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Compact Division

## CONTENTS

This manual describes how to operate HANDYCOMPACT. The first part serves as an overview, and assumes a working knowledge of HP-41C operation and programming. The second part demonstrates applications with examples. The Appendix serves as a reference guide.
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## NOTE

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## WARNING

The HANDY-COMPACT ROM is easily damaged by static electricity. It should be stored in its special static protection envelope when not in the calculator port. Failure to turn off the calculator before inserting or removing any peripheral may result in damage to both the calculator and the peripheral.

## INTRODUCTION

HANDY-COMPACT is an HP-41C programmable calculator-based program which provides steadystate analysis for structures which can be modeled as interconnected two-port networks. Analyses are valid from very low frequencies through the millimeter wavelengths. A standard element library is provided which contains lumped and distributed elements. Special twoport networks such as an ideal transformer and voltage- and current-controlled sources are included for special applications. In addition to the element library, the program can accept measured one- or two-port data, allowing analysis and characterization of structures containing active devices. All internal calculations are based on scattering parameters, although Z, Y, G, and H parameter conversions are provided in case you prefer them.

Background
The routines contained in HANDY-COMPACT are extensions of those described in Microwave Circuit Design Using Programmable Calculators by Medley and Allen, published by Artech House. Although similar in the way they are rum, the published routines differ from those in HANDYCOMPACT. HANDY-COMPACT provides increased accuracy (especially at the lower frequencies), ease of use, and execution speed. Although the book mentioned above is not required for using HANDY-COMPACT, it provides background information and an overview of CAD techniques in general.

Hardware
HANDY-COMPACT is provided in the form of a plug-in ROM for the HP-41C or HP-41CV
calculator. Unlike previous calculator-based programs, the entire program is resident in the ROM and does not impact program or data memory. Additionally, networks can be analyzed without additional programs. A camplex network may be modeled and analyzed across a range of frequencies without having to make key entries during the run.

HANDY-COMPACT can rum on the basic HP-41C calculator. Before running HANDY-COMPACT, the calculator memory must be sized to $\emptyset 35$ (see page 73 of the HP-41C manual). The remaining memory (28 registers) of the basic HP-41C calculator may then be used for either data storage or program memory. When using the HP-4lC calculator with single memory modules, additional memory will allow you to store the element values and measured data and a circuit file for autanatic analysis of complex structures. No more than two memory modules may be used when using the HP-82143A printer. However, there is no limit to the size of the circuit structure when using just the basic calculator- but you will be required to key-in the element values and measured data for each two-port when memory is not sufficient to store this information.

For added flexibility, the HP-41CV or HP-41C with the Quad-Memory Module (HP-8217ØA) is recommended. The HP-82143A printer is recommended for use with either system.

## PROGRAM STRUCTURE

HANDY-COMPACT provides you with over 85 functions, including the element library, interconnections, mappings, and characterizations. Since there are so many functions and almost as many applications, no key assigrments are made. You may design your own custam keyboard to fit specific applications. For example, for microwave applications, you might include the standard interconnections, all distributed elements, and a few of the lumped elements which usually occur in the form of parasitics. For low frequencies, you will not require the distributed elements. It is suggested that the card reader function "WSTS" (write status) be used to store the key assigments on a magnetic card. In fact, several keyboards can be designed for different applications.

Two analysis modes are featured, two-port and ladder. The two-port analysis mode is intended for the analysis of networks which consist of interconnections of two-ports, while the ladder analysis mode provides a much faster means of analysis of simple one-port or ladder structures. In the two-port analysis mode, two two-ports may be in use at any time. These twoports are called two-port "A" and two-port "B", and each has a specific purpose. All library elements are placed in "B" while the interconnections connect " $A$ " and " $B$ ", the result is then placed in "A". Thus, another element may be calculated, autamatically stored in twoport B, then connected with two-port A. Two-port " A " is contained in data registers $\emptyset 1$ through Ø8, and two-port "B" in registers 11 through 18. The S-parameters are stored as magnitude of Sll, S12, S21 and S 22 in registers Øl through 04, respectively. The angles of Sll, Sl2, S2l, and S22 are in 05 through 08, respectively. The data for two-port "B" is offset by $1 \varnothing$ fram that of " A ", and is in exactly the same order. (These and other memory locations are summarized in the Appendix Tables.)

Using the Appendix Tables

## NOTE

You should read this text for a discussion of the available options, then use the Appendix tables for actual program operation and register reference.

The conventions used in this manual are that all data registers are shown circled, and the input and output data are shown in the order entered into the calculator, or rolled down from the stack for display. The series $\mathrm{R}-\mathrm{L}-\mathrm{C}$ combination, for example, calls for you to enter $R$ (resistance in ohms), L (inductance in nanohenrys), and $C$ (capacitance in picofarads). Thus, you enter R, ENTER , L, ENTER , C, then XEQ "SRZ". At the time of execution of program "SRZ", the stack is: "x" = C; "y" = L; "z" = R.

The tables also show that there are five additional data registers which are set aside for the user. None of these registers are modified by the program. Data register Øø contains the reference impedance, and $2 \varnothing$ contains the analysis frequency ( GHz ).
Frequencies must be specified before use. The reference impedance is that impedance to which the S -parameter calculations are referenced as well as the reference used for conversions between reflection coefficient and impedance or admittance. The frequency in register $2 \varnothing$ is the frequently used for the S -parameter calculations for frequency-dependent elements. Registers 21 and 22 are allocated for the stop and step frequencies, respectively, and register 34 is allocated for use as an index register. The
program does not use the latter registers; however, you can use them as part of the circuit file to increment the analysis frequency and recall or save two-port data. There are three flags which are frequency used for the program. These are flag øø, the ladder analysis flag; flag Øl, shunt element flag; and flag Ø4, autamatic execution. You should remember that flag 24, the calculator Range Error Ignore, is set by this program, and should be cleared for other programs which require a range error.

The following seven sections of this manual explain the corresponding seven tables in the Appendix.

## Executing Functions

With each program routine, you enter the data as shown, then XEQ the function name. The result of each routine is shown.
(Although we normally call sets of program steps "programs," we sametimes call them functions, routines, subroutines, carmands, or subprograms, depending upon the context.)

The method of assigning programs to calculator keys is described in the calculator's user guide.

## ELEMENT LIBRARY

S-parameters for the elements shown are calculated using the frequency in register 20 , then stored as two-port "B" in registers 11 through 18. These S-parameters are nomalized to the impedance in register øø. The first 11 elements are lumped elements (consisting of various combinations of resistors, inductors, and capacitors).

## Series and Parallel Connections

Flag Øl is used to connect the elements in either series or shunt (flag l set is the shunt connection). You may want to place two short programs into the calculator, "PA" (parallel) to set flag Øl for the shunt connection, and "SE" to clear flag Øl (although not necessary since each program will automatically clear flag Ø1 before the return). With this feature, you can simply enter the element data as shown, XEQ either SE or PA, depending on the connection, then XEQ the function name.

Another approach is to assign the series element to a key, and the shunt element to the shifted function on the same key. This technique can be implemented for each element as follows:

1. Place the calculator in program mode and enter the following program statements:

Ø1 SF Ø1 Ø2 XEQ "elementname"
2. At this point, the calculator will autamatically convert statement $\varnothing 2$ to

Ø2 XROM "elementname"
which indicates the program (called "elementname") is contained in the ROM. (The calculator could not find the program in its own memory, and assumes that it is in a ROM.)
3. Enter the following program statement:

$$
\emptyset 3 \text { RTN }
$$

4. Leave program mode, go to program step 00Ø, re-enter program mode, and insert the following program statement:
$\emptyset 1$ LBL "elementname"
5. Assign "elementname" to the desired shifted key.

With the shifted key assigned to XEQ, the calculator will find your program before finding
the ROM program. Therefore, your program "elementname" will set flag Ø1, then execute the ROM program "elementname". The unshifted key (assigned to XROM "elementname") will execute (XROM) the ROM program directly. This technique may be used to add "pre-processing" to any of the programs contained in the ROM. (You may wish to change the program units or modify the elements using this technique.)

Lumped Elements
Lumped elements include R,L, and C elements and all cambinations in series and parallel configurations.

## Distributed Elements

Lossless distributed elements provided include a transmission line, open stub, and shorted stub. The latter two can be connected in either series or shunt. However, the shunt-connected transmission line has no meaning and cannot be used; flag $\mathrm{Ol}_{\mathrm{l}}$ is ignored for this element and not cleared by the return. Data for transmission line elements are entered in terms of characteristic impedance and length (mils) in an air dielectric. The physical length in a dielectric medium may be converted to air by multiplying it by the square root of the effective dielectric constant. These distributed elements, as well as lumped elements, may be entered as negative elements. Values for negative lumped elements are entered as negative values; however, with distributed elements, only the length of the element can be
entered as negative. Although a negative
impedance may be specified, an error will occur when the negative impedance is the same as the reference found in register 00 . In addition to the above distributed elements, a four-port coupled line structure is also featured as part of the element library. This structure is the inhomogenous case; that is, unequal even- and odd-mode effective dielectric constants may be specified. This four-port structure is converted into a two-port network for analysis when the termination on any two-ports is specified. As the Appendix shows, the reflection coefficient at port $k$ is stored in registers $3 \varnothing$ and 31, while that for port 1 is in 32 and 33 (magnitude and phase respectively). Port $k$ is always the lower-numbered port when the numbering convention shown by the diagram is used. The input port is always port 1, and the flag which corresponds to the desired output port is set before execution. Even-mode impedance and length data is entered first, then odd-mode impedance and length. The air length is calculated as above; however, the square root of the even- and odd-mode effective dielectric constant is used to compute the even- and oddmode length, respectively. This element is extremely useful for determining the effect of the unequal effective dielectric constants in the microstrip case. In addition, arbitrary terminations may be used to investigate the effects of fringing capacitance of an open, or the inductance associated with a short at microwave frequencies.

Additional Elements
Additional elements can be found in the library for special applications. The ideal transformer is specified using either impedance or turns ratio. This element is useful for computing the s-parameters for a two-port with a different reference impedance at each port. For example, the insertion loss of a transformer structure may be desired. The structure may be calculated referenced to the source impedance at one port, and the load impedance at the other. The insertion loss may then be determined directly fram S21. Without normalization, additional calculations are required. You are also provided with current- and voltage-controlled sources, both voltage- and current-dependent. These sources are useful for certain (usually lowfrequency) models, and may be specified with complex coefficients.

## INTERCONNECTIONS

Five standard two-port interconnections, cascade ("CAS"), series ("SER"), parallel ("PAR"), Series Parallel ("SPC"), and parallel-series ("PSC") are offered. These interconnections connect two-port "A" with two-port "B" and place the result in two-port " $A$ " as shown in the Appendix. In addition, a hybrid ("HYB")interconnection, cammonly used in the design of microwave amplifiers, is featured. This function connects the input and output ports of "A" and "B" to the quadrature ports of two distributed couplers and places the results in two-port " A ". The two identical couplers are assumed to be ideal, and have a characteristic impedance equal to the reference impedance found in register Øø. The characteristics of these couplers are specified by entering the coupling in $+d B$ at the center frequency and the center frequency.

PBR and SBR
Parallel branch ("PBR") and the series branch ("SBR") are provided for converting one-port networks into two-ports. This allows structures to be interconnected using one of the standard functions. The branches may be calculated from the input reflection coefficient of two-port "A" with a specified load termination which is entered before execution, or with flag $\sigma 2$ set, directly from a specified impedance. The parallel branch is particularly useful for transistor bias networks which can be modeled as a one-port.

## LADDER ANALYSIS

The ladder analysis mode is active when flag øø is set. The ladder analysis mode is three to four times faster than the two-port analysis. The same reference impedance and frequency is used, as well as the element names. Two-port "A" is not changed by any of the ladder analysis functions, and the only two-port element which will change the ladder analysis registers is the "CPL" function. You may switch between the two modes when necessary. The ladder analysis may be used with two-port analysis to reduce execution time. The impedance of any one-port network, such as a bias network, may be calculated, then the "SBR" or "PBR" function used to interconnect the branch, or the parasitics associated with an open or short for the coupled lines may be calculated in this mode. The ladder analysis mode may be used with lossless two-port networks when the input VSWR and insertion loss is desired. In this case, the input impedance may be converted to reflection coefficient, then VSWR. The insertion loss may be calculated from the familiar relationship for lossless two-port networks, $|s 21|^{2}=1-|s 11|^{2}$.

Ladder analysis is limited to series or shunt elements, and any of the R-L-C elements, as well as the TRL, SST, and OST elements may be used. The data entry procedure for the ladder mode is the same as that of the two-port mode. The ladder analysis mode calculates the input impedance for a one-port network. The magnitude of the load impedance is stored in register 25 , and the angle in 26 . You then enter the element values, then execute the desired element. The program computes the input impedance at this
point of the network, stores the results in 25 and 26, then displays the impedance in "x" and " $y$ ". Another element may now be connected. The program does not read the values displayed in " $x$ " and " $y$ ", and you may overwrite or convert them to reflection coefficients as desired.

## MANIPULATION COMMANDS

Seven Special Commands are provided to manipulate two-ports " A " and " B ".

SVA and SVB
The "SVA" and "SVB" commands (save "A" and save "B") are used to save two-ports "A" or "B".
These commands are implemented by entering a number which corresponds to two-port " N ", then XEQ either command. Tho-port " A " or " B " will be saved in registers $27+8 * \mathrm{~N}$ through $34+8^{*} \mathrm{~N}$; note that the calculator must be sized for $35+$ $8^{*} \mathrm{~N}$ as shown in the Appendix. For example, to save two-port "A" as two-port "2", first enter 2, then XEQ "SVA". Two-port "A" will then be saved in registers 43 through 50 . This option is useful in conjunction with the "USA" and "USB" cormands (see below).

USA and USB
"USA" and "USB" commands (use "A" and use "B") are used in exactly the same manner as SVA and SVB. That is, you enter " N " and XEQ either "USA" or "USB" to recall the saved two-port into either "A" or "B". Since only two two-ports may be active in the calculator, these commands are used to save temporary data. For example, the input matching network may be saved while feedback is added to a transistor, then recalled and cascaded. These cammands are also used in conjunction with the index register to recall measured data for frequency analysis. You first store the S-parameters by entering the data from
the keyboard, then use "SVA" or "SVB" to store the data as " N ", " $\mathrm{N}+1$ ", etc., in the order which corresponds to the frequency. During program execution, you can recall the index register (34), then "USA" or "USB" to retrieve the data. The index register is then incremented for use at the next frequency. Commonly-used data can be loaded from a data card if desired. The sparameters may be stored for many frequencies (e.g., l to 10 GHz ) as two-port "l" through " 10 ". The index register can be started at any number to recall data at the desired frequency. You can even add a program to interpolate between the measured data points. You should use the above equations to determine where these data are stored, and remember not to store any other data in this location. The index register may also be used to recall one-port data, although you will have to write a small subroutine or make it a part of the circuit file. Another suggestion for the use of these commands is to insert a third memory module during program execution to save the computed S-parameters. When the analysis is complete, the data may be moved to lower location, the memory module removed and the printer reconnected to print the results.

## EXC

The "EXC" command is used to exchange two-ports "A" and "B". The interconnections connect twoports "A" and "B", and the elements from the library are stored as two-port "B". This approach works well since the network may be analyzed without unnecessary data manipulation; however, when the first element is calculated, there is no two-port "A". The "EXC" command may be used to place the first element into " A ", then the second element may be calculated as "B" and connected.

EQU and CHA
The "EQU" (equate) and "CHA" (change) commands are useful for reducing execution time. The first half of a symmetrical network may be cascaded, then "EQU" used to copy "A" into "B". The "CHA" command is then used to exchange ports 1 and 2 which forms the second half of the network.

## CONVERSION COMMANDS

Multi-Port Conversions
Conversions are provided to convert fram twoport data obtained from a three-terminal device with one cammon terminal, to another cormon-lead configuration. The convention used for these conversions is shown in the Appendix. The input terminal is 1 , the output 3, and the common lead 2 before the conversion. The cammon lead may be exchanged with the input ("X12"), or the output ( "X23"). Although the diagram in the Appendix shows an FET which is converted fram cammon source to common gate and cormon drain. In fact, a valid transformation can be made for any three terminal networks with one common teminal.

Parameter Conversions
Conversions are also provided between the S, Y, Z, G, and H parameter sets. All parameter sets are normalized and, as with the "X12" and "X23" functions, only two-port "A" is converted. The "EXC" cormand may be used if a conversion for " B " is desired. Four additional cormands may be used to convert fram reflection coefficient to impedance ("R-Z") or admittance ("R-Y"). The commands, "Z-R" and "Y-R" may be used to convert from impedance or admittance to reflection coefficient, respectively. The reference impedance in register $\varnothing \varnothing$ is used for these conversions with the impedance specified in ohms and the admittance in mmhos. The " $\mathrm{Z}-\mathrm{R}$ " and " $\mathrm{Y}-\mathrm{R}$ " commands are useful for converting the impedance output fram the ladder analysis mode into reflection coefficient. You will note in the

Appendix that these commands require you to enter the magnitude, then angle for impedance, but that the output from the ladder analysis gives magnitude in " $x$ " and angle in " $y$ ". The " $x$ " and " $y$ " registers must be exchanged when using the output from the ladder analysis as input to these functions.

## CHARACIERIZATIONS

The functions found in this section are useful for the calculation of parameters of two-port "A". Two-ports "A" and "B" are not modified by any of the programs of this section, and may be used at any time during analysis.

## CHR

The characterization command ("CHR") is used to calculate the stability factor, maximum available gain, and the simultaneous matched source and load for a network when the stability factor is greater than l. When the stability factor is less than 1 , the stability factor and maximum stable gain is returned instead. This command has an automatic execution feature to print results rather than the normal displayed output. This feature is active when flag 94 is set. When this flag is set, the program returns irmediately with the calculated results in the data registers shown in the Appendix. You should test the stability factor before printing the results since the matched source and load reflection coefficients do not exist when the stability factor is less than 1 ; The program does not clear these registers, and the contents do not contain meaningful data.

## STB

When designing with active devices which have stability factors less than 1 , complete stability information is necessary. These calculations are provided with the "STB"
(stability) camand, which determines the location and radius of the stability circle on either the input or output planes, and indicates by means of a code whether the stable region is inside or outside the stability circle. The feature is interactive; that is, the program will request whether the input or output plane is desired, calculate the parameters, then ask for another calculation as shown. However, the "STB" function also has an autamatic execution option using flag 04 to request printed results. With this option, you can enter a code (l for the input plane, or 2 for the output plane), and XEQ "STB". The data will then be returned in the data registers indicated in the Appendix. When using the printer, you may wish to print "INSIDE", "OUTSIDE", OR "ABSOLUTE" instead of the code returned in register 10 .

## GIB

The "GTP" (gain-transducer, power) function may be used to calculate the transducer gain of two-port "A" for specified load- and sourcereflection coefficients. "CGC" (constant-gain circles) may be used to construct contours of constant gain on the input or output plane. "MMC" (mismatch contours) are used to construct contours of constant mismatch around a specified reflection coefficient. "MML" can be used to calculate the actual mismatch between a complex source and load. "S1P" and "S2P" (Sll prime and S22 prime) are used to calculate the input and output reflection coefficient with a specified load or source reflection coefficient, respectively.

## Program Control

With the exception of the "CHR" and "STB" commands, the normal application of the functions in this section is interactive. That is, most information is used directly from the display without the requirement to print any output. However, the output can be printed fram all the functions except the "CGC" and "MMC". These programs are in a loop waiting to calculate new values of constant gain or mismatch, and a subroutine to print the output cannot return program control to the ROM. However, the "LBL xx" (found in the Appendix beside these cammands) can be used for this purpose. For example, the constant gain contours can be calculated, then a subroutine can be used to print the gain and location and radius of the circle. The subroutine can then be re-entered with a "GIO CGC", then "GIO xx" (GIO 29 in this case), and "R/S". The program will again ask for the desired gain. When this technique is used to print the output, you should note that the prompt " $\mathrm{G}=$ " or " $\mathrm{L}=$ " is in the alpha register and may be used as part of the printed output.

## MAPPING

The mapping feature will map the parameters shown for two-port "A". The series and shunt mappings change the contents of two-port "A", as well as "B". These two-ports should be saved if you wish to use them following the mappings. The MAPSOURCE and MAPLOAD mappings produce a mapping of all possible source impedances on the S 22 plane, and all possible load impedances on the Sll plane, respectively. These mappings are actually the Sll' and S22' mappings, and are useful for determining the necessary reflection coefficient from a point on the constant gain contours. The transducer gain can then be used to verify the accuracy. The series and shunt feedback allows you to investigate the effects of feedback on any of the four S-parameters. All four S-parameters may be mapped fram a single calculation for a specified feedback configuration; however, you must reload two-port " A " when a mapping for another feedback configuration is desired. Although the mappings are usually desired for the range of positive real impedances, you are free to specify negative real impedances if necessary. As with the "CGC" and "MMC" options, the mapping routine may be interrupted to print the output. The return is "GIO MAP", "GTO 16", and "R/S". The last prampt, " $\mathrm{R}=$ " or " $\mathrm{X}=$ " is in the alpha register and may be used with the print routine to label constant resistance or reactance.

## Polar Coordinates

When using any of the mappings, including the contours described on pages 21 and 22. location and radius of the various circles are with respect to the chart used to plot the parameters. Thus, the center of any of the circles are found using the magnitude and angle fram the chart, and measured from the center. The radius is set using the magnitude scale, and constructed around the location of the center. The Smith chart is nomally used to plot the input and output reflection ooefficients since impedance is usually desired; however, a polar plot is used for the transmission coefficients. In those cases where the purchased Smith Chart is not an appropriate size, such as might be the case with a large stability circle, the "chart" option of the "MAP" function may be used to construct a Smith Chart with any convenient scale factor.

## EXAMPLES

The following examples will illustrate same of the applications and techniques used with HANDY-COMPACT. It is assumed that you are familiar with the design techniques used, as it is beyond the scope of this document to explain the theory and techniques behind the various examples. These examples all include the program listings and a detailed explanation of the circuit files used for the analysis. The listings also include most of the printer routines used to produce the output shown in each example.

Register Numbers
In the example illustrations, the numbers enclosed in circles next to the data correspond to the data register numbers where the parameter will be stored for analysis. This convention will be followed throughout these examples.

## Printer Routines

You can write printer routines to suit your specific application, which can then be saved on a magnetic card and loaded as a subroutine when necessary, or deleted as required for more memory.

One 60-byte utility subroutine called "FMT" is not included with the listings in its final form. This subroutine formats data similar to the FORTRAN "F" format, and loads the formatted data into the print buffer via the "ACX"
command. When an overflow occurs, the specified fieldwidth is filled with "*"s. The call to this subroutine can be seen in the listings as the entry of a number, "xx.y" (fieldwidth.number of decimal places), then "XEQ FMT". The subroutine used here will fix the display to " y ", then accumulate the number in the " $y$ " register into the print buffer.

## Example 1

## Analysis of a Parallel-Coupled Filter

The four-section filter shown in Figure 1 has been designed for 0.25 dB ripple in a passband which extends from 3.7 to 4.2 GHz , and should have a minimum of 25 dB rejection at 4.5 GHz . The computed even- and odd-mode impedance for each coupled section is shown. The air length of 747.01601 mils for each coupled section is the same and is calculated from the requirement that each section must have an electrical length of 90 degrees at the center frequency of 3.95 GHz .

(36) $\ell_{E_{r}}=747.01601 \mathrm{mils}$


Figure 1. Parallel-Coupled Filter

The listing for the circuit file which is used for the analysis is shown in Figure 2. You must store the reference impedance in register 00 , and the start, stop, and step frequencies in registers $2 \varnothing$ through 22, respectively, before execution, as well as the data shown in the diagram.

| 014LBL EEXI* | 28 RCL 21 |
| :---: | :---: |
| 82 XEE 88 | 21 RCL 22 |
| 63 RCL 35 | 22 RCL 29 |
| 84 RCL 36 | $23+$ |
| 85 RCL 37 | 2451020 |
| 86 RCL 36 | $25 \mathrm{X}=\mathrm{Y}$ Y? |
| 87 XROH ${ }^{\text {CPPL }}$ | 26 GTO EEXI* |
| 88 XROH "EXC" | 27 RTN |
| 89 XEE 98 | 280LEL 98 |
| 19 RCL 49 | 291 |
| 11 RCL 36 | 3057030 |
| 12 RCL 42 | 3151032 |
| 13 RCL 36 | 320 |
| 14 XROH 'CPL- | 3351031 |
| 15 XROM "CAS" | 34 STO 33 |
| 16 XROM "EQU" | 35 SF 63 |
| 17 XROM "CHO" | 36 END |
| 18 XROH "CAS" |  |
| 19 XEQ PPRD* |  |

[^0]The circuit file, which is labeled "EXI", makes use of the symmetry of this filter to reduce the execution time. Note in the above figure that the last two coupled line sections is a mirror image of the first two. Therefore, the first two sections can be cascaded with the mirror image to produce the overall parameters. The "CPL" element requires that the reflection coefficient for the two terminated ports be entered in registers 30 through 33, and a flag set which corresponds to the output port, port 3 in this case. The teminations and output ports are the same for all the coupled sections; therefore, a common subroutine, "LBL Ø日" located at steps 28 through 36, is used for this purpose. Program step $\emptyset 2$ executes subroutine $\emptyset \emptyset$ which sets flag 3 and loads the termination of $1 / \varnothing$ degrees (open circuit) into registers 30 through 33. Steps $\emptyset 3$ through $\emptyset 6$ recall the even-mode impedance and length, then the odd-mode impedance and length for the first section. Step $\varnothing 7$ is the command to compute the $S$-parameters for the coupler. The S-parameters are stored as two-port "B" (registers ll through 18). At this point there is no two-port "A" which can be connected; therefore, these parameters must be loaded into " A " for later connection. The exchange cormand, "EXC", in step $\varnothing 8$ is used for this purpose. Steps $\emptyset 9$ through 14 duplicate those above, but with the data for the second coupled section. Two-port "A", the first section, can now be cascaded with two-port "B", the second section, via the cascade, "CAS" cammand in step 15. Twoport "A" now contains the S-parameters for the first half of the filter. The equate cammand, "EQU", in step l6, copies the first half of the filter into " B ", and the change cammand, "CHA", in step 17 exchanges ports 1 and 2 of two-port
" B " to form the mirror image of " A " in " B ". The cascade connection in step 18 forms the S parameters for the overall filter, then the print routine, "PRD", is called to print the output data. Step 20 through 22 recalls the stop, step, and current frquencies from registers 21, 22, and 20, respectively. Steps 23 and 24 adds the step to the current frequency and stores the result in register 20. A test is made in step 25 to determine if the current frequency is greater than the stop frequency. If it is, the program stops; otherwise the program loops to "EXI" to analyze the filter at the next frequency.

```
This program actually uses two printer
subroutines, "PRL" and "PRD", which are shown in
Figure 3.
```

| 81+LBL *PRL* |  | 25 XEQ -FMT- |
| :---: | :---: | :---: |
| 62 SF 12 |  | 262 |
| 63 CLA |  | 27 SKPCHR |
| 844 |  | 281 |
| 85 SKPCHR |  | 29 RCL 01 |
| 86 ARCL 45 |  | $30+$ |
| 97 ACA | 81018L -FMT* | 311 |
| 08 PrBuF | 81 FRC ${ }^{\text {a }}$ | 32 RCL 91 |
| 09 CF 12 | 82 FRC | 33 - |
| 18* FRE日* | 8310 | 34 , |
| 11 ACA | 69 FIX IND X | 357.2 |
| 124 | 95 FIX IND X | $36 \times$ XEP FMT= |
| 13 SKPCHK | 86 | 372 |
| 14 -YSUR- | 07 ACX | 38 SKPCHR |
| 15 ACA | 82 EMD | 39 RCL 03 |
| 165 |  | $40 \times 12$ |
| 17 SKPCHK |  | 41 LOG |
| 18 "LOSS* |  | 4210 |
| 19 ACA |  | 43* |
| 29 PREUF |  | 447.3 |
| 21 RTH |  | 45 XEZ -FMT- |
| 22+LEL =PRI- |  | 46 PRBUF |
| 23 RCL 28 |  | 47 END |
| 246.2 |  |  |

Figure 3. Two Printer Subroutines, "PRL" and "PRD"
"PRL" is used to print a label, and "PRD" is used to print data. Program "PRL" recalls the filename as alpha data from register 45 and prints this name along with the FREQ, VSWR, and LOSS headings. "PRL" is executed before execution of the circuit file, and "PRD" is called during execution to print the output data. Steps 23 through 25 recall the frequency and accumulate these data into the print buffer. A space of 2 character widths is accumulated; then steps 28 through 36 calculate and accumulate the input VSWR. The input VSWR is calculated from the relationship, VSWR $=$ ( $1+\mid$ Sll| $) /(1-\mid$ Sll|). Two character widths are again accumulated in steps 37 and 38; then the insertion loss given by $10 * \log [521$ ] is calculated and accumulated in steps 39 through 45. Steps 46 and 47 print the print buffer and return to the circuit file.

The output shown in Figure 4, below indicates that the filter has a ripple of 0.316 dB instead of the design goal of $\emptyset .25 \mathrm{~dB}$. The rejection of 25 dB at 4.5 GHz also has not been met. The analyzed value is 19.269 dB . Three separate runs have been made. The first from 1 to 3 GHz with a step of 1 GHz , the second from 3.5 to 4.5 with a step of $\emptyset .1 \mathrm{GHz}$, and the last from 5 to 8 GHz with a step of 1 GHz . In this case, the evenand odd-mode impedances should be recalculated with more accuracy in order to achieve the desired 0.25 dB . However, when the ripple is decreased, the rejection at 4.5 GHz will be even less which indicates that a five section filter must be used.

The five section must be analyzed in a slightly different manner since the symmetry about the center is not present. The first two sections should be cascaded and saved using the "SVA" command. The center section is created, then cascaded with the first two sections. The saved data is reloaded via the "USB" command into two-port "B". The "CHA" cammand is again used to generate the image of the first two sections and cascaded to form the overall parameters.

|  |  |  | 4.80 | 1.31 | -0.079 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | E×1 |  | 4.10 | 1.54 | -0.199 |
| FREE | VSHE | LOSS | 4.20 | 1.72 | -8.316 |
| 1.06 | ******* | -68.641 | 4.30 | 13.87 | -6.084 |
| 2.80 | ******* | -55.125 | 4.48 | 84.55 | -13.353 |
| 3.98 | ******* | -34.725 | 4.50 | 336.07 | $-19.269$ |
| 3.50 | 84.55 | -13.35: | 5.80 | ******* | -37.512 |
| 3.68 | 13.37 | -6. 884 | 6.86 | ******* | -56.616 |
| 3.78 | 1.72 | -0.316 | 7.00 | ******* | -69.995 |
| 3.86 | 1.54 | -8.193 | 8.80 | ******* | -90.892 |
| 3.99 | 1.31 | -0.079 |  |  |  |

## Figure 4. Parallel-Coupled Filter Analysis

Another technique which may be used is to use the equivalent two-port model for coupled lines (see Matthaei, Young, and Jones, "Microwave Filters, Impedance-Matching Networks, and Coupling Structures"). The ladder analysis mode may then be used. The model for each coupled section will consist of three transmission lines, and since the ladder analysis is much faster than the two-port mode, execution time can be saved in same cases. However, in this case, the two-port mode is the preferred technique because of the symmetry.

## Example 2

## Microstrip Coupled Line Filter

Most filters similar to the one in Example 1 are constructed using either microstrip or stripline techniques. The microstrip filter is simple to fabricate and often used; however, the even- and odd-mode phase velocities are not the same due to the field patterns, and will cause a modification of the calculated response. This effect can easily be seen in the parameters of a microstrip coupler where the isolation is much less than expected.

The model of the microstrip version of the filter in Example 1 is shown in Figure 5. The even- and odd-mode effective dielectric constants have been calculated for each section, as well as the fringing capacitance at the end of each microstrip line. The average of the even- and odd-mode effective dielectric constants have been used to determine the physical length of each section (the air length divided by the square root of the average value). The physical length is then converted to the equivalent air length when multiplied by the square root of the appropriate dielectric constant.


Figure 5. Microstrip Coupled Line Filter

The circuit file, "EX2", shown in Figure 6, is used for the analysis of this structure.

| 01*LBL EX2* | 17 XROM -CAS ${ }^{\text {- }}$ | 33 5T0 25 |
| :---: | :---: | :---: |
| 02 RCL 39 | 18 XROM ${ }^{\text {E EQU }}$ | 34 STO 26 |
| 03 KEP 88 | 19 XROH "CHA | 35 R⿴囗 |
| 04 RCL 35 | 20 XROM "CAS ${ }^{-}$ | 36 XROH ${ }^{\text {CAPP }}$ |
| 85 RCL 36 | 21 XED "PRD" | 37 CF 00 |
| 66 RCL 37 | 22 RCL 21 | 38 XXY |
| 87 RCL 38 | 23 RCL 22 | 39 XROM ${ }^{\text {-2-R" }}$ |
| 88 XROM -CPL- | 24 RCL 29 | 40 ST0 38 |
| 69 XROH ${ }^{\text {E EXC* }}$ | 25 + | 41 STO 32 |
| 18 RCL 44 | 26 ST0 29 | 42 RDN |
| 11 XEE 88 | $27 \mathrm{~K}=Y$ ? | 43 STO 31 |
| 12 RCL 48 | 28 GTO "EX2* | 44 STO 33 |
| 13 RCL 41 | 29 RTN | 45 SF 83 |
| 14 RCL 42 | $30+$ LEL 80 | 46 END |
| 15 RCL 43 | 31 SF 88 |  |
| $16 \mathrm{XROH}{ }^{-C P L}$ | 328 |  |

Figure 6. Microstrip Coupled Line Filter Circuit Fil
Label 06 is used similar to Example 1 to set flag 3 and load the coupler terminations into registers $3 \varnothing$ through 33. However, in this case, the reflection coefficient due to the fringing capacitance is desired rather than an open. This subroutine is called with the value of capacitance in register " x ". Ladder analysis is by far the most efficient method for calculating the reflection coefficient, and the set flag $\varnothing \varnothing$ in step 31 sets this mode. The zero in step 32 is stored in registers 25 and 26 which result in a $\emptyset$ ohm at $\emptyset$ degree termination. The value of capacitance is returned to the "x" register in step 35, and step 36 calculates the input impedance of a series capacitor teminated with
a $\emptyset$ ohm load. Step 37 returns the program to the two-port mode, and 38 interchanges the " $x$ " and " $y$ " registers for the conversion fram impedance to reflection coefficient. You should be careful about this step; the conversion routine is set up for the nomal entry of magnitude and angle for the impedance, and the output fram the ladder analysis displays magnitude in "x" and angle in " y " which requires the interchange. Steps 40 through 46 then store the reflection coefficients, set flag 3, and return control to the circuit file.

The only other differences between the circuit files for Examples 2 and 3 are that the fringing capacitance which must be in "x" when subroutine $0 \varnothing$ is called, and that the even- and odd-mode lengths are called from different data registers since they are not the same. The results of the analysis is shown in Figure 7.

|  | Eか2 |  | 4.06 | 1.47 | -0.158 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| FREQ | USHE | LOSS | 4.18 | 2.45 | -0.848 |
| 1.00 | ******* | -77.63: | 4.26 | 16.63 | -6.695 |
| 2.89 | ******* | -61.469 | 4.36 | 75.53 | -12.875 |
| 3.80 | ******* | -35.495 | 4.48 | 235.51 | -17.736 |
| 3.50 | 13.81 | -5.998 | 4.56 | 576.86 | -21.595 |
| 3.60 | 1.44 | -0.142 | 5.80 | ******* | -33.195 |
| 3.76 | 1.45 | -0.149 | 6.00 | ******* | -48.269 |
| 3.80 | 1.80 | 0.96 [ | 7.00 | ******* | -31.77i |
| 3.90 | 1.65 | -6.270 | 8.86 | 31.84 | -9.174 |

Figure 7. Microstrip Coupled Line Filter Analysis

This analysis indicates that the passband is shifted to a lower frequency, the rejection on the low side has been improved, and the rejection on the high side has been dramatically decreased. If you have designed, built, and tested a parallel, coupled microstrip filter, you probably know that this is exactly the measured response. The question is whether the fringing capacitance or the unequal phase velocities cause the problem. In practice, the physical length of each section is reduced slightly to compensate for the capacitance; however, an analysis of this filter with the fringing set to zero shows that the phase velocity effect daminates. The filter should be redesigned, perhaps with an additional section, to achieve the desired passband and rejection.

## Example 3

## Two-Port Analysis of a Transformer Structure

The transformer structure shown in Figure 8 has been designed to transform a 100 ohm load into 50 ohms across a frequency band which extends from 2 to 8 GHz .

(38) $A_{c_{r}=1}=590.14265 \mathrm{mi} / \mathrm{s}$

Figure 8. Transformer Structure
The design ripple is $\emptyset . \emptyset 5 \mathrm{~dB}$, and the minimum insertion loss is 0.001 dB . Thus, the response should ripple between $0 . \varnothing 01$ and $\varnothing . \boxed{01 d B}$ in this passband. The easiest method to analyze this structure is to incorporate the ideal 100:50 ohm transformer at the output port as shown above. This transformer will provide the desired lagohr temination for this structure, and will actually change the reference impedance at port 2. Thus, the calculated data are actually the S-parameters for a two-port with a reference impedance of 50 ohms at port 1 , and $10 \emptyset$ ohms at port 2. This approach will allow |S2l| to be used directly to determine the insertion loss, and $|S 11|$ to be used for the VSWR calculation.

The circuit file for this analysis is shown in Figure 9.

| 010LBL EX3* | 11 RCL 37 | 21 RCL 21 |
| :---: | :---: | :---: |
| 82 RCL 35 | 12 RCL 38 | 22 RCL 22 |
| 03 RCL 38 | 13 KROM -TRL- | 23 RCL 28 |
| 94 SF 01 | 14 XROM *CAS* | $24+$ |
| 85 XROH -SST* | 15100 | 25 ST0 20 |
| 86 XROH -EXC* | 16 EHTER + | $26 \mathrm{X}=3$ ? |
| 07 RCL 36 | 1758 | 27 GTO 'EX3* |
| 08 RCL 38 | 18 XROH 'TRF* | 28 EHD |
| 09 XROH -TRL* | 19 XROH -CAS* |  |
| 18 XROH "CAS* | 28 XEQ PRRD |  |

## Figure 9. Transformer Structure Circuit File (Two-Port)

Steps $\varnothing 2$ and $\varnothing 3$ recall the impedance and length of the input shunt shorted stub, and the set flag $\varnothing 1$ in step $\varnothing 4$ specifies that this element will be connected in shunt. The "SST" cammand in step $\varnothing 5$ computes the S-parameters as two-port "B". The "EXC" command in step $\varnothing 6$ places the parameters for the stub in "A" since this is the first element. Steps 07 through 10 recall the data for the first transmission line, then cascade this two-port with the shunt stub. Steps 11 through 14 do the same for the second transmission line. Steps 15 through 17 recall the impedance ratio for the transformer, and step 18 computes "B" as the parameters for this element. Note that the input impedance for the transformer can be stored in a data register, and the reference impedance in register $\emptyset 0$ used for the output impedance. The "CAS" in step 18 computes the overall S-parameters, and the call to "PRD" computes and prints the results.

The output is shown in Figure 10.

| E×3 |  |  |
| :---: | :---: | :---: |
| FREQ | VSHR | 1055 |
| 1.88 | 3.96 | -1.914 |
| 2.88 | 1.28 | -0.834 |
| 3.08 | 1.27 | -8.060 |
| 4.88 | 1.25 | -0.053 |
| 5.08 | 1.82 | 0.808 |
| 6.00 | 1.25 | -8.853 |
| 7.00 | 1.27 | -6.068 |
| 8.89 | 1.20 | -0.634 |
| 9.08 | 3.96 | -1.914 |

Figure 10. Transformer Structure Two-Port Analysis
The analysis indicates that the design values are not exact. The response at the center of the band should be Ø.øøldB, and at both band edges, Ø.051dB. However, the results do show that this network would be acceptable for most applications.

## Example 4

## Ladder Analysis of a Transformer Structure

The Transformer Structure shown in Figure 8 can be analyzed using ladder analysis. The circuit file is shown in Figure 11.

| 01+LBL EX4* | 13 RCL 35 | 25 ST0 63 |
| :---: | :---: | :---: |
| 02 SF 80 | 14 RCL 38 | 26 XEE -PRD* |
| 03100 | 15 SF 81 | 27 RCL 21 |
| 04 ST0 25 | 16 XROH -SST* | 28 RCL 22 |
| 850 | $17 \mathrm{X} \backslash \gg$ | 29 RCL 20 |
| 06 STO 26 | 18 XROM -Z-R- | $30+$ |
| 87 RCL 37 | 19 STO 01 | 315 STO 20 |
| 88 RCL 38 | $29 \mathrm{x}+2$ | $32 \mathrm{X}=\mathrm{Y}$ ? |
| 09 XROM -TRL* | 21 CHS | 33 GTO EX4- |
| 10 RCL 36 | 221 | 34 CF 96 |
| 11 RCL 38 | $23+$ | 35 END |
| 12 XROM -TRL* | 24 SQRT |  |

Figure 11. Transformer Structure Circuit File (Ladd
The ladder method will result in a much faster analysis, and should be almost as accurate as the two-port method.

Ladder analysis can only provide the input impedance to the network; however, the impedance may be used to directly campute the input VSWR, and a relationship for lossless two-ports may be used to compute the loss. $|s 21|^{2}$ for a lqssless two-port can be calculated fram : l-|sil| ${ }^{2}$. Thus, the input impedance can be used to
detemine the insertion loss as well. Flag $\varnothing \varnothing$ is set in step $\varnothing 2$ to specify ladder analysis. The magnitude of the terminating impedance ( $1 \varnothing 0$ ohrs) is stored in register 25, and the angle ( $\varnothing$ degrees) in register 26 in steps $\varnothing 3$ through $\varnothing 6$. You should be aware that these steps must be within the frequency loop since at the conclusion of the analysis these registers will contain the input impedance, and must be initialized to the terminating impedance. Steps 07 through 16 are similar to Example 3 above, except the structure is analyzed from the output to the input, and it is not necessary to cascade the elements. Steps 17 and 18 exchange the magnitude and angle of the impedance in " $x$ " and " $y$ " for the conversion to reflection coefficient in step 18. The magnitude of the reflection coefficient is stored in register $\varnothing 1$, and the magnitude of $S 21$ calculated and stored in register Ø3 in steps 19 through 25. The call to "PRD" in step 26 prints the results, the frequency is incremented, and the stop test is made. When the analysis is complete, step 34 clears flag (resetting the two-port mode) and stops. The results of the analysis are identical to those shown in Figure 10.

In most cases the ladder analysis will agree with the two-port analysis. However, when the insertion loss is high, the agreement will not be good and the two-port analysis should be used. This problem is caused when $\mid$ Sll| is squared and subtracted from one to calculate $|\mathrm{s} 21|^{2}$. When the insertion loss is high, |Sll| is almost one, and the accuracy is lost when it is squared and subtracted from one. This problem starts to occur samewhere near 60 to $7 \varnothing \mathrm{~dB}$. It may be worthwhile in a very complicated analysis
to have two circuit files. The ladder analysis can be used unless the insertion loss is greater than some preset value, in which case the analysis would shift to the two-port mode until the insertion loss again rises above the test value.

The network was analyzed using a $100-$ ohm temination as the load. However, there is no reason why the network could not be computed in reverse order. In this case, the termination would be $5 \emptyset$ ohms, and the network analyzed starting with the shorted stub. The reference impedance in register $\varnothing \varnothing$ should be changed to 100 ohms so that the reflection coefficient is referenced to this value. Two-port analysis can also be performed in this manner with a løy-ohm reference. The network would be analyzed in the reverse order, and the transformer would transform fram 100 to 50 ohms. You should also note that $|S 11|$ and $|S 21|$ was calculated and stored in registers $\varnothing 1$ and $\emptyset 3$ for a call to "PRD". which uses these data to compute the VSWR and insertion loss. These data can be computed and printed as a part of the circuit file without a call to an external file. However, "PRD" is used by several of these examples and represents a camon subroutine.

## Example 5

## Plotting Network Response

The plotting capability of the printer can be used to plot the network response as well as to print the output. The requirement of these built-in routines is that the function be called with the value $x$ in the " $x$ " register, and the value of $y, f(x)$, be returned in the " $x$ " register. The plotting routines also use registers $\emptyset \varnothing$ through 11 which conflicts with HANDY-COMPACT, although there is a way around this problem. The listings in Figure 12 show the circuit file for "EX5" and a plot routine named "PLOT" .

| 01*LBL EXX5* | 38*LBL B6 |
| :---: | :---: |
| 82 STO 20 | 39 RCL IHD 52 |
| 03 XEQ "EXK" | 40 X ( $)$ IND 53 |
| 64 SF 08 | 41 STO IND 52 |
| 65109 | 42 ISG 52 |
| 06 ST0 25 | 43 ISG 53 |
| 070 | 44 GTO 80 |
| 08 STO 26 | 45 EHD |
| 89 RCL 37 |  |
| 18 RCL 38 |  |
| 11 XROM -TRL" |  |
| 12 RCL 36 | 81*LBL "PLOT* |
| 13 RCL 38 | 02 - 8 HIN ? ${ }^{\text {c }}$ |
| 14 XROM "TRL* | 03 PROMFT |
| 15 RCL 35 | 04 STO 68 |
| 16 RCL 38 | 85 - X M $\mathrm{SAX}^{\text {? }}$ ? |
| 17 SF 01 | 06 PRPHPT |
| 18 XROH -SST= | 87 STO 99 |
| 19 XC ) 4 | 08 -X INC ? |
| 20 XROM "2-R" | 69 PRORPT |
| 21 CF 80 | 10 STO 10 |
| 22 Xt 2 | 11 FIX IND 05 |
| 23 CHS | 12*LBL 80 |
| 241 | 13 RCL 88 |
| $25+$ | 14 ACX |
| 26 L0G | 153 |
| 2710 | 16 SKPCOL |
| 28 * | 17 RCL 88 |
| 29 STO L | 18 XEQ IND 11 |
| 38 XEQ "EXR" | 19 REGPLOT |
| 31 RCL L | 28 RCL 16 |
| 32 RTH | 21 ST+ 88 |
| 330LBL EEXR" | 22 RCL 69 |
| 34.012 | 23 RCL 88 |
| 35 STO 52 | $24 \mathrm{X}=\mathrm{Y}$ ? |
| 3648.65 | 25 GT0 86 |
| 375705 | 26 END |

Figure 12. Circuit File with Plotting Routine

The circuit file is the same as "EX4" above with some minor changes. This file will be called fram the plot routines with the value of $x$ (the frequency) in the "x" register. Step $\varnothing 2$ stores this value in frequency register 20 . Since the plot routines use registers $\varnothing \varnothing$ through 11 and cause a conflict with the ladder analysis, a subroutine named "EXR" is called from step 03. This subroutine found in steps 33 through 45 exchange the contents of registers $\varnothing \square$ through 11 with the contents of registers 40 through 51 . The remainder of the circuit file fram steps 04 through $2 \varnothing$ is identical to that portion of Example 4; in fact, a modified version of "EX4" could be called at this point. Step 21 clears flag Ø0, and steps 22 through 29 calculate the insertion loss in $d B$ and store this value in register " $L$ " for return to the plot routine. The data registers are again exchanged, the insertion loss recalled fram "L", and execution returned to the plot routine to plot this point.

A review of the technique which must be used in the plot mode is:

1. Store the frequency from the "x" register into register 20 ,
2. Exchange registers $\varnothing \varnothing$ through 11 with registers not used by the circuit file,
3. Analyze the circuit and compute the parameter which is to be plotted, and
4. Save the parameter, restore registers Ø0 through 11, and return to the plot routine with the plot parameter in register " $x$ ".

The results are shown in Figure 13, below.

| PLOT OF EXS |  |
| :---: | :---: |
| $X$ < ${ }^{\text {LUNITS }}$ = | 1.) $\downarrow$ |
| $Y$ <UNITS $=1.\rangle \rightarrow$ |  |
| -2. 60 | 6.00 |
| -2.08 |  |
| 1.801 |  |
| 1.25: | - |
| 1.58 ! | - |
| 1.751 | $\square$ |
| 2.001 | ! |
| 4.801 |  |
| 6.881 |  |
| 8.88: | - |
| 8.251 | $\square$ |
| 8.501 | $\square$ |
| 8.751 | $\square$ |
| 9.081 |  |

Figure 13. Network Response Plot
The initial analysis from 1 to 2 GHz was performed using the standard "PRPLOT" function of the printer. Note that the reference impedance must either be stored in register 40, or stored in register $\varnothing$ and "EXR" executed fram the keyboard since registers 40 through 51 will be loaded into 00 through 11 before the analysis. The plot is desired with a change in the scale for the $x$ parameter (frequency); it is desired to plot the upper and lower skirts in steps $\emptyset .25 \mathrm{GHz}$, and the passband in steps of 2 GHz. Neither the "PRPLOT" or the "REGPLOT" routines have provisions to continue a plot and
label the x axis. The "PLOT" routine is used for this purpose. The "PLOT" routine shown above prampts for the minimum, maximum and step value for the $x$ variable, then uses the data already stored by the "PRPLOT" function to accumulate the label, and executes a call to "REGPLOT" for the actual plot. The program also increments $x$, and tests for a stop. The plot shown above was made with one call to "PRPLOT" and two calls to "PLOT" .

## Example 6

## Analysis of a Feedback Armplifier

The feedback amplifier, shown in Figure 14, has been designed to provide lodB gain fram 250 to 1060 MHz . This structure will be analyzed fram 250 to 1600 MHz in 250 MHz steps.

(80)

Figure 14. Feedback Anplifier

The S-parameters are shown in Figure 15 in the order of increasing frequency.

| TWO-PORT A |  |  |
| :---: | :---: | :---: |
| S11= | 8.56 |  |
| -75.68 |  |  |
| \$12= | 8.82 |  |
|  | 65.80 |  |
| $521=$ | 21.80 | 0.25 cma |
|  | 145.88 |  |
| 522= | 0.78 |  |
|  | -18.00 |  |

TWO-PORT A
S-PARAMETERS
$S 11=0.58$
-126.00

| TWO-PORT A S-PARAMETERS |  |  |
| :---: | :---: | :---: |
| S11 $=0.58$ |  |  |
|  | -144.80 |  |
| \$12= | 8.85 |  |
|  | 49.68 |  |
| \$21= | 4.58 | 1.00 cmz |
|  | 102.08 |  |
| \$22 | 0.46 |  |
|  | -38.88 |  |

## Figure 15. Feedback Antplifier S-Parameters

These parameters may be saved in data memory and recalled during the analysis. This approach will require that the calculator be sized for a minimum of 967 (see the Appendix under the "SVA" cammand) plus the required storage for the element values. Actually, one additional twoport must be saved during the analysis, which will require a size of 975 for the two-port data. However, if you do not have sufficient memory, these parameters may be entered at execution time, either directly from the
keyboard, or using magnetic cards. The temporary data may be saved on a data card as well, or these values recorded for reentry from the keyboard. If you elect to use the latter technique, you can use the "PROMPT" cammand to prompt for data entries, reducing the possibility of entering data for the wrong frequency.

The circuit file used for the analysis is shown in Figure 16 below.

| 91*LBL EX6* | 325 | 63 * |
| :---: | :---: | :---: |
| 021 | 33 XROM -USR" | 646.2 |
| 83 STO 34 | 34 XROH ${ }^{\text {CCAS }}$ | 65 XEQ "FHT* |
| 040LBL 80 | 35 SF 81 | 66 PRBUF |
| 65 SF 01 | 36 RCL 82 | 67 -1SUR=* |
| 86 RCL 75 | 37 XROM -RES* | 68 ACA |
| 07 XROH *CAP* | 38 XROM "CAS" | 691 |
| 88 XROH "EXC" | 39 XEQ "PR* | 70 RCL 01 |
| 69 RCL 76 | 48 RCL 21 | $71+$ |
| 18 XROH -IND- | 41 RCL 22 | 721 |
| 11 XROH "CAS" | 42 RCL 28 | 73 RCL 01 |
| 12 SF 81 | 43 + | 74 - |
| 13 RCL 77 | 4457020 | 75 / |
| 14 XROM "RES" | $45 \mathrm{X}<=\mathrm{Y}$ ? | 766.2 |
| 15 XROH "CAS" | 46 GTO 60 | 77 XEQ -FMT- |
| 165 | 47 RTN | 782 |
| 17 XROM -SYA* | 48*LBL -PR- | 79 SKPCHR |
| 18 RCL 34 | 49 FIX 2 | 80 -0SUR=" |
| 19 XROM -USA* | 59 -FREQ=* | 81 ACA |
| 281 | 51 ACA | 821 |
| $21 \mathrm{ST}+34$ | 52 RCL 28 | 83 RCL 84 |
| 22 SF 81 | 536.2 | 84 + |
| 23 RCL 88 | 54 XEQ -FMT* | 851 |
| 24 RCL 81 | 552 | 86 RCL 84 |
| 25 XROH -PRC* | 56 SKFCHR | 87 - |
| 26 XROM -SER" | 57 -GAIH=* | 88 \% |
| 27 RCL 78 | 58 ACA | 896.2 |
| 28 RCL 79 | 59 RCL 83 | 90 XEQ -FMT* |
| 29 XROM - SRL* | 60 Xt 2 | 91 PRBUF |
| 30 XROM -PAR ${ }^{\text {- }}$ | 61 LOG | 92 ADY |
| 31 XROM ${ }^{\text {EXC" }}$ | 6218 | 93 EMD |

Figure 16. Feedback Armplifier Circuit File

This amplifier uses both series and shunt feedback requiring the use of temporary storage for one two-port. Recall that only two two-ports may be active at any time, and the connection of the feedback elements with the device will require both. During this process, the parameters for the input network must be saved. The procedure used for this analysis will be to analyze to input network, save the data, connect the series and shunt feedback elements, reload and cascade the input network, then connect the output network. However, there is no reason why the feedback elements could not be connected with the device, then saved while the input network is cascaded.

The index register, register 34 , will be used to recall the device $S$-parameters at the corresponding frequencies. Before execution, these parameters should be entered from the keyboard (or loaded from data cards) and saved in two-port 1 through two-port 4 using the "SVA" command. Two-port 5 will be used as temporary storage during the analysis. Steps $\varnothing 2$ and $\emptyset 3$ in the circuit file initialize the index register to 1 . Label 0 in step 04 will be used as the frequency loop. This label must be used since the index register will be incremented at each frequency, and should not be reset to 1 . Same program memory can be saved by loading the index register from the keyboard before execution; label 00 may be deleted as well (the GIO in step 46 must also be changed), but you must remember this step each time the circuit is analyzed. Steps $\varnothing 5$ through $\varnothing 7$ compute the 5 -parameters of the input shunt capacitor as two-port "B". The "EXC" command in step $\emptyset 8$ saves the parameters in "A" since this is the first element. Step $\varnothing 9$
through 11 computes the series inductor and cascades it with the capacitor, and steps 12 through 15 do the same for the shunt resistor. At this point, the entire input network is in two-port "A", and the carmands in steps 16 and 17 save this data in two-port 5 (registers 67 through 74). The index register (l at the first frequency) is recalled in step 18, then the corresponding two-port is recalled into " $A$ " by step 19. Steps $2 \varnothing$ and 21 increment the index register for the next frequency. Note that the calculator command "ISG" can be used if the index register is loaded with $l$ plus a fraction greater than .064, (1.064) may be entered and "ISG" used as the stop test. In this case, the frequency should be incremented before the test, and the stop frequency need not be used.

Steps 22 through 25 recall the data for the series feedback element, set the shunt flag, and calculate the S-parameters for this element. The "SER" cammand in step 26 connects this element with the device. Steps 27 through 30 do the same for the shunt feedback which is connected using the "PAR" cammand. Two-port "A" contains the parameters for the device with both series and shunt feedback, and the "EXC" command in the next step loads this data into "B". Steps 32 through 34 recall the input network and cascade it with the device, then the output element is calculated and cascaded in the next four steps to form the overall amplifier parameters. The subroutine "PR" is called to print the output data, the frequency is incremented, a stop test is then made in the usual manner.

The output routine in Figure 17 prints the frequency, then computes the gain fram $|521|$, the input VSWR from |S11|, and the output VSWR from $|\mathrm{s} 22|$. The output indicates that this amplifier does indeed have $1 \varnothing \mathrm{~dB}$ gain from 250 to 1060 MHz . Maximum VSWR is 1.74:1, confirming that the design is correct.

| EX'6 |  |  |  |
| :---: | :---: | :---: | :---: |
| FREQ $=$ | 0.25 | GAIN $=$ | 9.97 |
| [SHR $=$ | 1.19 | OSUR $=$ | 1.21 |
| FREQ $=$ | 8.58 | GAIN= | 9.82 |
| ISUR= | 1.51 | OSHR $=$ | 1.48 |
| FREQ $=$ | 0.75 | CAIN= | 10.81 |
| ISHF= | 1.71 | OSUR $=$ | 1.59 |
| FREQ $=$ | 1.88 | GAIN= | 10.84 |
| ISUR: | 1.74 | OSUR $=$ | 1.61 |

Figure 17. Feedback Amplifier Analysis

Two utility programs, "PTA" and "PTB" in Figure 18, can be used to print the s-parameters of either two-port " $A$ " or " B ", respectively.

| 91*LBL -PTA" | 22 -521* |
| :---: | :---: |
| 821 | 23 XEP 01 |
| 83 - ${ }^{\text {a }}$ | 24 - $522 \cdot$ |
| 04 GTO 08 | 254LEL 01 |
| 65*LBL "PTB" | 26 - $=$ - |
| 0611 | 27 ACA |
| 07 -8. | 28 RCL IND X |
| 084LBL 06 | 29 ACX |
| 09 ADY | 38 PRBUF |
| 10 ASTO L | 315 |
| 11 - TMO-PGRT - | 32 SKPCHR |
| 12 ARCL L | 33 RDN |
| 13 SF 12 | 344 |
| 14 PRA | $35 \mathrm{ST}+2$ |
| 15 "S-PARAMETERS" | 36 RCL IND ? |
| 16 PRA | 37 ACX |
| 17 CF 12 | 38 PRBUF |
| 18 -511* | 39 RT |
| 19 XEA 01 | 403 |
| 28 -512* | 41 - |
| 21 XEA 81 | 42 END |

Figure 18. Print Utility Programs
"PTA" was used to print the device parameters. These subroutines do not print the frequency as shown. However, it is suggested that several subroutines be written to print the various parameters, input VSWR, output VSWR, gain, frequency, etc., with the desired headings. These may then be called as desired. For example, subroutine "FRQ" may be called then subroutine "GAN" called to accumulate the frequency and gain similar to subroutine "PR" above. These routines may then be combined to produce the desired output.

## Example 7

## Analysis of a Matching Network

The matching network in Figure 19 has been designed to match a complex load into 50 ohms across the $1 . \emptyset$ to $2 . \emptyset \mathrm{GHz}$ band. The load impedance has been measured, and could represent an antenna impedance or the input to an active device.


Figure 19. Matching Network
The impedance is given in the form as shown in the form:

| FREQ | IMPEDANCE |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Real | register | Imag | register |
| 1.0 | 1.9 | 48 | +j 2.0 ohms | 49 |
| 1.2 | 2.0 | 50 | +j 2.1 ohms | 51 |
| 1.4 | 2.0 | 52 | +j 2.0 ohms | 53 |
| 1.6 | 1.9 | 54 | +j 1.8 ohms | 55 |
| 1.8 | 1.8 | 56 | +j 1.5 ohms | 57 |
| 2.0 | 1.7 | 58 | +j 1.0 ohms | 59 |

These data are stored in the indicated registers, However, they are stored in polar form, with magnitude in the lower numbered register and angle in the next highest. The ladder analysis will be used, requiring the impedance in polar form. These data may also be stored in rectangular form and converted when recalled. The circuit file shown below is similar to Example 4 with same minor exceptions. The temmination impedance is complex and must be recalled at each corresponding frequency. Steps 03 and 04 initialize the index register to the location of the magnitude for the first frequency. Step $\varnothing 8$ recalls the magnitude and stores it into the ladder analysis impedance magnitude register. Steps 10 through 13 increment the index register, then recall and store the angle of the measured impedance. The index register is then incremented for use at the next frequency in steps 14 and 15. Steps 16 through 32 connect each element of the matching network, and convert the input impedance to reflection coefficient. Steps 33 through 64 save the input reflection coefficient, accumulate the frequency, then compute and print the input VSWR. The input reflection coefficient is recalled and printed, the frequency incremented, and the stop test made.

As shown in the program listing (Figure 20), the program does not loop back to the beginning of the circuit file so that the index register is unchanged.

| 010LBL -EX7* | 26 RCL 63 | 516 |
| :---: | :---: | :---: |
| 02 SF 00 | 27 XROM 'TRL' | 52 RCCHR |
| 0348 | 28 RCL 68 | 53 - • |
| 04 ST0 34 | 29 RCL 61 | 54 ACA |
| 851 | 38 XROM -TRL- | 55 RCL 68 |
| 86 ST0 28 | 31 KOY | 568.5 |
| 870LRL 15 | $32-\mathrm{XROH}=2-8$. | 57 XEE "FHT" |
| 86 RCL IHD 34 | 33 STO 68 | 586 |
| 69 ST0 25 |  | 59 SKPCHP. |
| 181 | $35 \mathrm{ST0} 69$ | 68 RCL 69 |
| 11 ST+ 34 | 36 RCL 28 | 617.2 |
| 12 RCL IHD 34 | 374.1 | 62 XEQ - FHT = |
| 13 STO 26 | 38 XEE -FMT* | 63 PRBUF |
| 141 | 3918 | 64 ADY |
| $15 \mathrm{ST}+34$ | 40 SKPCH: | 65 RCL 21 |
| 16 RCL 67 | 411 | 66 RCL 22 |
| 17 SF 81 | 42 RCL 68 | 67 RCL 20 |
| 18 XROH -CAP- | $43+$ | 68 + |
| 19 RCL 65 | 441 | 69 ST0 20 |
| 28 RCL 66 | 45 RCL 68 | $78 \mathrm{X}=\mathrm{Y}$ ? |
| 21 XROH ${ }^{\text {[TRL* }}$ | 46 - | 71 CT0 15 |
| 22 SF 91 | 47 \% | 72 CF 88 |
| 23 RCL 64 | 486.3 | 73 END |
| 24 XROM -CAF | 49 XEE -FHT* |  |
| 25 RCL 62 | 58 PRBUF |  |

Figure 20. Matching Network Circuit File
Again, the index register may be initialized fram the keyboard before program execution, but you must be careful to remember this step. The
result of this analysis is shown in the listing in Figure 21. This matching network is not acceptable since the input VSWR ranges fram 2.444 to 3.972 :1. The matching network should either be redesigned with more care, or a CAD program with the capability of optimization should be used to reduce the VSWR to an acceptable level.

| EXT |  |
| :---: | :---: |
| FREQ | YSHR |
| 1.0 | 2.444 |
| $\Gamma=0.41928$ | $-53.23$ |
| 1.2 | 2.702 |
| $\Gamma=0.45977$ | -98.77 |
| 1.4 | 3.525 |
| $r=9.55888$ | -140.27 |
| 1.6 | 3.972 |
| $\Gamma=0.59774$ | -179.26 |
| 1.8 | 3.626 |
| $\Gamma=0.56764$ | 139.20 |
| 2.8 | 2.637 |
| $r=0.45989$ | 84.84 |

Figure 21. Matching Network Analysis

## Example 8

## Armplifier Design

HANDY-COMPACT can be used as a design tool. In this example, it will be used in the initial design phase to set design goals and define the required impedances for a matching network. The network may then be modeled and analyzed or optimized as desired. The design capability can be illustrated through the partial design of an amplifier.

The goal will be to design a 25 dB gain amplifier at 8.0 GHz . (The technique could be extended to the design of amplifiers with wider bandwidths.) The first task is to characterize the device so that the number of stages and gain per stage can be determined. The characterization ("CHR") and stability ("STB") functions can be used to determine the necessary information.

The S-parameters of a commercially available GaAs FET are shown below:

| FREQ | Sll | S12 | S21 | S22 |
| :---: | :---: | :---: | :---: | :---: |
| $8 . \varnothing$ | 0.717-57 | 0.028171 | 2.223138 | ¢. $851-20$ |
| 10.0 | $0.674-75$ | 0.041125 | 1.983125 | $0.762-21$ |
| 12.0 | $0.602-98$ | 0.056156 | 1.866113 | $0.611-30$ |
| 14.0 | Ø.582-121 | 0.077139 | 1.49587 | $0.761-79$ |

Both ROM programs are modified to include the autamatic execution feature, as well as format and add headings to the output. Both routines are shown in Figure 22, below. These programs have been implemented by programming the file as shown with the exception of the labels found in step Øl. This approach allows the calculator to convert the call to the ROM programs with the same name to "XROM" so that the ROM program will execute. The last step of the programing for each file is to go to step 60, and add the "LBL" "name". Thus when the program is executed, the program in RAM, which uses the program with the same name in ROM as a subroutine, will execute as desired. (This technique is described on Page 10.)

| $01+$ LBL -CHR" | 41 SF 13 | 86 XEQ 80 |
| :---: | :---: | :---: |
| 82 SF 84 | $42 \cdot \mathrm{~A}=-$ | 872 |
| 83 XROM "CHR- | 43 ACA | 88 XROM -STR* |
| 04 CF 84 | 44 RCL 89 | 89 CF 64 |
| 85 RDY | 459.5 | 18 -OUTPUT* |
| 863 | 46 XEQ -FHT* | 110LBL 80 |
| 87 SKPCHR | 47 PRBUF | 12 * STABILITY* |
| 88 -FREQ $=$ - | 486 | 134 |
| 89 ACA | 49 ACCHR | 14 SKPCHK |
| 10 RCL 20 | 59 -S=* | 15 ACA |
| 118.4 | 51 ACA | 16 PRBUF |
| 12 XEQ PFHT* | 52 RCL 24 | 17 "CTR=" |
| 13 - $\mathrm{CH}^{-}$ | 538.5 | 18 ACA |
| 14 ACA | 54 XEQ -FMT* | 19 RCL 31 |
| 15 SF 13 | 553 | 288.5 |
| 16 '2' | 56 SKPCHR | 21 XEQ -FMT* |
| 17 ACA | 57 RCL 27 | 222 |
| 18 CF 13 | 5818.5 | 23 SKPCHR |
| 19 PRBUF | 59 XEQ -FKT- | 24 RCL 32 |
| $28 \cdot k={ }^{\prime}$ | 68 PRBUF | 2516.5 |
| 21 ACA | 616 | 26 XEQ ${ }^{\text {PFMT* }}$ |
| 22 RCL 29 | 62 ACCHR | 27 PREUF |
| 237.4 | $63^{\circ} \mathrm{L}=-$ | 28 -RAD=* |
| 24 XEQ -FMT* | 64 ACA | 29 ACA |
| 253 | 65 RCL 19 | 38 RCL 33 |
| 26 SKPCHR | 668.5 | 318.5 |
| 271 | 67 XEQ -FMT- | 32 XEQ -FHT* |
| 28 RCL 29 | 683 | 332 |
| 29 X YY? | 69 SKPCHR | 34 SKPCHR |
| 38 GTO 80 | 70 RCL 23 | 35 -STABLE - |
| $31 .{ }^{\text {HSG* }}$ | 7116.5 | 361 |
| 32 ACA | 72 XEQ "FMT" | 37 RCL 18 |
| 33 RCL 89 | 73 PRBUF | $38 \mathrm{x}=9$ ? |
| 349.5 | 74 CF 13 | 39 "-OUT" |
| 35 XEQ -FKT* | 75 END | $48 \mathrm{X}=\mathrm{Y}$ ? |
| 36 PRRUF | 01*LBL -ST8* | 41 -riN- |
| 37 RTN | 82 SF 64 | 42 ACA |
| $38+L B L$ 80 | 021 | 43 PRBUF |
| 39 " 6 | 04 XROM -STE. | 44 END |
| 48 ACA | 05 -INPIT* |  |

Figure 22. Amplifier Design Aids

The characterization program, "CHR", shown in Figure 22, sets the autamatic execution flag (flag 04) and calls the ROM program which camputes the stability factor, gain, and simultaneous matched source and load for a stable network. The ROM program returns to RAM with the parameters in the data registers indicated in the Appendix. The program clears the autamatic execution flag, then prints the frequency, and accumulates the stability factor in steps $\varnothing 4$ through 24. A test is made in steps 27 through 30 to determine whether the stability factor is greater than one. When the stability factor is greater than one, execution transfers to label $\emptyset$ in step 38 where the maximum available gain as well as the simultaneous, matched load- and source-reflection coefficient is printed. Otherwise, execution continues where the maximum stable gain is printed.

The stability program, "STB" above, sets the autonatic execution flag, and calls the ROM program twice: once with the code for input plane and again with the output plane code. Following each call to the program, the title "INPUT" or "OUTPUT" is loaded into the alpha register and a call is made to label øø where the data is printed. Label $\varnothing \square$ at step 11 appends "STABILITY" to the data already in the alpha register and prints the heading. The magnitude and center of the stability circle is then printed in steps 17 through 27. Steps 28 through 35 accumulate the radius and "STABLE" into the print buffer. Steps 36 through 41 test the stability code to determine the location of the stable region. If the network is not unconditionally stable, either "IN" or "OUT" is accumulated into the buffer and the data printed.

The results of this analysis is shown in Figure 23.

| FREQ $=8.8980 \mathrm{CHz}^{\text {c }}$ |  |
| :---: | :---: |
|  |  |
| PUT STABILITY |  |
| $\mathrm{R}=1.19532$ | 51 |
| 0.30189 | 9 ST |
| TPUT STABIL |  |
| CTR $=1.09868$ |  |
| RAD $=0.14952$ |  |



FREQ $=10.0000 \mathrm{GHz}$
$\mathrm{K}=0.9904$ HSG 16.84539 INPUT STABILITY
CTR=1.31247 78.24105
RAB $=0.31476$ STAELE OUT OUTPUT STABILITY
$C T R=1.28969 \quad 17.93536$
$R A D=0.21136$ STRELE OUT

FREQ $=14.0000 \mathrm{CHz}$
$K=1.0863 \quad G a=11.89017$
$\Gamma s=0.84652 \quad 105.88059$
$\Gamma 1=0.91271 \quad 72.41855$
IHPUT STABILITY
$C T R=1.78842 \quad 105.08059$
RAD $=0.67403$ STABLE
OUTPUT STABILITY
CTR $=1.29870 \quad 72.41855$
RAB $=0.27996$ STRBLE

Figure 23. Amplifier Analysis

The data show that the device is not stable at 8.0 GHz and that the maximum stable gain is 18.99781 dB . Therefore, two gain stages, each with 12.5 dB gain, will be required for the design. Several approaches may be taken to achieve the desired gain, however, for purposes of this example it will be assumed that noise figure is a consideration, and a lossless reactive mismatch will be used. This approach will result in a mismatch at either the input or output, and will require some means to overcame this problem. The two methods most camonly used are the hybrid-coupled amplifier and the isolator. The isolator is a narrow-band device, and the impedances change very fast outside the passband. Since the device is unstable and out-of-band impedances will be critical to the stability, the balanced amplifier approach is used.

The source and load impedances must now be found which will result in the desired 12.5 dB gain, and do not fall within the unstable regions. One approach which may be used is to generate the constant gain contours on either the source or load planes, select an impedance, then compute the conjugate match on the opposite plane. Either plane may be used for the gain circles, however, the output impedance is usually less sensitive to variations in the input impedance, and gain circles on the input plane will allow the selection of an impedance which will provide low noise as well as the specified gain. Figures 24 and 25 show the respective input and output planes for this device at $8 . \varnothing \mathrm{GHz}$.


Figure 24. Device Input Plane at 8 GHz

| MAME | TITLE OUTPUT PLANE - O G HE | DWG. NO. |
| :--- | :--- | :--- | :--- |
| SMITH CHART FORM ZY-AH-N | ANALOG INSTRUMENTS COMPANY, NEW PROVIDENCE, M.J. OTETA | DATE |

NORMALIZED IMPEDANCE ANO ADMITTANCE COORDINATES


Figure 25. Device Output Plane at 8 GHz

Both planes show the stability circles constructed from the output of the stability analysis. The shaded portion is unstable, and the impedances must not be selected from these regions. Constant gain contours for the input plane were calculated for several values of gain, and are shown on the input plane. The output data from the "CGC" program is shown below:

| GAIN | CENIER |  | RADIUS |
| :--- | :--- | :--- | :--- |
| 12.5 | 0.50912 | 51.59367 | 0.51335 |
| 15.0 | 0.67996 | 51.59367 | 0.36410 |
| 17.0 | 0.80862 | 51.59367 | 0.26921 |
| 19.5 | 0.94199 | 51.59367 | 0.21242 |

These data may be saved by interrupting the program and returning to the label in ROM as mentioned in the text above, or as in this case, by using the print stack ("PRSTK") command. The 12.5 dB gain contour passes through the origin of the mapping, 50 ohms, and is a good candidate for the source impedance. No input matching network will be required. The corresponding output reflection coefficient, S22', calculated fram "S2P" with $\varnothing / \emptyset$ degrees, is shown on the output plane as S22'A, and is $0.851 \varnothing 6 /-20 . \varnothing$ degrees. The load reflection coefficient is the complex conjugate of this value, or $\varnothing .851 \varnothing 0 / 20 . \emptyset$ degrees. The transducer gain, "GTP", can be calculated using these points, and is 12.53286 dB .

It appears from the constant gain contours that a gain can be found which is higher than the
maximum stable value of $18.99781 d B$ without causing the input reflection coefficient to enter the unstable region. Point " C " is such a point on the 19.5 dB gain circle. This point is $0.74 / 51$ degrees. The corresponding output reflection is $0.94552 / 18.649$ degrees. This point does fall within the unstable region of the output stability circle, as shown. However, note that the reflection coefficient is less than one, thus positive real. The input reflection coefficient, Sll', calculated using this load with the "SlP" program, is $1.08479 /-51.40$ degrees which results in a negative real input impedance as expected.

Point " A " and the corresponding output load may be used to provide a simple 12.5 dB gain stage. However, in the case of a broadband design, it is desirable to find a source and load reflection coefficient which results in the desired gain at each frequency, and follows either the constant resistance or conductance contours with frequency. This approach results in a simple load which consists of either a series or parallel cambination of a resistor and a reactive element. There are many techniques available to match a load represented in this fashion. Therefore, it is desirable to be able to select a range of impedances in both planes. The mismatch contours, "MMC", can be used for this purpose. Point "B" is selected as the input impedance at this frequency, and is assumed to connect with the reflection coefficient at another frequency following the constant resistance or conductance contours. This point is $0.615 / 66$ degrees, and the corresponding 522', Ø.90217/-17.140 degrees, as shown on the output plane. Since 12.5 dB is the
desired gain, and point "B" provides 17dB gain, a 4.5 dB mismatch will be required on the output plane. The "MMC" program is used with S22' as the input to calculate the 4.5 dB mismatch contour. The center is located at $\emptyset .674 \emptyset 8 / 17.140$ degrees, and has a radius of 0.31476 . This mismatch contour is shown on the output plane, and any load impedance selected from this contour will result in the desired 12.5 dB gain. The point on this contour is selected for the same reasons as the input, and is shown as $\Gamma_{\text {LB }}$, which is Ø.48/44 degrees. Thus, the source reflection coefficient is $\varnothing .615 / 66$ degrees, and the load, $0.48 / 44$ degrees. These numbers should be checked before the design continues to check for possible errors. The transducer gain, "GIP", calculated from these points is $12.46131 d B$ (which is acceptable), and the design can continue.

The matching networks designed directly from the Smith chart are shown in Figure 26.


Figure 26. Input Matching Network
The input network is a simple two-element network which transforms $5 \emptyset$ orms into the desired source impedance.

The output network uses a quarter-wavelength transmission line to transform the real portion, and a shunt inductor to provide the desired output.

The ladder analysis mode is set, and the reflection coefficient presented by each network is calculated directly fram the keyboard as a check. The input reflection is $0.59484 / 66.46487$ degrees, and the output, $0.47868 / 43.18923$
degrees. The transducer gain corresponding to these terminations is 12.45101 dB . The program is returned to the two-port mode, and a complete analysis is then made directly from the keyboard.

The results are shown in Figure 27, and the gain calculated fram $|\mathrm{S} 21|$ is 12.45103 dB , almost exactly that predicted by the ladder analysis. Characterization of this network reveals that the stability factor and maximum stable gain is exactly that calculated for the device alone, as it should be using lossless matching networks.

TWO-PORT A<br>S-PARAMETERS<br>c11 $=0.35413$<br>-13.94719<br>$512=0.95282$<br>113.99843<br>$521=4.19326$<br>86.99843<br>$522=9.80801$<br>$-128.84733$

## Figure 27. Results of Camplete Analysis

Since it is assumed that this amplifier will be balanced, the final step in the design is the analysis of the overall stage. Assume that the amplifier is an 8 to 12 GHz design, which would have a coupler center frequency of $1 \varnothing \mathrm{GHz}$, and would be over-coupled at the center frequency. A coupling coefficient of 2.5 dB will be assumed for this analysis. The analysis of two identical stages is accomplished, again fram the keyboard, by executing the "EQU" camand which duplicates two-port "A" in "B", then entering the coupler parameters and executing the hybrid connection, "HYB". The results are shown in Figure 28.

| TWO-PORT A |  |
| ---: | :--- |
| $S$-PARAMETERS |  |
| $S 11=$ | 0.02656 |
|  | 10.31544 |
| $S 12=$ | 0.85267 |
|  | 48.26106 |
| $S 21=$ | 4.18144 |
|  | 15.26186 |
| $S 22=$ | 8.0681 i |
|  | -164.58470 |

Figure 28. Results of Hybrid Connection Analysis

The overall balanced amplifier has an input VSNR of $1.05: 1$, output VSWR of $1.13: 1$, gain of 12.43 dB , reverse isolation of -25.57 dB , and is unconditionally stable (the stability factor is 2.37). The final steps in the design should be to analyze the structure across a broad frequency range, especially at the lower frequencies where the device becames even more unstable.

The approach taken above is an extremely fast and effective method to define the initial design parameters, and provides sufficient accuracy even using graphical techniques. HANDY-COMPACT provides the necessary data to allow flexibility in the design tradeoffs. Another useful technique is to use the source and load mappings of "MAP". These mappings provide immediate information as to the required source or load impedance which corresponds to the termination in the opposite plane. This approach allows an impedance to be selected from one plane, which results in a desirable impedance in the other. Stability information is immediately available without the requirement for stability circles.

## APPENDIX

This Appendix serves as a reference guide to HANDY-COMPACT. The Tables in this Appendix correspond (to same extent) with the text discussions at the front of the manual:
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PROGRAM STRUCTURE ..... 85
ELFMENT LIBRARY ..... 86-87
INTERCONNECTIONS ..... 88
LADDER ANALYSIS ..... 89
MANIPULATION COMMANDS ..... 90
CONVERSION COMMANDS ..... 91
CHARACTERIZATION ..... 92-93
MAPPING ..... 94
SIZING
To size the calculator, enter: XEQ ALPHA SIZE ALPHA $\varnothing 35$

## STRUCTURE

## SIZE =035

PROGRAM UNITS:
$G H Z$ OHMS mm HO NH PF MILS $E_{r}=1$

$$
S_{A}=\left[\begin{array}{lll}
\theta & \angle \theta) & \theta(\theta) \\
\Theta<\theta & \theta<\theta
\end{array}\right]
$$

$$
s_{B}=\left[\begin{array}{ll}
\omega<\omega \\
\omega<\omega
\end{array}\right]
$$

$z_{\text {ref }} \Rightarrow 0 \quad$ INDEX $\Rightarrow 34$
予的wency $\Rightarrow$ (20) step freq $\Rightarrow 21$ Step Freq $\Rightarrow 22$.

Flags
Flag $O \Rightarrow$ Ladder Analysis $\mid$ Flag $\mid \Rightarrow$ Shunt Element
Flag $24 \Rightarrow$ set by program
Flag $4 \rightarrow$ Auto execution of chR 5 TB

Elament Liblary（ $S=S_{p}$ ）

|  | nat． | nat． |  |
| :---: | :---: | :---: | :---: |
| $\ldots$ | － | － $\mathrm{f}^{\text {c }}$ |  |
| m | $E$ | 4． | ＊ |
| － | $\pm$ |  | 2. |
| \％ | $\sim^{\prime}$ | T | 21 |
|  | L | T | $\ldots$ |
| － | 7 7 | 7 | $\cdots \times$ |
| cos | $7{ }^{7}$ | $7{ }^{\text {7 }}$ | 0 |
| us | T | 可里 | 0 |
|  |  | 運易 | 2\％ |

ELEMENT LIBRARY $\left(S=S_{B}\right)$


INTERCONNECTIONS

| CAS | $[5]=\sqrt{5}]$ |
| :---: | :---: |
| SER |  |
| PaR |  |
| swe |  |
| pse |  |
| HY8 |  |
| PBR |  |
| SBR |  |

## LADDER ANALYSIS

```
SF0日 fat lmopen muncysas mone.
```




```
Sm t* reer mompite
```






## MANIPULATION CONMANDS




## CONVERSION COMMANDS




CHARACTERIZATION: $S_{A}$


CHARACTERIZATION: $\mathrm{S}_{\mathrm{A}}$


MAPPIMG: $S_{A}$

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[^0]:    Figure 2. Parallel-Coupled Filter Circuit File

