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HP-35

SURVEYING PAC

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INTRODUCTION

The programs contained in this booklet are a brief representation of the many problems which may be solved on the HP-35 Pocket Calculator. The intention is to provide routines for the more widely encountered areas of surveying--traverses, intersects, curves, areas, and triangles.

We hope that you find this booklet useful in your day-to-day calculations.

Civil Engineering Products

Note: ENT is used to denote the ENTER ↑ key throughout the tables in this text.

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DEGREES, MINUTES, SECONDS TO DECIMAL EQUIVALENT

LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		6	0	STO			
2.	Degrees	ENT					
3.	Minutes	ENT					
4.	Seconds	RCL	÷	+			
5.		RCL	÷	+		Decimal Degrees	Record - See Note 1

Note 1: To convert bearing to azimuth:

If bearing is SE or NW, press $\boxed{\text{CHS}}$. Then if bearing is SE or SW, press $\boxed{\text{ENTER}}$ $\boxed{+}$ $\boxed{180}$ $\boxed{+}$. Then if bearing is NW, press $\boxed{\text{ENTER}}$ $\boxed{+}$ $\boxed{360}$ $\boxed{+}$.

DECIMAL DEGREES TO DEGREES, MINUTES, SECONDS

LINE	DATA	OPERATIONS					DISPLAY	REMARKS
1.	Decimal Degrees	ENT						
2.	Integer Degrees						Degrees	Record
3.		-	6	0	X			
4.	Integer Minutes						Minutes	Record
5.		-	6	0	X		Seconds	Record

FIELD ANGLE TRAVERSE

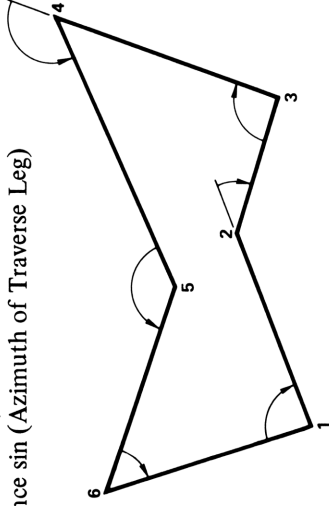
Azimuth of Traverse Leg = Reference Bearing + Field Angle

Horizontal Distance = Slope distance $\sin$ (Zenith)

$N_n = N_o + \text{Horizontal Distance} \cos$ (Azimuth of Traverse Leg)

$E_n = E_o + \text{Horizontal Distance} \sin$ (Azimuth of Traverse Leg)

Example:



Field Data

Reference Bearing 1 $\rightarrow$ 6: N 17° 23' 45"W

Starting Coordinates: $N_1 = 10,000.000$, $E_1 = 10,000.000$

Point	Field Angle	Zenith Angle	Slope Distance
1	87° 22' 17" Right	88° 07' 18"	745.832
2	38° 06' 54" Deflection Right	89° 54' 07"	510.089
3	92° 13' 06" Right	91° 13' 31"	853.760
4	133° 12' 46" Deflection Left	Horizontal	1053.916
5	137° 46' 30" Left	90° 48' 57"	789.671
6	53° 16' 47" Right	89° 41' 55"	784.406
1			

Computed Data

Point	N	E	Point	N	E
1	10,000.000	10,000.000	5	10,487.192	10,510.672
2	10,255.251	10,700.367	6	10,748.438	9,765.552
3	10,096.859	11,185.240	1	9,999.933	10,000.107
4	10,897.362	11,481.496			

FIELD ANGLE TRAVERSE (Continued)

Computed Azimuth $6 \rightarrow 1$: $162^{\circ} 36' 03''$

$\therefore$ Angular Closure = 12"

$$\sqrt{(\text{Corr}_N)^2 + (\text{Corr}_E)^2} = 0.126$$

Position Closure (Before Adjustment of Angles): Length of Traverse $\cong 4738$

$\text{Corr}_N = +0.067$, $\text{Corr}_E = -0.107$ Precision Ratio $\cong 1/37,600$

LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.	Reference Bearing Degrees	ENT					
2.	Minutes	ENT					
3.	Seconds	ENT	6	0	÷	+	
4.		6	0	÷	+	Decimal Ref. Bearing	See Note 1
5.		STO				Decimal Ref. Azimuth	
6.	Field Angle Degrees	ENT					
7.	Minutes	ENT					
8.	Seconds	ENT	6	0	÷	+	

9.		6	0	÷	<input "="" type="text" value="+"/>		Decimal Field Angle	See Note 2
10.		RCL	<input "="" type="text" value="+"/>					See Note 3
11.		STO					Decimal Azimuth of Traverse Leg	See Note 4
12.	Zenith (Vert) Angle Degrees	ENT						
13.	Minutes	ENT						
14.	Seconds	ENT	6	0	÷	<input "="" type="text" value="+"/>		
15.		6	0	÷	<input "="" type="text" value="+"/>		Decimal Zenith (Vert.) Angle	See Note 5
16.		SIN						
17.	Slope Distance	X					Horizontal Distance	
18.		RCL	ENT	COS	X↗Y	SIN		
19.		R↓	X				Latitude	
20.	Previous Northing	<input "="" type="text" value="+"/>					Current Northing	Record
21.		R↓	X				Departure	
22.	Previous Easting	<input "="" type="text" value="+"/>					Current Easting	Record See Notes 6 & 7

FIELD ANGLE TRAVERSE (Continued)

- Note 1:** If the first field angle is an angle right or angle left, the ref. bearing direction is **AWAY** from the first point. If the first field angle is a deflection right or left, the ref. bearing direction is **TOWARDS** the first point. For SE or NW ref. bearing, depress $\boxed{\text{CHS}}$. Then for SE or SW ref. bearing, depress $\boxed{\text{ENTER} \downarrow}$, 180, $\boxed{+}$ or for NW ref. bearing, depress $\boxed{\text{ENTER} \downarrow}$, 360, $\boxed{+}$. See Note 8.
- Note 2:** Depress $\boxed{\text{CHS}}$ for angle left or deflection left.
- Note 3:** If display is greater than 360, depress 360, $\boxed{-}$. If display is less than zero, depress 360, $\boxed{+}$. See Note 8.
- Note 4:** If a slope distance is to be entered, continue on line 12. If a horizontal distance is to be entered, enter the horizontal distance, skip to line 18 and continue.
- Note 5:** If vertical angles are observed instead of zenith angles, depress $\boxed{\text{COS}}$ instead of $\boxed{\text{SIN}}$ in line 16.
- Note 6:** If the next field angle is an angle right or angle left, depress $\boxed{\text{RCL}}$, then if display becomes 1) greater than 180, depress 180, $\boxed{-}$; or 2) less than 180, depress 180, $\boxed{+}$. Then return to line 5 and continue; or if the next field angle is a deflection right or left, return to line 6 and continue.
- Note 7:** After the last coordinates are computed, a check on the angular closure can be made as follows: Depress $\boxed{\text{RCL}}$ and convert the displayed decimal angle to degrees, minutes and seconds. This computed closing azimuth can then be checked against the actual closing azimuth.
- Note 8:** If a surveyor does not feel uncomfortable with azimuths greater than 360° or with negative azimuths, the statements about adding (or subtracting) 360 in notes (1) and (3) can be ignored. These operation were employed solely to keep the azimuth values in the range most used by the surveyor, i.e., in the range 0° to 360° . These "corrections" are not really necessary when using the Model 35.

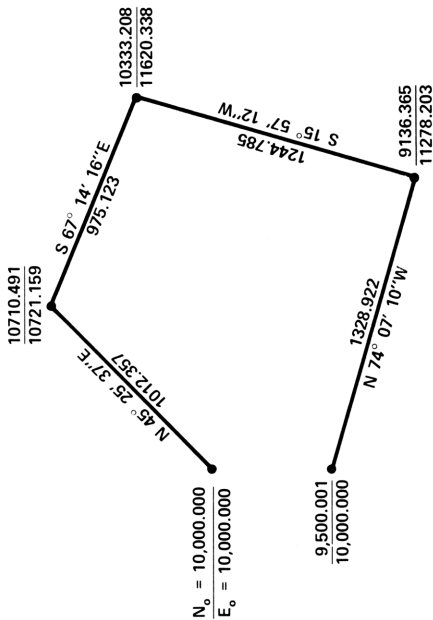
NOTES

BEARING TRAVERSE

$$N_{n+1} = N_n + \text{Distance} \cos (\text{Bearing})$$

$$E_{n+1} = E_n + \text{Distance} \sin (\text{Bearing})$$

Example:



LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.	Beginning North (N_o)	STO					
2.	Beginning East (E_o)	ENT					
3.	Bearing Degrees	ENT					
4.	Minutes	ENT	6	0	÷	+	
5.	Seconds	ENT	3	6	0	0	
6.		÷	+				See Note 1
7.		ENT	SIN	X↗Y	COS		
8.	Distance	X	RCL	+	STO		Record
9.	Distance	X	+				Record
10.							Go To Line 3 For Next Leg

Note 1: If bearing is SE or NW, press . Then if bearing is SE or SW, press , 180, . Then proceed to next line.

INVERSE - DISTANCE AND BEARING FROM COORDINATES

$$\text{Bearing} = \tan^{-1} \left(\frac{E_2 - E_1}{N_2 - N_1} \right)$$

$$\text{Distance} = \sqrt{(E_2 - E_1)^2 + (N_2 - N_1)^2}$$

14 *Example:*

$$N_1 = 10,000$$

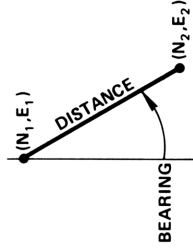
$$E_1 = 10,000$$

$$N_2 = 9,000$$

$$E_2 = 10,500$$

$$\text{Distance} = 1118.034$$

$$\text{Bearing} = \text{S } 26^\circ 33' 54'' \text{E}$$



LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	Easting ₂	ENT							
2.	Easting ₁	-	ENT	ENT	X	STO			
3.	Northing ₂	ENT							
4.	Northing ₁	-	ENT	ENT	X	RCL			
5.		+	√X					Distance	Record
6.		R↓	÷	ARC	TAN			Decimal Bearing	See Note 1
7.		ENT							
8.	Integer Degrees							Bearing Degrees	Record
9.		-	6	0	STO	X			
10.	Integer Minutes							Bearing Minutes	Record
11.		-	RCL	X				Bearing Seconds	Record
12.									Return to Line 1

Note 1: If decimal bearing is positive, bearing is NE or SW. If decimal bearing is negative, bearing is SE or NW. If bearing is negative, press before proceeding to next line.

AREA OF A TRAVERSE FROM COORDINATES

$$A = \frac{1}{2} \left[E_1 (N_2 - N_n) + [E_2 (N_3 - N_1) + E_3 (N_4 - N_2) + \dots + E_{n-1} (N_n - N_{n-2})] + E_n (N_1 - N_{n-1}) \right]$$

Example:

	E	N
1	100.29	491.72
2	447.68	823.14
3	774.43	648.49
4	753.48	318.75
5	610.91	72.23
6	229.34	223.35
1	100.29	491.72

Area = 328,277.19

LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.		CLR							
2.	Starting Easting	ENT							
3.	Starting Northing	ENT							
4.	Next Easting	ENT	R↓	X	RCL	X↑Y			
5.		-	STO						
6.	Next Northing	ENT	R↓	X	RCL	+			
7.		STO	R↓	X↑Y					See Note 1
8.		RCL	ENT	2	÷		Area		See Note 2/Record

Note 1: Return to line 4 until starting coordinates have been re-entered, then proceed through to line 8 to obtain area.

Note 2: Negative values may result. Absolute value is recorded.

SLOPE DISTANCE REDUCTION

$$S = \left[(\text{Ht. of D. M.}) - (\text{Ht. of Theo.}) - (\text{Ht. of D. M. target}) + (\text{Ht. of Theo. target}) \right]$$

$$k = S \cdot \sin (\text{Zenith})$$

$$p = S \cdot \cos (\text{Zenith})$$

$$\text{Horizontal Distance} = \left(\sqrt{(\text{Slope distance})^2 - k^2} + p \right) (\sin (\text{Zenith}))$$

Example:

Ht. of D.M. = 5.87

Ht. of Theo. = 5.12

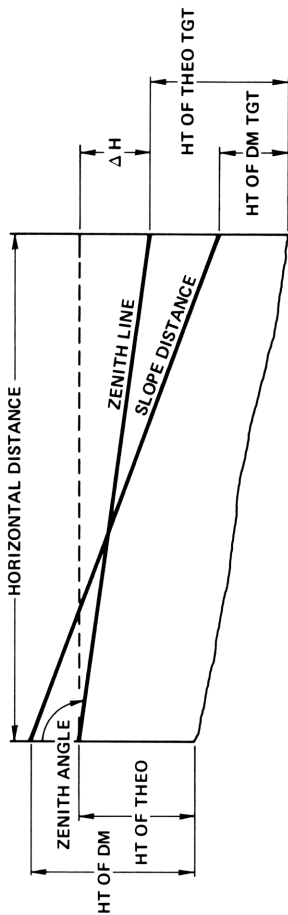
Ht. of D.M. Tgt. = 4.91

Ht. of Theo. Tgt. = 5.17

Zenith Angle = $93^{\circ} 13' 00''$

Slope Distance = 487.132

Horizontal Distance = 486.307



SLOPE DISTANCE REDUCTION (Continued)

LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		6	0	STO			
2.	Zenith Degrees	ENT					
3.	Minutes	ENT					
4.	Seconds	RCL	÷	+	RCL	÷	
5.		+	ENT				
6.	Ht. D.M.	ENT					
7.	Ht. Theo.	-					
8.	Ht. D.M. Tgt.	-					
9.	Ht. Theo. Tgt.	+	STO	R↓			
10.		COS	RCL	X		p	See Note 1/Record

11.		R↓	SIN	RCL	X		k	See Note 1/Record
12.		X↑Y	SIN	STO				
13.	Slope Distance	ENT	X					
14.	k	ENT	X	-	√X			
15.	p	+	RCL	X		Horizontal Dist.	Record	

Note 1: Values of p and k may be negative. Be sure to retain sign when reentering at lines 14 and 15.

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NOTES

DISTANCE - DISTANCE INTERSECT

Example:

$$N_1 = 1000$$

$$E_1 = 1000$$

$$N_2 = 1250$$

$$E_2 = 2000$$

$$N_3 = 1614.409$$

$$E_3 = 1657.649$$

$$N_4 = 767.353$$

$$E_4 = 1869.411$$

$$B = 500$$

$$A = 900$$

$$\phi = 29.017^\circ$$

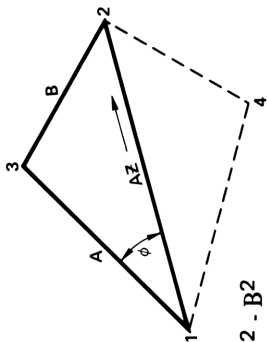
$$\text{Azimuth}_{1 \rightarrow 2} = 75^\circ 57' 50''$$

$$\text{Distance}_{1 \rightarrow 2} = 1030.776$$

$$\phi = \cos^{-1} \frac{(\text{Distance}_{1-2})^2 + A^2 - B^2}{2 (A) (\text{Distance}_{1-2})}$$

$$N = N_1 + A \cos (Az \pm \phi)$$

$$E = E_1 + A \sin (Az \pm \phi)$$



DISTANCE - DISTANCE INTERSECT (Continued)

LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	N ₂	ENT							
2.	N ₁	—	ENT	X					
3.	E ₂	ENT							
4.	E ₁	—	ENT	X	+	STO	(Distance ₁₋₂) ²		
5.		RCL							
6.	Distance B	ENT	X	—					
7.	Distance A	ENT	ENT	R↓	X	+			
8.		RCL	√X	÷	2	÷			
9.		X↔Y	÷	ARC	COS	STO			
10.	Azimuth 1 → 2 Degrees	ENT							

11.	Minutes								
12.	Seconds								
13.								ϕ	See Note 1
14.									
15.	Distance A								
16.	N_1							N_3	Record
17.									
18.	E_1							E_3	Record

Note 1: If solution desired is to left of line 1 $\rightarrow$ 2, press before proceeding to line 14.

NOTES

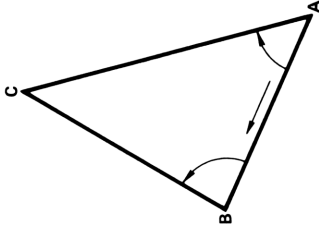
ANGLE - ANGLE INTERSECT

Example:

A = 76° 30' 00"	N _B = 3200.000
B = 38° 20' 00"	E _B = 4200.000
N _A = 5200.000	N _C = 6143.552
E _A = 6100.000	E _C = 4467.774

$$N_C = \frac{E_A - E_B + N_B \cot A + N_A \cot B}{\cot A + \cot B}$$

$$E_C = \frac{N_B - N_A + E_B \cot A + E_A \cot B}{\cot A + \cot B}$$



ANGLE - ANGLE INTERSECT (Continued)

LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		6	0	STO			
2.	Angle B Degrees	ENT					
3.	Minutes	ENT					
4.	Seconds	RCL	÷	+			
5.		RCL	÷	+	TAN	1/X	
6.	Angle A Degrees	ENT					
7.	Minutes	RCL	÷	+			
8.	Seconds	RCL	÷	RCL	÷	+	
9.		TAN	1/X	STO	R↓		
10.		ENT	ENT				

11.	E_A	X	$\square$	$\square$	$\square$	$\square$	$\square$		
12.	N_A	$-$	RCL	$\square$	$\square$	$\square$	$\square$		
13.	E_B	X	$+$	$\square$	$\square$	$\square$	$\square$		
14.	N_B	$+$	$X \rightarrow Y$	ENT	ENT	RCL	RCL		
15.		$+$	$X \rightarrow Y$	$R \downarrow$	$\div$	$\square$	$\square$	E_C	Record
16.		$R \downarrow$	$R \downarrow$	ENT	ENT	$\square$	$\square$		
17.	E_A	$X \rightarrow Y$	$\square$	$\square$	$\square$	$\square$	$\square$		
18.	N_A	X	$+$	$\square$	$\square$	$\square$	$\square$		
19.	E_B	$-$	$\square$	$\square$	$\square$	$\square$	$\square$		
20.	N_B	RCL	X	$+$	$X \rightarrow Y$	$\square$	$\square$		
21.		RCL	$+$	$\div$	$\square$	$\square$	$\square$	N_C	Record

TRIANGLE SOLUTION - GIVEN THREE SIDES

Example:

$$A = 2489.621 \quad a = 48^{\circ} 00' 00''$$

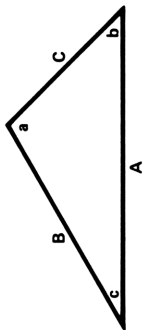
$$B = 2543.150 \quad b = 49^{\circ} 23' 13''$$

$$C = 3322.312 \quad c = 82^{\circ} 36' 47''$$

$$c = 2 \tan^{-1} \left(\frac{r}{S-C} \right)$$

$$r = \sqrt{\frac{(S-A)(S-B)(S-C)}{S}}$$

$$S = \frac{1}{2} (A + B + C)$$



LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.	Side A	ENT	ENT				
2.	Side B	ENT	R↓	+			
3.	Side C	STO	+	2	÷	RCL	
4.		X↗Y	STO	X↗Y	−	ENT	
5.		R↓	R↓	RCL	X↗Y	−	
6.		X↗Y	RCL	X↗Y	−		
7.		X	X	RCL	÷	√X	
8.		X↗Y	÷	ARC	TAN	2	
9.		X					See Note 1
10.	Integer Degrees					Degrees	Record
11.		−	6	0	X		
12.	Integer Minutes					Minutes	Record
13.		−	6	0	X	Seconds	Record

Note 1: Angle b may be obtained by reversing the data entries at lines 2 and 3.

TRIANGLE SOLUTION - GIVEN TWO ANGLES AND INCLUDED SIDE

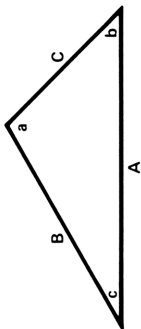
Example:

$$\begin{aligned} A &= 2489.621 & a &= 48^{\circ} 00' 00'' \\ B &= 2543.150 & b &= 49^{\circ} 23' 13'' \\ C &= 3322.312 & c &= 82^{\circ} 36' 47'' \end{aligned}$$

$$A = \frac{B \sin a}{\sin b}$$

$$C = \frac{B \sin c}{\sin b}$$

(LAW OF SINES)



LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		CLR	6	0	STO		
2.	Angle a Degrees	ENT					
3.	Minutes	ENT					
4.	Seconds	RCL	÷	+			
5.		RCL	÷	+			
6.	Angle c Degrees	ENT					
7.	Minutes	RCL	÷	+			
8.	Seconds	RCL	÷	RCL	÷	+	
9.		ENT	R↓	+	SIN		
10.	Side B	X↗Y	÷	X↗Y	SIN	X↗Y	
11.		ENT	R↓	X		Side A	Record
12.		R↓	SIN	X		Side C	Record

TRIANGLE SOLUTION **GIVEN TWO SIDES & ANGLE OPPOSITE ONE OF THEM**

Example:

A = 6.00	a = 30° 23' 17"	A = 6.00	a = 30° 23' 17"
B = 10.70	b = 64° 26' 11"	B = 10.70	b = 115° 33' 49"
C = 11.82	c = 85° 10' 32"	C = 6.64	c = 34° 02' 54"

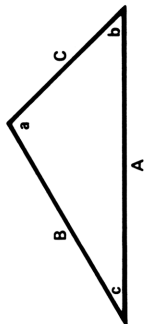
$$b = \sin^{-1} \left(\frac{B \sin a}{A} \right)$$

$$c = 180 - (a + b)$$

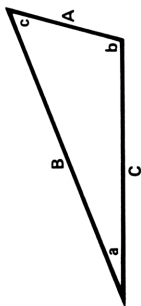
$$C = \frac{A \sin c}{\sin a}$$

(LAW OF SINES)

Acute Angle b



Obtuse Angle b



LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		CLR	6	0	STO		
2.	Angle a Degrees	ENT					
3.	Minutes	RCL	÷	+			
4.	Seconds	RCL	÷	RCL	÷	+	
5.		STO	SIN				
6.	Side B	ENT	R↓	X	X↗Y	+	
7.	Side A	÷	ENT	ARC	SIN		See Note 1/Record
8.		RCL	+				See Note 2
9.		1	8	0	X↗Y	—	Record
10.		SIN	X↗Y	÷	X		Record

Note 1: To solve the problem where angle b is obtuse, press:

180, $\boxed{\text{X} \rightarrow \text{Y}}$, $\boxed{-}$ before proceeding to line 8.

Note 2: Since the sum of angles of a triangle must be 180° , the sum of angles b and a cannot be greater than 180 . If the display exceeds 180° there is only one solution, with angle b acute.

AREA OF A TRIANGLE - GIVEN THREE SIDES

Example:

$$\text{Area} = \sqrt{S(S-A)(S-B)(S-C)}$$

$$\text{Where } S = \frac{1}{2} (A + B + C)$$

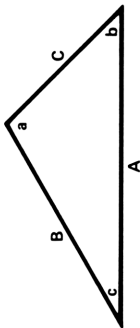
A, B, C = Lengths of Individual Sides

$$A = 2489.621$$

$$B = 2543.150$$

$$C = 3322.312$$

$$\text{Area} = 3139465.857$$



LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	Side A	ENT							
2.	Side B	ENT							
3.	Side C	STO	$X \rightarrow Y$	ENT	R↓	+			
4.		$X \rightarrow Y$	ENT	R↓	+	2			
5.		÷	RCL	$X \rightarrow Y$	STO	$X \rightarrow Y$			
6.		−	RCL	X	RCL	$X \rightarrow Y$			
7.		R↓	$X \rightarrow Y$	−	$X \rightarrow Y$	RCL			
8.		$X \rightarrow Y$	−	X	X	$\sqrt{X}$	Area	Record	

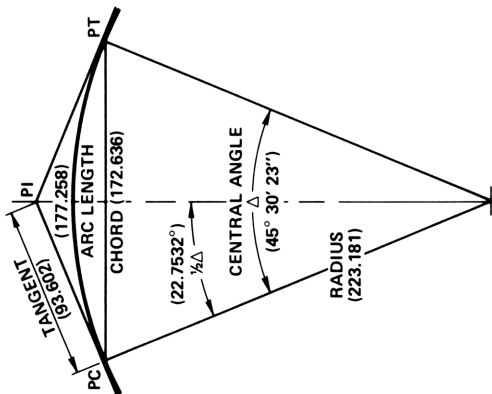
CURVE SOLUTION - GIVEN CENTRAL ANGLE AND TANGENT DISTANCE

Example:

$$R = \text{Tangent} / \tan (\Delta / 2)$$

$$\text{Chord} = 2R \sin (\Delta / 2)$$

$$\text{Arc Length} = R \Delta \pi / 180$$



LINE	DATA	OPERATIONS					DISPLAY	REMARKS
1.		6	0	STO				
2.	Δ Degrees	ENT						
3.	Minutes	ENT						
4.	Seconds	RCL	÷	+ RCL	÷			
5.		+ 2	÷	STO			Decimal ½ Δ	
6.	Tangent Distance	ENT	RCL	TAN	÷		Radius	Record
7.		ENT	ENT	RCL	SIN	X		
8.		2	X				Chord	Record
9.		R↓	RCL	X				
10.		π	X	9	0	÷	Arc	Record

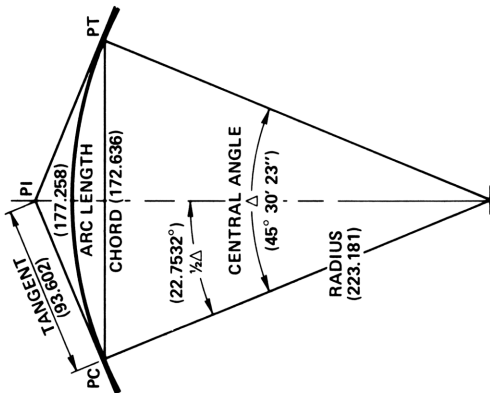
CURVE SOLUTION - GIVEN CENTRAL ANGLE & RADIUS

Example:

$$\text{Chord} = 2 R \sin (\Delta / 2)$$

$$\text{Tangent} = R \tan (\Delta / 2)$$

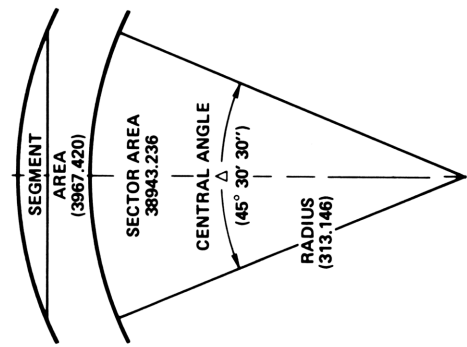
$$\text{Arc Length} = R \Delta \pi / 180$$



LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	Δ Degrees	ENT							
2.	Minutes	ENT							
3.	Seconds	ENT	6	0	STO				
4.		$\div$	+	RCL	$\div$	+			
5.		2	$\div$				Decimal $\frac{1}{2} \Delta$		
6.		ENT	ENT	TAN					
7.	Radius	STO	X				Tangent Distance	Record	
8.		R $\downarrow$	SIN	RCL	X	2			
9.		X					Chord	Record	
10.		R $\downarrow$	RCL	X	π	X			
11.		9	0	$\div$			Arc Length	Record	

CURVE AREA - GIVEN CENTRAL ANGLE & RADIUS

Example:



$$\text{Segment Area} = \pi R^2 \left(\frac{\Delta^{\circ}}{360^{\circ}} \right) - \frac{1}{2} R^2 \sin (\Delta^{\circ})$$

$$\text{Sector Area} = \pi R^2 \left(\frac{\Delta^{\circ}}{360^{\circ}} \right)$$

LINE	DATA	OPERATIONS					DISPLAY	REMARKS
1.		6	0	STO				
2.	Δ Degrees	ENT						
3.	Minutes	ENT						
4.	Seconds	RCL	$\div$	+	RCL	$\div$		
5.		+	ENT	ENT	π	X		
6.		3	6	0	$\div$			
7.	Radius	ENT	X	ENT	R $\downarrow$	X	Sector Area	Record
8.		X $\rightarrow$ Y	SIN	X $\rightarrow$ Y	R $\downarrow$	X		
9.		2	$\div$	X $\rightarrow$ Y	R $\downarrow$	—	Segment Area	Record

CURVE LAYOUT - DEFLECTION ANGLES FROM TANGENT

$$\text{Deflection/ft} = 180/(2\pi R)$$

$$\text{Deflection Angle} = \text{Arc} \times \text{Deflection/ft.}$$

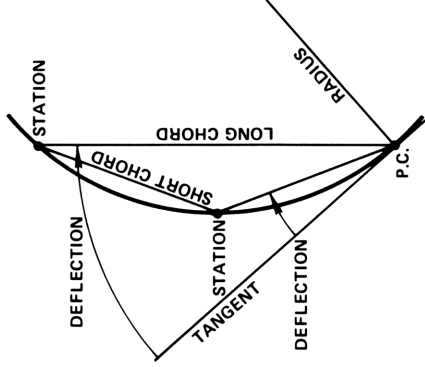
$$\text{Long Chord} = 2 \text{ Radius Sin (Deflection Angle)}$$

Example:

$$\text{Radius} = 900.00 \text{ Ft.}$$

Station	Arc Length	Deflection	Long Chord
12 + 57.00	(Point of Curvature, P.C.)		
12 + 75.00	18.00	00° 34' 23"	18.00
12 + 88.50	31.50	01° 00' 10"	31.50
13 + 00.00	43.00	01° 22' 07"	43.00
13 + 25.00	68.00	02° 09' 52"	67.98
13 + 50.00	93.00	02° 57' 37"	92.96

$$\text{Arc Length} = \text{Difference in Stations}$$



LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	Radius	ENT	2	X	ENT	ENT			
2.		1	8	0	ENT	π			
3.		÷	X↗Y	÷	STO				
4.		RCL							
5.	Arc Length From P.C.	X					Decimal Deflection		
6.		ENT	ENT						
7.	Integer Degrees						Deflection Degrees	Record	
8.		−	6	0	X				
9.	Integer Minutes						Deflection Minutes	Record	
10.		−	6	0	X		Deflection Seconds	Record	
11.		R↓							
12.		SIN	X				Long Chord	See Note 1	
13.		CLX						Return to Line 4	

Note 1: Computation of the long chord can be omitted if regular intervals are used for which the short chord remains constant. Calculation then only needed for odd intervals.

ELEVATIONS ALONG A VERTICAL CURVE

$$E_s = E_o + G_1(\text{Distance in Stations}) + \left[\frac{50(G_2 - G_1)}{L} \right] (\text{Distance in Stations})^2$$

Example:

Beginning Grade (G_1) = -1.065%

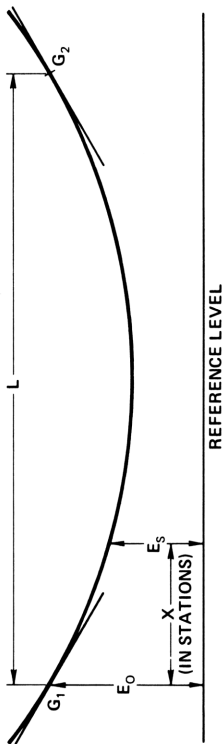
Ending Grade (G_2) = +1.600%

Elevation at Beginning (E_o) = 614.00 Ft.

Length of Curve (L) = 340 Ft.

Stationing Intervals = 100 Ft.

STATION	ELEVATION (E_s)
17 + 00.00	614.000
18 + 00.00	613.327
19 + 00.00	613.438
20 + 00.00	614.332
20 + 40.00	614.910



LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	G_2	ENT							Grades in %
2.	G_1	-	5	0	X				
3.	Length of Curve (L)	÷	STO						
4.	Beginning Elevation (E_0)	ENT							
5.	Distance in Stations	ENT	ENT	X	RCL	X			
6.		X↔Y							
7.	G_1	X	+	+				Elevation (E_S)	Record
8.		CLX							Return to step 5

NOTES



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