## HP-34C <br> APPLICATIONS



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# HEWLETT PACKARD 

## HP-34C

# Applications 

## October 1980

## Introduction

Congratulations on owning an HP-34C. We know you will be pleased with its quality, versatility and ease of use. Its programmable capability and powerful built-in functions combined with Continuous Memory make it a uniquely useful calculator.

This applications book is designed to help you get the best from your calculator. It provides programs to give you answers to "real world" problems, as well as games and other programs of general interest. The programs include interesting techniques which you may find useful in writing your own software. We are confident you will find this book useful and we welcome your comments and suggestions.

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## A Word About Program Usage

Each program is accompanied by a brief description of the problem, the applicable equations, a listing of program keystrokes, a set of instructions for using the program and one or more example problems, showing the actual keystrokes required for the solution.

Program listings are provided in the following format: (This example is from Curve Fitting, the first program in this book.)

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :---: | :---: | :---: | :---: |
| TCLEAR PRGM | 000- | GTO 6 | 026- 226 |
| ( LBL A | 001-25, 13, 11 | (t) Et | 027-1474 |
| flclear Reg | 002- 1433 | GTO 9 | 028- 229 |
| (f) FIX 2 | 003-14, 11, 2 | (b) LBL 6 | 029-25, 13, 6 |
| ENIERA | 004- 31 | (9) 5 | 030- 1574 |
| ENIER4 | 005- 31 | (b) CF 2 | 031-25, 61, 2 |
| 6 | 006- 6 | GTO 9 | 032- 229 |
| $\pm$ | 007- 51 | (b) LBL B | 033-25, 13, 12 |

The leftmost column, headed KEY ENTRY, shows the keys which must be pressed to enter the program into program memory. All the key designations are identical with the way they appear on your keyboard. The second column, headed DISPLAY, shows the appearance of the display on the calculator as you key in the program. The first three numerals on the left are the line number, followed by a dash, then the numeric keycode corresponding to the keystrokes in the KEY ENTRY column. Storage register contents are shown at the end of the program listing.

The USER INSTRUCTIONS form is your guide to using the program to solve your own problem. The first column, labeled STEP, gives the instruction step number. Steps are executed in sequential order except where otherwise noted. the INSTRUCTIONS column gives instructions and comments concerning the operations to be performed. The INPUT DATA/UNITS column specifies the input data to be supplied, and, if applicable, the units of the data. Data input keys consist of 0 thru 9 and decimal point (the numeric keys), EEX (enter exponent) and CHS (change sign). The KEYS column specifies the keys to be pressed after keying in the corresponding input data. The OUTPUT DATA/UNITS column specifies intermediate and final outputs and, where applicable, their units.

The form is illustrated below for the same program, Curve Fitting.

| STEP | INSTRUCTIONS | INPUT DATA/UNITS | KEYS | OUTPUT DATAUUNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Select the type of curve fit: |  |  |  |
|  | Exponential | 1 | (A) | 1.00 |
|  | Logarithmic | 2 | (A) | 2.00 |
|  | Power | 3 | (A) | 3.00 |
| 3 | Input $x_{\text {i }}$ value | $x_{i}$ | ENIER4 |  |
|  | and $y_{i}$ value. | $y_{i}$ | R/S | $i$ |
|  | (Repeat step 3 for all |  |  |  |
|  | data points.) |  |  |  |
| 4 | Calculate regression |  |  |  |
|  | coefficients. |  | B | a |
|  |  |  | R/S | $b$ |
|  | and coefficient of determin- |  |  |  |
|  | ation. |  | R/S | $r^{2}$ |

Step 1 requires you to key in the program. Switch the HP-34C to PRGM mode, press the keys $\ddagger$ CLEAR PRGM and key in the program steps as shown on the complete listing. Then switch the calculator to RUN mode and proceed with the USER INSTRUCTIONS.
Step 2 asks you to select the type of curve fit desired and input a corresponding code number. Key in the desired code number and press (A) Step 3 requests input of pairs of $x$ - and $y$-values. Each $x$-value is keyed in and ENTER4 is pressed. Then the y-value is keyed in and $\mathbf{R} / \mathbf{S}$ is pressed. This procedure is repeated until all pairs of values have been input.
Step 4 calculates the regression coefficients. The user presses $B$ and sees the regression coefficient, $a$, displayed. Pressing R/S displays coefficient $b$. Press R/S to display $r^{2}$, the coefficient of determination.

## Mathematics

## Curve Fitting

Your HP-34C calculator is equipped with a powerful built-in function, linear regression, L.R. , which quickly and conveniently fits data to a straight line. (Refer to your HP-34C Owner's Handbook and Programming Guide for full details.)
This capability is used here in a program to fit data to other types of curves:

1. Exponential curves; $y=a e^{\mathrm{bx}}(a>0)$
2. Logarithmic curves; $y=a+b \ln x$
3. Power curves; $y=a x^{\mathrm{b}}(a>0)$
which may be transformed to the general linear form $Y=A+b X$.
The regression coefficients $a$ and $b$ are found by solving the following system of linear equations.

$$
\left[\begin{array}{ll}
n & \Sigma X_{\mathrm{i}} \\
\Sigma X_{\mathrm{i}} & \Sigma X_{\mathrm{i}}^{2}
\end{array}\right] \quad\left[\begin{array}{l}
A \\
b
\end{array}\right]=\left[\begin{array}{l}
\Sigma Y_{\mathrm{i}} \\
\Sigma\left(Y_{\mathrm{i}} X_{\mathrm{i}}\right)
\end{array}\right]
$$

The relations of the variables are defined as the following:

| Regression | $\mathbf{A}$ | $\mathbf{X}_{\mathbf{i}}$ | $\mathbf{Y}_{i}$ | Code |
| :--- | :---: | :---: | :---: | :---: |
| Exponential | $\ln a$ | $x_{i}$ | $\ln y_{i}$ | 1 |
| Logarithmic | $a$ | $\ln x_{i}$ | $y_{i}$ | 2 |
| Power | $\ln a$ | $\ln x_{i}$ | $\ln y_{i}$ | 3 |

The coefficient of determination is:

$$
r^{2}=\frac{A \Sigma Y_{\mathrm{i}}+b \Sigma X_{\mathrm{i}} Y_{\mathrm{i}}-\frac{1}{n}\left(\Sigma Y_{\mathrm{i}}\right)^{2}}{\Sigma\left(Y_{\mathrm{i}}^{2}\right)-\frac{1}{n}\left(\Sigma Y_{\mathrm{i}}\right)^{2}}
$$

The type of curve fit to be run is determined before data input begins by inputting the code number.
The coefficient of determination indicates the quality of fit achieved by the regression. Values of $r^{2}$ close to 1.00 indicate a better fit than values close to zero. The regression coefficients $a$ and $b$ define the curve generated, according to the equations at the beginning of this discussion.

## Exponential Curve Fit Code $=1$

> Logarithmic Curve Fit Code $=2$



Power Curve Fit

$$
\text { Code }=3
$$



## Remarks:

- The program applies the least squares method, either to the original equations (logarithmic curve) or to the transformed equations (exponential curve and power curve).
- Negative and zero values of $x_{\mathrm{i}}$ will cause a machine error for logarithmic curve fits. Negative and zero values of $y_{i}$ will cause a machine error for exponential curve fits. For power curve fits both $x_{1}$ and $y_{1}$ must be positive, non-zero values.
- As the differences between $x$ and/or $y$ values become small, the accuracy of the regression coefficients will decrease.
- During operation of the program all storage registers are cleared. Any data stored in extra registers will therefore be destroyed.

| KEY ENTRY | DISPLAY |
| :---: | :---: |
| (fCLEAR PRGM | 000- |
| (n) [BL $A$ | 001-25, 13, 11 |
| ( CLEAR REG | 002- 1433 |
| (1) FIX 2 | 003-14, 11, 2 |
| ENIERA | 004- 31 |
| ENTER | 005- 31 |
| 6 | 006- |
| $\pm$ | 007- 51 |
| STO (f) 1 | 008-23, 14, 23 |
| (9) $\mathrm{RO}_{6}$ | 009- 1522 |
| (n) SF 0 | 010-25, 51, 0 |
| (b) SF 1 | 011-25, 51, |
| GTO 1 D | 012-22, 14, 23 |
| [ HBL 7 | 013-25, 13, 7 |
| (b) CF 1 | 014-25, 61, |
| GTO) 9 | 015- 229 |
| [ 4 LBL 8 | 016-25, 13, 8 |
| (b) CF 0 | 017-25, 61, 0 |
| (b) [BL 9 | 018-25, 13, 9 |
| R/S | 019- 74 |
| (b) Fr 0 | 020-25, 71, 0 |
| (1) LT | 021- 141 |
| $x=y$ | 022- 21 |
| ( $\square_{\text {F }} 1$ | 023-25, 71, 1 |
| (f) LT | 024-14 |
| (b) Fr 2 | 025-25, 71, 2 |


| KEY ENTRY | DISPLAY |  |  |
| :---: | :---: | :---: | :---: |
| GTO 6 | 026- | 22 | 6 |
| (1) E+ | 027- | 14 |  |
| GTO 9 | 028- | 22 | 9 |
| (b) LBL 6 | 029-25, 13, 6 |  |  |
| (9) $5-$ | 030- | 15 | 74 |
| ( $\square_{\text {CF }} 2$ | 031-25, 61, 2 |  |  |
| GTO 9 | 032- | 22 | 9 |
| (b) LBL B | 033-25, 13, 12 |  |  |
| D L. R | 034- | 25 | 6 |
| (b) For 0 | 035-25, 71, |  |  |
| (9) $e^{x}$ | 036- | 15 | 1 |
| [ $\mathrm{B} / \mathrm{s}$ | 037- |  | 74 |
| $x \geqslant y$ | 038- |  | 21 |
| [//s | 039- |  | 74 |
| (n) $\square$ | 040- | 25 | 5 |
| (9) $x^{2}$ | 041 - | 15 | 3 |
| $\square$ RTN | 042- | 25 | 12 |
| (b) LBL 0 | 043-25, 13, 0 |  |  |
| (n) SF 2 | 044-25, 51, |  |  |
| GTO 9 | 045- 22 |  |  |
| (b) LBL 1 | 046-25, 13, 1 |  |  |
| (b) FF 1 | 047-25, 71, |  |  |
| (1) LN | 048- 14 |  |  |
| (b) 匂 | 049- 25 |  |  |
| (b) Fr 0 | 050-25, 71, 0 |  |  |
| (9) $e^{x}$ | 051 - | 15 | 1 |


| REGISTERS |  |  | I Code +6 |
| :--- | :--- | :--- | :--- |
| $R_{0} n$ | $R_{1} \Sigma X_{i}$ | $R_{2} \Sigma X_{i}^{2}$ | $R_{3} \Sigma Y_{i}$ |
| $\mathrm{R}_{4} \Sigma Y_{i}^{2}$ | $R_{5} \Sigma X_{i} Y_{i}$ | $R_{6}-R_{.9}$ Unused |  |


| STEP | INSTRUCTIONS | INPUT DATANUNITS | KEYS | OUTPUT <br> DATAUNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program |  |  |  |
| 2 | Select the type of curve fit: |  |  |  |
|  | Exponential | 1 | (A) | 1.00 |
|  | Logarithmic | 2 | (A) | 2.00 |
|  | Power | 3 | ( $A$ | 3.00 |
| 3 | Input $x_{i}$ value and $y_{i}$ value. | $x_{i}$ | ENTER4 |  |
|  |  | $y_{i}$ | R/S | $i$ |
|  | (Repeat step 3 for all data |  |  |  |
|  | points) |  |  |  |
| 4 | Calculate regression coef- |  |  |  |
|  | ficients |  | B | a |
|  |  |  | R/S | $b$ |
|  | and coefficient of determin- |  |  |  |
|  | ation. |  | R/S | $r^{2}$ |
| 5 | Make projection of new $\hat{\mathbf{y}}$ for |  |  |  |
|  | a known $x$ value. | $x$ | GSB 1 | $\hat{y}$ |
|  | (Repeat step 5 for all $x$ |  |  |  |
|  | values of interest.) |  |  |  |
| 6 | Error Deletion: |  |  |  |
|  | Erroneous inputs at step 3 may |  | GSB 0 |  |
|  | be corrected by pressing | $x_{i}$ err | ENTER4 |  |
|  | GSB 0 and reinputting the | $y_{i}$ err | R/S | i-1 |
|  | erroneous data. Then return to |  |  |  |
|  | step 3 and enter the correct |  |  |  |
|  | data. |  |  |  |

## Example 1:

$($ Exponential, Code $=1)$

| $x_{i}$ | .72 | 1.31 | 1.95 | 2.58 | 3.14 |
| :--- | ---: | ---: | ---: | ---: | :--- |
| $y_{i}$ | 2.16 | 1.61 | 1.16 | .85 | 0.5 |

Solution:

$$
\begin{aligned}
& a=3.45, b=-0.58 \\
& y=3.45 e^{-0.58 \mathrm{x}} \\
& r^{2}=0.98
\end{aligned}
$$

## Keystrokes: Display:

| A |  | 1.00 |
| :---: | :---: | :---: |
| . 72 ENIER4 $2.16 \mathrm{R} / \mathrm{S}$ |  |  |
| 1.31 ENTER4 $1.61 \mathrm{R} / \mathrm{S}$ |  |  |
| 1.95 ENTER4 $1.16 \mathrm{R} / \mathrm{S}$ |  |  |
| 2.58 ENTER $.85 \mathrm{R} / \mathrm{S}$ |  |  |
| 3.14 ENTER4 $.5 \mathrm{R} / \mathrm{S}$ |  |  |
| (B) | 3.45 | $a$ |
| R/S | -0.58 | $b$ |
| R/5 | 0.98 | $r^{2}$ |
| 1.5 GSB | 1.44 | $\hat{y}$ |

## Example 2:

(Logarithmic, Code $=2$ )

| $x_{i}$ | 3 | 4 | 6 | 10 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y_{i}$ | 1.5 | 9.3 | 23.4 | 45.8 | 60.1 |

Solution:

$$
\begin{aligned}
& a=-47.02, b=41.39 \\
& y=-47.02+41.39 \ln x \\
& r^{2}=0.98
\end{aligned}
$$

For $x=8, \hat{y}=39.06$
For $x=14.5, \hat{y}=63.67$

## Example 3:

(Power, Code $=3$ )

| $x_{\mathrm{i}}$ | 10 | 12 | 15 | 17 | 20 | 22 | 25 | 27 | 30 | 32 | 35 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y_{\mathrm{i}}$ | 0.95 | 1.05 | 1.25 | 1.41 | 1.73 | 2.00 | 2.53 | 2.98 | 3.85 | 4.59 | 6.02 |

Solution:

$$
\begin{aligned}
& a=.03, b=1.46 \\
& y=.03 x^{1.46} \\
& r^{2}=0.94
\end{aligned}
$$

For $x=18, \hat{y}=1.76$
For $x=23, \hat{y}=2.52$

## Hyperbolic Functions

This program calculates the hyperbolic functions and their inverses with special algorithms that provide excellent accuracy. Calculation of the hyperbolic functions, as defined below, will yield errors in many instances for small arguments (i.e., $x<0.5$ ) due to roundoff errors. However, this program has been specially written to avoid these errors and should provide accurate answers to better than eight significant figures.

## Equations:

## Hyperbolic Functions

$$
\sinh x=\frac{e^{\mathrm{x}}-e^{-\mathrm{x}}}{2}
$$

$$
\operatorname{csch} x=\frac{1}{\sinh x} \quad(x \neq 0)
$$

$\cosh x=\frac{e^{\mathrm{x}}+e^{-\mathrm{x}}}{2}$

$$
\operatorname{sech} x=\frac{1}{\cosh x}
$$

$$
\tanh x=\frac{e^{\mathrm{x}}-e^{-\mathrm{x}}}{e^{\mathrm{x}}+e^{-\mathrm{x}}}
$$

$$
\operatorname{coth} x=\frac{1}{\tanh x} \quad(x \neq 0)
$$

Inverse Hyperbolic Functions

$$
\begin{aligned}
& \sinh ^{-1} x=\ln \left[x+\left(x^{2}+1\right)^{1 / 2}\right] \\
& \cosh ^{-1} x=\ln \left[x+\left(x^{2}-1\right)^{1 / 2}\right] \quad x \geqslant 1 \\
& \tanh ^{-1} x=1 / 2 \ln \left[\frac{1+x}{1-x}\right] \quad x^{2}<1 \\
& \operatorname{csch}^{-1} x=\sinh ^{-1}\left[\frac{1}{x}\right] \quad x \neq 0 \\
& \operatorname{sech}^{-1} x=\cosh ^{-1}\left[\frac{1}{x}\right] \quad 0<x \leqslant 1 \\
& \operatorname{coth}^{-1} x=\tanh ^{-1}\left[\frac{1}{x}\right] \quad x^{2}>1
\end{aligned}
$$

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: | :---: | :---: |
| TCLEAR Pracm | 000－ | GSE 2 | 029－ | 132 |
|  | 001－25，13， 11 | $\oplus$ | 030－ | 71 |
| 回吅 1 | 002 25，61， 1 | 囫 78 | 031－2 | ，13， 7 |
| 回 0 | 003－25，61， 0 | 囫 1 | 032－ | 5，71， 1 |
| sto 团 | 004－23，14， 23 | 产 | 033－ | $25 \quad 2$ |
| 句 $\mathrm{B}_{6}$ | 005－ 1522 | R／S | 034－ | 74 |
| GTo $\square^{10}$ | 006－22，14， 23 | ［亩 LBL | 035－2 | ，13， 0 |
| （n） 4 | 007－25，13， 4 | EEIER | 036－ | 31 |
| ［困5 | 008－25，13， 5 |  | $037-$ | 2534 |
| ［产6 | 009－25，13， 6 | $\odot$ | 038－ | 73 |
| （6） 5 | 010－25，51， 1 | 5 | 039－ | 5 |
| （9）DSE | 011－ 1523 | （1）$x \leq y$ | 040－ | 1441 |
| （9）DSE | 012－ 1523 | GTO 8 | 041 － | 228 |
| （9）DSE | 013－ 1523 | （9）四 | 042－ | 1522 |
| GGo ${ }^{\text {a }}$ | 014－22，14， 23 | （9）${ }^{\text {a }}$ | 043－ | 15 |
| ［困 1 | 015－25，13， 1 | （1） | 044－ | 141 |
| （n）SF 0 | 016－25，51， 0 | （9） $\mathrm{x}=0$ | 045－ | 1571 |
| GSE 0 | 017－ 13 | GTO 9 | 046－ | 229 |
| 四（cra | 018－25，61， 0 | 1 | 047－ | 1 |
| GTO 7 | 019－ 22 | H LSTx | 048－ | 250 |
| ［国 2 | 020－25，13， 2 | $\square$ | 049－ | 41 |
| GSE 2 | 021－ 132 | ［ LSTx | 050－ | 250 |
| GTO 7 | 022－ 227 | （9） $\mathrm{RO}^{\text {d }}$ | 051 － | 1522 |
| ［［BL 3 | 023－25，13， 3 | $\square$ | 052 － | 71 |
| STOO 0 | 024－ 23 0 | $\oplus$ | 053－ | 71 |
| ［ SF 0 | 025－25，51， 0 | $\mathrm{CHS}^{\text {che }}$ | 054－ | 32 |
| GSE 0 | 026－ 130 | $\bigcirc$ | 055－ | 73 |
| 回吅 0 | 027－25，61， 0 | 5 | 056－ | 5 |
| ECL 0 | 028－ 240 | ENIER | 057－ | 31 |


| KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: |
| (180 | 058- | 1422 |
| $\pm$ | 059- | 71 |
| $\pm$ | 060- | 51 |
| 区 | 061 - | 61 |
| (b) RTN | 062- | 2512 |
| - LBL 9 | 063-25, 13, 9 |  |
| $x \geqslant y$ | 064- | 21 |
| $\square$ RTN | 065- | 2512 |
| (b) 8 | 066-25, 13, 8 |  |
| (9) 8 \% | 067- | 1522 |
| $\pm$ | 068- | 71 |
| - LSTx | 069- | 250 |
| (b) LBL 2 | 070-25, 13, 2 |  |
| (9) $e^{x}$ | 071- | 151 |
| n LSTX | 072- | 250 |
| CHS | 073- | 32 |
| (9) $e^{x}$ | 074- | 151 |
| (b) For 0 | 075-25, 71, 0 |  |
| CHS | 076- | 32 |
| $\pm$ | 077- | 51 |
| 2 | 078- | 2 |
| $\dagger$ | 079- | 71 |
| (b) For 0 | 080-25, 71, 0 |  |
| 区 | 081 - |  |
| $\square$ RTN | 082- 2512 |  |
| (b) LBL B | 083-25, 13, 12 |  |
| (b) CFO | 084-25, 61, 0 |  |
| STO 1 | 085-23, 14, 23 |  |
| (9) R ${ }_{\text {a }}$ | 086- | 1522 |


| KEY ENTRY | DISPLAY |
| :---: | :---: |
| GTO $)^{1}$ | 087-22, 14, 23 |
| (b) LBL 4 | 088-25, 13, 4 |
| - LBL 5 | 089-25, 13, 5 |
| (b) LBL 6 | 090-25, 13, 6 |
| (1) $1 / x$ | 091- 252 |
| (9) DSE | 092-1523 |
| (9) DSE | 093- 1523 |
| (9) DSE | 094-1523 |
| GTO (t) 1 | 095-22, 14, 23 |
| (b) LBL 1 | 096-25, 13, 1 |
| GSB 4 | 097- 134 |
| (9) $x^{2}$ | 098- 153 |
| ENITRA | 099- 31 |
| ENIERA | 100- 31 |
| 1 | 101- 1 |
| $\pm$ | 102- 51 |
| $1{ }^{(1)}$ | 103- 143 |
| 1 | 104- 1 |
| $\pm$ | 105- 51 |
| $\dagger$ | 106- 71 |
| $\pm$ | 107- 51 |
| GSB 0 | 108- 130 |
|  | 109-25, 71, 1 |
| CHS | 110- 32 |
| D RTN | 111- 2512 |
| - 4 LBL 3 | 112-25, 13, 3 |
| GSB 4 | 113- 134 |
| ENTERA | 114- 31 |
| 1 | 115- 1 |


| KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: |
| $x<y$ | 116- | 21 |
| $\square$ | 117- | 41 |
| $\square$ | 118- | 71 |
| ENTER | 119- | 31 |
| $\pm$ | 120- | 51 |
| GSB 0 | 121 - | 130 |
| (b) For 1 | 122-2 | 71, 1 |
| CHS | 123- | 32 |
| 2 | 124- | 2 |
| $\square$ | 125- | 71 |
| ( $n$ RTN | 126- | 2512 |
| ( $\square$ LBL 2 | 127-2 | 13, 2 |
| 1 | 128- | 1 |
| $\square$ | 129- | 41 |
| ENTER | 130- | 31 |
| ENTER | 131 - | 31 |
| ENTER | 132- | 31 |
| 2 | 133- | 2 |
| $\pm$ | 134- | 51 |
| $\pm$ | 135- | 61 |
| $\pm \sqrt{x}$ | 136- | 143 |
| $\dagger$ | 137- | 51 |
| ¢ LBL 0 | 138-2 | 13, 0 |
| ENTERA | 139- | 31 |
| ENTERA | 140- | 31 |


| KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: |
| 1 | 141 - | 1 |
| (1) $x>y$ | 142- | 1451 |
| GTO 0 | 143- | 220 |
| $\pm$ | 144- | 51 |
| (4) LT | 145- | 141 |
| ( H RTN | 146- | 2512 |
| (b) LBL 0 | 147-25, 13, 0 |  |
| $\pm$ | 148- | 51 |
| (1) LN | 149- | 141 |
| - LSTx | 150- | 250 |
| 1 | 151 - | 1 |
| $\square$ | 152- | 41 |
| (9) $\times$ x0 | 153- | 1561 |
| $\square$ | 154- | 71 |
| 区 | 155- | 61 |
| (9) $x=0$ | 156- | 1571 |
| $x<y$ | 157- | 21 |
| ( $n$ RTN | 158- | 2512 |
| (b) LBL 4 | 159-25, 13, 4 |  |
| (n) CF 1 | 160-25, 61, 1 |  |
| (9) $x<0$ | 161- 1541 |  |
| (n) SF 1 | 162-25, 51, 1 |  |
| (b) ABS | 163- | 2534 |
| ENTERA | 164- | 31 |


| REGISTERS |  | I Control |
| :--- | :--- | :--- |
| $R_{0} \times$ | $R_{1}-R_{5}$ Unused |  |


| STEP | INSTRUCTIONS | INPUT DATAUNITS | KEYS | OUTPUT <br> DATAUNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | For hyperbolics go to step 3, |  |  |  |
|  | for inverse hyperbolics go to |  |  |  |
|  | step 4. |  |  |  |
|  | HYPERBOLIC FUNCTIONS: |  |  |  |
| 3 | Key in the argument and the |  |  |  |
|  | code: | $x$ | ENTER |  |
|  | - hyperbolic sine ( $\operatorname{code}=1$ ) | 1 | (A) | $\sinh x$ |
|  | - hyperbolic cosine (code=2) | 2 | (A) | $\cosh x$ |
|  | - hyperbolic tangent (code=3) | 3 | A | $\tanh x$ |
|  | - hyperbolic cosecant |  |  |  |
|  | (code $=4$ ) | 4 | A | $\operatorname{csch} x$ |
|  | - hyperbolic secant (code=5) | 5 | A | $\operatorname{sech} x$ |
|  | - hyperbolic cotangent |  |  |  |
|  | (code $=6$ ) | 6 | A | coth $x$ |
|  | INVERSE HYPERBOLIC |  |  |  |
|  | FUNCTIONS: |  |  |  |
| 4 | Key in the argument and |  |  |  |
|  | the code: | $x$ | ENTER |  |
|  | - inverse hyperbolic sine |  |  |  |
|  | (code $=1$ ) | 1 | B | $\sinh ^{-1} x$ |
|  | - inverse hyperbolic cosine |  |  |  |
|  | (code $=2$ ) | 2 | B | $\cosh ^{-1} x$ |
|  | - inverse hyperbolic tangent |  |  |  |
|  | (code $=3$ ) | 3 | B | $\tanh ^{-1} x$ |
|  | - inverse hyperbolic cosecant |  |  |  |
|  | (code $=4$ ) | 4 | B | $\operatorname{csch}^{-1} x$ |
|  | - inverse hyperbolic secant |  |  |  |


| STEP | INSTRUCTIONS | INPUT <br> DATANUNTS | KEYS | OUTPUT <br> DATA/UNTT |
| :--- | :--- | :---: | :---: | :---: |
|  | $($ code $=5)$ | 5 | $B$ | sech $^{-1} x$ |
|  | $\bullet$ inverse hyperbolic cotangent |  |  |  |
|  | $($ code $=6)$ | 6 | $B$ | $\operatorname{coth}^{-1} x$ |

## Example 1:

Evaluate the following hyperbolic functions:
$\sinh 2.5$; $\cosh 3.2 ; \tanh 1.9 ; \operatorname{csch}(-0.25)$; $\operatorname{coth}(-2.01)$. Also, evaluate $\sinh x$ and compare to $\frac{e^{x}-e^{-x}}{2}$ where $x=1.2345 \times 10^{-8}$.

Keystrokes: Display:

| 2.5 ENTER4 1 A | 6.0502 | $\sinh 2.5$ |
| :---: | :---: | :---: |
| 3.2 ENTER4 2 A | 12.2866 | cosh 3.2 |
| 1.9 ENTER4 3 A | 0.9562 | $\tanh 1.9$ |
| 25 CHS ENTER4 4 A | -3.9586 | $\operatorname{csch}(-0.25)$ |
| 2.01 CHS ENTER4 |  |  |
| 6 A | -1.0366 | coth (-2.01) |
| 1.2345 EEX CHS 8 |  |  |
| ENTER4 1 A | 1.2345-08 | $\sinh \left(1.2345 \times 10^{-8}\right)$ |
| 1.2345 EEX CHS |  |  |
| 8 9 $\mathrm{e}^{x}$ ¢ LST $x$ |  |  |
| CHS g ex- |  |  |

$2 \div 1.2150-08$ incorrect due to round-off

## Example 2:

Evaluate the following inverse hyperbolic functions:
$\sinh ^{-1}$ (2.4); $\cosh ^{-1}(90) ; \tanh ^{-1}(-0.65) ; \operatorname{sech}^{-1}(0.4) ; \operatorname{coth}^{-1}(3.4)$.

## Keystrokes: Display:

| 2.4 ENTERA 1 B | 1.6094 | $\sinh ^{-1}$ (2.4) |
| :---: | :---: | :---: |
| 90 ENTER4 2 B | 5.1929 | $\cosh ^{-1}(90)$ |
| . 65 CHS ENTER4 3 B | -0.7753 | $\tanh ^{-1}(-0.65)$ |
| . 4 ENTERA 5 B | 1.5668 | $\operatorname{sech}^{-1}$ (0.4) |
| 3.4 ENTER4 6 B | 0.3031 | $\operatorname{coth}^{-1}$ (3.4) |

## Polynomial Evaluation

This program performs several useful operations on polynomial functions of the form

$$
f(x)=a_{0}+a_{1} x+a_{2} x^{2} \ldots+n_{\mathrm{n}-1} x^{\mathrm{n}-1}+a_{\mathrm{n}} x^{\mathrm{n}}
$$

where the order, $n$, of the polynomial is 9 or less.
The following operations may be accomplished:

## Evaluation of $f(x)$ :

The value, $f(x)$, may be calculated for a known value of $x$.

## Zeros of $f(x)$ :

The real zeros of the polynomial (values of $x$ for which $f(x)=0$ ) may be found. This operation uses the SOLVE operation of the HP-34C.

## Find $x$ for a given value of $f(x)$ :

The real values of $x$ satisfying the polynomial for a given value of $f(x)$ may be found. This operation also uses the SOLVE operation of the HP-34C.

## Definite integral of $\mathbf{f}(\mathbf{x})$ :

The definite integral, $\int_{\mathrm{a}}^{\mathrm{b}} f(x) d x$, of the polynomial $f(x)$, between the limits $a$ and $b$ may be evaluated. This operation uses the $\times x$ built into the HP-34. (See remarks below.)

## Remarks:

- This program illustrates basic but valuable ways in which the SOLVE function may be used. The program is useful for all polynomials up to order 9 , having real coefficients. It can easily be expanded for use with higher order polynomials or altered for use on other types of functions.
- Since the integral of a polynomial can be readily written in closed form and easily evaluated, it is not really necessary to use the powerful INTEGRATE, 团, capability of the HP-34. It is used here primarily for illustrative purposes.
- The user is urged to consult the discussion in the owner's handbook on the use of the SOLVE and $\int_{y}^{x}$ capabilities for a more thorough understanding of their usefulness and limitations.
- The program will not solve for complex zeros. If it is unsuccessful in finding a real zero, Error 4 will be displayed.

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :---: | :---: | :---: | :---: |
| 1 CLEAR PRGM | 000－ | （b）SF 0 | 029－25，51， 0 |
| （ $\square$ LBL 0 | 001－25，13， 0 | （1）图 3 | 030－14，72， 3 |
| STOO 1 | 002－ 23.1 | R／S | 031－74 |
| STO 01 | 003－23，14， 23 | （b）LBL 1 | 032－25，13， 1 |
| （n）LBL 8 | 004－25，13， 8 | （1）FIX 4 | 033－14，11， 4 |
| R／S | 005－ 74 | （b）CF 0 | 034－25，61， 0 |
| STO（f）（ii） | 006－23，14， 24 | STO－ 0 | 035－ 23.0 |
| （9）DSE | 007－1523 | （9）Rot | 036－1522 |
| GTO 8 | 008－ 228 | 1 SOLVE 3 | 037－14，73， 3 |
| R／S | 009－ 74 | R／S | 038－ 74 |
| RCL $\square^{-1}$ | 010－ 24.1 | GTO 7 | 039－ 227 |
| STO（1） 1 | 011－23，14， 23 | （n）LBL 3 | 040－25，13， 3 |
| （9）R ${ }_{\text {d }}$ | 012－ 1522 | ［RCL（f）（ii） | 041－24，14， 24 |
| STO 0 | 013－ 230 | 区 | 042－ 61 |
| R／S | 014－ 74 | （0）DSE | 043－1523 |
| （b）LBL 4 | 015－25，13， 11 | （b）LBL 9 | 044－25，13， 9 |
| （1）FIX 4 | 016－14，11 4 | RCL（1i） | 045－24，14， 24 |
| （b）SF 0 | 017－25，51， 0 | $\pm$ | 046－ 51 |
| ENIER ${ }^{\text {a }}$ | 018－ 31 | 区 | 047－ 61 |
| ENTER ${ }^{\text {a }}$ | 019－ 31 | （9）DSE | 048－15 23 |
| ENTER | 020－ 31 | GTO 9 | 049－ 229 |
| GTO 3 | 021－ 223 | RCL） 0 | 050－ 240 |
| （ 4 LBL B | 022－25，13， 12 | $\pm$ | 051－ 51 |
| （1）FIX 4 | 023－14，11， 4 | RCL $\bullet 1$ | 052－ 24.1 |
| （b）SF 0 | 024－25，51， 0 | STO 10 | 053－23，14， 23 |
| SOLVE 3 | 025－14，73， 3 | （9）R | 054－ 1522 |
| R／S | 026－ 74 | （b）Fr 0 | 055－25，71， 0 |
| GTo 7 | 027－ 227 | D RTN | 056－ 2512 |
| （n）LBL 2 | 028－25，13， 2 | RCL -0 | 057－ 24.0 |


| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :--- | :--- | :--- | :--- |
| - | $058-\quad 41$ |  |  |


| REGISTERS |  |  | I Control |
| :--- | :--- | :--- | :--- |
| $R_{0} a_{0}$ | $R_{1} a_{1}$ | $R_{2} a_{2}$ | $R_{3} a_{3}$ |
| $R_{4} a_{4}$ | $R_{5} a_{5}$ | $R_{6} a_{6}$ | $R_{7} a_{7}$ |
| $R_{8} a_{8}$ | $R_{9} a_{9}$ | $R_{.0} f(x)$ | $R_{.1} n$ |
| $R_{.2}-R_{.9}$ Unused |  |  |  |


| STEP | INSTRUCTIONS | INPUT DATA/UNITS | KEYS | OUTPUT DATA/UNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Input the order of the poly- |  |  |  |
|  | nomial (value of largest |  |  |  |
|  | exponent). | $n$ | GSB 0 | $n$ |
| 3 | Input coefficients starting with |  |  |  |
|  | $a_{n}$ | $a_{n}$ | R/S | $a_{n}$ |
|  | (Repeat until all $a_{n}$ through $a_{0}$ |  |  |  |
|  | are entered) | $a_{n-1}$ | R/S | $a_{n-1}$ |
|  |  | : |  |  |
|  |  | $a_{0}$ | R/S | $a_{0}$ |
| 4 | To Evaluate the Polynomial: |  |  |  |
|  | Input $x$ and see $f(x)$. (Repeat |  |  |  |
|  | for all values of interest.) | $x$ | A | $f(x)$ |
| 5 | To Find a Zero of the |  |  |  |
|  | Polynomial: |  |  |  |
|  | Input two initial guesses in the |  |  |  |
|  | approximate range, for the | Guess 1 | R/S |  |
|  | initial search. | Guess 2 | B | a zero |
|  | (Repeat for other zeros.) |  |  |  |


| STEP | INSTRUCTIONS | INPUT DATA/UNTTS | KEYS | OUTPUT DATA/UNITS |
| :---: | :---: | :---: | :---: | :---: |
| 6 | To Find x for a Given $f(x)$ : |  |  |  |
|  | Input upper and lower guesses | Guess 1 | R/S |  |
|  | of the expected value of $x$, then | Guess 2 | R/S |  |
|  | input the known value of $f(x)$. | $f(x)$ | GSB 1 | $x$ |
| 7 | To Find Integral of the |  |  |  |
|  | Polynomial: |  |  |  |
|  | Set the desired display format |  | (f) SCl |  |
|  | to control uncertainty.* Then |  | or, $f$ ENG $n$ |  |
|  | input the lower limit of the inte- | a | ENTER4 |  |
|  | gral and the upper limit of the | $b$ | GSB 2 | $\int_{b}^{a} f(x) d x$ |
|  | integral. |  |  |  |
|  |  |  |  |  |
|  | * Consult the HP-34C Owner's |  |  |  |
|  | Handbook and Programming |  |  |  |
|  | Guide for information on the |  |  |  |
|  | proper user of the display |  |  |  |
|  | format when using $\int_{5}^{x}$ |  |  |  |

## Example 1:

A ball is thrown straight up at a velocity of 20 meters per second, from a height of 2 meters. Neglecting air resistance, how long will it take the ball to reach the ground? The acceleration of gravity is 9.81 meters per second. From physics:

$$
\begin{aligned}
h(t) & =x_{0}+v_{0} t+\frac{1}{2} a t^{2}=0 \\
& =2+20 t+(-9.81 / 2) t^{2}=0
\end{aligned}
$$

## Keystrokes: Display:

| 2 GSB 0 | 2.0000 | Input order, $n$ |
| :--- | ---: | :--- |
| 9.81 CHS ENTER |  |  |
| 2 R R/S | -4.9050 | Coefficient $a_{2}$ |
| 20 R/S 2 R/S | 2.0000 | Coefficients $a_{1}, a_{0}$ |
| 10 ENTERA 0 B | 4.1751 | Seconds |

There is also a negative root to this equation, but it is not relevant to this problem. To find it:
10 CHS ENTER4 0 B -0.0977
Seconds

## Example 2:

The standard heat of formation of ammonia $\left(\mathrm{NH}_{3}\right)$ is given as a function of Kelvin temperature by:

$$
\Delta H_{\mathrm{T}}^{\circ}=-9140-7.596 T+4.243 \times 10^{-3} T^{2}-0.742 \times 10^{-6} T^{3}(\mathrm{cal})
$$

Determine the heat of formation for temperatures of 400 K and 800 K . Also, find the temperature at which the heat of formation is $-12,330.39$ cal.

## Keystrokes:

Display:

3 GSB $0 \quad 3.0000$

| .742 CHS EEX |
| :--- | :--- |
| CHS 6 R/S |

4.243 EEX CHS

| $3 \mathrm{R} / \mathrm{S}$ |  | 0.0042 |
| :--- | :--- | :--- |
| 7.596 CHS R/S | -7.5960 |  |
| $9140 \mathrm{CHS} \mathrm{R} / \mathrm{S}$ | $-9,140.0000$ |  |
| 400 A | $-11,547.0080$ | $\Delta H^{\circ}{ }^{\circ}{ }_{400}$ |
| 800 A | $-12,881.1840$ | $\Delta H^{\circ}{ }_{800}$ |

1000 ENTERA

| 0 ENTER4 | 0.0000 | (guess for temperature) |
| :--- | :--- | :--- |
| 12330.39 CHS |  |  |
| GSB 1 | 599.9994 | $K$ |

$\Delta H_{\mathrm{T}}{ }^{\circ}=-12,330.39$ calories at approximately 600 K .

## Example 3:

Find the two real roots of the equation $f(x)=4 x^{4}-8 x^{3}-13 x^{2}-10 x$ $+22=0$. Then evaluate the area under the curve (integral of $f(x)$ ) between the roots.

Keystrokes: Display:

| 4 GSB 0 | 4.0000 | $n$ |
| :--- | :--- | :--- |
| 4 R/S 8 CHS R/S |  |  |

$13 \mathrm{CHS} \mathrm{R} / \mathrm{S}$

| 22 R/S |
| :--- |
| 0 ENTERA 50 B |
| 1 ENTER 50 B |
| EST 3 |
| .882 ENTER 3.118 |


| GSB | 2 | -7.640 |
| :--- | ---: | :--- |
| $x \geqslant y$ | 9.745 | -03 |$\quad \int_{v}^{x} f(x) d x$

## Finance

## Annuities and Compound Amounts

This program can be used to solve a variety of problems involving money, time and interest. The following variables can be either inputs or outputs:
$n$, which is the number of compounding periods. (For a 30 year loan with monthly payments, $n=12 \times 30=360$.)
$i$, which is the periodic interest rate expressed as a percent. (For other than annual compounding, divide the annual percentage rate by the number of compounding periods in a year, i.e., $8 \%$ annual interest compounded monthly equals $8 / 12$ or $0.667 \%$.)
$P V$, which is the present value of the cash flow or compound amounts.
$P M T$, which is the periodic payment.
$F V$, which is the future value of a compounded amount or a series of cash flows.
$B A L$, which is the balloon or remaining balance at the end of a series of payments.
Accumulated interest and remaining balance may also be computed with this program.
The program accommodates payments which are made at the beginning or end of compounding periods. Payments made at the end of compounding periods (ordinary annuity) are common in direct reduction loans and mortgages while payments at the beginning of compounding periods (annuity due) are common in leasing. For ordinary annuity press $A$ until 1 is displayed. For annuity due press $A$ until 0 is displayed.
This program uses the convention that cash outlays are input as negative, and cash incomes are input as positive.

Pressing $f$ CLEAR REG provides a safe, convenient, easy to remember method of preparing the calulator for a new problem. However, it is not necessary to use $f$ CLEAR REG between problems containing the same combination of variables. For instance, any number of $n, i, P V, P M T, F V$ problems involving different numbers and/or
different combinations of knowns could be done in succession without clearing the registers. Only the values which change from problem to problem would have to be keyed in. To change the combination of variables without using $\quad$ CLEAR REG, simply input zero for any variable which is no longer applicable. To go from $n, i, P M T, P V$ problems to n, i, PV,FV problems, a zero would be stored (0 STO 4) in place of $P M T$. Table I summarizes these procedures.

Table I
Possible Solutions Using Annuities and Compound Amounts

| Allowable Combination of Variables | Applications |  | Initial Procedure |
| :---: | :---: | :---: | :---: |
|  | Ordinary Annuity | Annuity Due |  |
| n, i, PV, PMT (Input any three and calculate the fourth.) | Direct reduction loan Discounted notes Mortgages | Leases | Use 1 CLEAR REG or set BAL to zero |
| $n, i, P V, P M T$ BAL (Input any four and calculate the fifth.) | Direct reduction loan with balloon Discounted notes with balloon | Leases with residual values | None |
| n, i, PMT, FV (Input any three and calculate the fourth.) | Sinking fund | Periodic savings Insurance | Use $f$ CLEAR REG or set $P V$ to zero |
| $n, i, P V, F V$ (Input any three and calculate the fourth.) | Compound amount Savings (Annuity mode is not applicable and has no effect) |  | Use flelear Reg or set PMT to zero. |

## Equations:

$$
-P V=\frac{P M T}{i} A\left[1-(1+i)^{-\mathrm{n}}\right]+(B A L \text { or } F V)(1+i)^{-\mathrm{n}}
$$

where

$$
A= \begin{cases}1 & \text { ordinary annuity } \\ (1+i) & \text { annuity due }\end{cases}
$$

## Remarks:

- This program uses the SOLVE operation to find $i$. Since this is an iterative method it will take longer than the other calculations (up to 2 minutes or more). It is quite possible to define problems which cannot be solved by the technique. Such problems usually result in an error message but may simply continue to run indefinitely.
- Problems with an interest rate of 0 will give an "Error 0 " display.
- Problems with extremely high $\left(10^{6}\right)$ or low values $\left(10^{-6}\right)$ for $n$ or $i$ may give invalid results.
- Interest problems with balloon payments of opposite sign to the periodic payments may have more than one mathematically correct answer (or no answer at all). This program may find one of the answers but has no way of finding or indicating other possibilities.

| KEY ENTRY | DISPLAY |
| :---: | :---: |
| f(CLEAR PRGM | 000- |
| (h) LBL $A$ | 001-25, 13, 11 |
| f FIX 2 | 002-14, 11, 2 |
| ( $n$ F? 0 | 003-25, 71, 0 |
| GTO 7 | 004-72 |
| (h) SF 0 | 005-25, 51, 0 |
| 0 | 006- 0 |
| R/S | 007-74 |
| (h) LBL 7 | 008-25, 13, 7 |
| (h) CF 0 | 009-25, 61, 0 |
| 1 | 010- 1 |
| R/S | 011- 74 |
| (h) LBL 1 | 012-25, 13, 1 |
| 0 | 013- 0 |
| STO 1 | 014-23 1 |
| GSB 6 | 015-136 |
| RCL 5 | 016- 245 |
| h LST $x$ | 017- 250 |
| $\square$ | 018- 41 |
| RCL 3 | 019- 243 |
| ( h LST $x$ | 020- 250 |
| $\pm$ | 021- 51 |
| $\pm$ | 022-71 |
| CHS | 023-32 |
| (1) LN | 024-14 1 |
| RCL 6 | 025- 246 |
| (1) LN | 026-14 1 |
| $\dagger$ | 027-71 |
| STO 1 | 028-23 |


| KEY ENTRY | DISPLAY |
| :---: | :---: |
| n RTN | 029- 2512 |
| (h) LBL 4 | 030-25, 13, 4 |
| 1 | 031 - 1 |
| STO 4 | 032- 234 |
| GSB 6 | 033-136 |
| (b) $1 / x$ | 034-25 |
| RCL 3 | 035-24 3 |
| GSB 8 | 036-138 |
| $x$ | 037-61 |
| CHS | 038- 32 |
| STO 4 | 039- 234 |
| h RTN | 040- 2512 |
| (h) LBL 3 | 041-25, 13, 3 |
| GSB 6 | 042-136 |
| GSB 8 | 043-138 |
| CHS | 044- 32 |
| STO 3 | 045- 23 - |
| n RTN | 046- 2512 |
| (h) LBL 5 | 047-25, 13, 5 |
| GSB 6 | 048-136 |
| RCL 3 | 049-24 3 |
| $\pm$ | 050- 51 |
| RCL 7 | 051-74 |
| $\pm$ | 052-71 |
| CHS | 053-32 |
| STO 5 | 054-23 |
| h RTN | 055-2512 |
| h LBL 2 | 056-25, 13, 2 |
| $\square$ | 057-73 |


| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :---: | :---: | :---: | :---: |
| 2 | 058- 2 | STOO 6 | 087- 236 |
| ENTER4 | 059- 31 | (b) For 0 | 088-25, 71, 0 |
| EEX | 050- 33 | STO 0 | 089- 230 |
| CHS | 061- 32 | ECL 1 | 090- 241 |
| 3 | 062- 3 | CHS | 091- 32 |
| (b) CF 1 | 063-25, 61, 1 | (b) $y^{x}$ | 092- 25 3 |
| (f) Solve B | 064-14, 73, 12 | STO 7 | 093- $23 \quad 7$ |
| GTO 7 | 065- 227 | 1 | 094- |
| GTO 0 | 066- 220 | $x=y$ | 095- 21 |
| (b) LBL 7 | 067-25, 13, 7 | $\square$ | 096- 41 |
| EEX | 068- 33 | STO 9 | 097- 23 9 |
| 2 | 069- 2 | RCL 0 | 098- 240 |
| 区 | 070- 61 | $\pm$ | 099- 61 |
| STO 2 | 071- 232 | RCL 4 | 100- 244 |
| R/S | 072- 74 | ECL 8 | 101- 248 |
| ( $)_{\text {LBL }}$ B | 073-25, 13, 12 | $\square$ | 102- 71 |
| STO 8 | 074- 238 | STO - 0 | 103- 23.0 |
| GTO 9 | 075- 229 | 区 | 104- 61 |
| (n) LBL 6 | 076-25, 13, 6 | (b) F 1 | 105-25, 71, 1 |
| (b) SF 1 | 077-25, 51, 1 | n RTN | 106- 2512 |
| 1 | 078- 1 | GSB 8 | 107- 138 |
| ECL 2 | 079- 242 | (RCL 3 | 108- 243 |
| (n) \% | 080- 2541 | $\pm$ | 109- 51 |
| STO 8 | 081- 238 | CHS | 110- 32 |
| (n) LBL 9 | 082-25, 13, 9 | (b) RTN | 111- 2512 |
| (RCL 8 | 083- 248 | (n) LBL 8 | 112-25, 13, 8 |
| 1 | 084- 1 | RCL 5 | 113- 245 |
| STOO 0 | 085- 230 | RCL 7 | 114- 247 |
| $\pm$ | 086- 51 | $\pm$ | 115- 61 |


| KEY ENTRY | DISPLAY |  |
| :--- | :--- | :---: |
| $\square$ | $116-\quad 51$ |  |


| KEY ENTRY | DISPLAY |
| :---: | :---: |
|  |  |


| REGISTERS |  |  | I Unused |
| :--- | :--- | :--- | :--- |
| $\mathrm{R}_{0} \mathrm{i}$ or $1+i$ | $\mathrm{R}_{1} \mathrm{n}$ | $\mathrm{R}_{2} \mathrm{i}(\%)$ | $\mathrm{R}_{3} \mathrm{PV}$ |
| $\mathrm{R}_{4} \mathrm{PMT}$ | $\mathrm{R}_{5} \mathrm{FV}(\mathrm{BAL})$ | $\mathrm{R}_{6} 1+i$ | $\mathrm{R}_{7}(1+i)^{-n}$ |
| $\mathrm{R}_{8} \mathrm{i} / 100$ | $\mathrm{R}_{9}\left[1-(\mathrm{i}+\mathrm{i})^{-n}\right]$ | $\mathrm{R}_{.0} \mathrm{PMT} / \mathrm{i}$ | $\mathrm{R}_{.1}$ Unused |
| $\mathrm{R}_{.2}$ Unused |  |  |  |


| STEP | IMSTRUCTIONS | $\begin{array}{\|c\|} \hline \text { INPUT } \\ \text { DATAUNITS } \end{array}$ | KEYS | OUTPUT DATAUNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Clear the storage registers. |  | (1) CLEAR REG |  |
| 3 | Set for ordinary annuity (1.00), |  | (A) | 1.00 |
|  | or, for annuity due (0.00). |  | (A) | 0.00 |
|  | (Press $\triangle$ until you see the |  |  |  |
|  | desired display.) |  |  |  |
| 4 | Input the known values: |  |  |  |
|  | Number of periods | $n$ | STOP 1 | $n$ |
|  | Periodic interest rate | $i(\%)$ | STO) 2 | $i(\%)$ |
|  | Present value | PV | STO 3 | PV |
|  | Periodic payment | PMT | $\mathrm{STO}^{4}$ | PMT |
|  | Future value, balloon or |  |  |  |
|  | balance | $F V(B A L)$ | STO) 5 | $F V(B A L)$ |
| 5 | Calculate the unknown value: |  |  |  |
|  | Number of periods |  | GSB 1 | $n$ |
|  | Periodic interest rate |  | GSB 2 | $i(\%)$ |
|  | Present value |  | GSB 3 | PV |
|  | Periodic payment |  | GSB 4 | PMT |
|  | Future value, balloon or |  |  |  |
|  | balance |  | GSB 5 | $F V(B A L)$ |


| STEP | INSTRUCTIONS | INPUT <br> DATA/UNITS | KEYS | OUTPUT <br> DATA/UNITS |
| :---: | :--- | :---: | :---: | :---: |
| 6 | For a new case go to step 4 and |  |  |  |
|  | change appropriate values. |  |  |  |
|  | Input zero for any value not |  |  |  |
|  | applicable in the new case. |  |  |  |
| 7 | For a new problem, go to step 2. |  |  |  |

## Example 1:

If you place $\$ 155$ in a savings account paying $53 / 4 \%$ compounded monthly, what sum of money can you withdraw at the end of 9 years?

FV?


Keystrokes:

## Display:

f CLEAR REG

| A | 0.00 |  |
| :---: | :---: | :---: |
| (A) | 1.00 | ordinary annuity |
| 9 ENTERA $12 \times$ |  |  |
| STO 1 | 108.00 | \# of months |
| 5.75 ENTER4 $12 \%$ |  |  |
| STO 2 | 0.48 | \% monthly interest rate |
| 155 CHS STO 3 | -155.00 | initial deposit |
| GSB 5 | 259.74 | FV |

If you desire a sum of $\$ 275$ what would be the required interest rate?

| 275 STO 5 | 275.00 |  |
| :--- | :--- | :--- |
| GSB 2 | 0.53 | \% monthly interest rate |
| $12 x$ | 6.39 | \% yearly interest rate |

## Example 2:

You receive $\$ 30,000$ from the bank as a 30 year, $9 \%$ mortgage. What monthly payment must you make to the bank to fully amortize the mortgage?


Keystrokes:
Display:
$f$ CLEAR REG
30 ENTERA $12 x$
STO $1 \quad 360.00$

9 ENTERA $12 \div$

| STO 2 | 0.75 | \% monthly interest rate |
| :--- | :--- | :--- |
| 30000 STO 3 | $30,000.00$ | PV |
| GSB 4 | -241.39 | PMT |

## Example 3:

Two individuals are constructing a loan with a balloon payment. The loan amount is $\$ 3,600$ and it is agreed that the annual interest rate will be $10 \%$ with 36 monthly payments of $\$ 100$. What balloon payment amount, to be paid coincident with the $36^{\text {th }}$ payment, is required to fulfill the loan agreement?
(Note the cash flow diagram below is with respect to the lender. For the borrower, the appropriate diagram will be exactly the opposite.)


Keystrokes:
Display:
f CLEAR REG
36 STO 1136.00
10 ENTERA $12 \div$
STO $2 \quad 0.83$
3600 CHS STO $3-3,600.00$
100 STO 4 GSB 5675.27
BAL
(Note that the final payment is $\$ 675.27+\$ 100.00=\$ 775.27$ since the final payment falls at the end of the last period.)

## Example 4:

This program may also be used to calculate accumulated interest/ remaining balance for loans. The accumulated interest between two points in time, $n_{1}$ and $n_{2}$, is just the total payments made in that period less the principal reduction in that period. The principal reduction is the difference of the remaining balances for the two points in time. The following example demonstrates the concepts above:
For a 360 month, $\$ 50,000$ loan at $91 / 2 \%$ annual interest, find the remaining balance after the $24^{\text {th }}$ payment and the accrued interest for payments $13-24$ (between the $12^{\text {th }}$ and $24^{\text {th }}$ payments!).

First we must calculate the payment on the loan:

| Keystrokes: | Display: |  |
| :---: | :---: | :---: |
| (1)CLEAR REG |  |  |
| 360 STO 1 | 360.00 |  |
| 9.5 ENTERA 12 † |  |  |
| STO 2 | 0.79 |  |
| 50000 CHS STO 3 | -50,000.00 |  |
| GSB 4 | 420.43 | PMT |

The remaining balance at month 24 is:
24 STO 1 GSB 5 49,352.76 BAL @ month 24
Store this remaining balance and calculate the remaining balance at month 12 :

## STO $\cdot 112$ STO 1

GSB 5
49,691.68
BAL @ month 12

The principal reduction between payments 12 and 24 is:

```
RCL :- 1 | O38.92
```

The accrued interest is 12 payments less the principal reduction:

| RCL $412 \boxed{x}$ | $5,045.13$ | Total paid out |
| :--- | :--- | :--- |
| $x<y$ | $4,706.20$ | Accrued interest |

## Example 5:

A "third party" leasing firm is considering the purchase of a minicomputer priced at $\$ 63,000$ and intends to achieve a $13 \%$ annual yield by leasing the computer to a customer for a 5 -year period. Ownership is retained by the leasing firm, and at the end of the lease they expect to be able to sell the equipment for at least $\$ 10,000$. What should they establish as the monthly payment in order to realize their desired yield? (Since lease payments occur at the start of the periods, this is an annuity due problem.)


Keystrokes: Display:
f CLEAR REG
A
0.00
annuity due
5 ENTER4 $12 x$

STO $1 \quad 60.00$
13 ENTER4 12 +
STO 21.08
63000 CHS STO $3-63,000.00$
10000 STO 5 10,000.00
GSB $4 \quad \mathbf{1 , 3 0 0 . 1 6}$

If the price is increased to $\$ 70,000$ what should the payments be?

| 70000 | CHS STO 3 | $-70,000.00$ |
| :--- | :--- | :--- |
| GSB 4 | $1,457.73$ |  |

If the payments were increased to $\$ 1,500$ what would the yield be?

| 1500 STO 4 | $1,500.00$ |  |
| :--- | :--- | :--- |
| GSB 2 | 1.18 | \% per month |
| 12 母 | $\mathbf{1 4 . 1 2}$ | \% per year |

## Discounted Cash Flow Analysis

Two forms of discounted cash flow analysis are the net present value (NPV) approach and the internal rate of return (IRR) approach. This program calculates either $N P V$ or $I R R$ for up to 8 groups of cash flows.
The amount of the initial investment is input (observing the sign convention) followed by the positive or negative amounts of each group of future cash flows, and the number of times the series of cash flows occurs. The cash flows must occur at equal intervals.

After the initial investment and all cash flows have been entered, the user may: 1) Input an assumed interest rate and calculate the net present value ( $N P V$ ) of the investment, or 2 ) Calculate the internal rate of return ( $I R R$ ). The $I R R$ is an interest rate that equates the present value of a set of cash flows with an initial investment. It is the interest rate that is obtained when the calculated net present value of a series of cash flows is zero. IRR is also called the yield or discounted rate of return.

This program uses the convention that cash outlays are input as negative, and cash incomes are input as positive.

## Remarks:

- Calculation of IRR may take several minutes (5 or more) depending on the number of cash flow entries.
- The cash flow sequence (including the initial investment) must contain at least one sign change.
- Cash flows with multiple sign changes may have multiple answers. This program may find one answer but has no way of indicating other possibilities.
- The program is designed for optimum operation when $0 \%<I R R$ $\leqslant 100 \%$. It often will solve for interest rates outside these ranges but will display Error messages for zero interest rates or if it is unable to find a solution.

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :---: | :---: | :---: | :---: |
| (1)CLEAR PRGM | 000- | $\square$ | 029- 41 |
| (n) LBL | 001-25, 13, 11 | STO 10 | 030-23, 14, 23 |
| STO $\cdot 8$ | 002- 23.8 | STO $\square^{-1}$ | 031- 23.7 |
| 1 | 003- 1 | (G) R ( | 032- 1522 |
| $\bullet$ | 004- 73 | - F 1 | 033-25, 71, 1 |
| 0 | 005- 0 | GTO 2 | 034- 222 |
| 1 | 006- | 1 | 035- 1 |
| 6 | 007- 6 | ENTER | 036- 31 |
| STO 1 | 008-23, 14, 23 | EEX | 037- 33 |
| $x<y$ | 009- 21 | CHS | 038- 32 |
| (b) LBL 0 | 010-25, 13, 0 | 3 | 039- 3 |
| R/S | 011- 74 | (f) SOLVE 2 | 040-14, 73, 2 |
| $x=7$ | 012- 21 | GTO 3 | 041- 223 |
| STO (f) (ii) | 013-23, 14, 24 | GTO 9 | 042- 229 |
| (9) $\times$ R | 014- 1522 | (b) LBL 3 | 043-25, 13, 3 |
| (9) 156 | 015- 1524 | EEX | 044- 33 |
| STO 9 (1i) | 016-23, 14, 24 | 2 | 045- 2 |
| (9) 156 | 017- 1524 | 区 | 046- 61 |
| GTO 0 | 018- 220 | R/S | 047-74 |
| R/S | 019- 74 | (b) LBL 2 | 048-25, 13, 2 |
| ( $\square_{\text {LBL }} 1$ | 020-25, 13, 1 | 1 | 049- |
| (n) SF 1 | 021-25, 51, 1 | $\pm$ | 050- 51 |
| EEX | 022- 33 | STO) 0 | 051- 230 |
| 2 | 023- 2 | 0 | 052- 0 |
| $\square$ | 024- 71 | (n) LBL 4 | 053-25, 13, 4 |
| (b) LBL B | 025-25, 13, 12 | RCL 0 | 054- 240 |
| RCL 10 | 026-24, 14, 23 | (RCL ( ${ }^{\text {(ii) }}$ | 055-24, 14, 24 |
| n INT | 027- 2532 | CHS | 056- 32 |
| 1 | 028- 1 | (b) $y^{x}$ | 057- 253 |


| KEY ENTRY | DISPLAY |  |  | KEY ENTRY | DISPLAY |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 区 | 058 |  | 61 | RCL 0 | 068- |  | 0 |
| 1 | 059 |  | 1 | 1 | 069- |  | 1 |
| - LSTx | 060 | 25 |  | $\square$ | 070- |  | 41 |
| $\square$ | 061 |  | 41 | $\square$ | 071 - |  | 1 |
| 9 DSE | 062 | 15 |  | RCL -8 | 072- |  | . 8 |
| RCL (i) (ii) | 063 | 14, |  | $\pm$ | 073- |  | 51 |
| 区 | 064 |  | 61 | RCL $\cdot 7$ | 074- | 24 | . 7 |
| $\pm$ | 065 |  | 51 | STO 1 | 075- | 14, | 23 |
| 9 DSE | 066 | 15 |  | [9] R | 076- | 15 | 22 |
| GTO 4 | 067 | 22 | 4 | ( $\square_{\text {c }} 1$ | 077-25 | 61, | 1 |


| REGISTERS |  |  | I Control |
| :--- | :--- | :--- | :--- |
| $\mathrm{R}_{0} 1+i$ | $\mathrm{R}_{1} \mathrm{CF}_{1}$ | $\mathrm{R}_{2} \mathrm{~N}_{1}$ | $\mathrm{R}_{3} \mathrm{CF}_{2}$ |
| $\mathrm{R}_{4} \mathrm{~N}_{2}$ | $\mathrm{R}_{5} \mathrm{CF}_{3}$ | $\mathrm{R}_{6} \mathrm{~N}_{3}$ | $\mathrm{R}_{7} \mathrm{CF}_{4}$ |
| $\mathrm{R}_{8} \mathrm{~N}_{4}$ | $\mathrm{R}_{9} \mathrm{CF}_{5}$ | $\mathrm{R}_{.0} \mathrm{~N}_{5}$ | $\mathrm{R}_{.1} \mathrm{CF}_{6}$ |
| $\mathrm{R}_{.2} \mathrm{~N}_{6}$ | $\mathrm{R}_{.3} \mathrm{CF}_{7}$ | $\mathrm{R}_{.4} \mathrm{~N}_{7}$ | $\mathrm{R}_{.5} \mathrm{CF}_{8}$ |
| $\mathrm{R}_{.6} \mathrm{~N}_{8}$ | $\mathrm{R}_{.7}$ Used | $\mathrm{R}_{88} \mathrm{CF}_{0}$ |  |


| STEP | IMSTRUCTIONS | INPUT <br> DATNUNITS | KEYS | OUTPUT <br> DATAUNITS |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Optional: set display status |  |  |  |
|  | as desired. (suggest FIX 2.) |  |  |  |
| 3 | Input the initial investment. ${ }^{*}$ | INV | A | INV |
| 4 | Beginning with the first period, |  |  |  |
|  | key in each cash flow* and the |  |  |  |
|  | number of times it occurs, |  |  |  |
|  | pressing [R/S after each | CF | ENTER4 |  |
|  | group. (Be sure to key in 1 if | N | ER/S | N |
|  | the cash flow occurs only |  |  |  |
|  | once.) |  |  |  |


| STEP | INSTRUCTIONS | INPUT <br> DATA/UNITS | KEYS | OUTPUT <br> DATA/UNITS |
| :---: | :--- | :--- | :--- | :--- |
| 5 | Repeat step 4 until all cash |  |  |  |
|  | flows have been input. Then go |  |  |  |
|  | to step 6 for IRR or step 7 for |  |  |  |
|  | NPV. |  |  | B |
| 6 | T0 CALCULATE INTERNAL |  |  | IRR (\%) |
|  | RATE OF RETURN: |  |  |  |
| 7 | T0 CALCULATE NET |  |  | NPV |
|  | PRESENT VALUE: |  |  |  |
|  | Input the applicable periodic |  |  |  |
| 8 | interest (discount) rate. | $\mathrm{i}(\%)$ |  | GSB1 |
|  | Always return to step 3 for a |  |  |  |
|  | new case or a new calculation. |  |  |  |
|  |  |  |  |  |
|  | Be sure to observe proper sign |  |  |  |
|  | convention for initial investment |  |  |  |
|  | and cash flows. |  |  |  |

## Example 1:

An investor pays $\$ 80,000$ for a duplex that he intends to sell after 7 years. He must spend some money the first year for repairs. At the end of the seventh year the duplex is sold for $\$ 91,000$. Will he achieve a desired $9 \%$ after tax yield with the following after tax cash flows?

Keystrokes: Display:
(f) FIX 2
80000 CHS $A$-80,000.00
600 CHS ENTER

| R/S |  |  | 1.00 |
| :---: | :---: | :---: | :---: |
| 6500 | ENIER4 1 | R/S | 1.00 |
| 8000 | EmIER4 2 | R/S | 2.00 |
| 7500 | ENIER4 2 | R/S | 2.00 |
| 91000 | ENTER 1 | R/S | 1.00 |
| 9 GSB | ] |  | -4,108.06 |

Since the NPV is negative the investment does not achieve the desired $9 \%$ yield.

## Example 2:

An investment of $\$ 620,000,000.00$ is expected to have the following annual income stream for the next 15 years:

## Number of Years:

First 10 years next 5 years

## Cash Flow (\$):

100,000,000
5,000,000

What is the expected rate of return?
Keystrokes: Display:
620000000 CHS A -620,000,000.0
100000000 ENTER4
10 R/S 10.00
5000000 ENIER4
5 R/S 5.00
B
10.06
(annual IRR of $10.06 \%$ )

## Recreation

## Moon Rocket Lander

Imagine for a moment the difficulties involved in landing a rocket on the moon with a strictly limited fuel supply. You're coming down tailfirst, freefalling toward a hard rock surface. You'll have to ignite your rockets to slow your descent; but if you burn too much too soon, you'll run out of fuel 100 feet up, and then you'll have nothing to look forward to but cold eternal moon rocks coming faster every second. The object, clearly, is to space your burns just right so that you will alight on the moon's surface with no downward velocity.

The game starts off with the rocket descending at a velocity of 50 feet/second from a height of 500 feet. The velocity and altitude are shown in a combined display as -50.0500 , the altitude appearing to the right of the decimal point and the velocity to the left, with a negative sign on the velocity to indicate downward motion. Then the remaining fuel is displayed and the rocket fire count-down begins: "3", "2", "1", "0". Exactly at zero you may key in a fuel burn. A zero burn, which is very common, is accomplished by simply pressing R/S. After a burn the sequence is repeated unless:

1. You have successfully landed-flashing zeros.
2. You have smashed into the lunar surface-flashing crash velocity.

You must take care, however, not to burn more fuel than you have; for if you do, you will free-fall to your doom! The final velocity shown will be your impact velocity (generally rather high). You have 60 units of fuel initially.

## Equations:

We don't want to get too specific, because that would spoil the fun of the game; but rest assured that the program is solidly based on some old friends from Newtonian physics:

$$
x=x_{0}+V_{0} t+\frac{1}{2} a t^{2}, \quad V=V_{0}+a t, \quad V^{2}=V_{0}^{2}+2 a\left(x-x_{0}\right)
$$

where:
$x, V, a$, and $t$ are distance, velocity, acceleration, and time.

## Remarks:

- Only integer values for fuel burn are allowed. R/s can be used to stop Moon Rocket Lander at any time.

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :---: | :---: | :---: | :---: |
| $\square_{\text {dCLEAR PRGM }}$ | 000- | (1) FIX 0 | 029-14, 11, 0 |
| ( $\dagger$ LBL $\triangle$ | 001-25, 13, 11 | RCL 8 | 030- 248 |
| 5 | 002- 5 | ¢ PSE | 031- 2574 |
| 0 | 003- 0 | 3 | 032- 3 |
| 0 | 004- 0 | (b) PSE | 033- 2574 |
| STO) 6 | 005- 236 | 2 | 034- 2 |
| 5 | 006- 5 | n PSE | 035- 2574 |
| 0 | 007- 0 | 1 | 036- 1 |
| CHS | 008- 32 | D PSE | 037- 2574 |
| STO 7 | 009- 237 | 0 | 038- 0 |
| 6 | 010- 6 | (b) PSE | 039- 2574 |
| 0 | 011- 0 | (b) LBL 9 | 040-25, 13, 9 |
| STO 8 | 012- 238 | RCL 8 | 041- 248 |
| (n) LBL 0 | 013-25, 13, 0 | $x=y$ | 042- 21 |
| RCD 6 | 014- 246 | (f) $x>y$ | 043- 1451 |
| [f FIX 4 | 015-14, 11, 4 | GTO 6 | 044- 226 |
| EEX | 016- 33 | STO 8 | 045-23, 41, 8 |
| 4 | 017- 4 | 2 | 046- 2 |
| $\dagger$ | 018- 71 | $\pm$ | 047-61 |
| RCL 7 | 019- 2478 | 5 | 048- 5 |
| (b) ABS | 020- 2534 | $\square$ | 049- 41 |
| $\pm$ | 021- 51 | STO 9 | 050- 23 9 |
| RCL 7 | 022- 247 | 2 | 051- 2 |
| 9 $\times$ x>0 | 023- 1551 | $\dagger$ | 052- 71 |
| GSB 4 | 024- 134 | RCL 6 | 053- 246 |
| $x \geqslant y$ | 025- 21 | $\pm$ | 054- 51 |
| CHS | 026- 32 | (RCL 7 | 055- 247 |
| ( $\square_{\text {PSE }}$ | 027- 2574 | $\pm$ | 056- 51 |
| n PSE | 028- 2574 | RCL 9 | 057- $24 \quad 9$ |


| KEY ENTRY | DISPLAY |
| :---: | :---: |
| STO $\dagger 7$ | 058-23, 51, 7 |
| (9) $\mathrm{BO}_{6}$ | 059-1522 |
| STO 6 | 060- 236 |
| (b) INT | 061- 2532 |
| (9) $x>0$ | 062- 1551 |
| GTO 0 | 063- 220 |
| RCL 7 | 064- 247 |
| (n) LBL 7 | 065-25, 13, 7 |
| D PSE | 066- 2574 |
| GTO 7 | 067- 227 |
| [ 4 LBL 6 | 068-25, 13, 6 |
| RCL 8 | 069- 248 |
| 2 | 070- 2 |
| $\bullet$ | 071-73 |
| 5 | 072- 5 |
| $\square$ | 073- 41 |
| STO + 6 | 074-23,51, 6 |


| KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: |
| 2 | 075- | 2 |
| $\pm$ | 076- | 61 |
| STO +7 | 077-23, | 51, 7 |
| RCL 6 | 078- | 246 |
| 1 | 079- | 1 |
| 0 | 080- | 0 |
| 区 | 081 - | 61 |
| (RCL) 7 | 082- | 247 |
| (9) $x^{2}$ | 083- | 153 |
| $\pm$ | 084- | 51 |
| (f) $\sqrt{x}$ | 085- | 143 |
| CHS | 086- | 32 |
| GTO 7 | 087- | 227 |
| [ $\square$ LBL 4 | 088-25, | 13, 4 |
| x<y | 089- | 21 |
| CHS | 090- | 32 |
| $x<y$ | 091 - | 21 |


| REGISTERS |  |  | I Unused |
| :--- | :--- | :--- | :--- |
| $R_{0}$ | $R_{1}$ | $R_{2}$ | $R_{3}$ |
| $R_{4}$ | $R_{5}$ | $R_{6} X$ | $R_{7} V$ |
| $R_{8}$ FUEL | $R_{9}$ ACCEL. | $R_{.0}-R_{.6}$ Unused |  |


| STEP | IMSTRUCTIONS | ITPUT <br> DATAUNITS | KEYS | OUTPUT <br> DATAUMITS |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Assume manual control. |  | A | "V.ALT" |
|  |  |  |  | "FUEL" |
|  |  |  |  | $" 3$ " |
|  |  |  |  | $" 2$ " |


| STEP | INSTRUCTIONS | INPUT DATA/UNITS | KEYS | OUTPUT DATA/UNITS |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | "1" |
|  |  |  |  | "0' |
| 3 | Key in burn: |  |  |  |
|  | Upon " 0 ' ' display, |  |  |  |
|  | press R/S then |  | R/S |  |
|  | enter burn. | BURN | R/S | 'V.ALT' |
|  |  |  |  | "FUEL" |
|  |  |  |  | " 3 " |
|  |  |  |  | "2" |
|  |  |  |  | "1" |
|  |  |  |  | "0" |
| 4 | Go to step 3 until you land |  |  |  |
|  | (flashing zeros) or crash |  |  |  |
|  | (flashing impact velocity). |  |  |  |
| 5 | If you survived last landing |  |  |  |
|  | attempt, go to step 2 for another |  |  |  |
|  | try. |  |  |  |

## Nimb

The game of Nimb begins with a collection of N objects, or as the calculator plays it, with the positive number N. Each player alternately subtracts one, two, or more from the total until only one is left. The player forced to take the last one loses.
To begin the game you specify the maximum number that can be taken in a single move. Then you tell the calculator how many objects you wish to start with (i.e., the value of N ).

After each move the machine will display the remaining total. A negative sign indicates that it is the player's move next, while a positive display indicates that it is the HP-34C's move.

As the challenger you are allowed to make the first move. It is possible for you to win, but of course the HP-34C is a master player: it will not let you make an error and win. If you cheat by taking more than the specified limit the calculator will catch you and force you to repeat the move.

This program is based on an HP-25 program by James L. Horn.

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: | :---: | :---: |
| OCLEAR PRGM | 000- | $\pm$ | 029- | 51 |
| ( $\dagger$ LBL $\triangle$ | 001-25, 13, 11 | (g) $x<0$ | 030- | 1541 |
| (f) FIX 0 | 002 14, 11, 0 | GTO 0 | 031 - | 220 |
| STO 0 | 003- 230 | RCL 3 | 032- | 243 |
| 1 | 004- 1 | GTO 1 | 033- | 221 |
| $\pm$ | 005- 51 | (b) LBL 0 | 034-2 | 13, 0 |
| STO 1 | 006- 231 | D LSTX | 035- | 250 |
| 3 | 007- 3 | 1 | 036- | 1 |
| 5 | 008- 5 | (f)x>y | 037- | 1451 |
| 0 | 009- 0 | GTO) 2 | 038- | $22 \quad 2$ |
| 7 | 010- 7 | (g) R ${ }^{\text {a }}$ | 039- | 1522 |
| $\bullet$ | 011- 73 | RCL 1 | 040- | 241 |
| 1 | 012- | (f) $x \leq y$ | 041 - | 1441 |
| STO) 2 | 013- 232 | GTO 2 | 042- | $22 \quad 2$ |
| 5 | 014- 5 | $x=y$ | 043- | 21 |
| 5 | 015- 5 | STO 0 | 044-2 | , 41, 0 |
| 1 | 016- | RCL 0 | 045- | 240 |
| 7 | 017-7 | R/S | 046- | 74 |
| 8 | 018- 8 | 1 | 047 - | 1 |
| STO 3 | 019- 23 3 | $\square$ | 048- | 41 |
| RCL 0 | 020- 240 | RCL 1 | 049- | 241 |
| ( $\square_{\text {LBL }} 1$ | 021-25, 13, 1 | $\square$ | 050- | 71 |
| R/S | 022- 74 | ( $\square_{\text {FRAC }}$ | 051 - | 2533 |
| (b) LBL B | 023-25, 13, 12 | RCL 1 | 052 - | $24 \quad 1$ |
| (f) FIX 0 | 024-14, 11, 0 | $\pm$ | 053- | 61 |
| STO) 0 | 025- 230 | (9) $x=0$ | 054- | 1571 |
| (n) LBL 4 | 026-25, 13, 4 | 1 | 055- | 1 |
| CHS | 027- 32 | STO $\square 0$ | 056-2 | , 41, 0 |
| 8/5 | 028- 74 | (n) LBL 2 | 057-2 | , 13, 2 |


| KEY ENTRY | DISPLAY |  |  |
| :--- | :--- | :--- | :--- |
| KRL 0 | $058-$ | 24 | 0 |
| $\mathbf{R} \quad x \neq 0$ | $059-$ | 15 | 61 |
| GTO 4 | $060-$ | 22 | 4 |


| KEY ENTRY | DISPLAY |  |
| :--- | :--- | ---: |
| [RCL 2 | $061-24$ | 2 |
| [ FIX 1 | $062-14,11$, | 1 |
| GTO 1 | $063-\quad 22$ | 1 |


| REGISTERS |  |  | I Unused |
| :--- | :--- | :--- | :--- |
| $\mathrm{R}_{0}$ Total | $\mathrm{R}_{1}$ Max+1 | $\mathrm{R}_{2} 3507.1$ | $\mathrm{R}_{3} 55178$ |
| $\mathrm{R}_{4}-\mathrm{R}_{.9}$ Unused |  |  |  |


| STEP | INSTRUCTIONS | INPUT <br> DATA/UNITS | KEYS | OUTPUT <br> DATA/UNITS |
| :---: | :--- | :--- | :--- | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Indicate the maximum number |  |  |  |
|  | of objects which can be re- |  |  | A |
|  | moved in one move. | MAX |  | MAX |
| 3 | Indicate the total number of |  |  |  |
|  | objects with which you wish to |  |  | -N |
| 4 | start the game, (usually 15). | N the number in the display is |  |  |
|  | negative, key in your move and |  |  | R/S |
|  | see the number remaining. | MOVE |  | +REM |
| 5 | If the number in the display is |  |  | R/S |
|  | positive, let the HP-34C move. |  |  | -REM |
| 6 | Do steps 4 and 5 until the |  |  | BLISS |
|  | game is over. |  |  |  |
| 7 | At the end of the game turn the |  |  |  |
|  | calculator upside down to read |  |  |  |
|  | the message. |  |  |  |
|  | If calculator loses: |  |  |  |
|  | If calculator wins: |  |  |  |


| STEP | INSTRUCTIONS <br> 8 | INPUT <br> DATAUNITS | KEYS | OUTPUT <br> DATA/UNITS |
| :---: | :--- | :--- | :--- | :--- |
|  | If max. move remains same, go |  |  |  |
|  | to step 3. |  |  |  |
|  | For different max. move go to |  |  |  |
|  | step 2. |  |  |  |

## Example:

Starting with 15 objects, with a maximum allowable move of 3, play Nimb with the HP-34C.

## Keystrokes:



5 R/S
2 R/S R/S


1 R/S

## Display:

$$
3 .
$$

-15.
12.
$-9$.
-9.
7.
-5.
2.
-1.
55178.

Ready
Player takes 3
HP-34C takes 3
Player tries to cheat.
Player takes 2
HP-34C takes 2
Player takes 3
HP-34C takes 1
Player takes last one and loses.

Turn calculator upside down for message: BLISS

## General

## Timers

This program converts your HP-34C into a timer which can operate as 1) a count-down timer, counting down to display zero when the preset time has elapsed, or 2 ) a count-up timer, displaying the elapsed time since the timer was started. The upper limit of the count-up timer is approximately 10 minutes.
When using this program, you should remember that the clock circuits of the HP-34C are designed for calculator use, not for accurate timekeeping. Although the routine may be calibrated quite accurately, highly stable performance should not be expected.

## Equation:

$$
C_{\text {NEW }}=C_{\text {OLD }} \frac{\text { HP time }}{\text { Actual time }}
$$

## Remarks:

- All times are input or displayed in (H.MMSS) format.
- Your calibration constants may differ substantially from those given here.

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |
| :---: | :---: | :---: | :---: |
| TCLEAR［PRGM | 000－ | （sto ${ }^{\text {f }}$ 1 | 029－23，14， 23 |
| ［明（ A | 001－25，13， 11 | 0 | 030－ 0 |
| －［ 0 | 002－25，61， 0 | E／S | 031－ 74 |
| ［ FIX 4 | 003－14，11， 4 | ［6BL 7 | 032－25，13， 7 |
| STOO 0 | 004－ 230 | （9）ISG | 033－ 1524 |
| ［ 5 ［80 9 | 005－25，13， 9 | GTOO 7 | 034－ 227 |
| 0 | 006－ |  | 035－25，13， 12 |
| E／S | 007－ 74 | RCL $\square^{1}$ | 036－24，14， 23 |
| STOO 1 | 008－ 23 | W［1NT | 037－ 2532 |
| （9） | 009－ 156 | ［CCL 2 | 038－ 242 |
| ECL 0 | 010－ 240 | $\square$ | 039－ 71 |
| $\pm$ | 011－ 61 | （1）+ H．Ms | 040－ 146 |
| ［ ${ }_{\text {INT }}$ | 012－ 2532 | R／S | 041－ 74 |
| ［50］［1］ | 013－23，14， 23 | GTOO 6 | 042－ 226 |
| ［RCD 1 | 014－ 241 | ［ $\square 1$ | 043－25，13， 1 |
| R／S | 015－ 74 | （9 | 044－ 156 |
| ［ $\square_{\text {LBL }} 8$ | 016－25，13， 8 | x $\times 1$ | 045－ 21 |
| （9）DSE | 017－ 1523 | （9 －$^{\text {c }}$ | 046－ 156 |
| GTo 8 | 018－ 228 |  | 047－ 21 |
| GTO 9 | 019－ 22 | $\square$ | 048－ 41 |
|  | 020－25，13， 12 | RCL 1 | 049－ 24 |
| ［b SF0 | 021－25，51， 0 | （ $\square^{+}$ | 050－ 156 |
| （1）FIX 4 | 022－14，11， 4 | $\dagger$ | 051－ 71 |
| STOP 2 | 023－ 23 | W | 052－ 252 |
| ［n［BL 6 | 024－25，13， 6 | ［匆 0 | 053－25，71， 0 |
| $\square$ | 025－ 73 | GTO 0 | 054－ 22 |
| 9 | 026－ | RCL 0 | 055－ 24 |
| 9 | 027－ | 区 | 056－ 61 |
| 9 | 028－ | E／S | 057－ 74 |


| KEY ENTRY | DISPLAY |  |  |
| :---: | :---: | :---: | :---: |
| GTO (A) | 058- | 22 | 11 |
| (b) LBL 0 | 059-25, 13, 0 |  |  |
| RCL 2 | 060- | 24 | 2 |


| KEY ENTRY | DISPLAY |  |
| :--- | :--- | ---: |
| $\boxed{x}$ | $061-$ | 61 |
| R/S | $062-$ | 74 |
| GTO B | $063-$ | 2212 |


| REGISTERS |  |  | I Counter |
| :--- | :--- | ---: | :--- |
| $\mathrm{R}_{0} \mathrm{C}_{\mathrm{d}}$ | $\mathrm{R}_{1}$ Time | $\mathrm{R}_{2} \mathrm{C}_{\mathrm{u}}$ | $\mathrm{R}_{3}-\mathrm{R}_{.9}$ Unused |


| STEP | Instructions | $\begin{gathered} \text { IMPUT } \\ \text { DATAUNITS } \end{gathered}$ | KEYS | OUTPUT DATAUNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
|  | COUNT-DOWN TIMER: |  |  |  |
| 2 | Input count-down timer |  |  |  |
|  | constant (try 5600). | C ${ }_{\text {d }}$ | (4) | 0.0000 |
| 3 | Input desired time. | T (H.MMSS) | R/S | T (H.MMSS) |
| 4 | Start timer. |  | R/S |  |
| 5 | Timer display blinks until |  |  |  |
|  | 0.0000 is displayed and time |  |  |  |
|  | has elapsed. |  |  | 0.0000 |
| 6 | For a new time, T , go to step |  |  |  |
|  | 3. To recalibrate, go to |  |  |  |
|  | step 12. |  |  |  |
|  | COUNT-UP TIMER: |  |  |  |
| 7 | Input count-up timer constant |  |  |  |
|  | (try 5400). | $\mathrm{C}_{u}$ | B | 0.0000 |
| 8 | Start timer. |  | R/S |  |
| 9 | After desired period has |  |  |  |
|  | elapsed, stop timer. |  | R/S | 0.0000 |
| 10 | Display the elapsed time. |  | B | T (H.MMSS) |


| STEP | INSTRUCTIONS | INPUT DATA/UNITS | KEYS | OUTPUT DATA/UNITS |
| :---: | :---: | :---: | :---: | :---: |
| 11 | Reset the timer and go to step |  |  |  |
|  | 8 for another run. To recalibrate |  | R/S | 0.0000 |
|  | the timer, go to step 14. |  |  |  |
| 12 | To calibrate the count-down |  |  |  |
|  | timer, input the ending time | Te(H.MMSS) | ENTER |  |
|  | and the starting time and | Ts ${ }_{\text {(H.MMSS }}$ | GSB 1 | $\mathrm{C}_{\mathrm{D}}$ NEW |
|  | calculate new constant. |  |  |  |
| 13 | To proceed, press R/S |  |  |  |
|  | and go to step 3. |  | R/S | 0.0000 |
| 14 | To calibrate the count-up timer, |  |  |  |
|  | store the displayed elapsed | T (H.MMSS) | STO 1 | T (H.MMSS) |
|  | time. Then input the ending | Te(H.MMSS) | ENTER4 |  |
|  | time and the starting time. | Ts ${ }_{\text {(H.MMSS }}$ | GSB1 | $\mathrm{C}_{u}$ NEW |
| 15 | To proceed, press R/S and |  |  |  |
|  | go to step 8. |  | R/S | 0.0000 |

## Example 1:

Use the count-down time to measure an elapsed timer of 35 seconds, and another of 1 minute, 8 seconds. Try an initial calibration constant of 5600 .

## Keystrokes:

## Display:

| 5600 | $\mathbf{A}$ | 0.0000 |  |
| :--- | :--- | :--- | :--- |
| .0035 | $\mathrm{R} / \mathbf{S}$ | 0.0035 | Count-down time |
| $\mathrm{B} / \mathbf{S}$ |  | 0.0000 | Time has elapsed |

Suppose you recorded, from your watch, an ending time of 3:42:56 and a starting time of $3: 42: 23$, i.e., 33 seconds elapsed. Recalibrate the timer with this information.
3.4256 ENIER4
3.4223
GSB
5939.3937
$C_{\text {D New }}$

Now count-down for 1 minute, 8 seconds.

| .0108 R/S | 0.0108 |
| :--- | :--- |
| $R / S$ | 0.0000 |

The true elapsed time should now be quite close to that input. If it is not, recalibrate again.

Operate the count-up timer for a known elapsed time (say 40 seconds) and recalibrate as needed. Use an initial calibration constant of 5400.

| Keystrokes: | Display: |  |
| :--- | :--- | :--- |
| 5400 B | 0.0000 |  |
| $R / S$ |  |  |
| $R / S$ | 0.0000 | start timer |
| $B$ | 0.0039 | stop timer |
| $B$ |  | elapsed time |

True elapsed time was 40 seconds. Recalibrate:

| STO 1 | 0.0039 |  |
| :--- | :--- | :--- |
| .004 ENTERA | 0.0049 |  |
| 0 GSB 1 | $5,265.0000$ | $\mathrm{C}_{\mathrm{U} \text { NEw (you may get a }}$ <br> different number). |
| R/S | 0.0000 | Input new constant and <br> reset counter |
|  |  |  |

## Random Number Generator

Random numbers are useful in a wide variety of applications, for example: in simulation, sampling, computer programming, numerical analysis and games.
This program includes routines to calculate:

1. Uniformly distributed pseudo-random numbers in the range $0 \leqslant r \leqslant 1$.
2. Uniformly distributed integers from 0 to 9.

It also includes a routine to simulate dealing from an infinite deck of cards. The Ace is 1 ; the Jack, 11; the Queen, 12; the King, 13. All other cards count their face value.

The random number generator:

$$
r_{\mathrm{n}+1}=\operatorname{FRAC}\left(9821 \times r_{\mathrm{n}}+.211327\right)
$$

passes the spectral test (Knuth, V.2, no. 3.4) and, because its parameters satisfy Theorem A (op.cit., p. 15) it generates one million distinct random numbers between 0 and 1 regardless of the value selected for $r_{0}$. This generator was developed by Don Malm as part of an HP-65 Users' Library program.

| KEY ENTRY | DISPLAY | KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: | :---: | :---: |
| $\square^{6}$ CLEAR PRGM | 000- | 区 | 029- | 61 |
| ( LBL $^{4}$ | 001-25, 13, 11 | 1 | 030- | 1 |
| (f) FIX 4 | 002-14, 11, 4 | $\pm$ | 031 - | 51 |
| STO 0 | 003- 230 | D INT | 032- | 2532 |
| GSB 0 | 004- 130 | R/S | 033- | 74 |
| - LBL 3 | 005-25, 13, 3 | GTO 5 | 034- | 225 |
| GSB 9 | 006- 139 | - LBL 0 | 035- | 13, 0 |
| R/S | 007- 74 | 9 | 036- | 9 |
| GTO 3 | 008- 223 | 8 | 037 - | 8 |
| (n) LBL B | 009-25, 13, 12 | 2 | 038 - | 2 |
| (f) FIX 0 | 010-14, 11, 0 | 1 | 039- | 1 |
| STO 0 | 011- 230 | STO 1 | 040- | $23 \quad 1$ |
| GSB 0 | 012- 130 | $\bullet$ | 041 - | 73 |
| (b) LBL 4 | 013-25, 13, 4 | 2 | 042- | 2 |
| GSB 9 | 014-13 9 | 1 | 043- | 1 |
| 1 | 015- 1 | 1 | 044- | 1 |
| 0 | 016- 0 | 3 | 045- | 3 |
| $\pm$ | 017- 61 | 2 | 046- | 2 |
| (b) INT | 018- 2532 | 7 | 047 - | 7 |
| R/S | 019- 74 | STO 2 | 048- | 232 |
| GTO 4 | 020- 224 | (b) RTN | 049- | 2512 |
| - LBL 1 | 021-25, 13, 1 | - 4 LBL 9 | 050-2 | 13, 9 |
| (f) FIX 0 | 022-14, 11, 0 | RCL 0 | 051 - | 240 |
| STO) 0 | 023- 230 | RCL 1 | 052- | 241 |
| GSB 0 | 024- 130 | $\triangle$ | 053- | 61 |
| (b) LBL 5 | 025-25, 13, 5 | RCL 2 | 054- | 242 |
| GSB 9 | 026- 139 | $\pm$ | 055- | 51 |
| 1 | 027- 1 | (b) FRAC | 056- | 2533 |
| 3 | 028- 3 | STO 0 | 057- | 230 |


| REGISTERS |  |  | I Unused |
| :--- | :--- | ---: | :--- |
| $\mathrm{R}_{0} \mathrm{r}_{\mathrm{i}}$ | $\mathrm{R}_{1} 9821$ | $\mathrm{R}_{2} .211327$ | $\mathrm{R}_{3}-\mathrm{R}_{.9}$ Unused |


| STEP | INSTRUCTIONS | INPUT DATAUNITS | KEYS | OUTPUT DATAUNITS |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Input a seed: any number |  |  |  |
|  | between 0 and 1. | SEED |  |  |
|  | For random numbers go to step |  |  |  |
|  | 3. For random integers go to |  |  |  |
|  | step 5. For a simulated card |  |  |  |
|  | dealer go to step 7. |  |  |  |
| 3 | To generate a random number |  |  |  |
|  | $(0 \leqslant r \leqslant 1)$ |  | (A) | $\mathrm{r}_{1}$ |
| 4 | For another random number. |  | R/S | $\mathrm{r}_{2}$ |
|  | Repeat step 4 as desired for |  |  |  |
|  | further random numbers. |  |  |  |
| 5 | To generate random integers |  |  |  |
|  | $(0 \leqslant I N T \leqslant 9)$. |  | B | $\mathrm{INT}_{1}$ |
| 6 | For another random integer. |  | R/S | $\mathrm{INT}_{2}$ |
|  | (Repeat step 6 as desired for |  |  |  |
|  | further random integers.) |  |  |  |
| 7 | To deal cards: |  | GSB 1 | CARD ${ }_{1}$ |
| 8 | For further cards. |  | R/S | $\mathrm{CARD}_{2}$ |
|  | (Repeat step 8 as desired to |  |  |  |
|  | deal more cards.) |  |  |  |
| 9 | For a new start, go to step 2 to |  |  |  |
|  | input a new seed as desired. |  |  |  |

## Example 1:

Using an initial seed of 0.2356 generate a string of pseudo-random numbers.

| Keystrokes: | Display: |
| :--- | :--- | ---: |
| .2356 A | 0.0389 |
| $R / s$ | 0.5134 |
| $R / S$ | 0.2538 |
| etc. |  |

## Example 2:

Using an initial seed of . 12345 deal a hand of 5 cards.

## Keystrokes: Display:

| .12345 GSB I | 8. |  |  |
| :--- | :--- | :--- | :--- |
| R/S |  | 2. |  |
| R/S |  | 1. | Ace |
| R/S |  | 9. |  |
| $R / S$ | 11. | Jack |  |
|  |  |  |  |

## Moving Average

In a moving average, a specified number of data points is averaged. When there is a new piece of input data, the oldest piece of data is discarded to make room for the latest input. This replacement scheme makes the moving average a valuable tool in following trends. The fewer the number of data points, the more trend-sensitive the average becomes. With a large number of data points, the average behaves more like a regular average, responding slowly to new input data.

This program allows for a moving average span of 1 to 17 units. The number of units, $n$, must be specified before any data input begins by keying it in and pressing $B$. Then the data is input by keying in each value, $x_{\mathrm{k}}$, and pressing $A$ in turn. The calculator will display the current input number, $k$, until at least $n$ values have been entered. After the $n^{\text {th }}$ value (and for all succeeding values), the calculator will flash the current input number before halting with the moving average, $A V G$, in the display.

The value of the average may be displayed at any time by pressing GSB 1. This feature allows the average to be calculated before $n$ data points have been input. The average is based on the number of inputs or $n$, whichever is smaller.

## Remarks:

This program clears all registers during its execution. Therefore any data stored in extra registers will be destroyed.

| KEY ENTRY | DISPLAY |
| :---: | :---: |
| fCLEAR PRGM | 000- |
| (b) [BL | 001-25, 13, 12 |
| (1) FIX ${ }^{2}$ | 002-14, 11, 2 |
| fCLEAR REG | 003-1433 |
| STO $\cdot 8$ | 004- 23.8 |
| STO 10 | 005-23, 14, 23 |
| R/S | 006- 74 |
| ( $n$ LBL $A$ | 007-25, 13, 11 |
| RCL $\bullet 9$ | 008- 24.9 |
| 1 | 009- |
| $\pm$ | 010- 51 |
| $x \geq y$ | 011- 21 |
| RCL (1) (ii) | 012-24, 14, 24 |
| STO -0 | 013-23, 41, 0 |
| $x \geq y$ | 014- 21 |
| STO (1) (ii) | 015-23, 14, 24 |
| STO $\dagger 0$ | 016-23, 51, 0 |
| (9) R ${ }_{\text {a }}$ | 017-1522 |
| $x \geqslant y$ | 018- 21 |
| STO - 9 | 019- 23.9 |
| RCL $\square^{8}$ | 020- 24.8 |
| (f)x $x$ | 021- 1441 |
| GSB 0 | 022-13 0 |


| KEY ENTRY | DISPLAY |  |
| :---: | :---: | :---: |
| 9 DSE | 023- | 1523 |
| GTO 5 | 024- | 225 |
| RCL $\cdot 8$ | 025- | 24.8 |
| STO (1) 1 | 026-23, | 14, 23 |
|  | 027-25, | 13, 5 |
| (9) R $\square_{0}$ | 028- | 1522 |
| ( $n$ RTN | 029- | 2512 |
| (b) LBL 0 | 030-2 | 13, 0 |
| $x \geqslant y$ | 031 - | 21 |
| ( $\square_{\text {PSE }}$ | 032- | 2574 |
| RCL 0 | 033- | 240 |
| RCL - ${ }^{8}$ | 034- | 24.8 |
| $\square$ | 035- | 71 |
| ENTER | 036- | 31 |
| $\square$ RTN | 037 - | 2512 |
| (n) LBL 1 | 038-2 | 13, 1 |
| RCL 0 | 039- | 240 |
| RCL $\cdot 9$ | 040- | 24.9 |
| RCL - ${ }^{8}$ | 041 - | 24.8 |
| (f) $x \leq y$ | 042- | 1441 |
| $x=y$ | 043- | 21 |
| (9) Rot | 044- | 1522 |
| $\square$ | 045- | 71 |


| REGISTERS |  |  | I Control |
| :--- | :--- | :--- | :--- |
| $\mathrm{R}_{0} \Sigma$ | $\mathrm{R}_{1}$ Used | $\mathrm{R}_{2}$ Used | $\mathrm{R}_{3}$ Used |
| $\mathrm{R}_{4}$ Used | $\mathrm{R}_{5}$ Used | $\mathrm{R}_{6}$ Used | $\mathrm{R}_{7}$ Used |
| $\mathrm{R}_{8}$ Used | $\mathrm{R}_{9}$ Used | $\mathrm{R}_{.0}$ Used | $\mathrm{R}_{.1}$ Used |
| $\mathrm{R}_{.2}$ Used | $\mathrm{R}_{.3}$ Used | $\mathrm{R}_{.4}$ Used | $\mathrm{R}_{.5}$ Used |
| $\mathrm{R}_{.6}$ Used | $\mathrm{R}_{.7}$ Used | $\mathrm{R}_{.8} \mathrm{n}$ | $\mathrm{R}_{.9} \mathrm{~K}$ |


| STEP | INSTRUCTIONS | INPUT <br> DATAUNITS | KEYS | OUTPUT <br> DATAUUITS |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Key in the program. |  |  |  |
| 2 | Input number of points in the |  |  |  |
|  | average, $(1 \leqslant \mathrm{n} \leqslant 17)$. | n | B | n |
| 3 | Input data point and compute |  |  |  |
|  | moving average. * | $\mathrm{x}_{\mathrm{k}}$ |  | A |
| 4 | Optional: Display average at |  |  | ' '", AVG |
|  | any time. |  | GSB 1 | AVG |
| 5 | For a new case, go to step 2. |  |  |  |
|  |  |  |  |  |
|  | * If an error is made in data |  |  |  |
|  | input, you must start over. |  |  |  |
|  | The average is not displayed |  |  |  |
|  | until after the $\mathrm{n}^{\text {th }}$ point is |  |  |  |
|  | input. |  |  |  |

## Example 1:

A six-period moving average is used to project monthly sales. The first 6 months of sales are as follows:

| Month | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Sales | 125 | 183 | 207 | 222 | 198 | 240 |

Compute the moving average. Also compute the average after month three.

Keystrokes:
6 B
125 A
183 A
207 A
GSB 1
222 A
198 A
240 A

Display:
6.00
1.00
2.00
3.00
171.67
(average after month three)
4.00
5.00
'6.00", 195.83

The actual sales for the seventh month totalled 225 units. Calculate a new moving average.

225 ' A .00", 212.50

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