HEWLETT-PACKARD

HP-34C APPLICATIONS



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HP-34C

Applications

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Introduction

Congratulations on owning an HP-34C. We know you will be pleased with its quality, versatility and ease of use. Its programmable capability and powerful built-in functions combined with Continuous Memory make it a uniquely useful calculator.

This applications book is designed to help you get the best from your calculator. It provides programs to give you answers to "real world" problems, as well as games and other programs of general interest.

The programs include interesting techniques which you may find useful in writing your own software. We are confident you will find this book useful and we welcome your comments and suggestions.

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A Word About Program Usage

Each program is accompanied by a brief description of the problem, the applicable equations, a listing of program keystrokes, a set of instructions for using the program and one or more example problems, showing the actual keystrokes required for the solution.

Program listings are provided in the following format: (This example is from *Curve Fitting*, the first program in this book.)

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	бто 6	026- 22 6
h LBL A	001 - 25, 13, 11	f Σ+	027- 14 74
	002- 14 33	бто 9	028- 22 9
f FIX 2	003-14,11, 2	h LBL 6	029-25,13, 6
ENTER+	004 - 31	9 Σ-	030- 15 74
ENTER+	005- 31	h CF 2	031 - 25, 61, 2
6	006- 6	бто 9	032- 22 9
+	007- 51	h LBL B	033 - 25, 13, 12

The leftmost column, headed KEY ENTRY, shows the keys which must be pressed to enter the program into program memory. All the key designations are identical with the way they appear on your keyboard. The second column, headed DISPLAY, shows the appearance of the display on the calculator as you key in the program. The first three numerals on the left are the line number, followed by a dash, then the numeric keycode corresponding to the keystrokes in the KEY ENTRY column. Storage register contents are shown at the end of the program listing. The USER INSTRUCTIONS form is your guide to using the program to solve your own problem. The first column, labeled STEP, gives the instruction step number. Steps are executed in sequential order except where otherwise noted. the INSTRUCTIONS column gives instructions and comments concerning the operations to be performed. The INPUT DATA/UNITS column specifies the input data to be supplied, and, if applicable, the units of the data. Data input keys consist of 0 thru 9 and decimal point (the numeric keys), **EEX** (enter exponent) and **CHS** (change sign). The KEYS column specifies the keys to be pressed after keying in the corresponding input data. The OUTPUT DATA/UNITS column specifies intermediate and final outputs and, where applicable, their units.

The form is illustrated below for the same program, Curve Fitting.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program.			
2	Select the type of curve fit:			
	Exponential	1	A	1.00
	Logarithmic	2	A	2.00
	Power	3	A	3.00
3	Input x, value	x i	ENTER+	
	and y _i value.	y i	R/S	i
	(Repeat step 3 for all			
	data points.)			
4	Calculate regression			
	coefficients.		В	а
			R/S	Ь
	and coefficient of determin-			
	ation.		R/S	r ²

Step 1 requires you to key in the program. Switch the HP-34C to PRGM mode, press the keys f CLEAR **PRGM** and key in the program steps as shown on the complete listing. Then switch the calculator to RUN mode and proceed with the USER INSTRUCTIONS.

Step 2 asks you to select the type of curve fit desired and input a corresponding code number. Key in the desired code number and press Step 3 requests input of pairs of x- and y-values. Each x-value is keyed in and ENTER is pressed. Then the y-value is keyed in and **R/S** is pressed. This procedure is repeated until all pairs of values have been input.

Step 4 calculates the regression coefficients. The user presses **B** and sees the regression coefficient, a, displayed. Pressing **R/S** displays coefficient b. Press **R/S** to display r^2 , the coefficient of determination.

Mathematics

Curve Fitting

Your HP-34C calculator is equipped with a powerful built-in function, linear regression, **L.R.**, which quickly and conveniently fits data to a straight line. (Refer to your HP-34C Owner's Handbook and Programming Guide for full details.)

This capability is used here in a program to fit data to other types of curves:

- 1. Exponential curves; $y = ae^{bx}$ (a > 0)
- 2. Logarithmic curves; $y = a + b \ln x$
- 3. Power curves; $y = ax^{b}$ (a > 0)

which may be transformed to the general linear form Y = A + bX.

The regression coefficients a and b are found by solving the following system of linear equations.

$$\begin{bmatrix} n & \Sigma X_i \\ \Sigma X_i & \Sigma X_i^2 \end{bmatrix} \begin{bmatrix} A \\ b \end{bmatrix} = \begin{bmatrix} \Sigma Y_i \\ \Sigma (Y_i X_i) \end{bmatrix}$$

The relations of the variables are defined as the following:

Regression	Α	X,	Y i	Code
Exponential	ln <i>a</i>	x _i	Iny _i	1
Logarithmic	a	Inx _i	Yi	2
Power	Ina	Inx _i	Iny _i	3

The coefficient of determination is:

$$r^{2} = \frac{A\Sigma Y_{i} + b\Sigma X_{i} Y_{i} - \frac{1}{n} (\Sigma Y_{i})^{2}}{\Sigma (Y_{i}^{2}) - \frac{1}{n} (\Sigma Y_{i})^{2}}$$

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The type of curve fit to be run is determined before data input begins by inputting the code number.

The coefficient of determination indicates the quality of fit achieved by the regression. Values of r^2 close to 1.00 indicate a better fit than values close to zero. The regression coefficients *a* and *b* define the curve generated, according to the equations at the beginning of this discussion.





Remarks:

- The program applies the least squares method, either to the original equations (logarithmic curve) or to the transformed equations (exponential curve and power curve).
- Negative and zero values of x_i will cause a machine error for logarithmic curve fits. Negative and zero values of y_i will cause a machine error for exponential curve fits. For power curve fits both x₁ and y₁ must be positive, non-zero values.
- As the differences between x and/or y values become small, the accuracy of the regression coefficients will decrease.
- During operation of the program all storage registers are cleared. Any data stored in extra registers will therefore be destroyed.

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	бто б	026- 22 6
h LBL A	001 - 25, 13, 11	f Σ+	027- 14 74
	002- 14 33	бто 9	028- 22 9
f FIX 2	003-14, 11, 2	h LBL 6	029-25, 13, 6
ENTER+	004– 31	9 Σ-	030- 15 74
ENTER+	005- 31	h CF 2	031 - 25, 61, 2
6	006- 6	бто 9	032- 22 9
Ŧ	007– 51	h LBL B	033 - 25, 13, 12
STO f I	008 - 23, 14, 23	h L.R.	034- 25 6
9 R+	009- 15 22	h F? 0	035-25, 71, 0
h SF O	010-25, 51, 0	9 e ×	036- 15 1
h SF 1	011 - 25, 51, 1	R/S	037- 74
GTO f I	012 - 22, 14, 23	XEY	038- 21
h LBL 7	013–25, 13, 7	(R/S)	039- 74
h CF 1	014 - 25, 61, 1	h r	040- 25 5
бто 9	015- 22 9	9 x ²	041– 15 3
h LBL 8	016-25, 13, 8	h RTN	042 - 25 12
h CF 0	017–25, 61, 0	h [BL] 0	043 - 25, 13, 0
h LBL 9	018–25, 13, 9	h SF 2	044 - 25, 51, 2
R/S	019– 74	бто 9	045- 22 9
h F? 0	020-25, 71, 0	h [LBL] 1	046 - 25, 13, 1
f LN	021– 14 1	h F? 1	047 - 25, 71, 1
(X & Y	022 - 21	f LN	048- 14 1
h F? 1	023 - 25, 71, 1	h ŷ	049- 25 4
f LN	024 - 14 1	h F? 0	050 - 25, 71, 0
h F? 2	025 - 25, 71, 2	9 <i>e</i> ^x	051 - 15 1

	I Code + 6		
R₀ n	$R_1 \Sigma X_i$	$R_3 \Sigma Y_i$	
$R_4 \Sigma Y_i^2$	$R_5 \Sigma X_i Y_i$	$R_6 - R_{.9}$ Unused	

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program			
2	Select the type of curve fit:			
	Exponential	1	A	1.00
	Logarithmic	2	A	2.00
	Power	3	A	3.00
3	Input x_i value and y_i value.	xi	ENTER+	
		y i	(R/S)	i
	(Repeat step 3 for all data			
	points)			
4	Calculate regression coef-			
	ficients		В	а
			R/S	b
	and coefficient of determin-			
	ation.		R/S	<u>r</u> 2
5	Make projection of new \hat{y} for			
	a known x value.	x	GSB 1	ŷ
	(Repeat step 5 for all x			
	values of interest.)			
6	Error Deletion:			
	Erroneous inputs at step 3 may		GSB ()	
	be corrected by pressing	x _i err	ENTER+	
	GSB 0 and reinputting the	y, err	R/S	<i>i</i> -1
	erroneous data. Then return to			
	step 3 and enter the correct			
	data.			

Example 1:

(Exponential, Code = 1)

X :	.72	1.31	1.95	2.58	3.14
y i	2.16	1.61	1.16	.85	0.5

Solution:

$$a = 3.45, b = -0.58$$

 $y = 3.45 e^{-0.58x}$
 $r^2 = 0.98$

Keystrokes:

Display:

1 A	1.00
.72 ENTER+ 2.16 R/S	
1.31 ENTER+ 1.61 R/S	
1.95 ENTER+ 1.16 R/S	
2.58 ENTER+ .85 R/S	
3.14 ENTER+ .5 R/S	
В	3.45 <i>a</i>
R/S ·	-0.58 b
R/S	0.98 r^2
1.5 GSB 1	1.44 ŷ

Example 2:

(Logarithmic, Code = 2)

x i	3	4	6	10	12
y i	1.5	9.3	23.4	45.8	60.1

Solution:

a = -47.02, b = 41.39 $y = -47.02 + 41.39 \ln x$ $r^{2} = 0.98$ For $x = 8, \hat{y} = 39.06$ For $x = 14.5, \hat{y} = 63.67$

Example 3:

 $(Power, Code = 3) \\ x_i \quad 10 \quad 12 \quad 15 \quad 17 \quad 20 \quad 22 \quad 25 \quad 27 \quad 30 \quad 32 \quad 35 \\ y_i \quad 0.95 \quad 1.05 \quad 1.25 \quad 1.41 \quad 1.73 \quad 2.00 \quad 2.53 \quad 2.98 \quad 3.85 \quad 4.59 \quad 6.02 \\$

Solution:

$$a = .03, b = 1.46$$

$$y = .03x^{1.46}$$

$$r^2 = 0.94$$

For $x = 18, \hat{y} = 1.76$
For $x = 23, \hat{y} = 2.52$

Hyperbolic Functions

This program calculates the hyperbolic functions and their inverses with special algorithms that provide excellent accuracy. Calculation of the hyperbolic functions, as defined below, will yield errors in many instances for small arguments (i.e., x < 0.5) due to roundoff errors. However, this program has been specially written to avoid these errors and should provide accurate answers to better than eight significant figures.

Equations:

Hyperbolic Functions

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Inverse Hyperbolic Functions

$$\sinh^{-1} x = \ln \left[x + (x^{2} + 1)^{\frac{1}{2}} \right]$$
$$\cosh^{-1} x = \ln \left[x + (x^{2} - 1)^{\frac{1}{2}} \right] \quad x \ge 1$$
$$\tanh^{-1} x = \frac{1}{2} \ln \left[\frac{1 + x}{1 - x} \right] \qquad x^{2} < 1$$
$$\operatorname{csch}^{-1} x = \sinh^{-1} \left[\frac{1}{x} \right] \qquad x \ne 0$$
$$\operatorname{sech}^{-1} x = \cosh^{-1} \left[\frac{1}{x} \right] \qquad 0 < x \le 1$$
$$\operatorname{coth}^{-1} x = \tanh^{-1} \left[\frac{1}{x} \right] \qquad x^{2} > 1$$

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	GSB 2	029- 13 2
h LBL A	001 - 25, 13, 11	+	030- 71
h CF 1	002 25, 61, 1	h LBL 7	031 - 25, 13, 7
h CF 0	003 - 25, 61, 0	h F? 1	032 - 25, 71, 1
STO f I	004 - 23, 14, 23	h 1/x	033- 25 2
g R+	005- 15 22	R/S	034 – 74
GTO f I	006 - 22, 14, 23	h LBL O	035-25, 13, 0
h LBL 4	007 - 25, 13, 4	ENTER+	036 - 31
h LBL 5	008 - 25, 13, 5	h ABS	037- 25 34
h LBL 6	009-25, 13, 6	·	038 - 73
h SF 1	010-25, 51, 1	5	039- 5
9 DSE	011- 15 23	f x ≤y	040- 14 41
9 DSE	012- 15 23	бто 8	041– 22 8
9 DSE	013- 15 23	9 R+	042- 15 22
GTO f I	014 - 22, 14, 23	9 e×	043- 15 1
h LBL 1	015–25, 13, 1	f LN	044– 14 1
h SF O	016-25, 51, 0	9 <u>x=0</u>	045- 15 71
GSB 0	017- 13 0	бто 9	046- 22 9
h CF 0	018–25, 61, 0	1	047 – 1
бто 7	019- 22 7	h LST X	048- 25 0
h LBL 2	020-25, 13, 2	Ξ	049- 41
GSB 2	021– 13 2	h LST X	050- 25 0
бто 7	022- 22 7	9 R+	051- 15 22
h LBL 3	023 - 25, 13, 3	÷	052 – 71
<u>(sto</u> 0	024– 23 0	÷	053 – 71
h SF O	025-25, 51, 0	СНЗ	054 – 32
GSB 0	026- 13 0	•	055- 73
h CF 0	027 - 25, 61, 0	5	056- 5
RCL 0	028- 24 0	ENTER+	057- 31

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
f R+	058- 14 22	GTO f I	087 - 22, 14, 23
+	059– 71	h LBL 4	088-25, 13, 4
+	060 - 51	h LBL 5	089-25, 13, 5
×	061 - 61	h LBL 6	090-25, 13, 6
h RTN	062 - 25 12	h 1/x	091– 25 2
h LBL 9	063 - 25, 13, 9	9 DSE	092 - 15 23
XZY	064 - 21	9 DSE	093 - 15 23
h RTN	065- 25 12	9 DSE	0 9 4 – 15 23
h LBL 8	066 - 25, 13, 8	GTO f I	095 - 22, 14, 23
9 R+	067- 15 22	h [LBL] 1	096 - 25, 13, 1
+	068 - 71	GSB 4	097- 13 4
h LST X	069- 25 0	9 x²	098- 15 3
h LBL 2	070-25, 13, 2	ENTER+	099- 31
9 e ×	071- 15 1	ENTER+	100- 31
h LST X	072- 25 0	1	101– 1
СНЗ	073 - 32	+	102 – 51
9 e×	074- 15 1	f 🗐	103- 14 3
h F? 0	075-25, 71, 0	1	104– 1
СНЗ	076- 32	+	105– 51
+	077– 51	+	106– 71
2	078 - 2	+	107– 51
+	079– 71	GSB 0	108- 13 0
h F? ()	080-25, 71, 0	h F? 1	109–25, 71, 1
×	081 - 61	СНS	110- 32
h RTN	082- 25 12	h RTN	111- 25 12
h LBL B	083 - 25, 13, 12	h LBL 3	112-25, 13, 3
h CF ()	084 - 25, 61, 0	GSB 4	113- 13 4
STO f I	085-23, 14, 23	ENTER+	114- 31
9 R+	086- 15 22	1	115– 1

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
XZY	116- 21	1	141– 1
—	117- 41	f	142- 14 51
÷	118- 71	GTO 0	143- 22 0
ENTER+	119– 31	+	144- 51
+	120- 51	f LN	145- 14 1
GSB ()	121- 13 0	h RTN	146- 25 12
h F? 1	122-25, 71, 1	h LBL (147–25, 13, 0
CHS	123 - 32	+	148- 51
2	124- 2	f LN	149- 14 1
÷	125– 71	h LST X	150- 25 0
h RTN	126- 25 12	1	151– 1
h LBL 2	127–25, 13, 2	-	152- 41
1	128- 1	9 x ≠0	153- 15 61
—	129- 41	÷	154– 71
ENTER+	130- 31	×	155- 61
ENTER+	131– 31	g <u>x=0</u>	156- 15 71
ENTER+	132- 31	Xzy	157– 21
2	133- 2	h RTN	158- 25 12
+	134– 51	h LBL 4	159–25, 13, 4
×	135- 61	h CF 1	160-25, 61, 1
f IX	136- 14 3	9 x<0	161– 15 41
+	137- 51	h sf 1	162-25, 51, 1
h LBL O	138–25, 13, 0	h ABS	163- 25 34
ENTER+	139– 31	ENTER+	164- 31
ENTER+	140- 31		

	REGISTERS	I Control
R₀ x	R₁—R₅ Unused	

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program.			
2	For hyperbolics go to step 3,			
	for inverse hyperbolics go to			
	step 4.			
	HYPERBOLIC FUNCTIONS:			
3	Key in the argument and the			
	code:	x	ENTER+	
	• hyperbolic sine (code= 1)	1	A	sinh x
	• hyperbolic cosine (code=2)	2	A	cosh x
	• hyperbolic tangent (code=3)	3	A	tanh x
	 hyperbolic cosecant 			
	(code=4)	4	A	csch x
	• hyperbolic secant (code= 5)	5	A	sech x
	hyperbolic cotangent			
	(code=6)	6	A	coth x
	INVERSE HYPERBOLIC			
	FUNCTIONS:			
4	Key in the argument and			
	the code:	x	ENTER+	
	• inverse hyperbolic sine			
	(code= 1)	1	В	sinh⁻¹ <i>x</i>
	• inverse hyperbolic cosine			
	(code=2)	2	В	cosh⁻¹ <i>x</i>
	• inverse hyperbolic tangent			
	(code=3)	3	В	tanh⁻¹ <i>x</i>
	• inverse hyperbolic cosecant			
	(code=4)	4	В	csch⁻¹x
	• inverse hyperbolic secant			

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
	(code=5)	5	В	sech⁻¹ <i>x</i>
	• inverse hyperbolic cotangent			
	(code=6)	6	В	coth⁻¹ <i>x</i>

Example 1:

Evaluate the following hyperbolic functions:

sinh 2.5; cosh 3.2; tanh 1.9; csch (-0.25); coth (-2.01). Also, evaluate sinh x and compare to $\frac{e^x - e^{-x}}{2}$ where $x = 1.2345 \times 10^{-8}$.

Keystrokes:	Display:	
2.5 ENTER+ 1 A	6.0502	sinh 2.5
3.2 ENTER+ 2 A	12.2866	cosh 3.2
1.9 ENTER+ 3 A	0.9562	tanh 1.9
.25 CHS ENTER+ 4 A] -3.9586	csch (-0.25)
2.01 CHS ENTER+		
6 A	-1.0366	coth (-2.01)
1.2345 EEX CHS 8		
ENTER+ 1 A	1.2345-08	$\sinh (1.2345 \times 10^{-8})$
1.2345 EEX CHS		
$8 g e^{x} h LST x$		
СНЅ 9 ех -		
2 ÷	1.2150-08	incorrect due to round-off

Example 2:

Evaluate the following inverse hyperbolic functions:

sinh⁻¹ (2.4); cosh⁻¹ (90); tanh⁻¹ (-0.65); sech⁻¹ (0.4); coth⁻¹ (3.4).

Keystrokes:	Display:	
2.4 ENTER+ 1 B	1.6094	$\sinh^{-1}(2.4)$
90 ENTER+ 2 B	5.1929	$\cosh^{-1}(90)$
.65 CHS ENTER+ 3 B	-0.7753	$\tanh^{-1}(-0.65)$
.4 ENTER+ 5 B	1.5668	$\operatorname{sech}^{-1}(0.4)$
3.4 ENTER+ 6 B	0.3031	$\operatorname{coth}^{-1}(3.4)$

Polynomial Evaluation

This program performs several useful operations on polynomial functions of the form

$$f(x) = a_0 + a_1 x + a_2 x^2 \dots + n_{n-1} x^{n-1} + a_n x^n$$

where the order, n, of the polynomial is 9 or less.

The following operations may be accomplished:

Evaluation of f(x):

The value, f(x), may be calculated for a known value of x.

Zeros of f(x):

The real zeros of the polynomial (values of x for which f(x) = 0) may be found. This operation uses the **SOLVE** operation of the HP-34C.

Find x for a given value of f(x):

The real values of x satisfying the polynomial for a given value of f(x) may be found. This operation also uses the **SOLVE** operation of the HP-34C.

Definite integral of f(x):

The definite integral, $\int_a^b f(x) dx$, of the polynomial f(x), between the limits *a* and *b* may be evaluated. This operation uses the *f* operation built into the HP-34. (See remarks below.)

Remarks:

This program illustrates basic but valuable ways in which the SOLVE function may be used. The program is useful for all polynomials up to order 9, having real coefficients. It can easily be expanded for use with higher order polynomials or altered for use on other types of functions.

- Since the integral of a polynomial can be readily written in closed form and easily evaluated, it is not really necessary to use the powerful INTEGRATE, [7], capability of the HP-34. It is used here primarily for illustrative purposes.
- The user is urged to consult the discussion in the owner's handbook on the use of the **SOLVE** and **[75]** capabilities for a more thorough understanding of their usefulness and limitations.
- The program will not solve for complex zeros. If it is unsuccessful in finding a real zero, **Error 4** will be displayed.

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KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	h SF O	029-25, 51, 0
h LBL O	001–25, 13, 0	f /3 3	030 - 14, 72, 3
STO • 1	002- 23.1	R/S	031– 74
STO f I	003–23, 14, 23	h LBL 1	032-25, 13, 1
h LBL 8	004-25, 13, 8	f FIX 4	033-14, 11, 4
R/S	005- 74	h CF O	034–25, 61, 0
STO (f) (ii)	006-23, 14, 24	STO • 0	035- 23.0
9 DSE	007- 15 23	9 R+	036- 15 22
бто 8	008- 22 8	f Solve 3	037–14, 73, 3
R/S	009- 74	R/S	038- 74
RCL • 1	010- 24.1	бто 7	039- 22 7
STO f I	011 - 23, 14, 23	h LBL 3	040 - 25, 13, 3
9 R+	012- 15 22	RCL f (i)	041 - 24, 14, 24
STO 0	013- 23 0	×	042- 61
(R/S)	014– 74	9 DSE	043- 15 23
h LBL A	015–25, 13, 11	h LBL 9	044–25, 13, 9
f FIX 4	016- 14, 11 4	RCL f (i)	045 - 24, 14, 24
h sf 0	017-25, 51, 0	+	046 - 51
ENTER+	018- 31	×	047– 61
ENTER+	019– 31	9 DSE	048- 15 23
ENTER+	020- 31	бто 9	049- 22 9
бто З	021– 22 3	RCL 0	050- 24 0
h LBL B	022 - 25, 13, 12	+	051 – 51
f FIX 4	023-14, 11, 4	RCL • 1	052- 24.1
h sf 0	024-25, 51, 0	STO f I	053 - 23, 14, 23
f SOLVE 3	025 - 14, 73, 3	9 R+	054- 15 22
R/S	026- 74	h F? ()	055-25, 71, 0
бто 7	027- 22 7	h RTN	056- 25 12
h LBL 2	028 - 25, 13, 2	RCL • 0	057- 24.0

KEY ENTRY	DISPLAY		KEY ENTRY	DISPLAY
—	058 -	41		

	I Control		
$R_0 a_0$	R ₁ a ₁	R₂ a₂	R ₃ a ₃
R₄ a₄	R₅ a₅	R ₆ a ₆	R ₇ a ₇
R ₈ a ₈	R ₉ a ₉	R _{.0} f(x)	R _{.1} n
R.2-R.9 Unused			

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program.			
2	Input the order of the poly-			
	nomial (value of largest			
	exponent).	n	GSB 0	n
3	Input coefficients starting with			
	an	an	R/S	an
	(Repeat until all a_n through a_0			
	are entered)	a _{n-1}	R/S	a _{n-1}
		:		
		a _o	R/S	a _o
4	To Evaluate the Polynomial:			
	Input x and see $f(x)$. (Repeat			
	for all values of interest.)	x	A	f(x)
5	To Find a Zero of the			
	Polynomial:			
	Input two initial guesses in the			
	approximate range, for the	Guess 1	R/S	
	initial search.	Guess 2	В	a zero
	(Repeat for other zeros.)			

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STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
6	To Find x for a Given $f(x)$:			
	Input upper and lower guesses	Guess 1	R/S	
	of the expected value of x, then	Guess 2	R/S	
	input the known value of $f(x)$.	$f(\mathbf{x})$	GSB 1	x
7	To Find Integral of the			
	Polynomial:			
	Set the desired display format		f SCI N	
	to control uncertainty.* Then		or, f Eng n	
	input the lower limit of the inte-	а	ENTER+	
	gral and the upper limit of the	b	GSB 2	$\int_{b}^{a} f(x) dx$
	integral.			
	* Consult the HP-34C Owner's			
	Handbook and Programming			
	Guide for information on the			
	proper user of the display			
	format when using \int_{y}^{x}			

Example 1:

A ball is thrown straight up at a velocity of 20 meters per second, from a height of 2 meters. Neglecting air resistance, how long will it take the ball to reach the ground? The acceleration of gravity is 9.81 meters per second. From physics:

$$h(t) = x_0 + v_0 t + \frac{1}{2} at^2 = 0$$
$$= 2 + 20t + (-9.81/2)t^2 = 0$$

Keystrokes:	Display:	
2 GSB 0	2.0000	Input order, n
9.81 [CHS] [ENTER+] 2 ÷ R/S	-4.9050	Coefficient a_2
20 R/S 2 R/S 10 ENTER+ 0 B	2.0000 4.1751	Coefficients a_1, a_0 Seconds

There is also a negative root to this equation, but it is not relevant to this problem. To find it:

10 CHS ENTER+ 0 B -0.0977 Seconds

Example 2:

The standard heat of formation of ammonia (NH_3) is given as a function of Kelvin temperature by:

 $\Delta H_{\rm T}^{\,\circ} = -9140 - 7.596 \, T + 4.243 \times 10^{-3} T^2 - 0.742 \times 10^{-6} T^3 \, \text{(cal)}$

Determine the heat of formation for temperatures of 400 K and 800 K. Also, find the temperature at which the heat of formation is -12,330.39 cal.

Display:	
3.0000	
-7.4200 -07	
0.0042	
-7.5960	
-9,140.0000	
-11,547.0080	ΔH°_{400}
-12,881.1840	ΔH°_{800}
	Display: 3.0000 -7.4200 -07 0.0042 -7.5960 -9,140.0000 -11,547.0080 -12,881.1840

1000 ENTER+		
0 ENTER+	0.0000	(guess for temperature)
12330.39 Сня		
GSB 1	599.9994	Κ

 $\Delta H_{\rm T}^{\circ} = -12,330.39$ calories at approximately 600 K.

Example 3:

Find the two real roots of the equation $f(x) = 4x^4 - 8x^3 - 13x^2 - 10x + 22 = 0$. Then evaluate the area under the curve (integral of f(x)) between the roots.

Keystrokes:	Display:	
4 GSB 0	4.0000	n
4 R/S 8 CHS R/S		
13 CHS R/S		
10 CHS R/S		
22 R/S	22.0000	coefficients input
0 ENTER+ 50 B	0.8820	1 st real root
1 ENTER+ 50 B	3.1180	2 nd real root
f sci 3		
.882 ENTER+ 3.118		
GSB 2	-7.640 01	$\int_{v}^{h} f(x) dx$
XzY	9.745 -03	uncertainty about 1% max.

Annuities and Compound Amounts

This program can be used to solve a variety of problems involving money, time and interest. The following variables can be either inputs or outputs:

n, which is the number of compounding periods. (For a 30 year loan with monthly payments, $n = 12 \times 30 = 360$.)

i, which is the periodic interest rate expressed as a percent. (For other than annual compounding, divide the annual percentage rate by the number of compounding periods in a year, i.e., 8% annual interest compounded monthly equals 8/12 or 0.667%.)

PV, which is the present value of the cash flow or compound amounts.

PMT, which is the periodic payment.

FV, which is the future value of a compounded amount or a series of cash flows.

BAL, which is the balloon or remaining balance at the end of a series of payments.

Accumulated interest and remaining balance may also be computed with this program.

The program accommodates payments which are made at the beginning or end of compounding periods. Payments made at the end of compounding periods (ordinary annuity) are common in direct reduction loans and mortgages while payments at the beginning of compounding periods (annuity due) are common in leasing. For ordinary annuity press \land until 1 is displayed. For annuity due press \land until 0 is displayed.

This program uses the convention that cash outlays are input as negative, and cash incomes are input as positive.

Pressing **FCLEAR REG** provides a safe, convenient, easy to remember method of preparing the calulator for a new problem. However, it is not necessary to use **FCLEAR REG** between problems containing the same combination of variables. For instance, any number of n, i, PV, PMT, FV problems involving different numbers and/or

different combinations of knowns could be done in succession without clearing the registers. Only the values which change from problem to problem would have to be keyed in. To change the combination of variables without using **TCLEAR REG**, simply input zero for any variable which is no longer applicable. To go from n, i, *PMT*, *PV* problems to n, i, *PV*, *FV* problems, a zero would be stored (0 **STO** 4) in place of *PMT*. Table I summarizes these procedures.

Table I
Possible Solutions Using
Annuities and Compound Amounts

Allowable Applications		Applications Initial	
of Variables	Ordinary Annuity	Annuity Due	Procedure
n, i, PV, PMT (Input any three and calculate the fourth.)	Direct reduction loan Discounted notes Mortgages	Leases	Use T CLEAR REG or set BAL to zero
n, i, PV, PMT BAL (Input any four and calcu- late the fifth.)	Direct reduction loan with balloon Discounted notes with balloon	Leases with residual values	None
n, i, PMT, FV (Input any three and calculate the fourth.)	Sinking fund Periodic savings Insurance		Use ① CLEAR REG or set PV to zero
n, i, PV, FV (Input any three and calculate the fourth.)	Compound amount Savings (Annuity mode is not applicable and has no effect)		Use f CLEAR REG or set <i>PMT</i> to zero.

Equations:

$$-PV = \frac{PMT}{i} A \left[1 - (1+i)^{-n} \right] + (BAL \text{ or } FV)(1+i)^{-n}$$

where

 $A = \begin{cases} 1 & \text{ordinary annuity} \\ (1 + i) & \text{annuity due.} \end{cases}$

Remarks:

- This program uses the **SOLVE** operation to find *i*. Since this is an iterative method it will take longer than the other calculations (up to 2 minutes or more). It is quite possible to define problems which cannot be solved by the technique. Such problems usually result in an error message but may simply continue to run indefinitely.
- Problems with an interest rate of 0 will give an "Error 0" display.
- Problems with *extremely* high (10⁶) or low values (10⁻⁶) for n or i may give invalid results.
- Interest problems with balloon payments of opposite sign to the periodic payments may have more than one mathematically correct answer (or no answer at all). This program may find one of the answers but has no way of finding or indicating other possibilities.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY	
	000 -	h RTN	029- 25 12	
h LBL A	001 - 25, 13, 11	h LBL 4	030 - 25, 13, 4	
f FIX 2	002 - 14, 11, 2	1	031 - 1	
h F? ()	003 - 25, 71, 0	<u>вто</u> 4	032- 23 4	
бто 7	004- 22 7	GSB 6	033- 13 6	
h SF 0	005-25, 51, 0	h 1/x	034- 25 2	
0	006- 0	RCL 3	035- 24 3	
R/S	007 - 74	GSB 8	036- 13 8	
h LBL 7	008 - 25, 13, 7	×	037- 61	
h CF 0	009-25,61, 0	СНЅ	038 - 32	
1	010- 1	[ѕто] 4	039- 23 4	
R/S	011– 74	h RTN	040- 25 12	
h LBL 1	012 - 25, 13, 1	h LBL 3	041 - 25, 13, 3	
0	013- 0	GSB 6	042- 13 6	
<u>(sto)</u> 1	014- 23 1	GSB 8	043- 13 8	
GSB 6	015- 13 6	СНS	044 – 32	
RCL 5	016- 24 5	вто 3	045- 23 3	
h LST X	017- 25 0	h RTN	046- 25 12	
-	018- 41	h LBL 5	047 - 25, 13, 5	
RCL 3	019- 24 3	GSB 6	048- 13 6	
h LST X	020- 25 0	RCL 3	049- 24 3	
+	021 - 51	+	050 - 51	
÷	022 - 71	rcl 7	051– 24 7	
СНЅ	023 - 32	+	052 - 71	
f LN	024 - 14 1	СНS	053 - 32	
RCL 6	025- 24 6	<u>вто</u> 5	054-235	
f LN	026- 14 1	h RTN	055- 25 12	
+	027 – 71	h LBL 2	056-25, 13, 2	
STO 1	028- 23 1	·	057 - 73	

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
2	058- 2	БТО 6	087- 23 6
ENTER+	059- 31	h F? ()	088-25, 71, 0
EEX	050- 33	вто 0	089- 23 0
СНS	061 - 32	RCL 1	090- 24 1
3	062- 3	СНЗ	091 - 32
h CF 1	063-25, 61, 1	h yx	092- 25 3
f SOLVE B	064 - 14, 73, 12	(сто) 7	093- 23 7
бто 7	065- 22 7	1	094– 1
бто 0	066- 22 0	XZY	095– 21
h LBL 7	067–25, 13, 7	-	096- 41
EEX	068- 33	<u>вто</u> 9	097- 23 9
2	069- 2	RCL 0	098- 24 0
×	070- 61	×	099- 61
бто 2	071- 23 2	RCL 4	100- 24 4
R/S	072– 74	RCL 8	101– 24 8
h LBL B	073–25, 13, 12	+	102– 71
бто 8	074- 23 8	STO • 0	103- 23.0
бто 9	075- 22 9	×	104– 61
h LBL 6	076-25, 13, 6	h F? 1	105–25, 71, 1
h SF 1	077-25, 51, 1	h RTN	106- 25 12
1	078- 1	GSB 8	107- 13 8
RCL 2	079- 24 2	RCL 3	108- 24 3
h %	080- 25 41	+	109– 51
STO 8	081- 23 8	CHS	110- 32
h LBL 9	082 - 25, 13, 9	h RTN	111- 25 12
RCL 8	083- 24 8	h LBL 8	112-25, 13, 8
1	084– 1	RCL 5	113- 24 5
STO 0	085- 23 0	RCL 7	114- 24 7
+	086- 51	×	115- 61

KEY ENTRY	DISPLAY		KEY ENTRY	DISPLAY
+	116-	51		

REGISTERS			I Unused
R₀i or 1 + <i>i</i>	R₁n	R₂ i(%)	R₃ PV
R₄ PMT	R₅ FV(BAL)	R ₆ 1 + <i>i</i>	$R_7(1 + i)^{-n}$
R ₈ i/100	$R_9 \left[1 - (i+i)^{-n} \right]$	R _{.0} PMT/i	R _{.1} Unused
R.2 Unused			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program.			
2	Clear the storage registers.		f CLEAR REG	
3	Set for ordinary annuity (1.00),		A	1.00
	or, for annuity due (0.00).		A	0.00
	(Press A until you see the			
	desired display.)			
4	Input the known values:			
	Number of periods	n	<u>(</u> sto) 1	n
	Periodic interest rate	i (%)	[\$то]2	i (%)
	Present value	PV	[\$то]3	PV
	Periodic payment	PMT	[sто]4	PMT
	Future value, balloon or			
	balance	FV (BAL)	[\$то]5	FV (BAL)
5	Calculate the unknown value:			
	Number of periods		GSB 1	n
	Periodic interest rate		GSB 2	i (%)
	Present value		GSB 3	PV
	Periodic payment		GSB 4	PMT
	Future value, balloon or			
	balance		GSB 5	FV (BAL)

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
6	For a new case go to step 4 and			
	change appropriate values.			
	Input zero for any value not			
	applicable in the new case.			
7	For a new problem, go to step 2.			

Example 1:

If you place \$155 in a savings account paying $5\frac{3}{6}\%$ compounded monthly, what sum of money can you withdraw at the end of 9 years?



If you desire a sum of \$275 what would be the required interest rate?

275 STO 5	275.00	
GSB 2	0.53	% monthly interest rate
12 💌	6.39	% yearly interest rate

Example 2:

You receive \$30,000 from the bank as a 30 year, 9% mortgage. What monthly payment must you make to the bank to fully amortize the mortgage?



Example 3:

Two individuals are constructing a loan with a balloon payment. The loan amount is 3,600 and it is agreed that the annual interest rate will be 10% with 36 monthly payments of 100. What balloon payment amount, to be paid coincident with the 36^{th} payment, is required to fulfill the loan agreement?

(Note the cash flow diagram below is with respect to the lender. For the borrower, the appropriate diagram will be exactly the opposite.)



(Note that the final payment is 675.27 + 100.00 = 775.27 since the final payment falls at the end of the last period.)

Example 4:

This program may also be used to calculate accumulated interest/ remaining balance for loans. The accumulated interest between two points in time, n_1 and n_2 , is just the total payments made in that period less the principal reduction in that period. The principal reduction is the difference of the remaining balances for the two points in time. The following example demonstrates the concepts above:

For a 360 month, \$50,000 loan at $9\frac{1}{2}\%$ annual interest, find the remaining balance after the 24^{th} payment and the accrued interest for payments 13–24 (between the 12^{th} and 24^{th} payments!).

First we must calculate the payment on the loan:

Keystrokes:	Display:		
f CLEAR REG 360 STO 1 9.5 ENTER+ 12 +	360.00		
STO 2	0.79		
50000 CHS STO 3	-50,000.00		
GSB 4	420.43	PMT	

The remaining balance at month 24 is:

	24	STO 1	GSB	5	49,352.76	BAL @ month 2	24
--	----	-------	-----	---	-----------	---------------	----

Store this remaining balance and calculate the remaining balance at month 12:

STO • 1	12 STO 1	
GSB 5	49,691.68	BAL @ month 12

The principal reduction between payments 12 and 24 is:

RCL • 1 - 338.92

The accrued interest is 12 payments less the principal reduction:

RCL 4 12 ×	5,045.13	Total paid out	
X & Y -	4,706.20	Accrued interest	

Example 5:

A "third party" leasing firm is considering the purchase of a minicomputer priced at \$63,000 and intends to achieve a 13% annual yield by leasing the computer to a customer for a 5-year period. Ownership is retained by the leasing firm, and at the end of the lease they expect to be able to sell the equipment for at least \$10,000. What should they establish as the monthly payment in order to realize their desired yield? (Since lease payments occur at the start of the periods, this is an annuity due problem.)



Keystrokes:	Display:	
f CLEAR REG		
A	0.00	annuity due
5 ENTER+ 12 ×		
STO 1	60.00	
13 ENTER+ 12 +		
STO 2	1.08	
63000 CHS STO 3	-63,000.00	
10000 STO 5	10,000.00	
GSB 4	1,300.16	

If the price is increased to \$70,000 what should the payments be?

70000	CHS	STO 3	-70,000.00
GSB 4			1,457.73

If the payments were increased to \$1,500 what would the yield be?

1500 Sto 4	1,500.00	
GSB 2	1.18	% per month
12 💌	14.12	% per year

Discounted Cash Flow Analysis

Two forms of discounted cash flow analysis are the net present value (NPV) approach and the internal rate of return (IRR) approach. This program calculates either NPV or IRR for up to 8 groups of cash flows.

The amount of the initial investment is input (observing the sign convention) followed by the positive or negative amounts of each group of future cash flows, and the number of times the series of cash flows occurs. The cash flows must occur at equal intervals.

After the initial investment and all cash flows have been entered, the user may: 1) Input an assumed interest rate and calculate the net present value (NPV) of the investment, or 2) Calculate the internal rate of return (IRR). The *IRR* is an interest rate that equates the present value of a set of cash flows with an initial investment. It is the interest rate that is obtained when the calculated net present value of a series of cash flows is zero. *IRR* is also called the *yield* or *discounted rate of return*.

This program uses the convention that cash outlays are input as negative, and cash incomes are input as positive.

Remarks:

- Calculation of *IRR* may take several minutes (5 or more) depending on the number of cash flow entries.
- The cash flow sequence (including the initial investment) must contain at least *one* sign change.
- Cash flows with multiple sign changes may have multiple answers. This program may find one answer but has no way of indicating other possibilities.
- The program is designed for optimum operation when 0% <*IRR* ≤ 100%. It often will solve for interest rates outside these ranges but will display *Error* messages for zero interest rates or if it is unable to find a solution.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	-	029- 41
h LBL A	001 - 25, 13, 11	STO f I	030 - 23, 14, 23
STO • 8	002- 23.8	STO • 7	031- 23.7
1	003 - 1	9 R+	032- 15 22
·	004– 73	h F? 1	033 - 25, 71, 1
0	005- 0	GTO 2	034- 22 2
1	006- 1	1	035- 1
6	007- 6	ENTER+	036- 31
STO f I	008-23, 14, 23	EEX	037- 33
XEY	009- 21	СНЗ	038 - 32
h LBL (010-25, 13, 0	3	039- 3
R/S	011– 74	f SOLVE 2	040 - 14, 73, 2
XEY	012- 21	<u>бто</u> 3	041- 22 3
STO f (i)	013 - 23, 14, 24	6 от 9	042- 22 9
9 R+	014- 15 22	h LBL 3	043 - 25, 13, 3
9 ISG	015- 15 24	EEX	044 - 33
STO f (i)	016-23, 14, 24	2	045- 2
9 ISG	017- 15 24	×	046- 61
GTO 0	018- 22 0	R/S	047- 74
R/S	019- 74	h LBL 2	048 - 25, 13, 2
h lbl 1	020 - 25, 13, 1	1	049- 1
h SF 1	021 - 25, 51, 1	+	050- 51
EEX	022 - 33	STO 0	051- 23 0
2	023- 2	0	052 - 0
+	024 - 71	h LBL 4	053 - 25, 13, 4
h LBL B	025 - 25, 13, 12	RCL 0	054- 24 0
RCL f I	026 - 24, 14, 23	RCL f (i)	055-24, 14, 24
h INT	027- 25 32	СНЗ	056- 32
1	028 - 1	h y×	057- 25 3

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
×	058- 61	RCL 0	068- 24 0
1	059– 1	1	069- 1
h LST X	060- 25 0		070- 41
-	061 - 41	÷	071– 71
9 DSE	062- 15 23	RCL • 8	072- 24.8
RCL f (i)	063-24, 14, 24	Ŧ	073- 51
×	064- 61	RCL • 7	074- 24.7
+	065- 51	STO f I	075–23, 14, 23
9 DSE	066- 15 23	g R+	076- 15 22
бто 4	067- 22 4	h CF 1	077-25,61, 1

	R	EGISTERS	I Control
$R_0 1 + i$	R ₁ CF ₁	$R_2 N_1$	$R_3 CF_2$
$R_4 N_2$	R₅ CF ₃	$R_6 N_3$	R ₇ CF₄
R ₈ N₄	R₅CF₅	R. ₀ N ₅	R _{.1} CF ₆
R.2 N6	R.3 CF7	R.4 N7	R.5 CF8
R _{.6} N ₈	R _{.7} Used	R _{.8} CF ₀	

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program.			
2	Optional: set display status			
	as desired. (suggest FIX 2.)			
3	Input the initial investment.*	INV	A	INV
4	Beginning with the first period,			
	key in each cash flow* and the			
	number of times it occurs,			
	pressing R/S after each	CF	ENTER+	
	group. (Be sure to key in 1 if	N	R/S	N
	the cash flow occurs only			
	once.)			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT Data/Units
5	Repeat step 4 until all cash			
	flows have been input. Then go			
	to step 6 for IRR or step 7 for			
	NPV.			
6	TO CALCULATE INTERNAL			
	RATE OF RETURN:		В	IRR (%)
7	TO CALCULATE NET			
	PRESENT VALUE:			
	Input the applicable periodic			
	interest (discount) rate.	i (%)	GSB 1	NPV
8	Always return to step 3 for a			
	new case or a new calculation.			
	* Be sure to observe proper sign			
	convention for initial investment			
	and cash flows.			

Example 1:

An investor pays \$80,000 for a duplex that he intends to sell after 7 years. He must spend some money the first year for repairs. At the end of the seventh year the duplex is sold for \$91,000. Will he achieve a desired 9% after tax yield with the following after tax cash flows?



Keystrokes: Display: f FIX 2 80000 [CHS] [A] -80,000.00 600 [CHS] [ENTER+] 1 **R/S** 1.00 6500 ENTER+ 1 R/S 1.00 8000 [ENTER+] 2 [R/S] 2.00 7500 [ENTER+]2 [R/S] 2.00 91000 ENTER+ 1 R/S 1.00 9 **GSB** 1 -4,108.06

Since the NPV is negative the investment does not achieve the desired 9% yield.

Example 2:

An investment of \$620,000,000.00 is expected to have the following annual income stream for the next 15 years:

Number of Years:	Cash Flow (\$):
First 10 years	100,000,000
next 5 years	5,000,000

What is the expected rate of return?

Keystrokes:	Display:	
620000000 CHS A	-620,000,000.0	
100000000 ENTER+		
10 R/S	10.00	
5000000 ENTER+		
5 R/S	5.00	
B	10.06	(annual IRR of 10.06%)

Moon Rocket Lander

Imagine for a moment the difficulties involved in landing a rocket on the moon with a strictly limited fuel supply. You're coming down tailfirst, freefalling toward a hard rock surface. You'll have to ignite your rockets to slow your descent; but if you burn too much too soon, you'll run out of fuel 100 feet up, and then you'll have nothing to look forward to but cold eternal moon rocks coming faster every second. The object, clearly, is to space your burns just right so that you will alight on the moon's surface with no downward velocity.

The game starts off with the rocket descending at a velocity of 50 feet/second from a height of 500 feet. The velocity and altitude are shown in a combined display as -50.0500, the altitude appearing to the right of the decimal point and the velocity to the left, with a negative sign on the velocity to indicate downward motion. Then the remaining fuel is displayed and the rocket fire count-down begins: "3", "2", "1", "0". Exactly at zero you may key in a fuel burn. A zero burn, which is very common, is accomplished by simply pressing [R/S]. After a burn the sequence is repeated unless:

- 1. You have successfully landed—flashing zeros.
- 2. You have smashed into the lunar surface—flashing crash velocity.

You must take care, however, not to burn more fuel than you have; for if you do, you will free-fall to your doom! The final velocity shown will be your impact velocity (generally rather high). You have 60 units of fuel initially.

Equations:

We don't want to get too specific, because that would spoil the fun of the game; but rest assured that the program is solidly based on some old friends from Newtonian physics:

$$x = x_0 + V_0 t + \frac{1}{2} at^2$$
, $V = V_0 + at$, $V^2 = V_0^2 + 2a (x - x_0)$

where:

x, V, a, and t are distance, velocity, acceleration, and time.

Remarks:

• Only integer values for fuel burn are allowed. **R/S** can be used to stop Moon Rocket Lander at any time.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000-	f FIX 0	029-14,11, 0
h LBL A	001 - 25, 13, 11	RCL 8	030- 24 8
5	002- 5	h PSE	031- 25 74
0	003- 0	3	032- 3
0	004 - 0	h PSE	033- 25 74
<u>вто</u> 6	005- 23 6	2	034- 2
5	006- 5	h PSE	035- 25 74
0	007- 0	1	036- 1
СНS	008 - 32	h PSE	037- 25 74
<u>вто</u> 7	009- 23 7	0	038- 0
6	010- 6	h PSE	039- 25 74
0	011- 0	h LBL 9	040 - 25, 13, 9
<u>(</u> 5то) 8	012- 23 8	RCL 8	041- 24 8
h LBL O	013-25, 13, 0	Xty	042- 21
RCL 6	014- 24 6	f	043- 14 51
f FIX 4	015-14,11, 4	бто 6	044- 22 6
EEX	016- 33	STO - 8	045-23,41, 8
4	017- 4	2	046- 2
÷	018- 71	×	047 - 61
RCL 7	019- 24 7	5	048 - 5
h ABS	020- 25 34	—	049- 41
+	021 – 51	<u>вто</u> 9	050- 23 9
RCL 7	022- 24 7	2	051 - 2
9 x>0	023- 15 51	÷	052 – 71
GSB 4	024- 13 4	RCL 6	053- 24 6
XEY	025- 21	+	054 – 51
СНЅ	026- 32	RCL 7	055- 24 7
h PSE	027- 25 74	+	056- 51
h PSE	028- 25 74	RCL 9	057- 24 9

KEY ENTRY	DISPLAY	KEY ENTRY DISPLAY	
STO + 7	058 - 23, 51, 7	2	075- 2
9 R+	059- 15 22	×	076- 61
<u>(5то)</u> 6	060- 23 6	STO + 7	077 - 23, 51, 7
h INT	061 - 25 32	RCL 6	078- 24 6
9 x>0	062- 15 51	1	079- 1
бто 0	063- 22 0	0	080- 0
RCL 7	064- 24 7	×	081 - 61
h LBL 7	065 - 25, 13, 7	RCL 7	082- 24 7
h PSE	066- 25 74	9 x ²	083- 15 3
бто 7	067- 22 7	+	084 - 51
h LBL 6	068 - 25, 13, 6	f IX	085- 14 3
RCL 8	069- 24 8	СНЗ	086- 32
2	070- 2	бто 7	087- 22 7
·	071 - 73	h LBL 4	088 - 25, 13, 4
5	072- 5	X & Y	089- 21
-	073- 41	СНS	090- 32
STO + 6	074 - 23, 51, 6	Xzy	091 – 21

	I Unused		
R _o	R ₁	R₂	R ₃
R₄	R₅	R ₆ X	R ₇ V
R ₈ FUEL	R ₉ ACCEL.	R _{.0} —R _{.6} Unused	

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Key in the program.			
2	Assume manual control.		A	''V.ALT''
				"FUEL"
				''3''
				''2''

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
				''1''
				·''0''
3	Key in burn:			
	Upon ''O'' display,			
	press (R/S) then		R/S	
	enter burn.	BURN	R/S	''V.ALT''
				"FUEL"
				ʻ `3 ''
				''2''
				''1''
				·'0''
4	Go to step 3 until you land			
	(flashing zeros) or crash			
	(flashing impact velocity).			
5	If you survived last landing			
	attempt, go to step 2 for another			
	try.			

Nimb

The game of Nimb begins with a collection of N objects, or as the calculator plays it, with the positive number N. Each player alternately subtracts one, two, or more from the total until only one is left. The player forced to take the last one loses.

To begin the game you specify the maximum number that can be taken in a single move. Then you tell the calculator how many objects you wish to start with (i.e., the value of N).

After each move the machine will display the remaining total. A negative sign indicates that it is the player's move next, while a positive display indicates that it is the HP-34C's move.

As the challenger you are allowed to make the first move. It is possible for you to win, but of course the HP-34C is a master player: it will not let you make an error and win. If you cheat by taking more than the specified limit the calculator will catch you and force you to repeat the move.

This program is based on an HP-25 program by James L. Horn.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	Ŧ	029- 51
h LBL A	001 - 25, 13, 11	9 x<0	030- 15 41
f FIX 0	002 14, 11, 0	бто 0	031- 22 0
STO 0	003- 23 0	RCL 3	032- 24 3
1	004 - 1	бто 1	033- 22 1
+	005- 51	h LBL (034 - 25, 13, 0
STO 1	006- 23 1	h LST X	035- 25 0
3	007- 3	1	036 - 1
5	008 – 5	f	037- 14 51
0	009- 0	бто 2	038- 22 2
7	010- 7	9 R+	039- 15 22
·	011– 73	RCL 1	040- 24 1
1	012- 1	f x ≤y	041 - 14 41
<u>вто</u> 2	013- 23 2	бто 2	042- 22 2
5	014– 5	Xzy	043 - 21
5	015- 5	STO - 0	044 - 23, 41, 0
1	016- 1	RCL ()	045- 24 0
7	017– 7	(R/S)	046- 74
8	018- 8	1	047 – 1
<u>вто</u> 3	019- 23 3	-	048 - 41
RCL 0	020- 24 0	RCL 1	049- 24 1
h LBL 1	021 – 25, 13, 1	÷	050 - 71
R/S	022 – 74	h FRAC	051 - 25 33
h LBL B	023 - 25, 13, 12	RCL 1	052- 24 1
f FIX O	024 - 14, 11, 0	×	053 - 61
STO 0	025- 23 0	9 x=0	054- 15 71
h LBL 4	026-25, 13, 4	1	055- 1
СНЗ	027 – 32	STO - 0	056-23,41, 0
R/S	028 - 74	h LBL 2	057 - 25, 13, 2

KEY ENTRY	DIS	PLAY	KEY ENTRY	DISPLAY
RCL 0	058-	24 0	RCL 2	061- 24 2
9 x≠0	059 -	15 61	f FIX 1	062 - 14, 11, 1
бто 4	060 –	22 4	GTO 1	063- 22 1

	I Unused		
R₀ Total	R_1 Max + 1	R₃ 55178	
$R_4 - R_9$ Unused			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT Data/Units
1	Key in the program.			
2	Indicate the maximum number			
	of objects which can be re-			
	moved in one move.	MAX	A	MAX
3	Indicate the total number of			
	objects with which you wish to			
	start the game, (usually 15).	N	В	-N
4	If the number in the display is			
	negative, key in your move and			
	see the number remaining.	MOVE	R/S	+ REM
5	If the number in the display is			
	positive, let the HP-34C move.		R/S	- REM
6	Do steps 4 and 5 until the			
	game is over.			
7	At the end of the game turn the			
	calculator upside down to read			
	the message.			
	If calculator loses:			I LOSE
	If calculator wins:			BLISS

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
8	For another game:			
	If max. move remains same, go			
	to step 3.			
	For different max. move go to			
	step 2.			

Example:

Starting with 15 objects, with a maximum allowable move of 3, play Nimb with the HP-34C.

Keystrokes:	Display:	
3 🖪	3.	
15 B	-15.	Ready
3 R/S	12.	Player takes 3
R/S	-9 .	HP-34C takes 3
5 (R/S)	-9 .	Player tries to cheat.
2 R/S	7.	Player takes 2
R/S	-5.	HP-34C takes 2
3 R/S	2.	Player takes 3
R/S	-1.	HP-34C takes 1
1 R/S	55178.	Player takes last one and
		loses.

Turn calculator upside down for message: BLISS

Timers

This program converts your HP-34C into a timer which can operate as 1) a count-down timer, counting down to display zero when the preset time has elapsed, or 2) a count-up timer, displaying the elapsed time since the timer was started. The upper limit of the count-up timer is approximately 10 minutes.

When using this program, you should remember that the clock circuits of the HP-34C are designed for calculator use, not for accurate timekeeping. Although the routine may be calibrated quite accurately, highly stable performance should not be expected.

Equation:

$$C_{\text{NEW}} = C_{\text{OLD}} \frac{\text{HP time}}{\text{Actual time}}$$

Remarks:

- All times are input or displayed in (H.MMSS) format.
- Your calibration constants may differ substantially from those given here.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	STO f I	029-23, 14, 23
h LBL A	001 - 25, 13, 11	0	030- 0
h CF 0	002–25, 61, 0	R/S	031– 74
f FIX 4	003 - 14, 11, 4	h LBL 7	032 - 25, 13, 7
STO 0	004- 23 0	g isg	033- 15 24
h LBL 9	005–25, 13, 9	<u>бто</u> 7	034- 22 7
0	006- 0	h LBL B	035-25, 13, 12
R/S	007 – 74	RCL f I	036 - 24, 14, 23
STO 1	008- 23 1	h INT	037- 25 32
g +H	009- 15 6	RCL 2	038- 24 2
RCL 0	010- 24 0	÷	039- 71
×	011– 61	f +H.MS	040- 14 6
h INT	012- 25 32	R/S	041 - 74
STO f I	013 - 23, 14, 23	бто 6	042- 22 6
RCL 1	014- 24 1	h LBL 1	043 - 25, 13, 1
R/S	015- 74	g •H	044 - 15 6
h LBL 8	016-25, 13, 8	XZY	045- 21
9 DSE	017- 15 23	g +H	046- 15 6
бто 8	018- 22 8	XZY	047- 21
бто 9	019- 22 9	—	048 - 41
h LBL B	020 - 25, 13, 12	RCL 1	049- 24 1
h SF 0	021 - 25, 51, 0	9 +H	050- 15 6
f FIX 4	022 - 14, 11, 4	÷	051 – 71
STO 2	023- 23 2	h 1/x	052- 25 2
h LBL 6	024 - 25 , 13, 6	h F? 0	053 - 25, 71, 0
·	025– 73	бто 0	054 - 22 0
9	026- 9	RCL 0	055- 24 0
9	027– 9	×	056 - 61
9	028 - 9	R/S	057 – 74

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
GTO A	058- 22 11	×	061 - 61
h LBL O	059-25, 13, 0	R/S	062 – 74
RCL 2	060- 24 2	GTO B	063 - 22 12

REGISTERS			I Counter
$R_0 C_d$	R₁ Time	$R_2 C_u$	R ₃ —R _{.9} Unused

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program.			
	COUNT-DOWN TIMER:			
2	Input count-down timer			
	constant (try 5600).	C _D	A	0.0000
3	Input desired time.	T (H.MMSS)	R/S	T (H.MMSS)
4	Start timer.		R/S	
5	Timer display blinks until			
	0.0000 is displayed and time			
	has elapsed.			0.0000
6	For a new time, T, go to step			
	3. To recalibrate, go to			
	step 12.			
	COUNT-UP TIMER:			
7	Input count-up timer constant			
	(try 5400).	Cu	В	0.0000
8	Start timer.		R/S	
9	After desired period has			
	elapsed, stop timer.		R/S	0.0000
10	Display the elapsed time.		В	T (H.MMSS)

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
11	Reset the timer and go to step			
	8 for another run. To recalibrate		R/S	0.0000
	the timer, go to step 14.			
12	To calibrate the count-down			
	timer, input the ending time	T _e (H.MMSS)	ENTER+	
	and the starting time and	T _s (H.MMSS)	GSB 1	C_{D} NEW
	calculate new constant.			
13	To proceed, press R/S			
	and go to step 3.		R/S	0.0000
14	To calibrate the count-up timer,			
	store the displayed elapsed	T (H.MMSS)	STO 1	T (H.MMSS)
	time. Then input the ending	T _e (H.MMSS)	ENTER+	
	time and the starting time.	T _s (H.MMSS)	GSB 1	C _u NEW
15	To proceed, press R/S and			
	go to step 8.		R/S	0.0000

Example 1:

- ----

Use the count-down time to measure an elapsed timer of 35 seconds, and another of 1 minute, 8 seconds. Try an initial calibration constant of 5600.

Keystrokes:	Display:	
5600 A	0.0000	
.0035 R/S	0.0035	Count-down time
R/S	0.0000	Time has elapsed

Suppose you recorded, from your watch, an ending time of 3:42:56 and a starting time of 3:42:23, i.e., 33 seconds elapsed. Recalibrate the timer with this information.

3.4256	ENTER+		
3.4223	GSB 1	5939.3937	$C_{D NEW}$
R/S		0.0000	

Now count-down for 1 minute, 8 seconds.

.0108	R/S	0.0108
R/S		0.0000

The true elapsed time should now be quite close to that input. If it is not, recalibrate again.

Operate the count-up timer for a known elapsed time (say 40 seconds) and recalibrate as needed. Use an initial calibration constant of 5400.

Keystrokes:	Display:	
5400 B	0.0000	
R/S		start timer
R/S	0.0000	stop timer
В	0.0039	elapsed time

True elapsed time was 40 seconds. Recalibrate:

STO 1	0.0039	
.004 ENTER+	0.0049	
0 GSB 1	5,265.0000	$C_{U NEW}$ (you may get a different number).
R/S	0.0000	Input new constant and
		reset counter

Random Number Generator

Random numbers are useful in a wide variety of applications, for example: in simulation, sampling, computer programming, numerical analysis and games.

This program includes routines to calculate:

- 1. Uniformly distributed pseudo-random numbers in the range $0 \le r \le 1$.
- 2. Uniformly distributed integers from 0 to 9.

It also includes a routine to simulate dealing from an infinite deck of cards. The Ace is 1; the Jack, 11; the Queen, 12; the King, 13. All other cards count their face value.

The random number generator:

$$r_{n+1} = FRAC(9821 \times r_n + .211327)$$

passes the spectral test (Knuth, V.2, no. 3.4) and, because its parameters satisfy Theorem A (op.cit., p. 15) it generates one million distinct random numbers between 0 and 1 regardless of the value selected for r_0 . This generator was developed by Don Malm as part of an HP-65 Users' Library program.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
	000 -	×	029- 61
h LBL A	001 - 25, 13, 11	1	030- 1
f FIX 4	002–14, 11, 4	+	031 - 51
<u>(sto</u> 0	003- 23 0	h INT	032- 25 32
GSB 0	004- 13 0	R/S	033 - 74
h LBL 3	005–25, 13, 3	бто 5	034- 22 5
GSB 9	006- 13 9	h LBL O	035-25, 13, 0
R/S	007 – 74	9	036- 9
бто З	008- 22 3	8	037- 8
h LBL B	009–25, 13, 12	2	038- 2
f FIX 0	010-14,11, 0	1	039- 1
(сто) О	011- 23 0	<u>вто</u> 1	040- 23 1
GSB 0	012- 13 0	·	041 - 73
h LBL 4	013-25, 13, 4	2	042- 2
GSB 9	014- 13 9	1	043- 1
1	015- 1	1	044 - 1
0	016- 0	3	045- 3
×	017- 61	2	046- 2
h INT	018- 25 32	7	047 - 7
R/S	019- 74	<u>вто</u> 2	048- 23 2
бто 4	020- 22 4	h RTN	049- 25 12
h lbl 1	021 - 25, 13, 1	h LBL 9	050 - 25, 13, 9
f FIX 0	022 - 14, 11, 0	RCL 0	051– 24 0
<u>вто</u> 0	023- 23 0	RCL 1	052- 24 1
GSB 0	024- 13 0	×	053 - 61
h LBL 5	025-25,13,5	RCL 2	054- 24 2
GSB 9	026- 13 9	+	055- 51
1	027- 1	h FRAC	056- 25 33
3	028- 3	вто 0	057- 23 0

	R	I Unused	
R _o r _i	R₁ 9821	R₂.211327	R ₃ —R _{.9} Unused

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program.			
2	Input a seed: any number			
	between 0 and 1.	SEED		
	For random numbers go to step			
	3. For random integers go to			
	step 5. For a simulated card			
	dealer go to step 7.			
3	To generate a random number			
	(0 ≤ r ≤ 1)		A	r,
4	For another random number.		R/S	r ₂
	Repeat step 4 as desired for			
	further random numbers.			
5	To generate random integers			
	$(0 \leq INT \leq 9).$		В	INT,
6	For another random integer.		(R/S)	INT ₂
	(Repeat step 6 as desired for			
	further random integers.)			
7	To deal cards:		GSB 1	CARD₁
8	For further cards.		R/S	CARD₂
	(Repeat step 8 as desired to			
	deal more cards.)			
9	For a new start, go to step 2 to			
	input a new seed as desired.			

Example 1:

Using an initial seed of 0.2356 generate a string of pseudo-random numbers.

Keystrokes:	Display:	
.2356 🔺	0.0389	
R/S	0.5134	
R/S	0.2538	
etc.		

Example 2:

Using an initial seed of .12345 deal a hand of 5 cards.

Keystrokes:	Display:	
.12345 GSB 1	8.	
R/S	2.	
R/S	1.	Ace
R/S	9.	
R/S	11.	Jack

Moving Average

In a moving average, a specified number of data points is averaged. When there is a new piece of input data, the oldest piece of data is discarded to make room for the latest input. This replacement scheme makes the moving average a valuable tool in following trends. The fewer the number of data points, the more trend-sensitive the average becomes. With a large number of data points, the average behaves more like a regular average, responding slowly to new input data.

This program allows for a moving average span of 1 to 17 units. The number of units, n, must be specified before any data input begins by keying it in and pressing **B**. Then the data is input by keying in each value, x_k , and pressing **A** in turn. The calculator will display the current input number, k, until at least n values have been entered. After the n^{th} value (and for all succeeding values), the calculator will flash the current input number before halting with the moving average, AVG, in the display.

The value of the average may be displayed at any time by pressing **GSB** 1. This feature allows the average to be calculated before n data points have been input. The average is based on the number of inputs or n, whichever is smaller.

Remarks:

This program clears all registers during its execution. Therefore any data stored in extra registers will be destroyed.

KEY ENTRY	DISPLAY	KEY ENTRY	DISPLAY
f CLEAR prgm	000-	9 DSE	023- 15 23
h LBL B	001 - 25, 13, 12	бто 5	024- 22 5
f FIX 2	002-14,11, 2	RCL • 8	025- 24.8
	003- 14 33	STO f I	026 - 23, 14, 23
STO • 8	004- 23.8	h LBL 5	027 - 25, 13, 5
STO f I	005-23, 14, 23	g R+	028- 15 22
R/S	006- 74	h RTN	029- 25 12
h LBL A	007 - 25, 13, 11	h [BL] 0	030-25, 13, 0
RCL • 9	008- 24.9	XEY	031– 21
1	009- 1	h PSE	032- 25 74
+	010- 51	RCL 0	033- 24 0
Xzy	011– 21	RCL • 8	034- 24.8
RCL f (i)	012 - 24, 14, 24	÷	035- 71
STO - 0	013-23,41, 0	ENTER+	036- 31
Xty	014- 21	h RTN	037- 25 12
STO f (i)	015-23, 14, 24	h [BL] 1	038 - 25, 13, 1
STO + 0	016-23,51,0	RCL 0	039- 24 0
g R+	017- 15 22	RCL • 9	040- 24.9
Xty	018- 21	RCL • 8	041 - 24 .8
STO • 9	019- 23.9	f x ≤y	042- 14 41
RCL • 8	020- 24 .8	XzY	043- 21
f x ≤y	021 - 14 41	g R+	044 - 15 22
GSB 0	022- 13 0	÷	045- 71

	R	I Control	
R ₀ Σ	R₁ Used	R₂ Used	R_3 Used
R₄ Used	R₅ Used	R ₆ Used	R ₇ Used
R ₈ Used	R₀ Used	R _{.0} Used	R _{.1} Used
R.2 Used	R _{.3} Used	R _{.₄} Used	R _{.₅} Used
R.6 Used	R _{.7} Used	R _{.8} n	R _{.9} K

STEP	INSTRUCTIONS	INPUT Data/Units	KEYS	OUTPUT Data/Units
1	Key in the program.			
2	Input number of points in the			
	average, $(1 \le n \le 17)$.	n	В	n
3	Input data point and compute			
	moving average. *	X _k	A	''k'', AVG
4	Optional: Display average at			
	any time.		GSB 1	AVG
5	For a new case, go to step 2.			
	* If an error is made in data			
	input, you must start over.			
	The average is not displayed			
	until after the n th point is			
	input.			

Example 1:

A six-period moving average is used to project monthly sales. The first 6 months of sales are as follows:

Month	1	2	3	4	5	6
Sales	125	183	207	222	198	240

Compute the moving average. Also compute the average after month three.

Keystrokes:	Display:	
6 B	6.00	
125 🔺	1.00	
183 🛋	2.00	
207	3.00	
GSB 1	171.67	(average after month three)
222 A	4.00	
198 🗖	5.00	
240	" <mark>6.00", 195.8</mark> 3	

The actual sales for the seventh month totalled 225 units. Calculate a new moving average.

225 A "7.00", 212.50



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