HEWLETT-PACKARD

HP-33E STUDENT ENGINEERING Applications



For Continuous Memory Models

Although this book refers specifically to the HP-33E or HP-38E, the programs and calculations contained herein apply equally well to the HP-33C or HP-38C. The user should note, however, that the display format and data register contents are retained by the calculator even though it has been turned off. It may be desirable to reset or clear these conditions before running programs or making calculations.



5955-5259

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HP-33E

Student Engineering Applications

April 1978

00033-90032

Printed in U.S.A.

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Introduction

This Student Engineering Applications book was written to help you get the most from your HP-33E calculator. The programs were chosen to provide useful calculations for many common problems encountered in engineering.

They will provide you with immediate capabilities in your everyday calculations and you will find them useful as guides to programming techniques for writing your own customized software.

You will find general information on how to key in and run programs under "A Word about Program Usage" in the Applications book you received with your calculator.

We hope that this Student Engineering book will be a valuable tool in your work and would appreciate your comments about it.

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Ohm's Law and Reactance Chart

This program provides interchangeable solutions for many of the simple relationships involved in electrical engineering problems. Specifically one may solve for:

Frequency: given inductance and capacitance. Capacitance: given frequency and inductance Inductance: given frequency and capacitance Capacitive reactance: given frequency and capacitance Inductive reactance: given frequency and inductance Current or voltage: given resistance and E or I Resistance: given voltage and current Power dissipation: given I and R or E and R Current or voltage: given power and resistance

Formulas Used:

$f = \frac{1}{2\pi\sqrt{LC}}$	where:	f = resonant frequency in hertz
		L = inductance in henrys
v _ 1		C = capacitance in farads
$X_c = \frac{1}{2\pi fC}$		X_c = capacitive reactance in Ω
$X_{L} = 2\pi fL$		X_L = inductive reactance in Ω
E = IR		E = voltage
$P = I^2 R = E^2/R$		I = current in amps
$I = \sqrt{P/R}$		$R = resistance in \Omega$
$E = \sqrt{RP}$		P = power in watts

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	×	19– 61
×	01– 61	2	20- 2
f	02- 14 0	×	21– 61
GSB 18	03- 12 18	9 ½	22- 15 3
бто 00	04– 13 00	g rtn	23- 15 12
[X2y]	05– 21	9 ½	24– 15 3
GSB 18	06- 12 18	×	25– 61
9 x ²	07– 15 0	бто 00	26- 13 00
[X2y]	08– 21	9 1/x	27- 15 3
÷	09– 71	Xzy	28- 21
бто 00	10- 13 00	9 x ²	29– 15 0
×	11– 61	XEY	30- 21
GSB 18	12- 12 18	×	31– 61
бто 00	13- 13 00	GTO 00	32- 13 00
×	14– 61	9 1/x	33- 15 3
GSB 18	15- 12 18	×	34– 61
9 ½	16– 15 3	f 17	35- 14 0
бто 00	17- 13 00	GTO 00	36- 13 00
g <i>π</i>	18- 15 73		

REGISTERS			
R₀	R1	R ₂	R ₃
R₄	R₅	R₀	R ₇

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
	Reactance Chart			
2	To calculate f:			
	Input L and C	L, henrys	ENTER+	
		C, farads	GSB 01	f, hertz
3	To calculate L or C:			
	Input f	f, hertz	ENTER+	
	Input C or L	C or L,	GSB 05	L or C,
		farads, henrys		henrys, farads
4	To calculate $X_{\rm e}\!\!:$			
	Input f and C	f, hertz	ENTER+	
		C, farads	GSB 11	X _c
5	To calculate X _L :			
	Input f and L	f, hertz	ENTER+	
		L, henrys	GSB 14	X _L
	Ohm's Law			
6	To calculate E:			
	Input I and R	I, amps	ENTER+	
		R, Ω	GSB 25	E, volts
7	To calculate I or R:			
	Input E and R or I	E, volts	ENTER+	
		R or I,	GSB 24	I or R,
		Ω , amps		Ω , amps
	Power			
8	To calculate P:			
	a) Input E and R	E, volts	ENTER+	
		R, Ω	GSB 27	P, watts
	or			

	b) Input I and R	I, amps	ENTER+)	
		R , Ω	GSB 28	P, watts
9	To calculate I:			
	Input P and R	P, watts	ENTER+	
		R , Ω	GSB 33	I, amps
10	To calculate E:			
	Input P and R	P, watts	ENTER+	
		R , Ω	GSB 34	E, volts

Example 1:

 $C = 0.01 \ \mu F$, $L = 160 \ \mu h$, calculate f:

Keystrokes	Display	
f ENG 3		
160 EEX CHS 6		
ENTER+		
.01 EEX CHS 6		
GSB 01	125.8 03	or (125.8 \times 10 ³ Hz)

Example 2:

L = 2.5 H, f = 60 Hz, calculate C and X_L:

Keystrokes	Display	
60 ENTER+ 2.5		
GSB 05	2.814 -06	or (2.814 \times 10 ⁻⁶ μ F)
60 ENTER+ 2.5		
GSB 14	942.5 00	or (942.5 Ω)

Example 3:

E = 345 V, R = 1.25 MΩ. Calculate I and P: Keystrokes Display 345 ENTER• 1.25 EEX 6 GSB 24 276.0 -06 or $(276 \times 10^{-6} \text{ amps})$ 345 ENTER• 1.25 EEX 6 GSB 27 95.22 -03 or $(95.22 \times 10^{-3} \text{ watts})$

Resistors in Series or Parallel

This program calculates the total resistance of a group of resistors arranged in parallel or in series.

Formulas Used:

Resistors in Series: $R_T = R_1 + R_2 + R_3 \dots + R_n$ Resistors in Parallel: $R_T = \frac{1}{1/R_1 + 1/R_2 + 1/R_3 \dots + 1/R_n}$

- Note that this program can be used for summing capacitors in parallel or series instead of resistors. For series capacitors use instructions for parallel resistors. For parallel capacitors use instructions for series resistors.
- Several more advanced programs for circuit analysis may be found in: Anderson, L.H., "Calculator Aided Circuit Analysis," *Ham Radio* Magazine, pp. 38-46, October 1977. Although written for the HP-25 they will work equally well on the HP-33E.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	(RCL) 1	12- 24 1
0	01– 0	RCL 0	13- 24 0
бто) 04	02- 13 04	9 x=0	14– 15 71
1	03– 1	GSB 20	15- 12 20
STO 0	04– 23 0	CLX	16– 34
R/S	05– 74	STO 1	17– 23 1
RCL 0	06- 24 0	R+	18– 22
9 x=0	07- 15 71	GTO 00	1 9 – 13 00
GSB 20	08- 12 20	R+	20– 22
R+	09– 22	9 ½	21– 15 3
<u>вто</u> (+ 1	10- 23 51 1	ENTER+	22– 31
бто) 05	11– 13 05	9 RTN	23- 15 12

REGISTERS				
R ₀ Code: 0 or 1	$R_1 \Sigma R, \Sigma 1/R$	R ₂	R ₃	
R_4 R_5 R_6 R_7				

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Initialize		f REG f PRGM	
3	a) Set for parallel resistors		R/S	0.0000
	or			
	b) Set for series resistors		GSB 03	1.0000
4	Optional: Retrieve last $R_{\rm T}$			
	for use in next calculation		R♦	Previous $R_{\rm T}$
5	Input individual resistor values	R_{i}	R/S	
	(Repeat until all resistors in			
	group have been input.)			
6	Calculate total resistance of			
	the group		GSB 12	R_{T} , Ω
.7	Optional: Store $R_{\rm T}$ for use in			
	next calculation	R _T	STO 2	
8	Go to step 3a or 3b for next			
	group.			

Example:



Determine the total circuit resistance from A to B.

Keystrokes	Display	
f REG f PRGM		
Group 1: R/S	0.0000	Parallel mode
680 R/S 120 R/S		
GSB 12	102.0000	R_1, Ω
Group 2: GSB 03	1.0000	Series mode
R+	102.0000	Retrieve R_1
R/S 330 R/S		
680 R/S		P
GSB 12	1,112.0000	R_2, Ω
Group 3: [R/S]	0.0000	Parallel mode
R+	1,112.0000	Retrieve R_2
R/S 220 R/S		D
GSB 12	183.6637	R_3, Ω
STO 2		Save R_3
Group 4: R/S	0.0000	Parallel mode
680 R/S 470 R/S		
GSB 12	277.9130	R_4, Ω
Total R		
GSB 03	1.0000	Series mode
R♦	277.9130	Retrieve R ₄
R/S RCL 2 R/S		
GSB 12	461.5767	R_T , Ω

Exponential Growth or Decay

Many growth or decay phenomena encountered in science and engineering obey an exponential law of the general form:

 $X_t = X_{ss} - (X_{ss} - X_o) e^{-t} \tau$

where: $X_t = Value$ at any time, t, (i.e., the instantaneous value)

$$X_{ss}$$
 = Steady state value (i.e., at t = ∞)

 X_0 = Initial value (i.e., at t = 0)

t = Elapsed time (time after t = 0)

 τ = Exponential time-constant for specific phenomena

This program provides interchangeable solutions for any one of the four variables X_t , X_{ss} , X_o or t provided three variables and τ are known.

KEY ENTRY	DISPLAY		KEY ENTRY	DIS	SPLAY
	00		RCL 2	23-	24 2
RCL 0	01– 24	0	-	24-	41
RCL 2	02- 24	2	×	25-	61
—	03- 4	1	RCL 2	26 –	24 2
GSB 40	04- 12 4	0	+	27-	51
÷	05– 7	1	GTO 00	28-	13 00
RCL 2	06- 24	2	RCL 0	29 –	24 0
+	07– 5	1	RCL 2	30 –	24 2
GTO 00	08- 13 0	0	—	31-	41
GSB 40	0 9 – 12 4	0	RCL 1	32-	24 1
ENTER+	10– 3	1	RCL 2	33-	24 2
ENTER+	11– 3	1	—	34-	41
RCL 1	12– 24	1	÷	35–	71
×	13– 6	1	f LN	36 –	14 1
RCL 0	14– 24	0	RCL 4	37-	24 4
Ē	15– 4	1	×	38 –	61
Xzy	16– 2	1	GTO 00	39 –	13 00
1	17–	1	RCL 3	40-	24 3
Ē	18– 4	1	RCL 4	41-	24 4
÷	19– 7	1	÷	42-	71
GTO 00	20- 13 0	0	9 <i>e</i> ×	43-	15 1
GSB 40	21- 12 4	0	9 RTN	44-	15 12
RCL 1	22- 24	1			

REGISTERS				
R₀ X₀	R ₁ X _t	$R_2 X_{ss}$	R₃ t	
R₄ <i>τ</i>	R₅	R ₆	R ₇	

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Store time constant	au	STO 4	
3	Store variables:			
	Initial value	X _o	STO 0	
	Instantaneous value	X _t	STO 1	
	Steady state value	X _{ss}	STO 2	
	Elapsed time	t	STO 3	
	(Store any 3 of the 4			
	variables)			
4	To calculate:			
	X _o , initial value		GSB 21	X _o
	X _t , instantaneous value		GSB 01	X _t
	X_{ss} , steady state value		GSB 09	X _{ss}
	t, elapsed time		GSB 29	t
5	For a new case go to step 2.			

Example 1:

Given a 5μ F capacitor in series with a 1 megohm resistor. 1.5 seconds after the circuit is completed 125 volts are measured across R. To what voltage was the capacitor originally charged?

Note:

 π = the RC time-constant, and the voltage at t = ∞ is zero.

Keystrokes	Display	
5 EEX CHS 6		
ENTER+ EEX 6		
× STO 4		
125 STO 1		
0 STO 2		
1.5 STO 3		
GSB 21	168.7324	volts

Example 2:

A cobalt 60 source (half life = 5.26 years) had an activity of 3.54 curies when purchased 8.5 years ago. What is its present activity?

Note:

Activity at $t = \infty$ will be zero, π = half life/ln2.

Keystrokes	Display	
5.26 [ENTER+]		
2 f LN÷		
STO 4		
3.54 STO 0		
0 STO 2		
8.5 STO 3		
GSB 01	1.1549	curies

Heat and Thermal Engineering

Black Body Thermal Radiation

Bodies with finite temperatures emit thermal radiation. The higher the absolute temperature, the more thermal radiation emitted. Bodies which emit the maximum possible amount of energy at every wavelength for a specified temperature are said to be black bodies. While black bodies do not actually exist in nature, many surfaces may be assumed to be black for engineering considerations.



Figure 1 is a representation of black body thermal emission as a function of wavelength. Note that as temperature increases the area under the curves (total emissive power $E_{b-(0-\infty)}$) increases. Also note that the wavelength of maximum emissive power λ_{max} shifts to the left as temperature increases.

This program can be used to calculate the wavelength of maximum emissive power for a given temperature, the temperature corresponding to a particular wavelength of maximum emissive power, the total emissive power for all wavelengths and the emissive power at a particular wavelength.

Equations:

$$\lambda_{\max} T = c_3$$

$$E_{b(0-\infty)} = \sigma T^4$$

$$E_{b\lambda} = \frac{2\pi c_1}{\lambda_5 (e_{c_2}/\lambda T - 1)}$$

where: λ_{max} is the wavelength of maximum emissivity in microns;

T is the absolute temperature in $^{\circ}R$ or K;

 $E_{b(0-\infty)}$ is the total emissive power in Btu/hr-ft² or watts/cm²;

EbA is the emissive power at λ in Btu/hr-ft²- μ m or watts/ cm² - μ m;

- $c_1 = 1.8887982 \times 10^7 \text{ Btu-}\mu\text{m}^4/\text{hr-}\text{ft}^2$
 - $= 5.9544 \times 10^3 \,\mathrm{W}\mu\,\mathrm{m}^4/\mathrm{cm}^2$
- $c_2 = 2.58984 \times 10^4 \,\mu \text{m}^{\circ}\text{R} = 1.4388 \times 10^4 \,\mu \text{m}^{-K}$
- $c_3 = 5.216 \times 10^3 \,\mu m^{\circ} R = 2.8978 \times 10^3 \,\mu m^{\circ} K$
- $\sigma = 1.713 \times 10^{-9} \,\mathrm{Btu/hr}$ -ft²-°R⁴ = 5.6693 × 10⁻¹² W/cm²-K⁴
- $\sigma_{\rm exp} = 1.731 \times 10^{-9} \text{ Btu/hr-ft}^2\text{-}^\circ\text{R}^4 = 5.729 \times 10^{-12} \text{ W/cm}^2 \text{K}^4$
- Sources differ on values for constants. This could yield small discrepancies between published tables and HP-33E outputs.

Reference:

Robert Siegel and John R. Howell, *Thermal Radiation Heat Transfer*, Volume 1, National Aeronautics and Space Administration, 1968.

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY	
	00	×	1 9 – 61	
STO 5	01- 23 5	RCL 6	20- 24 6	
GSB 34	02- 12 34	5	21– 5	
STO 6	03- 23 6	fyx	22- 14 3	
R/S	04– 74	÷	23– 71	
STO 6	05- 23 6	RCL 2	24- 24 2	
GSB 34	06- 12 34	RCL 6	25– 24 6	
STO 5	07- 23 5	÷	26– 71	
R/S	08- 74	RCL 5	27- 24 5	
RCL 5	09- 24 5	÷	28– 71	
4	10- 4	9 <i>e</i> ×	2 9 – 15 1	
fyx	11- 14 3	1	30- 1	
RCL 4	12- 24 4	Ē	31– 41	
×	13– 61	÷	32– 71	
f PAUSE	14- 14 74	GTO 00	33- 13 00	
RCL 1	15– 24 1	RCL 3	34- 24 3	
2	16- 2	(X2)	35– 21	
×	17– 61	÷	36- 71	
g <i>π</i>	18- 15 73	9 RTN	37- 15 12	

REGISTERS						
R₀	R ₁ c ₁	$R_2 c_2$	$R_3 c_3$			
$R_4 \sigma$ $R_5 T$ $R_6 \lambda$ R_7						

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Set display			
3	Store constants		f SCI 4	
	a) For SI (W, μ m, cm, K)			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	$c_1 = 5.9544 \times 10^3$	C ₁	STO 1	
	$c_2 = 1.4388 \times 10^4$	C ₂	STO 2	
	$c_3 = 2.8978 \times 10^3$	C ₃	STO 3	
	$\sigma = 5.6693 \times 10^{-12}$	σ	(сто) 4	
	or			
	$\sigma_{ m exp} = 5.729 imes 10^{-12}$	$\sigma_{ m exp}$	STO 4	
	b) For English (Btu, μ m, hr,			
	ft, °R)			
	$c_1 = 1.8887982 \times 10^7$		<u>(</u> sto) 1	
	$c_2 = 2.58984 \times 10^4$		(сто) 2	
	$c_3 = 5.216 \times 10^3$		(сто) 3	
	$\sigma = 1.713 \times 10^{-9}$		STO 4	
	or			
	$\sigma_{ m exp}=$ 1.731 $ imes$ 10 ⁻⁹		<u>вто</u> 4	
4	To calculate λ_{max}	Т	GSB 01	$\lambda_{max}, \mu m$
5	To calculate temp. at which			
	λ is maximum	λ	GSB 05	T, °
6	To calculate black			
	body total emissive			
	power and total			
	emissive power at any λ .			
	a) For $\lambda_{max},$ do step 3 or			
	step 4 then		GSB 09	(E _{b(0-∞)})*
				$E_b \lambda_{max}$
	b) For other $\boldsymbol{\lambda}$	λ	STO 6 GSB 09	$(E_{b(0-\infty)})^*$
				Εbλ
	* $(E_{b(0-\infty)})$ displayed			
	by pause only.			

Example:

If the human eye was designed to work most efficiently in sunlight and the visible spectrum peaks at about .550 μ m, what is the sun's temperature in K? Assume that the sun is a black body. What is the total emissive power and the emissive power at λ_{max} ? What is the emissive power at $\lambda = 0.400 \ \mu$ m (ultraviolet limit) and 0.700 μ m (infrared limit).

Keystrokes	Display	
f sci 4		
5.9544 EEX 3		
STO 1		
1.4388 EEX 4		
STO 2		
2.8978 EEX 3		
STO 3		
5.6693 EEX CHS 12		
STO 4		
.55 GSB 05	5.2687 03	$(5.2698 \times 10^3 \text{ K})$
GSB 09	4.3687 03	$(4.3687 \times 10^3 \text{ watts/cm}^2)$,
		$E_{b(0-\infty)}$)
		(Pause only)
	5.2229 03	$(5.2229 \times 10^3 \text{ watts/cm}^2)$
		$-\mu m$, Edlmax)
.4 STO 6 GSB 09	4.3687 03	(Ignore)
	3.9649 03	$(3.9649 \times 10^3 \text{ watts/cm}^2)$
		-µm, Ебл)
.7 Sto 6 GSB 09	4.3687 03	(Ignore)
	4.5934 03	$(4.5934 \times 10^3 \text{ watts/cm}^2)$
		$-\mu m$, Eba)

Ideal Gas Equation of State

Many gases obey the ideal gas laws quite closely at reasonable temperatures and pressures. This program calculates any one of the four variables when data for the other three and the universal gas constant are entered. Likewise, the value of the universal gas constant can be determined by entering data for the four variables.

Equation:

$$PV = n RT$$

- where: P is the absolute pressure
 - V is the volume
 - n is the number of moles present
 - R is the universal gas constant
 - T is the absolute temperature

TABLE 1 Values of the Universal Gas Constant

Value of R	Units of R	Units of P	Units of V	Units of T
8.314	N-m/g mole- K	N/m²	m³/g mole	к
83.14	cm3-bar/g mole- K	bar	cm³/g mole	к
82.05	cm3-atm/g mole- K	atm	cm³/g mole	К
0.08205	ℓ -atm/g mole- K	atm	ℓ /g mole	к
0.7302	atm-ft ³ /lb mole-°R	atm	ft ³ /lb mole	°R
10.73	psi-ft³/lb mole-°R	psi	ft ³ /lb mole	°R
1545	psf-ft ³ /lb mole-°R	psf	ft ³ /lb mole	°R

Remarks:

- At low temperatures or high pressures the ideal gas law does not represent the behavior of real gases.
- The value of R used must be compatible with the units of P, V, T.
- In running the program be sure to enter zero for the variable to be calculated.

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	RCL 4	17- 24 4
GSB 28	01- 12 28	×	18– 61
STO 2	02- 23 2	RCL 5	19– 24 5
R+	03– 22	×	20– 61
GSB 28	04– 12 28	RCL 1	21- 24 1
<u>(sto)</u> 1	05– 23 1	RCL 2	22- 24 2
R+	06– 22	×	23– 61
R/S	07– 74	÷	24– 71
GSB 28	08- 12 28	R/S	25– 74
(STO) 5	09– 23 5	9 1/x	26– 15 3
R+)	10– 22	GTO 00	27- 13 00
GSB 28	11- 12 28	9 x≠0	28- 15 61
STO 4	12– 23 4	9 RTN	29– 15 12
R+	13– 22	R+	30– 22
GSB 28	14- 12 28	1	31– 1
(STO) 3	15– 23 3	9 RTN	32- 15 12
RCL 3	16– 24 3		

REGISTERS				
R _o	R₁ P	R ₂ V	R₃ n	
$R_4 R$ $R_5 T$ R_6 R_7				

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Set display and initialize		f FIX 2 f PRGM	
3	Input variables*			
	Pressure	Р	ENTER+	
	Volume	v	R/S	
	Number of moles	n	ENTER+	
	Universal gas constant**	R	ENTER+	
	Absolute temp.	Т		
4	a) To calculate P or V		R/S	P or V
	or			
	b) To calculate n, R or T		R/S R/S	n, RorT
5	To change conditions:			
	a) Go to step 3, or,			
	b) Store new variable in			
	in proper register (see			
	register contents) and			
	store 1 in register of			
	variable to be calculated,			
	then,			
	for P or V		GSB 16	P or V
	or,			
	for n, R or T		GSB 16 R/S	n, R or T
	* Note: variables must be in-			
	put in order shown. Input			
	zero for variable to be calcu	lated		
	** Be sure R is in units com-			
	patible with units of			
	variables			

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Example:

0.63 moles of air are enclosed in 25000 cm^3 at 1200K. What is the pressure in bars? In atmospheres? Assume an ideal gas.

 $(R = 83.14 \text{ cm}^3\text{-bar/g mole-K or } 82.05 \text{ cm}^3\text{-} \text{ atm/g mole-K})$

Keystrokes	Display	
f FIX 2 f PRGM		
0 ENTER+		
25000 R/S		
.63 ENTER+		
83.14 ENTER+		
1200 R/S	2.51	bars
82.05 STO 4		
GSB 16	2.48	atm.

Mechanical Engineering

Equations of Motion

This program provides solutions for many problems involving motion of an object given a constant acceleration and initial velocity. Velocity, distance traveled and acceleration may be found if time is known. Given the distance traveled, velocity or time may be calculated or, given velocity, time or acceleration may be calculated.

Equations:

 $V = V_0 + at$ $V = (V_0^2 + 2 aS)^{12}$ $S = V_0 + \frac{1}{2} at^2$ $t = \frac{V - V_0}{a} \text{ or } a = \frac{V - V_0}{t}$ where: V = velocity

 V_0 = initial velocity a = acceleration S = distance t = time

These same equations also hold for circular motion where:

 ω [angular velocity (radians/sec)] replaces V

 ω_0 replaces V_0

 α replaces a

 θ [angular displacement (radians)] replaces S

 Generally accepted values for the frequently used gravitational constant are 980.665 cm/sec² or 32.17398 ft/sec².

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	RCL 3	23- 24 3
(STO) 2	01- 23 2	×	24– 61
R+	02- 22	R/S	25– 74
[5ТО] 0	03- 23 0	Xzy	26– 21
R/S	04– 74	RCL 0	27- 24 0
RCL 2	05- 24 2	—	28– 41
×	06– 61	Xzy	29– 21
RCL 0	07- 24 0	÷	30– 71
+	08– 51	R/S	31– 74
9 RTN	09- 15 12	GSB 10	32- 12 10
2	10- 2	<u>вто</u> 7	33– 23 7
×	11– 61	RCL 0	34– 24 0
RCL 2	12– 24 2	CHS	35– 32
×	13– 61	+	36– 51
RCL 0	14– 24 0	RCL 2	37– 24 2
9 x ²	15– 15 0	÷	38– 71
+	16– 51	g x<0	39– 15 41
f	17- 14 0	бто 42	40- 13 42
9 RTN	18- 15 12	R/S	41– 74
(сто) 3	19– 23 3	rcl 7	42- 24 7
2	20- 2	СН	43- 32
÷	21– 71	бто] 34	44- 13 34
GSB 05	22- 12 05		

REGISTERS				
$R_0 V_0$	R ₁	R₂ a	R₃t	
R_4 R_5 R_6 R_7 Used				

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Input initial velocity	Vo	ENTER+	
	and acceleration	а	GSB 01	
	To solve for velocity:			
3	Input time	t	GSB 05	V
	or			
	Input distance	S	GSB 10	V
	To solve for distance:			
4	Input time	t	GSB 19	S
	To solve for time:			
5a	Input velocity	v	ENTER+	
	and acceleration	а	GSB 26	t
	or		RCL 2 GSB 26	t
	or			
5b	Input distance	S	GSB 32	t
	To solve for acceleration:			
6	Input velocity	v	ENTER+	
	and time	t	GSB 26	а

Example:

A stone is thrown from a 100 meter high bridge with an initial velocity of 15 meters per second. What will be the velocity when it strikes the river below? How long will it take to hit the water? (The acceleration of gravity is 9.80665 m/sec^2)

Keystrokes	Display	
15 ENTER+		
9.80665 GSB 01		
100 GSB 10	46.7582	V, meters/sec
100 GSB 32	3.2384	t, seconds

Natural Frequency of Oscillators

This program solves for the natural frequency, the spring constant or the mass (alternatively, weight) of a simple oscillator. Examples of this are a spring or torsional pendulum obeying Hooke's law or a pendulum undergoing small oscillations.

Equations:

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}} \text{ for spring}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{k_T}{J}} \text{ for torsional pendulum}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{1}{\frac{\ell}{g}}} \text{ for pendulum in small oscillation (i.e., } \theta \simeq \sin\theta)$$

$$m = \frac{W}{g}$$

where: m = mass, W = weight g = acceleration due to gravity f = natural frequency of the oscillator (hertz) k = spring constant (wt/l) $k_T = torsional constant (wt l/radian)$ $J = mass moment of inertia (wt l sec^2)$ l = length

- Note that for a simple pendulum, length is equivalent to weight.
- In running the program be sure to enter zero for the variable to be calculated.

This program is based on an HP-65 Users' Library program by Lane R. Pendleton.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	÷	20– 71
бто 3	01- 23 3	fr	21- 14 0
R+	02– 22	9 <i>m</i>	22- 15 73
<u>вто</u> 2	03- 23 2	2	23- 2
R+	04– 22	×	24– 61
(sto) 1	05– 23 1	÷	25– 71
9 x=0	06– 15 71	бто 00	26- 13 00
бто 18	07- 13 18	RCL 1	27– 24 1
RCL 2	08- 24 2	9 <i>T</i>	28- 15 73
9 x=0	09– 15 71	×	29– 61
бто 14	10- 13 14	2	30– 2
GSB 27	11- 12 27	×	31– 61
÷	12– 71	9 x ²	32– 15 0
бто 00	13- 13 00	9 RTN	33- 15 12
GSB 27	14– 12 27	RCL 0	34- 24 0
RCL 3	15- 24 3	÷	35– 71
×	16– 61	бто 00	36- 13 00
бто 00	17- 13 00	RCL 0	37- 24 0
RCL 2	18- 24 2	×	38– 61
RCL 3	19– 24 3	бто 00	39– 13 00

REGISTERS				
R₀ g	R₁ f	R₂k	R₃m	
R_4 R_5 R_6 R_7				

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STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Store the gravitational			
	acceleration constant:			
	a) If SI	980.665,	STO 0	g, cm/sec ²
		(cm/sec ²)		
	b) If English	386.088,	STO 0	g, in/sec ²
		(in/sec²)		
3	Input data in order shown			
	(use zero for unknown			
	variable):			
	Frequency	f, (sec ⁻¹)	ENTER+	
	Spring constant	k (w t/Ջ)	ENTER+	
	Mass	m	f PRGM	
	or Weight	w	GSB 34	
4	Calculate unknown variable:		R/S	
	Frequency			f, Hz.
	or spring const.			k, (wt/Ջ)
	or mass			m
5	To convert mass to weight	m	GSB 37	w
6	To convert weight to mass	W	GSB 34	m

Example 1:

A weight of 10 lbs. is attached to a spring whose constant is 100 lbs/in. Find the frequency of the system.

Keystrokes	Display	
386.088 бто 0		
100 ENTER+ 10		
GSB 34		
R/S	9.8892	Hz

Example 2:

A torsional pendulum has a natural frequency of 200 Hz. Its mass moment of inertia is 400 kg in. \sec^2 . Find the torsional constant.

Keystrokes	Display	
980.665 Sto 0		
200 ENTER+		
0 ENTER+		
400 f PRGM		
R/S f SCI 4	6.3165 08	(6.3165×10^8)
		kg in/radian

Example 3:

Find the length of a pendulum which has a 1Hz natural frequency.

hes

Note:

The length of the pendulum is equivalent to its weight.)

Keystrokes	Display	
386.088 бто 0		
1 ENTER+		
1 ENTER+ 0 R/S		
GSB 37	9.7797	inc

Kinetic Energy

This program calculates an interchangeable solution among the variables weight (or mass), velocity, and kinetic energy, for an object moving at constant velocity. The program operates in either English or metric units. For metric units, any consistent set of units may be used; the quantity mass must be used. For English units, the energy must be in foot-pounds, the velocity in feet per second, and the quantity weight in pounds.

where: K.E. = kinetic energy W = weight (lb) m = mass (kg, g) v = velocity g = acceleration due to gravity = 980.665 cm/sec² or 32.17398 ft/sec²

Equations:

English

Metric

K.E.
$$=\frac{1}{2} \frac{W}{g} v^2$$
 K.E. $=\frac{1}{2} mv^2$

 $1 \text{ ft-lb} = 1.98 \times 10^{6} \text{ hp}$

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
T CLEAR PRGM	00	1	19– 1
2	01- 2	9	20- 9
STO 0	02- 23 (8	21– 8
GTO 13	03- 13 13	EEX	22– 33
6	04- 6	4	23- 4
4	05- 4	÷	24– 71
•	06– 73	бто 13	25- 13 13
3	07- 3	9 x ²	26- 15 0
4	-80	X2y	27– 21
7	09– 7	RCL 0	28- 24 0
9	10- 9	X	2 9 – 61
6	11- 6	Xty	30– 21
(sto) 0	12- 23 () ÷	31– 71
R/S	13– 74	GTO 13	32- 13 13
9 x ²	14- 15 (÷	33– 71
×	15– 61	RCL 0	34– 24 0
RCL 0	16- 24 (35– 61
÷	17– 71	fx	36- 14 0
бто 13	18- 13 13	<u>сто</u> 13	37- 13 13

REGISTERS				
R₀ Used	R ₁	R₂	R₃	
R_4 R_5 R_6 R_7				

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STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Initialize:			
	for metric (SI)		GSB 01	2.0000
	for English		GSB 04	64.3480
	To calculate Kinetic Energy:			
3	Input weight (mass)	W (m)	ENTER+	
	and velocity	٧	R/S	K.E.
	To calculate Weight (mass):			
4	Input kinetic energy	K.E.	ENTER+	
	and velocity	۷	GSB 26	W (m)
	To calculate Velocity:			
5	Input kinetic energy	K.E.	ENTER+	
	and weight (mass)	W (m)	GSB 33	V
	Optional:			
	Convert K.E. (ft-lb) to K.E.			
	(hp)	K.E. (ft-lb)	GSB 19	K.E. (hp)
7	For a new case go to step 2.			

Example 1:

The slider of a slider-crank mechanism is used to punch holes in a slab of metal. It is found that the work required to punch a hole is 775 ft-lb. If the slider weighs 5.25 lbs., how fast must it be moving when it strikes the metal? What is the required work in horsepower?

Keystrokes	Display	
GSB 04		
775 ENTER+		
5.25 GSB 33	97.4627	ft/sec
775 ENTER+		
GSB 19		
f sci 4	3.9141-04	$3.9141 \times 10^{-4} \text{ hp}$

joules

Example 2:

An object weighing 4.8 kg is moving with constant velocity of 3.5 m/sec. Find its kinetic energy.

Keystrokes	Display
f FIX 4 GSB 01	
4.8 ENTER+ 3.5 R/S	29.4000

RPM/Torque/Power

This program provides an interchangeable solution for RPM, torque, and power in both Système International (metric) and English units.

	SI	English
RPM	RPM	RPM
Torque	nt-m	ft-lb
Power	watts	hp

Equations:

 $RPM \times Torque = Power$ 1 hp = 745.7 watts1 ft-lb = 1.356 joules $1 \text{ hp} = 550 \frac{\text{ft-lb}}{\text{sec}}$

$$s = 330$$

1 RPM = $\pi/30$ radians/sec

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
F CLEAR PRGM	00	Xty	21– 21
3	01– 3	9 ½	22- 15 3
0	02- 0	бто 5	23- 23 5
9 <i>m</i>	03- 15 73	÷	24– 71
÷	04– 71	×	25– 61
<u>вто</u> 7	05– 23 7	(STO) 7	26- 23 7
7	06- 7	R/S	27– 74
4	07- 4	÷	28– 71
5	08- 5	RCL 7	29– 24 7
	09– 73	×	30– 61
7	10- 7	R/S	31– 74
вто 5	11- 23 5	RCL 6	32- 24 6
1	12– 1	÷	33– 71
	13– 73	GTO 27	34– 13 27
3	14– 3	×	35– 61
5	15– 5	rcl 7	36- 24 7
6	16– 6	÷	37– 71
STO 6	17- 23 6	R/S	38– 74
R/S	18– 74	RCL 5	39– 24 5
9 1/x	19–	÷	40- 71
STO 6	20- 23 6	бто 27	41- 13 27

REGISTERS			
R₀	R ₁	R ₂	R ₃
R₄	R₅ Used	R ₆ Used	R ₇ Used

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Initialize:			
	For metric (SI)		GSB 01	1.3560
	For English		GSB 01 R/S	5,251.4089
	To calculate RPM			
3	Input power	power	ENTER+	
	Input torque	torque	GSB 28	RPM
	To calculate Torque:			
4	Input power	power	ENTER+	
	Input RPM	RPM	GSB 28	torque
	Optional:			
4b	Convert torque to other			
	system		R/S	torque
	To calculate Power:			
5a	Input torque	torque	ENTER+	
	Input RPM	RPM	GSB 35	power
	Optional:			
5b	Convert power to other			
	system		R/S	power

Example 1:

Compute the torque from an engine developing 11 hp at 6500 RPM. Find the SI equivalent.

Keystrokes	Display	
GSB 01 R/S		
6500 GSB 28	8.8870	ft-lb English
R/S	12.0508	nt-m, SI

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Example 2:

A generator is turning at 1600 RPM with a torque of 20 nt-m. If it is 90% efficient what is the power input in watts? In horsepower?

Keystrokes	Display	
GSB 01		
20 ENTER+ .9 ÷		
1600 GSB 35	3,723.3691	watts
R/S	4.9931	hp

Stress Analysis

Static Equilibrium at a Point

This program calculates the two reaction forces necessary to balance a given two-dimensional force vector. The direction of the reaction forces may be specified as a vector of arbitrary length or by Cartesian coordinates using the point of force application as the origin.



Equations:

 $\mathbf{R}_1 \cos \theta_1 + \mathbf{R}_2 \cos \theta_2 = \mathbf{F} \cos \phi$

 $R_1 \sin \theta_1 + R_2 \sin \theta_2 = F \sin \phi$

where: F is the known force; ϕ is the direction of the known force; R_1 is one reaction force; θ_1 is the direction of R_1 ; R_2 is the second reaction force; θ_2 is the direction of R_2 ;

The coordinates x_1 and y_1 are referenced from the point where F is applied to the end of the member along which R_1 acts; x_2 and y_2 are the coordinates referenced from the point where F is applied to the end of the member along which R_2 acts.

Remarks:

This program assumes the calculator is set in DEG mode.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	RCL 2	25- 24 2
9 • P	01- 15 4	×	26– 61
(X2y)	02- 21		27- 41
1	03– 1	(RCL) 1	28- 24 1
f +R	04- 14 4	RCL 2	29- 24 2
(STO) ()	05- 23 0	×	30- 61
[X2y]	06– 21	RCL 0	31- 24 0
STO 1	07- 23 1	RCL 3	32- 24 3
9 RTN	08- 15 12	×	33– 61
9 • P	0 9 – 15 4	—	34– 41
X \$ y	10– 21	÷	35– 71
1	11– 1	R/S	36– 74
f +R	12– 14 4	f LST X	37- 14 73
STO 2	13- 23 2	STO 6	38- 23 6
Xzy	14– 21	RCL 5	39– 24 5
STO 3	15– 23 3	RCL 0	40- 24 0
9 RTN	16- 15 12	×	41– 61
f +R	17– 14 4	RCL 4	42- 24 4
STO 4	18- 23 4	RCL 1	43- 24 1
Xzy	1 9 – 21	×	44– 61
STO 5	20- 23 5		45– 41
RCL 4	21- 24 4	RCL 6	46- 24 6
RCL 3	22- 24 3	÷	47– 71
×	23– 61	9 RTN	48- 15 12
RCL 5	24- 24 5		

REGISTERS			
$R_0 \cos \theta_1$	$R_1 \sin \theta_1$	$R_2 \cos \theta_2$	$R_3 \sin \theta_2$
R₄ F cos φ	R₅ F sin φ	R₀ Used	R ₇

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STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Define reaction directions as			
	Cartesian coordinates or as			
	vectors of arbitrary magnitude.			
	(Use the point of force			
	application as the origin):			
	Define direction one in			
	rectangular form	y ₁	ENTER+	у 1
		X ₁	GSB 01	$\sin \theta_1$
	or			
	in polar form	θ_1	GSB 03	$\sin \theta_1$
	and			
	Define direction two in			
	rectangular form	y ₂	ENTER+	
		X_2	GSB 09	$\sin \theta_2$
	or			
	polar form	θ_2	GSB 11	$\sin \theta_2$
3	Key in known force: direction,	φ	ENTER+	
	then magnitude and			
	compute reactions.	F	GSB 17	R ₁
			R/S	R ₂
4	To change force, go to step 3.			
	To change either or both			
	reaction directions, go to			
	step 2.			

Example 1:

Find the reaction forces in the pin-jointed structure shown below.



Keystrokes	Display	
8 CHS ENTER+		
7 Снз		
GSB 01	-0.7526	sin θ_1
0 ENTER+ 10 CHS		
GSB 09	0.0000	$\sin \theta_2$
90 CHS ENTER+		
500 GSB 17	-664.3841	R_1
R/S	437.5000	R_2

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Example 2:

Find the reaction forces for the diagram below:



Vector Cross Product

If $A = (a_1, a_2, a_3)$ and $B = (b_1, b_2, b_3)$ are two dimensional vectors then the cross product of A and B is denoted by $A \times B$ and is calculated as follows:

$$\mathbf{A} \times \mathbf{B} = \left(\begin{vmatrix} \mathbf{a}_2 & \mathbf{a}_3 \\ \mathbf{b}_2 & \mathbf{b}_3 \end{vmatrix}, - \begin{vmatrix} \mathbf{a}_1 & \mathbf{a}_3 \\ \mathbf{b}_1 & \mathbf{b}_3 \end{vmatrix}, \begin{vmatrix} \mathbf{a}_1 & \mathbf{a}_2 \\ \mathbf{b}_1 & \mathbf{b}_2 \end{vmatrix} \right) =$$

 $(a_2 \, b_3 - a_3 \, b_2, a_3 \, b_1 - a_1 \, b_3, a_1 \, b_2 - a_2 \, b_1)$

Let the solution be represented by (c_1, c_2, c_3) .

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	RCL 6	13– 24 6
RCL 2	01- 24 2	×	14– 61
RCL 6	02- 24 6		15– 41
×	03– 61	R/S	16– 74
RCL 3	04– 24 3	RCL 1	17– 24 1
RCL 5	05– 24 5	RCL 5	18– 24 5
×	06– 61	×	1 9 – 61
-	07- 41	RCL 2	20- 24 2
R/S	08- 74	RCL 4	21- 24 4
RCL 3	0 9 – 24 3	×	22– 61
RCL 4	10- 24 4	-	23– 41
×	11– 61	GTO 00	24- 13 00
RCL 1	12– 24 1		

REGISTERS					
R₀	R ₁ a ₁	$R_2 a_2$	R₃ a₃		
R ₄ b ₁ R ₅ b ₂ R ₆ b ₃ R ₇					

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STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Store A	a 1	STO 1	
		a_2	STO 2	
		a_3	STO 3	
3	Store B	b ₁	STO 4	
		b_2	STO 5	
		b_3	STO 6	
4	Calculate cross product		GSB 01	C ₁
			R/S	C ₂
			R/S	C ₃
5	For a new case, go to step 2.			

Example:

Let A = (2, 5, 2) and B = (3, 3, -4).

Solution:

 $A \times B = (-26, 14, -9)$

Keystrokes Display

2 STO 1 5 STO 2		
2 STO 3		
3 STO 4		
3 STO 5		
4 CHS STO 6		
GSB 01	-26.0000	c ₁
R/S	14.0000	c ₂
R/S	-9.0000	c_3

Angle Between, Norm and **Dot Product of Vectors**

Let $\vec{a} = (a_1, a_2 \dots, a_n)$ and $\vec{b} = (b_1, b_2, \dots, b_n)$ be two vectors. The norm of a is denoted by $|\vec{a}|$ and is calculated by the following formula:

$$|\vec{a}| = \sqrt{a_1^2 + a_2^2 + \dots + a_n^2}$$

similarly,

$$|\vec{b}| = \sqrt{b_1^2 + b_2^2 + \dots + b_n^2}$$

The dot product of \vec{a} and \vec{b} is denoted by $\vec{a} \cdot \vec{b}$ and is calculated by the following formula:

$$\vec{a} \cdot \vec{b} = a_1 b_1 + a_2 b_2 + \ldots + a_n b_n$$

The angle between \vec{a} and \vec{b} is denoted by θ and is calculated by the following formula:

$$\theta = \cos^{-1}\left(\frac{\vec{a} \cdot \vec{b}}{|\vec{a}| \cdot |\vec{b}|}\right)$$

The angle is calculated in any angular mode. When calculated in degrees, decimal degrees are assumed.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	00	STO + 2	11-23 51 2
ENTER+	01– 31	GTO 00	12- 13 00
g x ²	02– 15 0	RCL 2	13– 24 2
STO + 1	03-23 51 1	RCL 0	14- 24 0
R+	04– 22	RCL 1	15- 24 1
Xty	05– 21	×	16– 61
ENTER+	06- 31	f /x	17- 14 0
g <u>x</u> ²	07– 15 0	÷	18– 71
STO + 0	08-23510	9 Cos-1	1 9 – 15 8
R+	09– 22	бто 00	20- 13 00
×	10– 61		

REGISTERS					
$R_0 \Sigma a_i^2$	$R_1 \Sigma b_i^2$	$R_2 \Sigma a_i b_i$	R ₃		
R ₄ R ₅ R ₆ R ₇					

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STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Initialize		f REG f PRGM	
3	Perform for $i = 1, \dots, n$:			
	Key in a_i and b_i	a _i	ENTER+)	
		b _i	R/S	
4	Find norm of \vec{a}		RCL 0 f 7	a
5	Find norm of $\vec{\mathbf{b}}$		RCL 1 fr	b
6	Find $ \vec{a} \cdot \vec{b} $		RCL 2	a · b
7	Calculate angle between			
	\vec{a} and \vec{b}		GSB 13	θ

Example:

Let $\vec{a} = (2, 5, 2)$ and $\vec{b} = (3, 3, -4)$

Solution:

 $\begin{vmatrix} \dot{a} \\ \dot{b} \end{vmatrix} = 5.7446$ $\begin{vmatrix} \dot{b} \\ \dot{b} \end{vmatrix} = 5.8310$ $\dot{a} \cdot \vec{b} = 13.0000$ $\theta = 67.1635$

Keystrokes	Display	
f REG f PRGM 2 ENTER+) 3 R/S 5 ENTER+) 3 R/S 2 ENTER+) 4 CHS		
R/S	5 7440	
	5.7440	
RCL 1 fr	5.8310	b
RCL 2	13.0000	$ \vec{a} \cdot \vec{b} $
GSB 13	67.1635	θ

Discounted Cash Flow: Net Present Value, Internal Rate of Return

The primary purpose of this program is to compute the net present value of a series of cash flows. In general, an initial investment V_0 is made in some enterprise which is expected to bring in periodic cash flows $C_1, C_2, ..., C_n$. Given a discount rate i, which must be entered as a decimal, then for each cash flow C_k , the program will compute the net present value at period k, NPV_k. A negative value for NPV_k indicates that the enterprise has not yet been profitable. A positive NPV_k means that the enterprise has been profitable, to the extent that a rate of return i on the original investment has been exceeded.

The program may also be used iteratively to calculate an internal rate of return. The objective here is to find the discount rate i which will make the final net present value, NPV_n , equal to zero. The procedure, then, is to store V_0 and a first guess at the rate of return i, input the cash flows C_1 through C_n , and thus find NPV_n . If NPV_n is negative, the estimated rate of return was too high; if NPV_n is positive, the estimate for i was too low. Adjust the estimate for i accordingly, store the new i, and input the cash flows again. Inspect the new value of NPV_n to obtain a new estimate for i and repeat the process. The entire procedure is repeated until NPV_n is zero, or very close to it. The last value of i input is then regarded as the internal rate of return.

Each figure for net present value is found by

$$NPV_k = V_0 + \sum_{j=1}^k \frac{C_j}{(1 + i)^j}$$

This program employs the convenient sign convention used in the most recent HP calculators and programs. Cash received is represented by a positive value (+). Cash paid out is represented by a negative value (-).

KEY ENTRY	DISPLA	Y	KEY ENTRY	DIS	PLAY
f CLEAR PRGM	00		STO 3	12-	23 3
RCL 1	01- 24	1	R/S	13-	74
1	02-	1	RCL 2	14-	24 2
STO 4	03– 23	4	RCL 4	15–	24 4
+	04–	51	1	16-	1
STO 2	05– 23	2	+	17-	51
÷	06–	71	STO 4	18–	23 4
RCL 0	07– 24	0	fyx	19–	14 3
+	-80	51	÷	20-	71
RCL 4	09– 24	4	RCL 3	21-	24 3
f PAUSE	10- 14	74	+	22-	51
Xzy	11-	21	бто 09	23-	13 09

REGISTERS			
$R_0 V_0$	R₁i	$R_{2}(1 + i)$	$R_3 NPV_k$
R₄ k	R₅	R ₆	R ₇

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program			
2	Store initial investment and			
	discount rate			
	Initial investment	V _o *	STO 0	
	Interest rate	i (decimal)	STO 1	
3	Perform for $k = 1$,, n:		f PRGM	
	Input $C_{\mathbf{k}}$ cash flow and			
	compute NPV_k	С _к *	R/S	(k)
				NPV _k *
4	For a new case, go to step 2.			
	* Note: Cash received is re-			
	presented by a positive			
	value (+). Cash paid out is			
	represented by a negative			
	value (-).			

Example:

You are contemplating installing a processing machine for \$150,000 at a capital cost of 10% after taxes. Based on the following cash flows, will this investment be profitable?

Year	Cash Flow
1	\$30,000
2	26,300
3	50,000
4	55,600
5	45,200

Keystrokes	Display	
f FIX 2		
15 CHS EEX 4		
STO 0		
0.1 STO 1 F PRGM		
3 EEX 4 R/S	-122,727.27	1 st year
26300 R/S	-100,991.74	2 nd year
5 EEX 4 R/S	-63,426.00	3 rd year
55600 R/S	-25,450.45	4 th year
45200 R/S	2,615.20	5 th year

Since C_5 is positive the investment is profitable to the extent that the cost of capital is 10%.

Compound Amount



This program applies to an amount of principal that has been placed into an account and compounded periodically, with no further deposits. The important variables in this case are the number of compounding periods n, the periodic interest rate i, the principal or present value PV, the future value of the account FV, and the amount of interest accrued I. Any of these may be calculated from the others by these formulas:

$$n = \frac{\ln |FV/PV|}{\ln (1 + i)}$$
$$i = \left| \frac{FV}{PV} \right|^{1 n} - 1$$
$$PV = -FV (1 + i)^{-n}$$
$$FV = -PV (1 + i)^{n}$$
$$= -PV [(1 + i)^{n} - 1]$$

I

where: n = total number of periods i = periodic interest rate (expressed as decimal) i.e., an annual interest rate of 6% is expressed as 0.06, which is a monthly rate of $\frac{0.06}{12} = 0.005$ PV = present value (value at beginning of first period) FV = future value (value at end of last period)

This program employs the convenient sign convention used in the most recent HP calculators and programs. Cash received is represented by a positive value (+). Cash paid out is represented by a negative value (-).

KEY ENTRY	DISPLA	(KEY ENTRY	DIS	SPLAY
	00		RCL 5	24-	24 5
RCL 5	01– 24	5	СНS	25-	32
RCL 4	02- 24	4	×	26-	61
÷	03–	71	бто 00	27–	13 00
9 ABS	04– 15	34	GSB 44	28 –	12 44
f LN	05– 14	1	RCL 1	29 –	24 1
GSB 44	06– 12	44	fyx	30 –	14 3
f LN	07– 14	1	RCL 4	31–	24 4
÷	-80	71	СНЅ	32-	32
бто 00	0 9 – 13	00	×	33–	61
RCL 5	10– 24	5	бто 00	34–	13 00
RCL 4	11– 24	4	GSB 44	35–	12 44
÷	12-	71	RCL 1	36 –	24 1
9 ABS	13– 15	34	fyx	37–	14 3
RCL 1	14– 24	1	1	38 –	1
9 1/x	15– 15	3	-	39 –	41
fyx	16- 14	3	RCL 4	40-	24 4
1	17-	1	СНS	41-	32
	18–	41	×	42-	61
GTO 00	1 9 – 13	00	бто 00	43-	13 00
GSB 44	20- 12	44	RCL 2	44–	24 2
RCL 1	21- 24	1	1	45-	1
СНЅ	22-	32	+	46 –	51
fyx	23– 14	3	9 RTN	47-	15 12

REGISTERS			
R₀	R₁ n	R₂i	R ₃
R₄ PV	R₅ FV	R ₆	R ₇

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	To compute number of			
	periods	i (decimal)	STO 2	
		PV*	STO 4	
		FV*	STO 5	
			GSB 01	n
3	To compute periodic interest			
	rate	n	STO 1	
		PV*	STO 4	
		FV*	STO 5	
			GSB 10	i (decimal)
4	To compute principal	n	STO 1	
		i (decimal)	STO 2	
		FV*	STO 5	
			GSB 20	PV
5	To compute future value	n	STO 1	
		i (decimal)	STO 2	
		PV*	STO 4	
			GSB 28	FV
6	To compute accrued interest	n	STO 1	
		(i decimal)	STO 2	
		PV*	STO 4	
			GSB 35	Ι
7	For a new case, go to step 2,			
	3, 4, 5, or 6.			
	* Note: Cash received is re-			
	presented by a positive value			
	(+). Cash paid out is repre-			
	sented by a negative value $(-)$.			

Example 1:

Find the rate of return on \$1000 compounded quarterly if it amounts to \$1500 in 5 years.

Note:

n = 20

Keystrokes	Display	
20 STO 1		
1000 CHS STO 4		
1500 STO 5 GSB	10 0.0205	(quarterly)
4 🗙	0.0819	(8.19% annually)

Example 2:

How much will you need to invest today at 534% compounded quarterly to have \$3000 in 5 years?

Note:

n = 20

Keystrokes:	Display
f FIX 2	
20 STO 1	
.0575 ENTER+	
4 ÷ (STO) 2	
3000 STO 5 GSB 20) -2,255.02 (\$)



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