E
I19 FEL
Iこ日 FTH
「トにににこ」ル＝9144
FE1 LEL F：
FQ2 KEO I
$\mathrm{FG} \mathrm{FCL}+\mathrm{H}$
F04 2
F65－
FEG FOL－E
FET FCL E：
FQS RCL H
F69 GTO M

EG1 LEL E
EG2 XEO I
E03－
E64 3
EQ5 GORT
EGE：

EGT FCL E
EGG FOL＋I
E69 2
E19 $\times$
E11 FEL－ H
E12 3
E13 $\div$
E14 FCL $A$
E15 GTO
EREにKこムM＝BHEG
G区1 LEL
E区E IHFUT S
S63 IHFUIT $\because$
G区4 IHFIIT \％
E6 1
GQE STO ，
SGT STO F
GQE FUL G
Eg＋－
G1区 FEL＇$'$
$S 11$ FLL $X$

HE1 LEL 1
ME ETOL

M04 2
10．5 $\div$
MEG STOK－
MET FOL－L
MES FES

川16 STO\％ F
M11 シ्ञ
サ12 2
$113 \div$
M14 ETD
M15 FCL E

| M1G FLL + － | M29 SIH |
| :---: | :---: |
| M17 STG | MBE LAST天 |
| M18 UIEM い | HS1 E0S |
| M19 FCL | 132 FL （\％ F |
| M2G FCL－ F | $13 \mathrm{ECL}+\ldots$ |
| Mご STOL | 184 ST0 ${ }^{1}$ |
| Mこと UIEN L | HS5 UIEN F |
| M23 YIEM F | M36 Ft |
| M24 UIEN G | M37 FLCL E |
| MES IHFIIT W | H3E STOT |
| MEG FOLC G | HE9 YIEA T |
| M27 2 | M40 ETH |
| Mzs $\times$ | ChEにくこ」m $=$ |

Flags Used．None．
Memory Required． 142.5 bytes．

## Remarks．

－Tensile forces are considered positive，compressive stresses negative．
－This program calculates the principal stresses for a two dimensional stress state only．A knowledge of the stresses in the $z$－direction is necessary to determine the overall maximum and minimum stresses．
－Angles must be consistent with the angular mode currently set in the calculator．

## Program Instructions．

1．Key in the program listings of the routines to be used；press $C$ when finished．

2．Select the appropriate routine：
－Press XEQ $E$ if equiangular strain gage readings are known．
－Press XEQ $R$ if rectangular strain gage readings are known．
－Press XEQ $S$ if stresses are known directly．
3．Key in the variables at each prompt and press R／S．
4．See each result as it＇s displayed．Press R／S to display the next one．
5．Optional：At the prompt，key in rotation angle $W$ and press $R / \mathrm{S}$ to obtain the normal stress at that orientation；press $R / S$ again to see the shear stress．

## Variables Used.

$A=\varepsilon_{0}$.
$B=\varepsilon_{45}$ or $\varepsilon_{60}$.
$C=\varepsilon_{90}$ or $\varepsilon_{120}$.
$E=$ Young's modulus.
$V=$ Poisson's ratio.
$X=$ normal stress on the $x$-face, $\sigma_{x}$.
$Y=$ normal stress on the $y$-face, $\sigma_{y}$.
$S=$ shear stress, $\tau_{x y}$.
$U=$ maximum principal stress, $\sigma_{1}$.
$L=$ minimum principal stress, $\sigma_{2}$.
$R=$ maximum shear stress, $\tau_{\text {max }}$.
$G=$ clockwise angle from the specified $x$-axis to the maximum principal axis.
$W=$ arbitrary angle counterclockwise from the specified $x$-axis, $\beta$.
$P=$ normal stress at angle $\beta$.
$T=$ shear stress at angle $\beta$.
$J=$ variable used for intermediate results.

Example 1：Equiangular Strain Gage．An equiangular rosette strain gage measures the following strains：

$$
\begin{aligned}
& \varepsilon_{0}=180 \mu . \\
& \varepsilon_{60}=200 \mu . \\
& \varepsilon_{120}=-290 \mu .
\end{aligned}
$$

Find the principal stresses and their orientation．The material properties are $E=30 \times 10^{6}$ psi and $\nu=0.3$ ．

## Keys：

－MODES \｛DG
$\mathrm{XEQ} \mathrm{E} \quad \mathrm{E}$ ？value

30 因 6 R／S
． 3 R／S
180 因 6 ＋／－ $\mathrm{R} / \mathrm{S}$
200 因 6 ＋R R／S
290 ＋／－国 $6+/ \rightarrow$
R／S
R／S
R／S
R／S

Display：

E ？value

V？value
A？value
B ？value
C？value

$$
\begin{aligned}
& U=8,675.1358 \\
& L=-6,103.7072 \\
& R=7,389.4215 \\
& G=31.0333
\end{aligned}
$$

## Description：

Sets degrees mode．
Begins equiangular rosette routine．

## Inputs strain gage

 readings．Displays $\sigma_{1}$ ．
Displays $\sigma_{2}$ ．
Displays $\tau_{\text {max }}$ ．
Displays $\theta$ ．

Example 2: Known Stresses. The stresses acting on an element are shown below (all stresses are in MPa).


Find the principal stresses and their orientation, and the stresses on the face of the element oriented $45^{\circ}$ counterclockwise from the $x$-axis.

Keys:
XEQ S
30 R/S
20 +/- R/S
75 R/S
R/S
R/S
R/S
R/S
45 R/S
R/S

Display:
S?value
Y?value
X ?value
U = 83.6805
$\mathrm{L}=-28.6805$
$R=56.1805$
$\mathrm{G}=-16.1378$
W?value
$\mathrm{P}=57.5000$
$\mathrm{T}=47.5000$

Description:
Begins stress routine.
Inputs stresses.

Displays $\sigma_{1}$.
Displays $\sigma_{2}$.
Displays $\tau_{\text {max }}$.
Displays $\theta$.
Inputs angle.
Displays $\sigma$.
Displays $\tau$.

## Field Angle Traverse

This program calculates the coordinates of a traverse, the total horizontal distance traversed, and the enclosed area (for a closed traverse). The user must input the northing and easting of the starting point, the reference azimuth, and the direction and distance from each point in the traverse to the next point. The direction may be input either as a deflection right or left or as an angle right or left. The distance may be input either as a horizontal distance or as a slope distance with a zenith angle.

$$
\begin{gathered}
H D=S D \sin (Z A) \\
N_{k+1}=N_{k}+H D \cos (A Z) \\
E_{k+1}=E_{k}+H D \sin (A Z) \\
L A T_{k}=N_{k+1}-N_{k} \\
D E P_{k}=E_{k+1}-E_{k} \\
\text { Area }=\sum_{k=1}^{n} L A T_{k}\left(\frac{1}{2} D E P_{k}+\sum_{j=1}^{k-1} D E P_{j}\right)
\end{gathered}
$$

where:
$N, E=$ northing, easting of a point.
$k=$ a current point.
$n=$ number of points in the survey.
$A Z=$ azimuth of a course.
$H D=$ horizontal distance.
$S D=$ slope distance.
$Z A=$ zenith angle.

## Program Listing．

| FQ1 LEL F | 565 SH |
| :---: | :---: |
| F6E EF 区 | S6e $\times$ |
| F63 ELWHES | SET STOH |
| Fe4 IHFIUT H | S日S EF 日 |
| F65 IHFUTT E | Eheにksum＝505 |
| FEG IHFIIT F | HE1 LEL H |
| $\mathrm{FQT}+\mathrm{HF}$ | HE2 FS？日 |
| FGS 180 | HES IHFUT H |
| FQg ＋ | H04 ETO＋T |
| F1日 ET0 F | HES FLCL $F$ |
| F11 STOF | HEGEF 日 |
| Eちににくこ」m＝1001 |  |
| HQ1 LEL A |  |
| Heg IHFUT H | H09 ETO＋H |
| H6S +HF | H19 $\quad$－ |
| H04 186 | H11 STO＋E |
| H65＋ | H12 STO 8 |
| HQG STO＋F | H132 |
| H6T STOF | H14 |
| －heにksum＝0137 | H15 FCL +K |
| ［01 LEL D | H1E $\times$ |
| DEE IHFUT D | H17 ETO＋ F |
| ［09 $\rightarrow \mathrm{HF}$ | H1S FCL 8 |
| ［04 ETO＋F | H19 STO＋K |
| ［05 STOF | H2日 UIEN H |
| ChEにkこum＝बき5F | Hこ1 WIEN E |
| EQ1 LEL 5 | H2e UIEN T |
| Exz IHFUT S | HES YIEN F |
| S区S IHFITT 2 | H24 RETH |
| S64 +HF | Ch＠にksum $=\mathrm{ES50}$ |

Flags Used．Flag 0.
Memory Required． 98.5 bytes．

## Remarks.

- This program clears all variables stored in Continuous Memory.
- Right angles and deflections are positive; left angles and deflections are negative.
- This program requires the calculator to be set to degrees mode; angular inputs must be in degrees-minutes-seconds (D.MS) format.
- The program uses zenith angles to calculate the horizontal distance from slope distance. If you are using vertical angles rather than zenith angles, convert the vertical angle to a zenith angle by using:

$$
\text { zenith angle }=90^{\circ}-\text { vertical angle. }
$$

(Remember to convert D.MS input to decimal degrees before subtracting from 90 .)

## Program Instructions.

1. Key in the program listing and press $C$ when finished.
2. Press XEQ $F$.
3. Key in $N$ and press $R / \mathbf{S}$; key in $E$ and press $R / \mathbf{S}$; key in $F$ and press R/S.
4. Select the appropriate routine to input the direction:

- For an angle right or an angle left:
- Press XEQ A.
- Key in $A$.
- If angle left, press $+/-$
- Press R/S.
- For a deflection right or a deflection left:
- Press XEQ D.
- Key in $D$.
- If deflection left, press $+/-$.
- Press R/S .

5. Select the appropriate routine to input the distance:

- For a horizontal distance:
- Press XEQ H .
- Key in $A$ and press R/S.
- See $N$ and press R/S.
- See $E$.
- For a slope distance with zenith angle:
- Press XEQ S.
- Key in $S$ and press R/S.
- Key in $Z$ and press R/S.
- See $N$ and press R/S.
- See $E$.

6. When the final distance and angle have been keyed in, press $R / S$ to see $T$.
7. Press R/S to see $R$.

## Variables Used.

$N=$ the northing of each point.
$E=$ the easting of each point.
$F=$ reference azimuth away from the starting point.
$A=$ angle change of direction.
$D=$ deflection change of direction.
$H$ = horizontal distance.
$S=$ slope distance.
$Z=$ zenith angle.
$T=$ total distance traversed.
$R=$ enclosed area.
$X, K=$ variables used for intermediate results.

Example: Field Angle Traverse. Find the coordinates of each point, the total distance, and the area enclosed for the following field:


## Keys:

MODES \{DG
XEQ F
150 R/S
400 R/S
311.3955 R/S

XEQ $A$
113.3455 R/S

XEQ H
177.966 R/S

R/S
XEQ D
100.2455 +/- R/S

XEQ S
161.88 R/S
86.0139 R/S

R/S
XEQ $A$
87.3559 R/S

XEQ H
203.69 R/S

R/S
XEQ D
100.4559 +/- R/S

XEQ H
124 R/S
R/S
R/S
R/S

## Display:

N?0.0000
E? 0.0000
F? 0.0000
491.6653

A? 0.0000
293.5819

H?0.0000
$\mathrm{N}=224.5150$
$\mathrm{E}=561.6150$
D?0.0000

- 100.4153

S? 0.0000
Z?0.000
$\mathrm{N}=356.5285 \quad$ Displays $N_{3}$.
$\mathrm{E}=468.5999 \quad$ Displays $E_{3}$.
A? 113.3455
267.5997

H?161.4911
$\mathrm{N}=232.3373 \quad$ Displays $N_{4}$.
$E=307.1498$
D? - 100.2455

- 100.7664

H?203.6900
$\mathrm{N}=149.9048 \quad$ Displays $N_{1}$.
$\mathrm{E}=399.7829 \quad$ Displays $E_{1}$.
$T=667.1471 \quad$ Displays total distance.
$R=26,558.8326 \quad$ Displays area.

## Description:

Sets degrees mode.

Inputs starting point data.

Displays $N_{2}$.
Displays $E_{2}$.

Displays $E_{4}$.

## 4

## Statistics

## t Statistics

This program performs t statistics calculations for either paired statistics or for two means.

## Paired t Statistics

Given a set of paired observations from two normal populations with unknown means $\mu_{1}$ and $\mu_{2}$ :

| $x_{i}$ | $x_{1}$ | $x_{2} \cdots x_{n}$ |
| :--- | :--- | :--- |
| $y_{i}$ | $y_{1}$ | $y_{2} \cdots y_{n}$ |

let:

$$
\begin{gathered}
D_{i}=x_{i}-y_{i} \\
\bar{D}=\frac{1}{n} \sum_{i=1}^{n} D_{i} \\
s_{D}=\left[\frac{\Sigma D_{i}^{2}-\frac{1}{n}\left(\Sigma D_{i}\right)^{2}}{n-1}\right]^{\frac{1}{2}}
\end{gathered}
$$

The test statistic

$$
t=\frac{\bar{D}}{s_{D}} \sqrt{n}
$$

has $n-1$ degrees of freedom ( $d f$ ) and can be used to test the null hypothesis $H_{0}: \mu_{1}=\mu_{2}$.

## t Statistic for Two Means

Suppose $\left\{x_{1}, x_{2}, \ldots, x_{n_{1}}\right\}$ and $\left\{y_{1}, y_{2}, \ldots, y_{n_{2}}\right\}$ are independent random samples from two normal populations having means $\mu_{1}$ and $\mu_{2}$ (unknown) and the same unknown variance $\sigma^{2}$.

To test the null hypothesis $H_{0}: \mu_{1}-\mu_{2}=d$, where $d$ is a given number, use the following equations:

$$
\begin{gathered}
\bar{x}=\frac{1}{n_{1}} \sum_{i=1}^{n_{1}} x_{i} \\
\bar{y}=\frac{1}{n_{2}} \sum_{i=1}^{n_{2}} y_{i} \\
{\left[\left(\frac{1}{n_{1}}+\frac{1}{n_{2}}\right)\left(\frac{\Sigma x_{i}^{2}-n_{1} \bar{x}^{2}+\Sigma y_{i}^{2}-n_{2} \bar{y}^{2}}{n_{1}+n_{2}-2}\right]\right]^{\frac{1}{2}}}
\end{gathered}
$$

You can use this t statistic, which has the t distribution with $n_{1}+n_{2}-2$ degrees of freedom (df), to test the null hypothesis $H_{0}$.

## Program Listing．

FG1 LEL F
FGE CLE
FGG IHFIIT H
Checksum＝FCFE
KG1 LEL K
KGE IHFIIT X
KGE IHFIIT $Y$
KG4 ROL X
K0．RCL－$Y$
KGE B＋
KG7 DSE H
K日G GTOK

K16 STo 0
$k 11 \equiv \%$
k 12 STO 5
K13－
K14
K 15 SQRT
k16 $\times$
K 17 ETO T
k18 ก
K19 1
K2－
K21 ST0 F
Ke VIEN D
Kes पIENS
K24 VIEN T
Ke5 UIEN F
KeE RTH
Cherksum＝16ET
TE1 LEL T
TGe IHFIJT H
TGS CLE
TG4 sTOF
T0．5 x
TGE STO A

TV7 8 sez
TQG STO E
TQ9
T1日 STO
T11 CLE
Tiz STOF
T13
T14 5T0．
T15 $\mathrm{x} \mathrm{x}^{2}$
T1E STOK
T17
T13 ETOL
T19 RCL E
Teg ROL A
TE1 x 2
Te2 FCLX C
T23－
Te4 $\mathrm{FCL}+\mathrm{K}$
Te5 RCL
TEE $x^{2}$
TEて RCLX L
Tes－
Te9 ROL C
TEU RCL＋L
$\mathrm{T} \geqslant 12$
TS2－
TSS STO F
$T \geqslant 4 \div$
TS5 SORT
TEG 1／x
TET RCL A
TES RCL－J
TSY RCL－H
T4日 x
T41 FOL C
T4E 1．x
T43 RCL L

| T44 12\％ | T49 \％IEN T |
| :---: | :---: |
| T4．5＋ | TS＠UIEN F |
| T4E SQRT | TS1 RTH |
| T47 $\div$ | Chににくこum |
| T4S ETO T |  |

Flags Used．None．
Memory Required． 120 bytes．

## Remarks．

－This program clears all statistical data stored in Continuous Memory．
－The two routines are independent of each other．

## Program Instructions．

1．Key in the programs to be used；press $C$ when finished．
2．For paired $t$ statistics：
－Press XEQ P．
－Key in $N$ and press R／S．
－Key in each $X$ and press R／S ；key in the corresponding $Y$ and press R／S．
－See the results as they are displayed．Press R／S to display the next result．

3．For t statistics of two means：
－Press XEQ T．
－Key in $H$ and press R／S．
－Key in each $x$－value and press $\Sigma+$
－When all of the $x$－values have been entered，press R／S．
－Key in each $y$－value and press $\Sigma+$ ．
■ When all of the $y$－values have been entered，press R／S to calculate the test statistic $T$ ．
$\square$ Press R／S to calculate the degrees of freedom．

## Variables Used.

$X=x$-value of a pair of observations.
$Y=y$-value of a pair of observations.
$N=$ number of paired values.
$D=$ average difference, $\bar{D}$.
$S=$ standard deviation, $s_{D}$.
$F=$ number of degrees of freedom, $d f$.
$H=$ null hypothesis difference, $d$.
$T=$ test statistic.
$A, B, C, J, K, L=$ variables used for intermediate results.

Example 1: Paired Observations. Calculate the test statistic and degrees of freedom of the following data pairs for the null hypothesis $H_{0}: \mu_{1}=\mu_{2}$.

| $\mathbf{x}$ | 15 | 16.9 | 15.3 | 17 | 19.1 | 15.3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | 18 | 19.3 | 17 | 20.3 | 19.7 | 18 |

Keys: Display: Description:

| XEQ P | N ? value |  |
| :---: | :---: | :---: |
| 6 R/S | X ? value | Inputs values. |
| $15 \mathrm{R} / \mathrm{S}$ | Y?value |  |
| 18 R/S | X? 15.0000 |  |
| 16.9 R/S | Y?18.0000 |  |
| 19.3 R/S | X?16.9000 |  |
| 15.3 R/S | Y? 19.3000 |  |
| 17 R/S | X? 15.3000 |  |
| 17 R/S | Y?17.0000 |  |
| 20.3 R/S | X?17.0000 |  |
| 19.1 R/S | Y?20.3000 |  |
| 19.7 R/S | X? 19.1000 |  |

$15.3 \mathrm{R} / \mathrm{S}$
Y?19.7000
18 R/S
R/S
R/S
$D=-2.2833$
Displays $\bar{D}$.
$\mathrm{S}=0.9908$
Displays $s_{D}$.
R/S
$T=-5.6450$
Displays $t$.
Displays $d f$.

Example 2: Two Means. Calculate the test statistic and degrees of freedom of the following data for the null hypothesis $H_{0}: \mu_{1}=\mu_{2}$.

| $\mathbf{x}$ | 86 | 109 | 112 | 91 | 103 | 121 | 107 | 100 | 97 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{y}$ | 93 | 101 | 111 | 117 | 105 | 97 | 99 |  |  |


| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| XEQ T | H ? value |  |
| 0 R/S | 0.0000 |  |
| 86 E+ | 1.0000 | Inputs $x$-values. |
| 109 E+ | 2.0000 |  |
| 112 E+ | 3.0000 |  |
| 91 E+ | 4.0000 |  |
| 103 E+ | 5.0000 |  |
| 121 E+ | 6.0000 |  |
| 107 [ E + | 7.0000 |  |
| 100 [ + | 8.0000 |  |
| 97 [ $2+$ | 9.0000 |  |
| R/S | 9.0000 |  |
| 93 E+ | 1.0000 | Inputs $y$-values. |
| 101 E+ | 2.0000 |  |
| 111 E+ | 3.0000 |  |
| 117 E+ | 4.0000 |  |
| 105 E+ | 5.0000 |  |
| 97 [ $2+$ | 6.0000 |  |
| 99 [ t | 7.0000 |  |
| R/S | $\mathrm{T}=-0.0801$ | Displays $t$. |
| R/S | $\mathrm{F}=14.0000$ | Displays $d f$. |

## Chi-Square Evaluation

This program calculates the value of the $\chi^{2}$ statistic for the goodness of fit test using the equation:

$$
\chi^{2}=\sum_{i=1}^{n} \frac{\left(O_{i}-E_{i}\right)^{2}}{E_{i}} \quad(d f=n-1)
$$

where:

$$
\begin{aligned}
& O_{i}=\text { the observed frequency } \\
& E_{i}=\text { the expected frequency. }
\end{aligned}
$$

If the expected values are equal:

$$
E=E_{i}=\frac{\Sigma O_{i}}{n} \text { for all } i
$$

then:

$$
\chi^{2}=\frac{n \Sigma O_{i}^{2}}{\Sigma O_{i}}-\Sigma O_{i}
$$

## Program Listing.

| U61 LEL U | D11 UIEN C |
| :---: | :---: |
| 162 - | D1E RTH |
| 1163 STO C | Checksum $=9890$ |
| U64 IHFIUT H | EQ1 LEL E |
| Checksum $=0.062$ | EGE CLE |
| DG1 LEL D | EGS IHFIUT H |
| DGE IWFUT 0 | Checksum $=22 \mathrm{E}$ |
| DGS IWFIIT E | K01 LEL K |
| 004 RCL | K日E IHFIUT |
| $005 \mathrm{FCL}-\mathrm{E}$ | k0s $\mathrm{E}+$ |
| $066 x^{2}$ | K64 DEE H |
| $0 \mathrm{Ca} 7 \mathrm{ECL} \div \mathrm{E}$ | K0.5 GTO K |
| DGE STO+ C | K6E ${ }^{1}$ |
| 0 dg DSE H | 1098 |
| D19 GTO D | k06 x |



K15
ト1G ETIE
K17 UIEH E
K1S FTH


Flags Used. None.
Memory Required. 55.5 bytes.

## Remarks.

- This program clears all statistical data stored in Continuous Memory.
- The two routines (the unequal case and the equal case) are independent of each other.


## Program Instructions.

1. Key in the program listing; press $C$ when finished.
2. Select the appropriate routine:

- Press XEQ $U$ if the expected values are unequal.
- Press XEQ E if the expected values are equal.

3. Key in the variables at each prompt and press R/S.
4. After all data is input, the $\chi^{2}$ value is calculated and displayed.
5. For a new case, go to step 2 .

## Variables Used.

$O=$ observed frequency.
$E=$ expected frequency.
$C=\chi^{2}$.
$N=$ number of data pairs (unequal case) or values (equal case).

Example 1: Unequal Expected Frequencies. Find the $\chi^{2}$ statistic for the goodness of fit for the following data set:

| Observed | 8 | 50 | 47 | 56 | 5 | 14 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Expected | 9.6 | 46.75 | 51.85 | 54.4 | 8.25 | 9.15 |

## Keys:

Display:
Description:

| XEQ U | N ? value |  |
| :---: | :---: | :---: |
| 6 R/S | O?value | Inputs values |
| 8 R/S | E ? value |  |
| 9.6 R/S | O?8.0000 |  |
| $50 \mathrm{R} / \mathrm{S}$ | E?9.6000 |  |
| 46.75 R/S | O?50.0000 |  |
| 47 R/S | E?46.7500 |  |
| 51.85 R/S | O?47.0000 |  |
| 56 R/S | E?51.8500 |  |
| 54.4 R/S | O?56.0000 |  |
| 5 R/S | E?54.4000 |  |
| 8.25 R/S | O?5.0000 |  |
| $14 \mathrm{R} / \mathrm{S}$ | E?8.2500 |  |
| $9.15 \mathrm{R} / \mathrm{S}$ | $\mathrm{C}=4.8444$ | Displays $\chi^{2}$. |

Example 2: Equal Expected Frequencies. The following table shows the frequencies observed in tossing a die 120 times. $\chi^{2}$ can be used to test if the die is fair $(d f=5)$. Assume that the expected frequencies are equal.

| i | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Observed | 25 | 17 | 15 | 23 | 24 | 16 |


| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| XEQ E | N ? value |  |
| 6 R/S | O?value | Inputs values. |
| $25 \mathrm{R} / \mathrm{S}$ | O?25.0000 |  |
| $17 \mathrm{R} / \mathrm{S}$ | O?17.0000 |  |
| $15 \mathrm{R} / \mathrm{S}$ | O?15.0000 |  |
| 23 R/S | 0?23.0000 |  |
| 24 R/S | O?24.0000 |  |
| 16 R/S | $\mathrm{C}=5.0000$ | Calculates and displays $\chi^{2}$. |

The value of $\chi^{2}$ for $d f=5$ and $5 \%$ significance ${ }^{*}$ is 11.070 . Since 5.00 is less than 11.070 , no statistically significant differences exist between the observed and expected frequencies.

[^0]
## F Distribution

This program evaluates the integral of the F distribution:

$$
Q(x)=\int_{x}^{\infty}\left[\frac{\Gamma\left(\frac{\nu_{1}+\nu_{2}}{2}\right) y^{\frac{\nu_{1}}{2}-1}\left(\frac{\nu_{1}}{\nu_{2}}\right)^{\frac{\nu_{1}}{2}}}{\Gamma\left(\frac{\nu_{1}}{2}\right) \Gamma\left(\frac{\nu_{2}}{2}\right)\left(1+\frac{\nu_{1}}{\nu_{2}} y\right)^{\frac{\nu_{1}+\nu_{2}}{2}}}\right] d y
$$

where $\mathrm{x}>0$ and $\nu_{1}$ and $\nu_{2}$ are the degrees of freedom, provided either $\nu_{1}$ or $\nu_{2}$ is even and both are greater than two.


The following series are used to evaluate the integral．
If $\nu_{1}$ is even：

$$
\begin{aligned}
Q(x)= & t^{\frac{\nu_{2}}{2}}\left[1+\frac{\nu_{2}}{2}(1-t)+\frac{\nu_{2}\left(\nu_{2}+2\right)}{2 \cdot 4}(1-t)^{2}+\cdots\right. \\
& \left.+\frac{\nu_{2}\left(\nu_{2}+2\right) \cdots\left(\nu_{2}+\nu_{1}-4\right)}{2 \cdot 4 \cdots\left(\nu_{1}-2\right)}(1-t)^{\frac{\nu_{1}-2}{2}}\right]
\end{aligned}
$$

If $\nu_{2}$ is even：

$$
\begin{aligned}
Q(x)= & 1-(1-t)^{\frac{\nu_{1}}{2}}\left[1+\frac{\nu_{1}}{2} t+\frac{\nu_{1}\left(\nu_{1}+2\right)}{2 \cdot 4} t^{2}+\cdots\right. \\
& \left.+\frac{\nu_{1}\left(\nu_{1}+2\right) \cdots\left(\nu_{2}+\nu_{1}-4\right)}{2 \cdot 4 \cdots\left(\nu_{2}-2\right)} t^{\frac{\nu_{2}-2}{2}}\right]
\end{aligned}
$$

where：

$$
t=\frac{\nu_{2}}{\nu_{2}+\nu_{1} x}
$$

## Program Listing．

| FQ1 LEL F | E日c EF 日 |
| :---: | :---: |
| FES EF | EGS FCL A |
| FES IHFUTT H | EG4 FCL E |
| Fe4 IHPITT E | EQS ST0 A |
| F6，IHFIIT 8 | EQ6 x＞ |
| FEG FCLX A | EQ7 ST0 E |
| FQ7 FCL +E | E68 1 |
| $\mathrm{FES} \mathrm{FCL} \div \mathrm{E}$ | EG9 FCLL T |
| F99 1 F | E19 ST0 T |
| F1日 STOT | Ehセロk Eum＝こFFE |
| F11 FETH | DE1 LEL 0 |
| Cheにksum＝4069 | D62 9 |
| EQ1 LEL E | D03 STO I |

01041
［G5 STOK
［GE STO H
［日G FCL $A$
0 DE 2
D69－
01日 2
D11 $\div$
［12 STO H
「ちににksum＝9R
F＇G1 LEL $\mathrm{F}^{\prime}$
FGE 1
FGB STO＋I
FQ4 $\mathrm{FCL}-\mathrm{T}$
FGS FCLXK
F曰G 2
FGT RCL I
FQ日
FQ9－
F1G FCL I
F11 1
F12－
F13 2
F14 $x$

F15 FCL $+E$
Fig＊
F17 STOK
Fis STO＋H
F19 FCL H
FCG FCL－I
Fこ1 ※キロ？
Fこe GTO F
FZ FEL E
Fこ4 2
F2S－
FこG FCL T

FCS
Fこg FCLX H
FSG1
FS1 $2 \gg$
FS2 FS？ 9
F33－
FB4 ST0 9
FSS UIEN Q
FBE RTH


## Flags Used．Flag 0.

Memory Required． 103.5 bytes．

## Program Instructions．

1．Key in the program listing；press $C$ when finished．
2．Press XEQ F．
3．Key in the variables as they are prompted for，pressing R／S after each entry．
4．Select the appropriate routine to calculate $Q(x)$ ：
－Press XEQ E if $\nu_{1}$ is odd and $\nu_{2}$ is even．
－Press XEQ D if $\nu_{1}$ is even and $\nu_{2}$ is odd．
－Press XEQ D if both $\nu_{1}$ and $\nu_{2}$ are even．
5．For a new case，go to step 2.

## Variables Used.

$$
\begin{aligned}
& A=\nu_{1} . \\
& B=\nu_{2} . \\
& X=x . \\
& Q=Q(x) .
\end{aligned}
$$

$T, I, K, H, N=$ variables used for intermediate results.

Example 1. Calculate $Q$ (3.92), where $\nu_{1}=9$ and $\nu_{2}=6$.
Keys:
Display:
Description:

XEQ F
$9 R / S$
6 R/S
3.92 R/S

XEQ E

A?value
B ? value
X ?value
0.1453
$\mathrm{Q}=0.0552$
Displays $Q$ (3.92).

Example 2. Calculate $Q$ (1.85), where $\nu_{1}=4$ and $\nu_{2}=16$.

## Keys:

XEQ F
4 R/S
16 R/S
$1.85 \mathrm{~B} / \mathrm{S}$
XEQ D

Display:
A?value
B ?value
X ?value
0.6838
$\mathrm{Q}=0.1687$

## Description:

Inputs values.

Displays $Q(1.85)$.

## Analysis of Variance (One Way)

One way analysis of variance tests the difference between the population means of $k$ treatment groups. Group $i(i=1,2, \ldots, k)$ has $n_{i}$ observations. Treatment groups may have equal or unequal numbers of observations.

$$
\begin{gathered}
\text { Sum }_{i}=\sum \text { of observations in treatment group } i=\sum_{j=1}^{n_{i}} x_{i j} \\
\text { Total } S S=\sum_{i=1}^{k} \sum_{j=1}^{n_{i}} x_{i j}^{2}-\frac{\left(\sum_{i=1}^{k} \sum_{j=1}^{n_{i}} x_{i j}\right)^{2}}{\sum_{i=1}^{k} n_{i}} \\
\text { Treat } S S=\sum_{i=1}^{k}\left[\left(\frac{\left.\sum_{j=1}^{n_{i}} x_{i j}\right)^{2}}{n_{i}}\right]-\frac{\left(\sum_{i=1}^{k} \sum_{j=1}^{n_{i}} x_{i j}\right)^{2}}{\sum_{i=1}^{k} n_{i}}\right. \\
\text { Error } S S=\text { Total } S S-\operatorname{Treat} S S \\
d f_{1}=\operatorname{Treat} d f=k-1 \\
d f_{2}=\text { Error } d f=\sum_{i=1}^{k} n_{i}-k \\
\text { Treat } M S=\frac{\operatorname{Treat} S S}{\operatorname{Treat} d f} \\
\text { Error } M S=\frac{\text { Error } S S}{\text { Error } d f} \\
F=\frac{\text { Treat } M S}{\text { Error } M S} \text { (with } k-1 \text { and } \sum_{i=1}^{k} n_{i}-k \text { degrees of freedom) }
\end{gathered}
$$

## Program Listing.

| F61 LEL A | L2e $\mathrm{x}^{2}$ |
| :---: | :---: |
| Hege Clvirs | L23 RCL +H |
| HES INFIUT K | L24 |
| H64 STO | L25 LfSTx |
| Checksum $=$ E956 | L26 + - |
| L01 LEL L | $\mathrm{L} 27 \mathrm{RCL}+\mathrm{C}$ |
| Las CLx | L28 |
| LG3 CLE | L29 Lrste |
| L64 STOF | L301 |
| L6.5 \% \% | L31 1/\% |
| LGE STO 5 | L3e RCL K |
| LG7 UIENS | LЗ3 1 |
| LGE STO+ H | L34 |
| L69 8\% ${ }^{\text {2 }}$ | LS5 STO D |
| L1日 STO+ E | LSE VIEND |
| L11 $\quad$ ! | L37 |
| Lie STO+ N | Lse RCL H |
| L13 E \% | L39 RCL-K |
| L14 $x^{2}$ | L49 STO D |
| L15 ${ }^{\text {a }}$ | L41 VIEN D |
| L1E | L42 $\times$ |
| L17 STO+ [ | L43 ST0 F |
| Lig DEE - | L44 UIEN F |
| L19 GTO L | L45 ETH |
| Leg FCL E | Checksum $=1443$ |
| Le1 RCL H |  |

Flags Used. None.
Memory Required. 73.5 bytes.
Remarks. This program clears all variables and statistical data stored in Continuous Memory.

## Program Instructions.

1. Key in the program listing; press when finished.
2. Press XEQ A.
3. Key in $K$ (the number of treatment groups) and press $R / S$.
4. Key in each observation and press $\Sigma+$.
5. Press R/S when all of the observations in the treatment group have been entered.
6. See the sum and press R/S .
7. See the treatment degrees of freedom $\left(d f_{1}\right)$ and press $R / S$.
8. See the error degrees of freedom $\left(d f_{2}\right)$ and press $R / \mathbf{S}$.
9. See the F ratio $(F)$.

## Variables Used.

$K=$ number of treatment groups.
$S=$ sum of observations in a treatment group.
$D=d f_{1}$ and $d f_{2}$.
$F=\mathrm{F}$ ratio.
$J, A, B, N, C=$ variables used for intermediate results.

Example. Find $\mathrm{Sum}_{1}, \mathrm{Sum}_{2}, \mathrm{Sum}_{3}, d f_{1}, d f_{2}$, and $F$ for the following:

| $\quad{ }^{j}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 10 | 13 | 12 | 15 | 17 |  |
| $\mathbf{2}$ | 8 | 10 | 12 | 13 | 11 | 9 |
| $\mathbf{3}$ | 8 | 9 | 12 | 7 |  |  |

Keys: Display: Description:

| XEQ $A$ | K?0.0000 | Prompts for number of treatment groups. |
| :---: | :---: | :---: |
| 3 R/S | 0.0000 |  |
| 10 [ E | 1.0000 | Inputs observations in |
| 13 E+ | 2.0000 | first treatment group. |
| 12 [ $\Sigma$ | 3.0000 |  |
| 15 E+ | 4.0000 |  |
| 17 E+ | 5.0000 |  |
| R/S | $S=67.0000$ | Displays $\mathrm{Sum}_{1}$. |
| R/S | 0.0000 | Inputs observations in |
| 8 [ $\quad$ + | 1.0000 | second treatment group |
| 10 Et | 2.0000 |  |
| 12 [ | 3.0000 |  |
| 13 [ $\mathrm{E}+$ | 4.0000 |  |
| $11\left[\begin{array}{l}\text { ¢ }\end{array}\right.$ | 5.0000 |  |
| 9 ¢ | 6.0000 |  |
| R/S | $\mathrm{S}=63.000$ | Displays $\mathrm{Sum}_{2}$. |
| R/S | 0.0000 | Inputs observations in |
| 8 [ E | 1.0000 | third observation group |
| 9 ¢ | 2.0000 |  |
| 12 Et | 3.0000 |  |
| 7 [ + | 4.0000 |  |
| R/S | $\mathrm{S}=36.0000$ | Displays $\mathrm{Sum}_{3}$. |
| R/S | $\mathrm{D}=2.0000$ | Displays $d f_{1}$. |
| R/S | $\mathrm{D}=12.0000$ | Displays $d f_{2}$. |
| R/S | $F=4.5700$ | Displays $F$. |

## Binomial Distribution

This program calculates the probability of a value falling within a specified range of values, that is, the cummulative distribution $\sum_{x=B}^{A} p(x)$, in a binomial distribution. It also calculates the mean, the variance, and the standard deviation of the distribution, and can be used to find the value of each term in the distribution.

$$
p(x)=\binom{n}{x} r^{x}(1-r)^{n-x}
$$

where $x=0,1,2, \ldots$ and $r<1$.

## Program Listing.

| EG1 LEL E | Y12 |
| :---: | :---: |
| EGE Clvars | Y13 LAETx |
| EGS IHFIIT H | Y14 RCL H |
| E064 IHFUT R | Y15 <<> |
| E065 IHFUIT E | Y16 En, |
| EGE IHFIUT A | Y17 F |
|  | Y18 |
| E06 - | Y19 FS? ${ }^{\text {¢ }}$ |
| Ed9 STO+ E | Ye STOF |
| Checksum $=6.651$ | Yel sTO+ F |
| Y日1 LEL Y | Yec ISGE |
| YGe 1 | Yes rio $\%$ |
| YGS RCL- R | Ye4 YIEN F |
| YG4 ROL H | Yes rol H |
| YG5 RCL E | YeG RCLx R |
| Y0e IF | Y27 ST0 M |
| 967 | Yes 1 |
| Y08 $4 \times$ | Ye9 RCL- F |
| Y69 RCL E | Y80 8 |
| Y10 RCL E | Ye1 STO Y |
| Y11 IF | Ye gort |

```
YG STO S
Y4 YIEW M
YS WIEW Y
```

```
YE UIEW S
OF FTH
ロトにににミリM= 2ロ13
```

Flags Used．Flag 0.
Memory Required． 77 bytes．

## Remarks．

－This program clears all variables stored in Continuous Memory．
－The upper and lower limits of the range are inclusive（ $B \leq x \leq A$ ）．If the limits are exclusive or noninteger values，round the lower limit to the next highest integer and the upper limit to the next lowest integer．
－The limits $A$ and $B$ have no effect on the mean，variance， and standard deviation．
－An invalid data error will result if $B<0$ or if $A>n$ ．

## Program Instructions．

1．Key in the program listing；press $C$ when finished．
2．Press XEQ B．
3．Key in the variables at each prompt and press $R / S$ ．
4．Optional：To see each term of the distribution，set flag 0 ；press R／S to continue execution．
5．See each result as it is displayed and press R／S．
6．For a new case，go to step 2 ．

## Variables Used.

$N=$ number of events.
$R=$ probability of the occurrence of a single event.
$A=$ upper limit of the range.
$B=$ lower limit of the range.
$P=$ probability of a value falling in the range.
$M=$ mean.
$V=$ variance.
$S=$ standard deviation.

Example 1. A fair coin $(r=0.5)$ is tossed 10 times. What is the probability that at least seven heads will occur? Find the mean, variance, and standard deviation.

## Keys:

- FLAGS \{DF\} 0

XEQ B
10 R/S
. 5 R/S
7 R/S
10 R/S
R/S
R/S
R/S

Display:
value
N?0.0000
R?0.0000
B? 0.0000
A?0.0000
$\mathrm{P}=0.1719$
$M=5.0000$
$V=2.5000$
$S=1.5811$

## Description:

Clears flag 0 .

Inputs values.

Displays probability.
Displays mean.
Displays variance.
Displays standard deviation.

Example 2. Find the terms of the binomial distribution with $n=5$ and $r=0.75$.

## Keys:

- FLAGS $\{\mathrm{SF}\} 0$ value

XEQ B N?0.0000
5 R/S
.75 R/S
R/S
5 R/S
R/S
R/S
R/S
R/S
R/S

## Display:

R?0.0000
B? 0.0000
A? 0.0000
0.0010
0.0146
0.0879
0.2637
0.3955
0.2373

## Description:

Sets flag to display each term of distribution.

Inputs values.

Displays $p(0)$.
Displays $p$ (1).
Displays $p$ (2).
Displays $p$ (3).
Displays $p$ (4).
Displays $p$ (5).

## Poisson Distribution

This program calculates the probability of a value falling within a specified range of values，that is，the cummulative distribution $\sum_{x=B}^{A} p(x)$ ，in a Poisson distribution．It also calculates the mean，the variance，and the standard deviation of the distribution，and can be used to find the value of each term in the distribution．

$$
p(x)=\frac{e^{-\lambda} \lambda^{x}}{x!}
$$

where $x=0,1,2, \ldots$ and $\lambda>0$

## Program Listing．

FQ1 LEL F
FGE CLVARS
FGS IHFIIT L
FO4 IHFIIT E
FG．IHFIIT A
FGE 1， 106
PG7 $\div$
FQS STO＋E
Checksum＝日edg
801 LEL 8
8Ge RCL L
803 RCL E
KO 4 IF
人0．5 日＊
XGE LfETs
8072 ！
x68 $\div$
$809 \mathrm{FCL} L$
$816+-$
$811 e^{2}$
x12 $\times$
X13 FS？ 6
$\times 14$ STOF
815 STO＋F
x16 ISG E
X17 GTO 8
X1E VIEN F
819 FCL L
xeg STOM
x 2 sTo V
xe2 gort
xes STO 5
K24 VIEN M
X25 UIEN $V$
x2G VIEN 5
8 CO RTH
ChE日k Eum＝E9ER

Flags Used. Flag 0.
Memory Required. 60.5 bytes.

## Remarks.

- This program clears all variables stored in Continuous Memory.
- The upper and lower limits of the range are inclusive $(B \leq x \leq A)$. If the limits are exclusive or noninteger values, round the lower limit to the next highest integer and the upper limit to the next lowest integer.
- The limits $A$ and $B$ have no effect on the mean, variance, and standard deviation. $A$ must be $\leq 999, B$ must be $\geq 0$.


## Program Instructions.

1. Key in the program listing; press $C$ when finished.
2. Press XEQ P.
3. Key in the variables at each prompt and press R/S .
4. Optional: To see each term of the distribution, set flag 0 ; press R/S to continue execution.
5. See each result as it is displayed and press $R / S$.
6. For a new case, go to step 2.

## Variables Used.

$$
L=\lambda .
$$

$A=$ upper limit of the range.
$B=$ lower limit of the range.
$P=$ probability of a value falling in the range.
$M=$ mean.
$V=$ variance.
$S=$ standard deviation.

Example 1. For a Poisson distribution with $\lambda=2$, find the probability that $0<x<2.5$; also find the mean, the variance, and the standard deviation. (Remember that the Poisson distribution deals only with integers. Therefore, the only $x$ values in this range are 1 and 2.)

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| - FLAGS \{CF\} 0 | value | Clears flag 0 . |
| XEQ P | L? 0.0000 |  |
| 2 R/S | B? 0.0000 | Inputs values. |
| 1 R/S | A? 0.0000 |  |
| 2 R/S | $\mathrm{P}=0.5413$ | Displays probability. |
| R/S | $\mathrm{M}=2.0000$ | Displays mean. |
| R/S | $\mathrm{V}=2.0000$ | Displays variance. |
| R/S | $\mathrm{S}=1.4142$ | Displays standard deviation. |

Example 2. Find the first six terms (from $x=0$ to $x=5$ ) of the Poisson distribution with $\lambda=3$.

## Keys:

- FLAGS \{SF\} 0 value
XEQ P

3 R/S
R/S
5 R/S
R/S
R/S
R/S
R/S
R/S

Display:

L?0.0000
B?0.0000
A? 0.0000
0.0498
0.1494
0.2240
0.2240
0.1680
0.1008

## Description:

Sets flag to display each term of distribution.

Inputs values.

Displays $p$ (0).
Displays $p$ (1).
Displays $p$ (2).
Displays $p$ (3).
Displays $p$ (4).
Displays $p$ (5).

## 5

## Mathematics

## Triangle Solutions

This program may be used to find the sides, angles, and area of a plane triangle.


In general, the specifications of any three of the six parameters of a triangle (three sides and three angles) is sufficient to define a triangle (the exception is that three angles will not define a triangle).
This program will handle all five cases:

- Three sides (SSS).
- Two angles and the included side (ASA).
- Two angles and the adjacent side (SAA).
- Two sides and the included angle (SAS).
- Two sides and the adjacent angle (SSA).

The last case listed (SSA) may result in two solutions to the triangle. This program will calculate both solutions.

If the three known input values are selected in a clockwise order around the triangle, the output values will also follow a clockwise order.

## Program Listing．

| H®1 LEL H | E6S FCL +E |
| :---: | :---: |
| HEz IHFUT A | CWE SIH |
| HES IHFUT © | CQ7 ECL 0 |
| F04 IHFUT E | E6S SIH |
| H0．5 RCL H | E09 - |
| HEG FCL E | E1E FCLX A |
|  | E11 STO |
| H08 2 己 | ■12 GTGK |
| H09 FCL E | Eヶに日に |
| H19 | EQ1 LEL E |
| H11－ | E日2 EF 2 |
| H12 2 | EG3 IHFUT A |
| $\mathrm{H} 13 \mathrm{FCL} \times \mathrm{H}$ | EQ4 IHFUT E |
| F14 FCLX C | EQS ECL A |
| F15－ | EGE FLL E |
| H1G FCOS | E®7－＞y？ |
| H17 STO E | E日S 5F 2 |
| H1G GTOK | E69 IHFUT D |
| 「トににkこum＝9E72 | E1ESIN |
| E®1 LEL E | E11 RCL $\div \mathrm{H}$ |
| EGZ IHFUT F | $\mathrm{E} 12 \times$ |
| E03 IHFUT H | E1S FSIH |
| E04 IHFIIT E | E14 FCL + ［ |
| E®S RCL F | E15 XEQ 2 |
| E06 SIH | E1G STO E |
| Eब7 RCL E | E17 XEQ K |
| $\mathrm{EQS} \mathrm{FOL}+\mathrm{F}$ | E1S ROL F |
| E09 EIH | E19 XEQ 2 |
| E19－ | E2Q STO F |
| E11 FCLX A | E21 FCL＋${ }^{\text {a }}$ |
| $\mathrm{E12}$ STO C | Eここ XEQ 2 |
| E13 GTOK | E23 STO E |
| Chににksum $=50 \mathrm{DE}$ | E24 GTOK |
| C01 LEL C | Lhe日ksum＝FESE |
| C02 IHFUT A | DG1 LEL D |
| C03 IHFUT E | Dez IHFIIT H |
| C04 IHFIIT D | D03 IHFIIT E |


| D04 IHFIIT E | K172 |
| :---: | :---: |
| Cheロksum＝2HE7 | K E － |
| K01 LEL K | K 9 STO |
| K02 FCL E | K2＠YIEN A |
| K03 FEL A | K21 YIEN E |
| K04 日，river | K2c YIEN E |
| K05 FCL－C | K3 WIEN D |
| K06＋ | K24 YIEN E |
|  | K25 UIEN F |
| K08 ST0 E | K2E UIEN G |
| 169 | K27 RTH |
| K1® STO 0 | Chセロksum＝80FG |
| K11 FCL +E | 201 LEL 2 |
| K12 KEQ 2 | 202 Cos |
| K13 STO F | $203+$ |
| K14 5IH | 204 ACOS |
| K15 $\times$ | 20.5 FTH |
| K1G FCLX H | ChEにksum $=929 \mathrm{E}$ |

Flags Used．Flag 2.
Memory Required． 154.5 bytes．

## Remarks．

－Angles must be consistent with the angular mode currently set in the calculator．
－Routines A through E are independent of each other．Therefore，key in only those routines that will be used．Routines K and Z must be keyed in to use any of the five routines．
－The triangle notation used by this program is not consistent with standard triangle notation；in other words，$A_{1}$ is not opposite $S_{1}$ ．
－The accuracy of the solution decreases for triangles containing extremely small angles．

## Program Instructions.

1. Key in the programs to be used; press $\square$ when finished.
2. Select the appropriate routine:

- Press XEQ $A$ if three sides are known (SSS).
- Press XEQ $B$ if two angles and an included side are known (ASA).
- Press XEQ $C$ if two angles and an adjacent side are known (SAA).
- Press XEQ D if two sides and an included angle are known (SAS).
- Press XEQ E if two sides and an adjacent angle are known (SSA).

3. Key in the variables at each prompt and press $R / S$.
4. See each result as it is displayed. Press R/S for subsequent results.
5. If flag 2 is displayed on the calculator screen while executing routine E, a second possible solution exists. Press R/S and return to step 4 to see the second set of results.

## Variables Used.

$A=$ side $_{1}$.
$B=$ angle $_{1}$.
$C=\operatorname{side}_{2}$.
$D=$ angle $_{2}$.
$E=$ side $_{3}$.
$F=$ angle $_{3}$.
$G=$ the area.

Example 1: Three Known Sides. A farmer uses three sections of straight fence to enclose a field. The lengths are 100 feet, 120 feet, and 150 feet. Find the area enclosed and the angles formed.

## Keys:

- MODES \{DG

XEQA
100 R/S
120 R/S
150 R/S
R/S
R/S
R/S
R/S
R/S
R/S

Display:

A?value
C?value
E ?value
$A=100.0000$
$B=85.4593$
$C=120.0000$
$D=41.6497$
$E=150.0000$
$\mathrm{F}=52.8910$
$\mathrm{G}=5,981.1684$

Description:
Sets degrees mode. Inputs lengths.

Displays $S_{1}$. Displays $A_{1}$. Displays $S_{2}$.
Displays $A_{2}$.
Displays $S_{3}$.
Displays $A_{3}$.
Displays area.

Example 2: Two Possible Solutions. Given two sides and a nonincluded angle, solve for the triangle.

$$
\begin{aligned}
S_{1} & =22.5 \\
S_{2} & =37.5 \\
A_{2} & =31.3^{\circ}
\end{aligned}
$$



## Keys:

MODES \{DIT
XEQE
$22.5 \mathrm{R} / \mathrm{S}$
$37.5 \mathrm{R} / \mathrm{S}$
31.3 R/S

R/S
R/S
R/S
R/S
R/S
R/S
R/S

| $\mathrm{R} / \mathrm{S}$ |
| :--- |
| $\mathrm{R} / \mathrm{S}$ |
| $\mathrm{R} / \mathrm{S}$ |
| $\mathrm{R} / \mathrm{S}$ |
| $\mathrm{R} / \mathrm{S}$ |
| $\mathrm{R} / \mathrm{S}$ |

## Display:

A? value
C?value
D?value
$A=22.5000$
$B=88.7184$
$C=37.5000$
$\mathrm{D}=31.3000$
$E=43.2984$
$\mathrm{F}=59.9816$
$\mathrm{G}=421.7695$
$A=22.5000$
$B=28.6816$
$C=37.5000$
$D=31.3000$
$E=20.7860$
$F=120.0184$
$G=202.4757$

## Description:

Sets degrees mode.

Inputs values.
Flag 2 is displayed.
Displays $S_{1}$.
Displays $A_{1}$
(first solution).
Displays $S_{2}$.
Displays $A_{2}$.
Displays $S_{3}$.
Displays $A_{3}$.
Displays area.
Displays $S_{1}$. (second soution).
Displays $A_{1}$.
Displays $S_{2}$.
Displays $A_{2}$.
Displays $S_{3}$.
Displays $A_{3}$.
Displays area.

## Derivative of a Function

This program calculates the derivative of a function at a given value. The function must be defined by a separate program label.

$$
f^{\prime}(x) \approx \frac{f(x+\delta)-f(x-\delta)}{2 \delta}
$$

## Program Listing.

| DG1 LEL D | [15 FCL $\%$ |
| :---: | :---: |
| DES IHFUT i | D1E FOL- $\%$ |
| [0] IHFUT $\%$ | [17 XEQCi) |
| D04 HES | D1S FGL 2 |
| [05 $2 \times 0$ | [19 - |
| DE6 LDG | D20 + |
| D07 IF | D21 FCL -9 |
| 0084 | D22 2 |
| D69 - | [23 |
| [10 16\% | [24 ETO 0 |
| D11 ST@ $Y$ | [25 WIEN [ |
| D12 FCL +8 | DEE FTH |
| [13 XEQCi) | Eh@にkEum $=200 \mathrm{CF}$ |
| 014 STO |  |

Flags Used. None.
Memory Required. 39 bytes.
Remarks. The program defining the function must place the value of the function in the $X$-register.

## Program Instructions.

1. Key in the program listing; press $C$ when finished.
2. Key in the program that defines the function. The program should take the value in the $X$-register as input and leave the resulting value of the function in the $X$-register as output.
3. Press XEQ D. When the prompt i?value is displayed, specify the function by entering the number between 1 and 26 corresponding to
the program label (in other words, $A=1, B=2$, and so on), then press $R / \mathrm{S}$.
4. Key in the $X$-value where the function is to be evaluated and press $\mathrm{R} / \mathrm{S}$ to display the derivative at that value.
5. For a new point, go to step 3 .
6. For a new function, go to step 2.

## Variables Used.

$D=$ derivative of the function.
$X=$ the value at which the derivative of the function is evaluated.
$i=$ the index variable, used to specify the label of the program that defines the function.
$Y, Z=$ variables used for intermediate results.
Example. If $f(x)=3 \ln \left(x^{2}-1\right)$, find $d f / d x$ when $x=1.5$.
First, enter the program for the function:

| F61 LEL F | F6. 5 LH |
| :---: | :---: |
| FG2 $<2$ | FQ6 3 |
| FG3 1 | FG7 $\times$ |
| FG4 - | FGE RTH |
|  | Checksum $=3 \mathrm{F9E}$ |

Then follow these keystrokes:

| Keys: | Display: | Description: |
| :--- | :--- | :--- |
| XEQ D | i?value | Prompts for number <br> corresponding to <br> program label that <br> defines the function. |
| $6 \boxed{R / S}$ | X ? value | Prompts for value where <br> the derivative of the <br> function is to be <br> evaluated. |
| $1.5 \boxed{R / S}$ | $\mathrm{D}=7.2000$ | Displays the derivative of <br> the function. |

## Linear Interpolation

Numerical relationships are often available in the form of tables．This program uses a straight line approximation to estimate a $y$－value given a corresponding $x$－value．Two pairs of $x$－and $y$－values of the relationship must be known．

$$
y=\left(\frac{y_{1}-y_{2}}{x_{1}-x_{2}}\right)\left(x-x_{1}\right)+y_{1}
$$

## Program Listing．

| LG1 LEL L | L11 $\div$ |
| :---: | :---: |
| L62 IHFUT 8 | L12 FCL $\%$ |
| LES IHFUTT A | L13 FCL－ A |
| L04 IHFUT E | L14 x |
| L05 IHFUT C | L15 FCL +E |
| LE6 IHFUT D | L1G STO $Y$ |
| LQ7 REL E | LIF UIEN $Y$ |
| LES FCL－${ }^{\text {a }}$ | L13 RTH |
| L69 ECL H | Eトににくこ」M＝96\％F |
| L10 FCL－E |  |

Flags Used．None．
Memory Required． 27 bytes．
Remarks．The approximation is most accurate when one of the tabulated $x$－values is greater than the desired $x$－value and the other is less．

## Program Instructions．

1．Key in the program listing；press $C$ when finished．
2．Press XEQ L．
3．Key in the variables at each prompt and press $R / S$ ．
4．See the $y$－value approximation．
5．For a new case，go to step 2.

## Variables Used.

$X=$ the $x$-value not found in the table.
$A=$ the $x$-value of the first pair of tabulated values.
$B=$ the $x$-value of the second pair.
$C=$ the $y$-value of the first pair of tabulated values.
$D=$ the $y$-value of the second pair.
$Y=$ the corresponding $y$-value approximation.

Example. The saturation pressure of steam at $110^{\circ} \mathrm{F}$ is 1.2763 psi , and at $120^{\circ} \mathrm{F}$ it is 1.6945 psi . What is the saturation pressure when the temperature is $113^{\circ} \mathrm{F}$ ?

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| XEQ L | X?value |  |
| 113 R/S | A?value | Inputs known values. |
| 110 R/S | B ? value |  |
| 120 R/S | C?value |  |
| 1.2763 R/S | D?value |  |
| 1.6945 R/S | $Y=1.4018$ | Displays approximation of the saturation pressure. |

## Circle Determined by Three Points

This program calculates the center $\left(x_{0}, y_{0}\right)$ and radius $(r)$ of the circle defined by three noncollinear points．

$$
r^{2}=\left(x-x_{0}\right)^{2}+\left(y-y_{0}\right)^{2}
$$

## Program Listing．

CQ1 LEL C
CGE INFIIT A
Cas IHFUT E
CO4 IHFIUT E
［0．5 IHFIIT D
CGE IHFUT E
CGT IHFIUT F
Cug RCL A
C09 STO－C
C10 STO－E
E11 FCL E
C12 STO－ 0
E13 STO－F
C14 FOL D
［15 RCL
C16 $1, \mathrm{xAB}_{\mathrm{B}}^{\mathrm{r}}$
$0175 \mathrm{TO} \%$
［18 $<\gg y$
019 STO T
Ceg ROL F
Ce1 RCL E

Ce3＜＞y
Ce4 ECL－T
C25＜＞y
C26 日，r－ $1, \%$
027 STO 2

029 sTo Y
030 $\div$
OS RCL 2
CEC RCL－ 8
－83 \％
C34 RCL＋Y
CS5 ROL 8

cos 2
$08 \div$
0 ETO E
C4G ROL T
C41
C4E CHFLS＋
C43 日，r－4．
044 RCL E
C45 ECL H
C4E CMFLX＋
$047 \mathrm{ETO} \%$
048 ＜》！
049 sTo Y
CSG YIEN $X$
CS1 VIEN $Y$
C5E YIEN R
C5S RTH
Checksum $=\mathrm{A} 34 \mathrm{E}$

Flags Used. None.
Memory Required. 79.5 bytes.
Remarks. A divide-by-zero error occurs if the three points are collinear. The program modifies the variables that store $x_{2}, y_{2}, x_{3}$, and $y_{3}$; so if you repeat the program, you must reenter these values.

## Program Instructions.

1. Key in the program listing; press $C$ when finished.
2. Press XEQ C.
3. Key in the $x$ - or $y$-coordinate ( $A$ through $F$ ) at each prompt and press R/S.
4. After the $y$-coordinate of the third point is entered (with $R / S$ ), the $x$-coordinate of the center of the circle is displayed.
5. Press R/S and see the $y$-coordinate of the center.
6. Press R/S and see the radius of the circle.
7. For a new case, go to step 2.

## Variables Used.

$A=$ the $x$-coordinate of the first point.
$B=$ the $y$-coordinate of the first point.
$C=$ the $x$-coordinate of the second point.
$D=$ the $y$-coordinate of the second point.
$E=$ the $x$-coordinate of the third point.
$F=$ the $y$-coordinate of the third point.
$X=$ the $x$-coordinate of the center of the circle.
$Y=$ the $y$-coordinate of the center of the circle.
$R=$ the radius of the circle.
T, $Z=$ variables used for intermediate results.

Example. Find the center and radius of the circle defined by the points $(1,0),(2,4.5)$, and ( $-4.4,3$ ).

| Keys: | Display: | Description: |
| :---: | :---: | :---: |
| XEQ C | A?value |  |
| $1 \mathrm{R} / \mathrm{S}$ | B?value | Inputs coordinates. |
| $0 \mathrm{R} / \mathrm{S}$ | C?value |  |
| 2 R/S | D?value |  |
| 4.5 R/S | E?value |  |
| $4.4+/-\mathrm{R} / \mathrm{S}$ | F ? value |  |
| $3 \mathrm{R} / \mathrm{S}$ | $X=-0.9775$ | Displays the $x$-coordinate of the center. |
| R/S | $Y=2.8005$ | Displays the $y$-coordinate of the center. |
| R/S | $\mathrm{R}=3.4283$ | Displays the radius. |

Step-by-Step Solutions for Your HP-32S Calculator

Engineering Applications contains a variety of programs, examples, and solutions to show how you can easily solve your engineering problems.

- Electrical Engineering

Reactance Chart • Impedance of a Ladder Network •Smith Chart Conversions • Transistor Amplifier Performance

- Mechangical Engineering

Black Body Thermal Radiation • Ideal Gas Equation • Conduit Flow - Static Equivalent at a Point - Composit Section Properties

- Soderberg's Equation for Fatigue
- Civil Engineering

Mohr's Circle for Stress • Field Angle Traverse

- Statistics
t Statistics • Chi-Square Evaluation •F Distribution • Analysis of Variance (One Way) • Binomial Distribution • Poisson Distribution
- Mathematics

Triangle Solutions • Derivative of a Function • Linear Interpolation - Circle Determined by Three Points

## Reorder Number 00032-90057


[^0]:    * See page 438 of J.E. Freund's Mathematical Statistics, 2nd edition.

