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# **HP-41C**

# Standard Applications Handbook

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## INTRODUCTION

This applications handbook contains a collection of programs that demonstrate the power and versatility of your HP-41C in programmed problem-solving. You will find the programs useful, entertaining, and fascinating. By entering and executing them, you'll get an immediate "hands-on" glimpse of the advanced capabilities of your HP-41C, and—thanks to its Continuous Memory —you'll have them available in the future ready to use.

Studying all of these professionally designed programs will help you develop your own programming expertise. The benefits of owning an HP-41C can be realized through the imaginative exploitation of its programming power and versatility, which enable you to customize your HP-41C to suit your particular needs.

For each of the 10 programs in this handbook we've included a description, instructions, one or more example problems, program highlights, and a program listing. Before entering any of the programs, take a few minutes to study the sections Keying a Program Into the HP-41C and Format of User Instructions at the front of this handbook. You might understand them better and learn a lot more from them if you've first read through the HP-41C Owner's Handbook and Programming Guide.

When you've selected a program you'd like to execute, key it in by following the program listing, then refer to the table of instructions for detailed information on how to use the program. You'll probably need to refer to these instructions only the first few times you run the program. Afterwards, the program's prompting should provide the necessary instructions, including which data should be input, the keys to press, and the kind of output.

The Program Highlights present programming techniques of particular interest. Studying them will help you understand the operation of parts of the program, and you may find uses for them as part of programs you write yourself. For an in-depth understanding of the program's operation, and to learn more about efficient and versatile programming techniques, also study the comments included in the program listings.

Except for the blackjack game, all programs in this handbook can be keyed into the basic HP-41C. The blackjack game requires one additional memory module. As you expand your HP-41C system, you will find that some of these programs work well as a basis for larger programs of your own. You might want to modify some programs slightly to suit your individual needs—that's the beauty of programmability.

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# FORMAT OF USER INSTRUCTIONS

The User Instructions which accompany each program are your guide to operating the programs in this handbook.

The form is composed of five labeled columns. Reading from left to right, the first column, labeled STEP, gives the instruction step number.

The INSTRUCTIONS column gives instructions and comments concerning the operations to be performed.

The INPUT column specifies the input data, the units of data if applicable, or the appropriate alpha response to a prompted question. Data Input keys consist of 0 to 9 and the decimal point (the numeric keys), [EEX] (enter exponent), and [CHS] (change sign).

The FUNCTION column specifies the keys to be pressed after keying in the corresponding input data.

Whenever a statement in the INPUT or FUNCTION column is printed in gold, the ALPHA mode must be on before the statement can be keyed in. For example, XEO A4C means press the following keys: XEO ALPHA A 4C ALPHA. Of course, you could assign the function A4C to any key you chose by pressing ASN ALPHA A 4C ALPHA KEY. Then you could simply press KEY in USER mode to execute the function.

The DISPLAY column specifies prompts as well as intermediate and final answers and (where applicable) their units.

Above the DISPLAY column is a box which specifies the SIZE or minimum number of data registers used by the program. Program memory should be SIZEd before keying in the program or it might not fit. Refer to pages 73 and 117 in the Owner's Handbook for a complete description of how to size calculator memory.

## **KEYING A PROGRAM INTO THE HP-41C**

There are several things that you should keep in mind while you are keying in programs from the program listings provided in this book. The output from the HP 82143A printer provides a convenient way of listing and an easily understood method of keying in programs without showing every keystroke. This type of output is what appears in this handbook. Once you understand the procedure for keying programs in from the printed listings, you will find this method simple and fast. Here is the procedure:

 At the end of each program listing is a listing of status information required to properly execute that program. Included is the SIZE allocation required. Before you begin keying in the program, press XEO (ALPHA) SIZE (ALPHA) and specify the allocation (three digits; e.g., 10 should be specified as 010).

Also included in the status information is the display format and status of flags important to the program. To ensure proper execution, check to see that the display status of the HP-41C is set as specified and check to see that all applicable flags are set or clear as specified.

- 2. Set the HP-41C to PRGM mode (press the PRGM key) and press GTO
   to prepare the calculator for the new program.
- 3. Begin keying in the program. Following is a list of hints that will help you when you key in your programs from the program listings in this handbook.
  - a. When you see " (quote marks) around a character or group of characters in the program listing, those characters are ALPHA. To key them in, simply press ALPHA, key in the characters, then press ALPHA again. So BE "SAMPLE" would be keyed in as ALPHA SAMPLE ALPHA.
  - b. The diamond in front of each LBL instruction is only a visual aid to help you locate labels in the program listings. When you key in a program, ignore the diamond.
  - c. The printer indication of the divide sign is /. When you see / in the program listing, press ÷ .
  - d. The printer indication of the multiply sign is ÷ . When you see ÷ in the program listing, press ∞.
  - e. The ⊢ character in the program listing is an indication of the APPEND function. When you see ⊢, press APPEND in ALPHA mode (press and the K key).

f. All operations requiring register addresses accept those addresses in these forms: nn (a two-digit number)
IND nn (INDIRECT: , followed by a two-digit number)
X, Y, Z, T, or L (a STACK address: followed by X, Y, Z, T, or L)
IND X, Y, Z, T, or L (INDIRECT stack: followed by X, Y, Z, T, or L)

Indirect addresses are specified by pressing and then the indirect address. Stack addresses are specified by pressing followed by X, Y, Z, T, or L. Indirect stack addresses are specified by pressing and X, Y, Z, T, or L.

#### **Printer Listing**

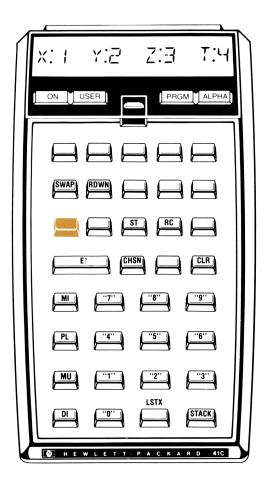
#### Keystrokes

Display

01♦LBL "SAM		01 LBL T SAMPLE
PLE" 02 "THIS IS	ALPHA THIS IS A ALPHA	02 <sup>T</sup> THIS IS A
A "	ALPHA SAMPLE	03 <sup>T</sup> ⊢ SAMPLE
03 "HSAMPLE "		04 AVIEW
04 AVIEW	6	05 6
05 6 06 ENTER†	ENTER+	06 ENTER /
07 -2	2 <b>CHS</b>	07 –2
08 / 09 ABS	÷	08 /
10 STO IND	XEQ ALPHA ABS ALPHA	09 ABS
L 11 "R3="	STO 💼 💽 I	10 STO IND L
12 ARCL 03	ALPHA R3= ARCL 03	11 <sup>⊤</sup> R3=
13 AVIEW 14 RTN		12 ARCL 03
14 RTN		13 AVIEW
	ALPHA	14 RTN
	RTN	

#### **RPN PRIMER**

This program is an aid to understanding and using RPN, the logic system used in the HP-41C. All four registers of the operational stack are visible simultaneously so that the effect of a given keystroke sequence can be seen rather than inferred. The functions provided, assigned as shown in the instructions, appear on the keyboard below. These functions all exit to a routine which displays the operational stack. It is possible to observe the effect on the stack of functions which are not included within this program. Simply execute the desired function, then press the **R/S** key, to which STACK is assigned. The only operational differences between this redefined calculator and the actual one are that only single-digit numbers can be keyed in and that STO/RCL address only a single register (thus requiring no address).



9

				SIZE: 001
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the the program			
2	Assign * its routines as shown and select USER mode. These suggested assignments result in the keyboard shown on the previous page.			
	SWAP       xiy         ST       STO       RDWN       R*         E↑       ENTER*       RC       RCL         CLR       CHSN       CHS         PL       MI       -         MU       ×       DI       +         9       9       8       8         7       7       6       6         5       5       4       4         3       3       2       2         1       0       0       LASTX       STACK       R/S			
3	Press desired keystroke sequence and watch stack contents change			
4	The functions RUP and CLSTK are obtained by and (or you could assign these functions as well)		XEO RUP XEO CLSTK	
	*To assign a function, say FCN, to a key, say the 📧 key,		(ASN) (ALPHA) FCN (ALPHA) (7)	

#### Example 1:

Evaluate the expression

$$\frac{(2 + b) b}{8 - b}$$

for b = 3

# **Keystrokes:**

Function	Display	
XEQ ALPHA CLSTK ALPHA	X:0 Y:0 Z:0 T:0	
2	X:2 Y:0 Z:0 T:0	
ENTER+	X:2 Y:2 Z:0 T:0	

10 RPN Primer	
3	X:3 Y:2 Z:0 T:0
+	X:5 Y:0 Z:0 T:0
LASTX	X:3 Y:5 Z:0 T:0
×	X:15 Y:0 Z:0 T:0
8	X:8 T:15 Z:0 T:0
LASTX	X:3 Y:8 Z:15 T:0
-	X:5 Y:15 Z:0 T:0
+	X:3 Y:0 Z:0 T:0

# Example 2:

Without disturbing the above results, compute

	$\frac{2+4(9-7)}{6-4}$	
Function	6 – 4 Display	
9 Enter+	X:9 Y:3 Z:0 T:0 X:9 Y:9 Z:3 T:0	After an ENTER+), the stack does not lift when new data is keyed in
7 - 4 x 2 + 6 ENTER+ 4 - +	X:7 Y:9 Z:3 T:0 X:2 Y:3 Z:0 T:0 X:4 Y:2 Z:3 T:0 X:8 Y:3 Z:0 T:0 X:2 Y:8 Z:3 T:0 X:10 Y:3 Z:0 T:0 X:6 Y:10 Z:3 T:0 X:6 Y:6 Z:10 T:3 X:4 Y:6 Z:10 T:3 X:2 Y:10 Z:3 T:3 X:5 Y:3 Z:3 T:3	Notice that the answer remaining from Example 1 did not cause a difficulty in Example 2

#### Example 3:

Convert the complex number 3 + 4i to polar form.

 4
 X:4 Y:5 Z:3 T:3

 ENTER•
 X:4 Y:4 Z:5 T:3

 3
 X:3 Y:4 Z:5 T:3

 R-P
 5

 STACK
 X:5 Y:53 Z:5 T:3

Remember that STACK is assigned to **R/S** 

#### **Programming Highlight**

What is especially useful in this program is the display routine STACK. You might like to keep it handy to view the entire stack from time to time as you solve your own problems.

		<b>FO F</b> COC <b>OF</b>	
01+LBL "CLS TK"		50 FS?C 05 51 CLX	
02 CLST	Clear stack.	52 0	Inputa 0.
03 GTO 14		53 GTO 14	
04+LBL "1" 05 FS?C 05	If lift disabled clear x	54♦LBL 13 55 CF 05	Enable stack lift.
06 CLX	first	56+LBL 14	
07 1	Input a 1.	57♦LBL "STA	
08 GTO 14 09◆LBL "2"		CK" 58 "X:"	
09+LBL "2" 10 FS?C 05	See note	59 ARCL X	Display stack.
11 CLX		60 "⊢ Y:"	
12 2	Input a 2.	61 ARCL Y	
13 GTO 14 14◆LBL "3"		62 "H Z:" 63 ARCL Z	
15 FS?C 05		64 "⊢ T:"	
16 CLX		65 ARCL T	
17 3 18 GTO 14	Input a 3.	66 AVIEW 67 RTN	
19 GTO 14 19 CBL "4"		68♦LBL "E↑"	
20 FS?C 05		69 SF 05	Disable stack lift.
21 CLX	Input o 4	70 ENTER↑ 71 GTO 14	
22 4 23 GTO 14	Input a 4.	72+LBL "RDW	
24+LBL "5"		N "	
25 FS?C 05		73 RDN 74 GTO 13	Roll down.
26 CLX 27 5	Input a 5.	74 GTO 13 75♦LBL "SWA	
28 GTO 14		P	
29+LBL "6"		76 X<>Y	Swap x and y.
30 FS?C 05 31 CLX		77 GTO 14 78♦LBL "RUP	
32 6	Input a 6.	"	
33 GTO 14		79 R1	Roll up.
34♦LBL "7" 35 FS?C 05		80 GTO 13 81◆LBL "PL"	
36 CLX		82 +	Plus.
37 7	Input a 7.	83 GTO 13	
38 GTO 14 39♦LBL "8"		84♦LBL "MI" 85 -	Minus.
39€LBL ~8~ 40 FS?C 05		86 GTO 13	WILLUS.
41 CLX		87♦LBL "MU"	h de aldéma la c
42 8 43 GTO 14	Input an 8.	88 * 89 GTO 13	Multiply.
43 GTO 14 44+LBL "9"		90♦LBL "DI"	
45 FS?C 05		91 /	Divide.
46 CLX 47 9	Input a 9.	92 GTO 13 93♦LBL "CLR	
47 9 48 GTO 14	input a 9.	" "	
49♦LBL "0"		94 SF 05	

R00 Storage

95 CLX 96 GTO 14 97+LBL "CHS	Disable stack lift and clear x.		
N" 98 CHS 99 GTO 14	Change sign.		
100+LBL "ST" 101 STO 00 102 GTO 14	Store.		
103+LBL "RC" 104 FS?C 05 105 CLX 106 RCL 00 107 GTO 14 108+LBL "LST	If lift disabled clear x first. Recall.		
X" 109 FS?C 05 110 CLX 111 LASTX 112 GTO 14			
112 610 14	This step need not be keyed in.		
Important Status Size = 001 Fix 0			
Flags used F05 Set = Stack lift disable F29 Clear for no radix point			
	1	L	

Note: You will find it convenient to assign FS?C to some key, for example **ASN ALPHA** FS?C **ALPHA IN** assigns FC?C to the **IN** key. You can then press **IN** once to get FS?C\_\_\_\_ in the display and a second time to create FS?C 05. Remember that you must be in USER mode or you will get two LN's instead.

# **CALENDAR FUNCTIONS**

This program provides an interchangeable solution of dates and days between dates. Given two dates, the program can determine the number of days between them, or it can compute a second date from a first one and a number of days. Dates are input in the form mm.ddyyyy. They are output as MONTH dd,yyyy.

Another feature of this program is that it can convert a date to its day of the week, displaying the result with the correct day name.

This program is valid from March 1, 1900 to February 28, 2100. The program does not check input data. Thus, if an improper format or an invalid date (i.e., February 30) is keyed in, erroneous answers will result.

				SIZE: 010
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status, key in the program and select USER mode DAY OF THE WEEK			
2a	Input date and calculate day	DATE*	E	Day of Week
3a	Repeat step 2a for a new date DAYS BETWEEN DATES			
2b	Input two of the following: First date Second date Days between dates	D 1* D 2* D	A B C	Date 1* Date 2* D
3b	Calculate one of the following: First date Second date Days between dates		A B C	Date 1* Date 2* D
4	Repeat step 2b for new data (values which do not change need not be re-entered)			
	* Dates are input in the form mm.ddyyyy; they are output in the form MONTH dd,yyyy.			

#### Example 1:

On what day of the week was February 19, 1946?

#### **Keystrokes:**

Display: TUESDAY

2.191946**E** 

#### Example 2:

What date is 10,000 days after August 4, 1978?

Keystrokes:	Display:
8.041978 1000	0CB DEC 20,2005

#### **Example 3:**

A man born on December 18, 1913, is the father of a boy born on February 19, 1946. On what date will the father be twice as many days old as his son?

Keystrokes:	Display:	
12.181913	DEC 18,1913	
2.191946 <b>B</b>	FEB 19,1946	
C	11751	Number of days.
2×CB	APR 23,1978	Twice as many
		days after Date 1.

#### **Programming Highlight**

This program utilizes the "selectable radix point" feature of the HP-41C to format its date display. With a date of the form mm.ddyyyy in the x-register,  $\overline{XEO}$  IND X executes a subroutine which places the three-letter month designation in the alpha-register. The program then multiplies the fractional part of X by 100, clears the decimal point flag, and appends the day and year to the alpha display. Thus an original x-value of 12.251978 yields a display of DEC 25,1978.

**Note:** Because of its length, this program was written using only local labels. If the program pointer should ever point to somewhere else in memory, you can move it back using CAT 1 as described on page 140 of your Owner's Handbook.

01♦LBL A 02 RCL 04 03 RCL 01 04 - 05 3	Calculate $\Delta$ days and put control 3 in display.	52 - 53 - 54 RCL 07 55 14 56 /	
06 GTO 20 07+LBL B 08 RCL 03 09 RCL 01 10 +	Calculate $\Delta$ days and put control 4 in display.	57 XEO 22 58 RCL 09 59 1 E6 60 / 61 +	
11 4 12◆LBL 20 13 STO 02 14 RDN	Store control code.	62 GTO 25 63♦LBL 21 64 RDN 65 FC? 06	Break date input into the individual com- ponents of mm,dd, yyyy.
15 365.25 16 STO 05	Store constants.	66 STO IND 02	
17 30.6001		67 ENTER1	
18 STO 06 19 RDN 20 RDN 21 FS?C 22	Return $\Delta$ days to display.	68 INT 69 STO 07 70 - 71 1 E2	
22 GTO 21 23 STO IND 02 24 122.1	Store $\Delta$ days according to control code.	72 * 73 ENTER↑ 74 INT 75 STO 08	
24 122.1 25 - 26 RCL 05 27 / 28 INT 29 STO 09 30 RCL 05 31 * 33 RCL IND 02 34 - 35 CHS 36 STO 00 37 RCL 06 38 / 39 INT 40 STO 07 41 RCL 00 42 X<>Y 43 RCL 06 44 * 45 INT 46 - 47 STO 08 44 RCL 07 49 1 50 RCL 08 51 %	Calculate day of month.	75 STO 08 76 - 77 1 E4 78 * 79 STO 09 80 RCL 07 81 1 82 + 83 ENTER1 84 1/X 85 .7 86 * 87 CHS 88 XE0 22 89 RCL 06 90 * 91 INT 92 RCL 09 93 RCL 05 94 * 95 INT 96 + 97 RCL 08 98 + 97 RCL 08 98 + 99 X<> IND 02 100 FS?C 06 101 RTN 102+LBL 25	Compute day number.
R00 = Scratch $R01 = \Delta days$ R02 = Pointer R03 = Day #1 R04 = Day #2		R05 = 365.25 R06 = 30.600 R07 = m R08 = d R09 = y	

X 105 FRC 106 1 E2 107 * 108 CF 28 109 FIX 4 110 ARCL X 111 RDN 112 AVIEW 113 SF 28 114 RTN 115 LBL 22 116 INT 115 LBL 22 116 INT 117 ST+ 09 118 12 119 * 120 - 121 RTN 122 LBL C 123 CF 29 124 FIX 0 125 STO 01 126 FS?C 22 127 RTN 128 RCL 03 130 - 131 STO 01 132 RTN 133 LBL E 134 SF 06 135 SF 22 136 RCL 05 137 S 138 XEQ 20 139 RCL IND 02 140 7 141 MOD 142 13 143 + 144 RTN 145 AVIEW 145 AVIEW 145 AVIEW 146 RTN 147 LBL 13 148 "FRIDAY" 150 LBL 14 151 "SATURDA Y" 152 RTN	Compute day of week.	155 RTN 156 + LBL 16 157 * MONDAY" 158 RTN 159 + LBL 17 160 * TUESDAY " 161 RTN 162 + LBL 18 163 * WEDNESD AY" 164 RTN 165 + LBL 19 166 * THURSDA Y" 167 RTN 168 + LBL 01 169 * JAN 170 RTN 170 RTN 170 RTN 177 + LBL 02 172 * FEB 173 RTN 176 RTN 177 + LBL 03 175 * MAR 177 * LBL 03 175 * MAR 176 RTN 177 * LBL 04 178 RTN 180 + LBL 05 181 * MAY 182 RTN 183 * LBL 05 181 * MAY 182 RTN 183 * LBL 05 181 * MAY 182 RTN 185 RTN 186 + LBL 07 187 * JUL 188 RTN 189 + LBL 08 190 RTN 191 RTN 192 * LBL 10 193 * SEP 194 RTN 195 * LBL 11 196 * NOY 200 RTN 201 * LBL 12 202 * DEC * 100	
		Important Status Size = 010 Fix 4 Flags used F06 F22 F28 F29	

# WORD GUESSING GAME

This program is a version of the word game "hangman." The first player makes up a six-character word and gives it to the calculator. The second player guesses various letters until he has completed the word. After each guess, the calculator displays all correctly guessed characters in their appropriate places. When the entire word has been guessed, the number of guesses is displayed.

				SIZE: 019
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program.			
2	Begin running the program		XEQ WORDS	KEY IN WORD
3	First player: Key in your word	any of six characters	R/S	LETTER?
4	Second player: Guess a character	any character	R/S	word so far LETTER?
5	Repeat step 4 to guess more characters. When word is complete, you will see DONE, WORD IS <word>, and YOU TOOK nn GUESSES.</word>			

#### **Example:**

Hide "HP-41C" and then guess it.

Keystrokes:	Display:	
XEQ ALPHA WORDS ALPHA	KEY IN WORD	
HP-41C R/S	LETTER?	(Notice that the
		program stops in
		ALPHA mode.)
A R/S		
	LETTER?	
P <b>R/S</b>	P	
	LETTER?	
CR/S	PC	
	LETTER?	
HR/S	HP C	
	LETTER?	
📕 4 R/S	HP 4 C	
	LETTER?	

🛑 1 (R/S)	HP 41C
	LETTER?
🛑 — R/S	DONE
	WORD IS < HP-41C>
	YOU TOOK 7 GUESSES

#### **Programming Highlight**

Two special routines were used while developing this program: SPEL and DESPEL. Their function was to build up a word from a collection of letters and to take apart a word into its component letters. Only DESPEL remains in the final program because the job performed by SPEL was already done by the letter-comparison portion of the program.

A code must be passed through the x-register to SPEL and DESPEL. This code tells SPEL where to find its letters, DESPEL, where to put its letters. The code is of the form

fl.0ll for SPEL or ll.0ff for DESPEL

where

fl = register for first letter ll = register for last letter

ff = fl - 1

SPEL and DESPEL or other similar routines may be used to encode and decode many types of strings. A similar routine was used in the hexadecimal conversion program (page 28).

01+LBL "SPEAssumes a cleared02 STO 07ALPHA register.03+LBL 08Store the counter fl.0ll.04 ARCL INDBuild the word.0705 ISG 0706 GTO 08If not last letter,07 RTNthen repeat loop.	01+LBL "DES PEL" 02 STO 07 03 ASTO 00 04+LBL 07 05 " " 06 ARCL 00 07 ASTO 00 08 ASHF 09 ASTO IND 07 10 DSE 07 11 GTO 07 12 RTN	Store the counter <i>ll.Off.</i> Save the word. Save all but the last letter. Save the last letter. If not all letters, then repeat loop.
--	---	--

01+LBL "WOR DS" 02 "KEY IN WORD" 03 AON		43 GTO 00 44 " " 45 ASTO X 46+LBL 00 47 CLA	Then display i. Else display blank.
04 PROMPT 05 ASTO 08 06 6 07 XEQ "DES PEL"	Store secret word. Place letters in R01 to to R06	48 ARCL 09 49 ARCL X 50 ASTO 09 51 AVIEW 52 10	Add a letter to the display.
08 .9 09 STO 17 10 " " 11 ASTO 09 12 16.01	6 spaces.	53 RCL 18 54 + 55 CLA 56 ARCL Y 57 ASTO IND	
13 XEQ "DES PEL" 14+LBL "LTT R"	Place blanks in R11 to R16.	X 58 ISG 18 59 GTO 06 60 CLA	Repeat loop six times.
15 CLA 16 ASTO 09 17 "LETTER? "	Ask player for letter.	61 ARCL 08 62 ASTO Y 63 CLA 64 ARCL 09	
18 AON 19 PROMPT 20 ASTO 10 21 ISG 17 22 1.006 23 STO 18	Save letter. Count # letters. Initialize counter.	65 ASTO X 66 X=Y? 67 GTO 00 68 PSE 69 PSE 70 GTO "LTT	If words are same, then done. Else ask for another guess.
24+LBL 06 25 " " 26 ASTO Y 27 RCL 18 28 10 29 +	Begin loop 6.	R" 71◆LBL 00 72 "DONE" 73 AVIEW 74 "WORD IS <"	
30 CLA 31 ARCL IND X 32 RDN 33 ASTO X 34 X≠Y?	If position already has letter, then display it.	75 ARCL 09 76 "H>" 77 AVIEW 78 PSE 79 PSE 80 RCL 17	Display word.
35 GTO 00 36 CLA 37 ARCL 10 38 ASTO Y 39 CLA 40 ARCL IND		81 INT 82 "YOU TOO K " 83 ARCL X 84 "H GUESS ES"	
18 41 ASTO X 42 X=Y?	If guess is correct	85 AVIEW 86 RTN 87◆LBL "DES PEL"	Display #guesses.
R00 = Temporary R01 = 1st letter, SW		R07 = Counter R08 = Secret word,	
$\begin{array}{l} R02 = \ 2^{nd} \ letter, \ SW \\ R03 = \ 3^{rd} \ letter, \ SW \\ R04 = \ 4^{th} \ letter, \ SW \\ R05 = \ 5^{th} \ letter, \ SW \\ R06 = \ 6^{th} \ letter, \ SW \end{array}$		R09 = Player's word R10 = Current letter R11 = 1 <sup>st</sup> letter, PW R12 = 2 <sup>nd</sup> letter, PW R13 = 3 <sup>rd</sup> letter, PW	1

	Subrouting to constant	
88 STO 07 89 ASTO 00 90♦LBL 07 91 " " 92 ARCL 00	Subroutine to separate a word into its letters.	
93 ASTO 00 94 ASHF		
95 ASTO IND 07		
96 DSE 07 97 GTO 07		
98 RTN		
Important Status Size = 019 Fix 0 CF 29		
Flags used F29 Clear to suppress decimal point		
R14 = 4 <sup>th</sup> letter, PW	I	
$R15 = 5^{th} \text{ letter, PW}$ $R16 = 6^{th} \text{ letter, PW}$		
R17 = Counter R18 = Counter		

# **ARITHMETIC TEACHER**

This program generates arithmetic practice problems. You may choose the maximum values of the numbers used and whether the problems are addition, subtraction, multiplication or division. After 10 problems have been worked, a percentage score is displayed.

The program can be started by **XEO** (ALPHA) TEACH (ALPHA). The calculator prompts for the largest number to use in the problems. After keying in the maximum number and pressing (R/S), you will see a display of "+, -, \*, /?" with the ALPHA annunciator turned on. Simply press the gold shift key, one of the arithmetic functions, and (R/S) to begin the exercise. ALPHA mode will be turned off automatically.

After each problem is presented, key in your answer and press **R/S**. A correct answer is rewarded with **YES** and a new problem is presented. An incorrect answer elicits an unpleasant sound and the message **NO**, and you are given a second chance. The machine tells you the answer if you make two mistakes on the same problem, then it continues with a new one. If all 10 were worked correctly the first time, a fanfare is played. The program then begins again with the ''+, -, **\***, /?'' question.

The series of problems is determined by a seed (number) between 0 and 1 that is in the X-register when you begin the program. If you want to repeat a particular series of problems, key in the same seed each time. If no seed is keyed in, the program simply uses the number already in the X-register.

				<b>SIZE</b> : 010
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program			
2	Input a seed (0 $\leq$ seed $<$ 1) and begin program.	seed	XEQ TEACH	MAX NUMBER?
3	Input the largest number to use	N	R/S	+, -, *, /?
4	Select addition subtraction multiplication division	+ - *	R/S R/S R/S R/S	$\begin{array}{l} \mbox{equation callouts} \\ (n_1) + (n_2) = ? \\ (n_1) - (n_2) = ? \\ (n_1) \gtrsim (n_2) = ? \\ (n_1) / (n_2) = ? \end{array}$
5	Key in your answer.	answer	R/S	YES or NO
6	After 10 problems have been worked, your score is displayed and you may continue at step 4.			(SCORE)% RIGHT

<b>Reference:</b>	Knuth, The Art of Computer Programming, Addison	Wesley,
	Reading, Mass., 1978.	

#### **Example:**

Using a seed of .021946, do some subtraction problems with arguments up to 14.

Keystrokes:	Display:
.021946	
XEQ ALPHA TEACH ALPHA	MAX NUMBER?
14 <b>R/S</b>	+, -,*, /?
🛑 — R/S	12-5=?
7 <b>R/S</b>	YES
	14-13=?
1 <b>R/S</b>	YES
	13-6=?
8 <b>R/S</b>	NO 13-6=?
7 <b>R/S</b>	YES
	14-11=?
3 <b>R/S</b>	YES
	14-7=?
6 <b>R/S</b>	NO 14-7=?
8 <b>R/S</b>	NO 14-7=7
	13-2=?
11 <b>R/S</b>	YES
	14-13=?
1 <b>R/S</b>	YES
	14-10=?
4 <b>R/S</b>	YES
	12-9=?
3 <b>R/S</b>	YES
	14-10=?
4 <b>R/S</b>	YES
	90% RIGHT
	+, -, *, /?

## **Programming Highlight**

This program uses a combination of the HP-41C's alpha capabilities: indirect subroutine calls together with output labels consisting of user-supplied alpha characters.

At one point in the program, you are asked to key in a + , - , \*, or / symbol depending on which type of problem you wish to work. The program stores this symbol in register 06, generates two numbers, and then executes the subroutine whose name was stored in  $R_{06}$ . That same symbol is then recalled to help create the display showing the problem you must work.

Another interesting portion of this program is the random number generator:

$$r_{n+1} = FRC (9821 \times r_n + .211327)$$

This generator was developed by Don Malm as part of an HP-65 Users' Library program. It passes the spectral test (Knuth, V.2, § 3.4) and, because its parameters satisfy Theorem A (op. cit., p. 15), it generates one million distinct random numbers between 0 and 1 regardless of the value selected for  $r_0$ .

Because the basic random number generator delivers numbers between 0 and 1, it is necessary to do further manipulation of the random numbers to get the integers required for the arithmetic problems. By multiplying the random numbers by an integer N, then taking the integer part, numbers from 0 to N-1 may be generated. This program uses your maximum desired number plus 1 to generate numbers from 0 to your desired maximum.

01+LBL "TEA CH" 02 CF 29 03 FIX 0 04 STO 00 05+LBL A	Initialize.	42 FS?C 00 43 GTO 00 44 SF 00 45 1 46 ST+ 09 47 GTO "TRY	If 2nd time, get new problem else count wrong answer and repeat problem
06 "MAX NUM BER?" 07 PROMPT 08 1 09 + 10 STO 04	Ask for max number.	" 48+LBL 00 49 ARCL 05 50 ARCL 06 51 ARCL 02 52 "⊢="	Display correct answer.
11◆LBL "AGN " 12 0 13 STO 08 14 STO 09 15 10	Label to start over.	53 ARCL 03 54 AVIEW 55 GTO 00 56◆LBL "YES "	
15 10 16 STO 07 17 "+, -, * , /?" 18 AON	Ask which operation.	57 CF 00 58 "YES" 59 AVIEW 60 1 61 ST+ 08	Display "YES". Count right answer.
19 PROMPT 20 AOFF 21 ASTO 06 22+LBL 09	Begin loop.	61 ST+ 08 62•LBL 00 63 DSE 07 64 GTO 09 65 RCL 09	If not all problems, then repeat loop.
23 XEQ "RND M" 24 STO 02 25 XEQ "RND M"	Generate operands.	66 X=0? 67 XEQ "FF" 68 RCL 08 69 .1 70 /	If no wrong answers, then play tune.
26 STO 05 27 RCL 02 28 XEQ IND 06	Generate problem.	71 CLA 72 ARCL X 73 "F% RIGH T"	Display %RIGHT.
29+LBL "TRY " 30 ARCL 05 31 ARCL 06 32 ARCL 02		74 AVIEW 75 PSE 76 PSE 77 GTO "AGN "	Start over.
33 "⊦=?" 34 PROMPT 35 RCL 03 36 X=Y? 37 GTO "YES	Pose problem. If correct, then "YES".	78♦LBL "+" 79 + 80 STO 03 81 LASTX 82 -	Make + problem.
" 38 "NO " 39 AVIEW 40 TONE 2 41 TONE 2		83 LASTX 84 CLA 85 RTN 86♦LBL "-" 87 -	Make – problem.
R00 = random numberR01 = not usedR02 = n2R03 = answerR04 = 1 + max number		R05 = n1 R06 = kind of proble R07 = counter R08 = # right R09 = # wrong	m

88 X<=0? 89 XEQ 00 90 STO 03 91 LASTX 92 + 93 LASTX 94 CLA 95 RTN 96 +LBL 00 97 CHS 98 RCL 02 99 X<> 05 100 X<> 02 101 RDN 102 RTN 103 +LBL "*" 104 * 105 STO 03 106 LASTX 107 / 108 LASTX 107 / 108 LASTX 107 CLA 110 RTN 111 +LBL "/" 112 X<>Y 113 STO 03 114 * 115 STO 05 116 CLA 117 RTN 118 +LBL "RND M" 120 9821 121 * 122 .211327 123 + 124 FRC 125 STO 00 126 SQRT 127 RCL 04 126 SQRT 127 RCL 04 126 SQRT 127 RCL 04 126 SQRT 127 RCL 04 127 RCL 04 128 * 130 RTN 131 +LBL "FF" 132 TONE 8 133 TONE 9 134 XEQ "O" 135 XEQ "O" 136 TONE 8	Make % problem. Make / problem. Random number generator Skew and scale the numbers. Play a tune.	137 TONE 8 138 TONE 7 140 TONE 8 141 TONE 8 141 TONE 7 143 TONE 7 143 TONE 7 144 TONE 9 145 XEQ "O" 146 XEQ "O" 146 XEQ "O" 147 TONE 9 148 TONE 8 149 XEQ "O" 150 TONE 8 151 TONE 7 152 XEQ "O" 153 TONE 7 152 XEQ "O" 153 TONE 7 154 TONE 6 155 RTN 156+LBL "O" 157 X<>Y 158 X<>Y 160 X<>Y 160 X<>Y 161 X<>Y 162 X<>Y 163 RTN Important status: Size = 010 Fix 0 CF 29 Flags used F00 set if wrong answer F 29 clear for no radix point	Subroutine to use up time.

Notes

# HEXADECIMAL-DECIMAL CONVERSION

This program converts numbers between the hexadecimal and decimal number systems. Decimal integers up to 1048575 and hexadecimal integers up to FFFFF can be converted by this program.

				SIZE: 021
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status, key in the program and select USER mode.			
2	Initialize		A	READY
3	To convert a decimal number to hexadecimal key in the number	D	E	н
4	To convert a hexadecimal number to decimal key in the number in ALPHA mode	н	E	D
5	To convert the number back, just press E again		E	H or D
	NOTE: D represents an integer less than 1048576 <sub>10</sub> H represents an integer less than 1000000 <sub>16</sub>			

#### Example 1:

Convert 123<sub>10</sub> to a hexadecimal number

Keystrokes	Display	Comments
Α	READY	Initialize program
123 E	7 B	

#### Example 2:

Convert  $123_{16}$  to a decimal number

Keystrokes	Display	
123 E	291.	

#### **Programming Highlight**

This program uses the digit-entry and alpha-entry flags, flags 22 and 23, to decide whether your number is in base 10 (decimal) or 16(hexadecimal). The first line of the program checks flag 22 to see if digits were input. If so, flag 23 is cleared so that the program can continue with step 6. If flag 22 is not set, flag 23 is tested, causing a branch to LBL04 if alpha data was keyed in. At the end of the program these flags are adjusted so that reconversion can be automatic.

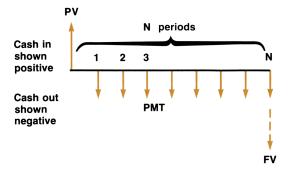
01+LBL E 02 FS?C 22		50 X=Y? 51 GTO 05	If character is null, then repeat loop 5.
02 FS?C 22 03 CF 23 04 FS? 23 05 GTO 04 06 STO 19 07 XEQ 08 08 + 09+LBL 01 10 LASTX 11 ISG 16 12+LBL 00 13 1 E2 14 / 15 INT	If alpha data GTO Label 04. Convert decimal # to coded hex Loop 1 Increment count Dummy label to be skipped.	52+LBL 06 53 RCL IND 18 54 X=Y? 55 GTO 07 56 RDN 57 ISG 18 58+LBL 00 59 GTO 06 60+LBL 07 61 RCL 18 62 RCL 17 63 INT 64 I0↑X	Build coded hex #.
16 X≠0? 17 GTO 01 18 CLA 19 LASTX	While digits remain, repeat loop 1.	65 * 66 ST+ 19 67 ISG 17 68 GTO 05	Count up to 5 hex characters.
20+LBL 03	Begin loop 3	69+LBL 08	Routine to
21 1 E2 22 * 23 ARCL IND X	Build up hex #.	70 16 71 STO 18 72 1 73 STO 17	store constants in proper registers and setup for conversion.
24 FRC 25 DSE 16 26 GTO 03 27 SF 23	Repeat loop 3 until R16 is 0.	74 0 75 STO 16 76 1 E2 77 STO 20	
28 ASTO X 29 BEEP 30 RTN 31◆LBL 04	Display hex #.	78 FS? 23 79 GTO 09 80 RCL 18	
32 ASTO 16 33 .00802 34 STO 17 35 0	Set up to convert hex to decimal.	82 STO 18 83◆LBL 09 84 RCL 19 85◆LBL 10	Begin loop 10. Convert number from
36 STO 19 37◆LBL 05 38 0 39 STO 18 40 " "	Begin loop 5.	86 RCL 20 87 / 88 STO 19 89 FRC 90 RCL 20	one base to the other.
41 ASTO Y 42 ARCL 16 43 ASTO 16 44 ASHF	Strip hex # apart.	91 * 92 RCL 17 93 * 94 ST+ 16	
45 ASTO X 46 X=Y? 47 GTO 08 48 CLA 49 ASTO Y	If character is blank, then jump out of loop.	95 RCL 18 96 ST* 17 97 RCL 19 98 INT 99 X≭0?	If not done,
R00 = "0" R01 = "1" R02 = "2" R03 = "3" R04 = "4"		R06 = "6" R07 = "7" R08 = "8" R09 = "9"	
R04 = ''4'' R05 = ''5''		R10 = "A" R11 = "B"	

	-		
100 GTO 10 101 X $\langle \rangle$ 16 102 CLA 103 FS?C 23 104 BEEF 105 RTN 106 +LBL A 107 CF 22 108 CF 23 109 $0^{\circ}$ 110 ASTO 00 111 $\cdot$ 1. 112 ASTO 01 113 $\cdot$ 2. 114 ASTO 02 115 $\cdot$ 3. 116 ASTO 03 117 $\cdot$ 4. 118 ASTO 04 117 $\cdot$ 4. 120 ASTO 05 121 $\cdot$ 6. 120 ASTO 05 121 $\cdot$ 6. 122 ASTO 06 123 $\cdot$ 7. 124 ASTO 07 125 $\cdot$ 8. 126 ASTO 08 127 $\cdot$ 9. 128 ASTO 09 129 $\cdot$ A. 130 ASTO 10 131 $\cdot$ B. 132 ASTO 11 133 $\cdot$ C. 134 ASTO 12 135 $\cdot$ D. 136 ASTO 13 137 $\cdot$ E. 138 ASTO 14 139 $\cdot$ F. 140 ASTO 15 141 $\cdot$ READY. 142 ASTO X	then repeat loop 10.		
Important status: Size =021 Fix 0 Flags used F22 Digit entry			
F23 Alpha entry R12 = "C" R13 = "D" R14 = "E" R15 = "F" R16 = alpha		R17 = loop counter, dig R18 = base constant, lo R19 = decimal-coded n R20 = base constant	oop counter

Notes

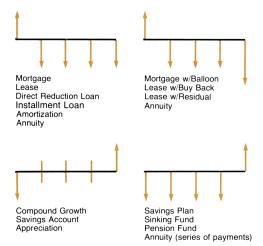
#### FINANCIAL CALCULATIONS

This program converts your HP-41C into a powerful financial calculator. It has the ability to solve for any of the unknowns relating to a cash flow situation as shown below.



- PV = Present Value: the amount loaned, borrowed, invested, etc.
- I = Periodic Interest rate.
- N = Number of periods.
- PMT = Payment amount: the amount paid on a loan or earned on an investment.
- FV = Future Value: the amount remaining, accumulated, saved, etc.

The sketch above shows a standard loan amortization cash flow from the borrower's point of view. From the lender's point of view, PV would be shown negative and the PMT stream would be positive. By changing the signs of PV, PMT, and FV, different cash flow situations may be realized. Cash flow diagrams for the four basic compound interest problems are presented below along with some of the more common terminology.



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The five top-row keys ( $\triangle$  through  $\boxdot$ ) are used to enter or calculate these financial parameters. If you key in any three parameters, pressing one of the other two keys calculates the corresponding value; if you key in any four parameters, pressing the remaining key calculates its corresponding value. Previously input values can be recalled by pressing  $\square CL$  followed by the appropriate key. The key sequence  $\square \square$  may be used to clear all the registers used by this program. When the registers have been cleared in this manner, the message *N*, *I*, *PV*, *PMT*, *FV* is put into the display to remind you of the functions of the keys.

For some combinations of values, this program fails to converge to a solution for periodic interest i. This effect may be avoided by using a different initial value for i.

#### **Reference:**

More information regarding cash-flow analysis may be found in Grant, E.L. and Ireson, W.G., *Principles of Engineering Economy*, Fourth Edition, The Ronald Press Company, New York, 1964.

				SIZE: 010
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in the program, check status, then place the calculator in USER mode.			
2	To clear the finance registers			N, I, PV, PMT, F
3	Store inputs as desired number of periods periodic interest rate, percent present value of investment periodic payment future value of investment	N I PV⁺ PMT⁺ FV⁺	() () () () () () () () () () () () () (	N I PV PMT FV
4	Compute desired output number of periods periodic interest rate present value of investment periodic payment future value of investment		A B C D E	
5	You may return to step 4 to re-compute any of the five values or you may return to step 3 to change any or all of them.			

.01 STO 09 XEQ 06

\*Positive for cash received, negative for cash paid out.

#### Example 1:

A couple purchases a \$50,000 house, borrowing \$40,000 at 8.5% for 30 years less one month. What is their monthly payment?

Keystrokes	Display
A 40000 C	40,000.00
8.5 ENTER+ 12 + B	0.71
30 ENTER+ 12 × 1 - A D	PMT=\$-307.75

#### Example 2:

The couple in example 1 sold their house 18 months later, netting \$25,000. At what interest rate would they have had to invest their original \$10,000 and \$307.75 monthly payments to obtain \$25,000?

Keystrokes	Display	
18 A 25000 E 10000 CHS C B	25,000.00 I = 3.21%	Monthly
12×	38.51	interest rate. Annual rate

## **Programming Tip**

This program demonstrates a technique called an "interchangeable solution." Each of the five variables in the equation can be written in terms of the remaining four. The five top-row keys are used both for storing inputs and computing outputs using the program structure outlined below.

- LBL  $\not\subset$  One of the labels A-J or a-e.
- STO r Store the variable in register r.

FS?C22 Test the digit-entry flag and clear it.

RTN Stop here if this data was just keyed in.

Compute the value of the unknown.

- STO r Store the computed value in register r.
- Bisplay the new value.

#### RTN

This building block may be repeated as many times as necessary depending on the number of variables.

01+LBL A 02 STO 01 03 FS?C 22 04 RTN 05 RCL 04 06 RCL 09 07 / 08 STO 00 09 RCL 05 10 - 11 RCL 03 12 RCL 00 13 + 14 / 15 LN 16 RCL 09 17 LN1+X 18 / 19 STO 01 20 "N=" 21 ARCL X 22 AVIEW 23 RTN 24+LBL B 25 STO 09 29 1 30 + 31 STO 02 26 1 E2 27 / 28 STO 09 29 1 30 + 31 STO 01 32 RCL 02 33 FS?C 22 34 RTN 35 RCL 04 36 X≠0? 37 GTO 01 38 RCL 03 40 / 41 CHS 42 RCL 01 43 1/X 44 STO 09 48 GTO 00	Store N If new data, then stop, else calculate new N. Display new N. Store I and some functions of I. If new data, then stop, else if PMT=0, then compute new I by simple formula.	51 ABS 52 RCL 04 53 RCL 01 54 * 55 RCL 03 56 + 57 ABS 58 - 59 RCL 04 60 RCL 01 61 * 62 RCL 05 63 RCL 03 66 ABS 67 - 68 ENTER 70 ABS 77 RCL 03 66 ABS 67 - 68 ENTER 70 ABS 77 RCL 04 77 RCL 04 78 * 79 RCL 08 80 RCL 08 83 * 84 + CL 08 83 * 84 RCL 08 83 * 84 RCL 08 83 * 84 RCL 08 83 RCL 09 91 RCL 08 83 RCL 09 91 RCL 08 84 RCL 08 87 RCL 08 87 RCL 08 87 RCL 08 87 RCL 08 87 RCL 09 91 RCL 08 87 RCL 09 92 RCL 09 94 RCL 09 95 RCL 04 98 RCL 09 94 RCL 09 95 RCL 04 98 RCL 09 94 RCL 09 95 RCL 04 98 RCL 04 99 RCL 04 90 RCL	Initial guess. Begin loop.
48 GTO 00 49+LBL 01 50 RCL 05	Else compute new I by Newton's method.	99 / 100 * 101 RCL 05	
R00 = used R01 = n R02 = i R03 = PV R04 = PMT R05 = FV	1	R06 = used R07 = 1 + i/100 R08 = used R09 = i/100	

102 RCL 06 103 * 104 - 105 $/$ 106 ST- 09 107 ABS 108 1 E-7 109 X(=Y? 110 GTO 06 111 RCL 09 112 LBL 00 113 1 E2 114 * 115 STO 02 116 "I=" 117 ARCL X 118 $+ \frac{1}{2}$ 119 AVIEW 120 RTN 121 LBL C 122 STO 03 123 FS?C 22 124 RTN 125 KCL 04 126 XEQ 08 127 * 129 RCL 08 127 * 133 STO 03 123 FS?C 22 124 RTN 126 XEQ 08 127 * 138 ACL 05 130 * 131 + 132 CHS 133 STO 04 137 RTN 138 ARCL X 136 AVIEW 137 STO 04 139 STO 04 140 FS?C 22 141 RTN 139 STO 04 140 FS?C 22 141 RTN 142 XEQ 08 143 I/X 144 RCL 03 145 RCL 05 146 RCL 08 147 * 149 * 150 CHS 151 STO 04 152 "PMT=\$*" 153 ARCL X	If I not small, then repeat loop. Display new I. Store PV. If new data, then stop, else compute new PV. Display new PV. Store PMT. If new value, then stop, else compute new PMT.	154 AVIEW 155 RTN 156 LBL E 157 STO 05 158 FS?C 22 159 RTN 160 XEQ 08 161 RCL 04 162 * 163 RCL 03 164 + 165 RCL 08 166 / 167 CHS 168 STO 05 169 "FV=\$" 170 ARCL X 171 AVIEW 172 RTN 173 LBL 08 174 1 175 XEQ 09 176 RCL 01 177 CHS 178 Y*X 179 STO 08 180 - 181 RCL 09 182 / 183 RTN 184 LBL 09 185 RCL 09 187 + 188 STO 07 189 RTN 190 LBL a 191 CLX 192 STO 04 193 STO 05 193 STO 04 196 STO 05 197 STO 09 198 "N, I, P V, PMT,F" 200 AVIEW 201 RTN	Store FV. If new data, then stop, else compute new FV. Subroutine to compute $\left(1 + \frac{i}{100}\right)^{-n}$ $\frac{1 - \left(1 + \frac{i}{100}\right)^{-n}}{i/100}$ Subroutine to compute 1 + i/100
		Important status Size = 010 Fix 2 Flags used	
		F22 Digit entry	

Notes

### **ROOT FINDER**

A root finder is used to find values of an independent variable, x, which cause some function f(x) of that variable to be equal to zero. These values are called the zeros of the function f(x), or the roots of the equation f(x) = 0. For example, in the equation

$$f(x) = 2x - 6$$

x = 3 is a root, because

$$f(3) = 2 \times 3 - 6 = 0$$

There are many techniques that can be employed to locate the roots of an equation. Usually root-finding algorithms (procedures) begin with an initial guess and then iterate, making better and better guesses until an acceptable solution is reached. Some algorithms fail to yield an answer (converge), iterating forever. Others, even though guaranteed to converge, require a long time.

The algorithm implemented in this program will always find a root when given initial guesses straddling an odd number of roots. If the guesses do not straddle a root properly, new ones must be chosen. Thus, the price of rapid, guaranteed convergence is that you must know certain information about your function before using this program.

Before running the root finder, it is necessary to program the function whose zeros you wish to find. This is done by pressing **GTO** • • and keying in your program. The sequence **XEO** ROOT then begins the root finding program. It requests you to key in the name you used for your function and then prompts for the two initial guesses. If both guesses yield function values on the same side of the x-axis, the message "**F1**\***F2**>**0**" appears briefly, and you will be prompted for new guesses.

The program needs registers 01 through 07 for its own use, so register 00 and as many as are available above register 07 may be used when evaluating your function. The answer is labeled and displayed when the value of the function is less than  $10^{-8}$ . A closer tolerance can be obtained simply by keying in a different value when the program is entered.

This program will calculate the closest obtainable approximations to a root, but may continue to iterate when the magnitude of the function evaluated at these approximations exceeds the tolerance. You can check the progress of the solution by inspecting the current guesses in registers 1 and 2 using the VIEW function. You may find it convenient to assign VIEW to some key.

**References:** The Illinois algorithm used here is described in M. Dowell & P. Jarratt, "A modified regula falsi method for computing the root of an equation", *BIT* 11 (1971), pp. 168-174.

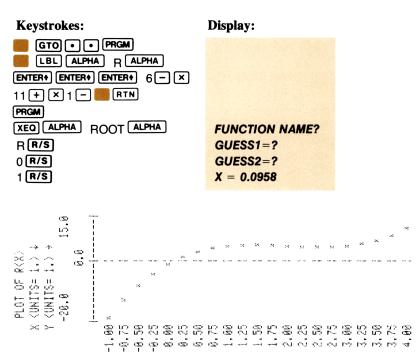
A similar algorithm with slightly faster convergence was developed by the same two authors: M. Dowell & P. Jarratt, "The Pegasas method for computing the root of an equation," *BIT* 12 (1972), pp. 503-508.

Root Finder 39

				SIZE: 008
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program.			
2	Key in your function, giving it a global name (i.e., not A-J, a-e, or 00-99).			
3	Begin executing this program		XEO ROOT	FUNCTION NAME?
4	Key in the name of your function	Name	R/S	GUESS1=?
5	Key in the first guess	X1	R/S	GUESS2=?
6	Key in the second guess and either a root will appear or, the program will return to step 5	X2	R/S	X=(R00T) F1≭F2>0

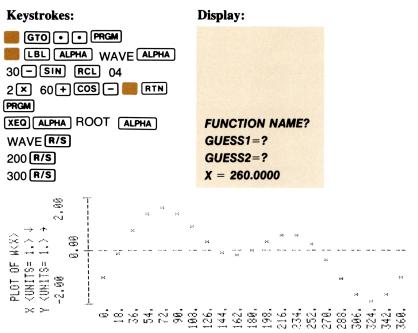
### **Example 1:**

Find a value of x such that  $R(x) = x^3 - 6x^2 + 11x - 1 = 0$ . Note that a sketch of the function indicates a root between 0 and 1.



# **Example 2:**

Find the root of W(x) = sin(x - 30) - cos(2x + 60) which is between 200 and 300 degrees.



# **Programming Highlight**

The root finder program asks you to key in the name of your function. It stores that name and then executes that function indirectly as needed. Note that the function AON is executed before PROMPT so that the HP-41C will stop in ALPHA mode. The function AOFF must be executed before the next PROMPT, however, or ALPHA mode will still be on. AON and AOFF are useful for controlling the mode in which the calculator stops as a further reminder of what sort of data you should provide.

With the name of your function in register 3, the program can execute it any time with XEQ IND 03. Thus, a program which might have required modification for each function you could have wished to use, requires only the names of those functions.

FUNCTION NAME?	
AON	
PROMPT	Display the message, stopping with ALPHA mode on.
ASTO 03	The name is stored in R3.
• •	
AOFF	Turn off ALPHA.
• •	
XEQ IND 93	Execute the program whose name is in R3.

01+LBL "ROC		44 1 E-8	Tolerance value.
T"		45 X>Y?	f(x)  < 1E - 8
02 "FUNCTIO N NAME?"	Ask user for the name	46 GTO 04 47 RCL 07	then done.
03 AON	of the function.	48 RCL 06	
04 PROMPT		49 *	Select new guesses per
05 AOFF		50 X>0?	requirements of Illinois
06 ASTO 03		51 GTO 01	algorithm.
07+LBL A		52 RCL 02	
08 "GUESS1= ?"		53 STO 01 54 RCL 06	
09 PROMPT		54 RCL 06 55 STO 05	
10 STO 01	Store guesses.	56+LBL 02	
11 "GUESS2=	3	57 RCL 04	
?"		58 STO 02	
12 PROMPT		59 RCL 07	
13 STO 02 14 RCL 01		60 STO 06 61 GTO 00	
15 STO 04		62+LBL 01	
16 XEQ IND		63 2	
03		64 STZ 05	
17 STO 05		65 GTO 02	Dura
18 RCL 02 19 STO 04		66♦LBL 04 47 "Y="	Done.
20 XEQ IND		67 "X=" 68 ARCL 04	Display answer.
03		69 PROMPT	Diopidy diferrent
21 STO 06		70♦LBL 05	
22 RCL 05		71 "F1*F2>0	
23 * 24 X>0?			Error message.
25 GTO 05		72 AVIEW 73 PSE	Entri message.
26+LBL 00	Begin loop.	74 GTO A	Return to input
27 RCL 02	5 1	75 .END.	
28 RCL 02			
29 RCL 01 30 -			
30 - 31 RCL 06		Important status:	
32 RCL 05		Size = 008 DEG	
33 -			
34 /		Fix 4	
35 RCL 06 36 *			
37 -			
38 STO 04	New x.		
39 XEQ IND			
03			
40 STO 07 41 X=0?	If $f(x)=0$ then done.		
42 GTO 04			
43 ABS			
R00 = unused			
R01 = X1			
R02 = X2			
R03 = Name			
R04 = X			
R05 = f(X1)			
R06 = f(X2)			
R07 = f(X3)			

# **CURVE FITTING**

For a set of data points  $(x_i, y_i)$ , i = 1, 2, ..., n, this program can be used to fit the data to any of the following curves:

- 1. Straight line (linear regression): y = a + bx.
- 2. Exponential curve:  $y = ae^{bx}$  (a > 0),
- 3. Logarithmic curve:  $y = a + b \ln x$ ,
- 4. Power curve:  $y = ax^b$  (a > 0).

The regression coefficients a and b are found by solving the following equivalent system of linear equations.

$$An + B\Sigma X_i = \Sigma Y_i$$

$$A\Sigma X_i + B\Sigma X_i^2 = \Sigma Y_i X_i$$

The relations of the variables are defined by the following:

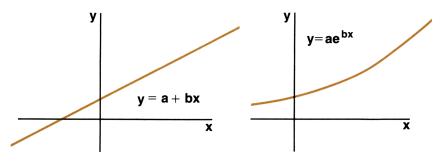
Regression	Α	В	$\mathbf{X_i}$	Yi
Linear	а	b	$\mathbf{x_i}$	Уi
Exponential	ln a	b	xi	lny <sub>i</sub>
Logarithmic	а	b	lnx <sub>i</sub>	y <sub>i</sub>
Power	ln a	b	lnx <sub>i</sub>	lny <sub>i</sub>

The coefficient of determination is:

$$R^{2} = \frac{A\Sigma Y_{i} + b\Sigma X_{i} Y_{i} - \frac{1}{n} (\Sigma Y_{i})^{2}}{\Sigma (Y_{i}^{2}) - \frac{1}{n} (\Sigma Y_{i})^{2}}$$

### **Linear Regression**

**Exponential Curve Fit** 



# Power Curve Fit Logarithmic Curve Fit y $y=ax^b$ y $y=a+b \ln x$ x

# **Remarks:**

- 1. The program applies the least square method, either to the original equations (straight line and logarithmic curve) or to the transformed equations (exponential curve and power curve).
- 2. Negative and zero values of  $x_i$  will cause a calculator error for logarithmic curve fits. Negative and zero values of  $y_i$  will cause a machine error for exponential curve fits. For power curve fits both  $x_i$  and  $y_i$  must be positive, non-zero values.
- 3. As the differences between x and/or y values become small, the accuracy of the regression coefficients will decrease.

				SIZE: 016
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program			
2	Initialize the program for STRAIGHT LINE or for EXPONENTIAL CURVE or for LOGARITHMIC CURVE or for POWER CURVE		xeo LIN xeo EXP xeo LOG xeo POW	LIN EXP LOG POW
3	Repeat step 3 and 4 for $i=1,2,,$ n input: $x_i$ $y_i$	Xi Vi	ENTER+)	(i)
4	If you made a mistake in inputting $x_k$ and $y_k$ , then correct by $\rightarrow$	Х <sub>к</sub> Ук	ENTER+) C	(k-1)
5	Calculate R <sup>2</sup> and regression coefficients a and b		E R/S R/S	R2=(R <sup>2</sup> ) a=(a) b=(b)

STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
6	Calculate estimated y from regression, input x	x	R/S)	Y.=(ŷ)
7	Repeat step 6 for different x's			
8	Repeat step 5 if you want the results again			
9	To use the same program for another set of data, initialize the program by $\rightarrow$ then go to step 3			LIN or EXP or LOG or POW
10	To use another program, go to step 2			

# Example 1:

Fit a straight line to the following set of data and compute  $\hat{y}$  for x = 37 and x = 35.

	40.5					
yi	104.5	102	100	97.5	95.5	94

# Keystrokes:

# **Display:**

XEQ ALPHA LIN ALPHA	LIN	
40.5 ENTER+ 104.5 A	1.00	
38.6 ENTER+ 102 A	2.00	
37.9 ENTER+ 100 A	3.00	
36.2 ENTER+ 97.5 A	4.00	
35.2 ENTER+ 95.5 A	5.00	Oops!
35.2 ENTER+ 95.5 C	4.00	Correct error.
35.1 ENTER+ 95.5 A	5.00	Use proper values.
34.6 ENTER+ 94 A	6.00	
E	R2 = 0.99	
R/S	a = 33.53	
R/S	b = 1.76	
37 <b>R/S</b>	Y. = 98.65	
35 <b>R/S</b>	Y. = 95.13	

# Example 2:

Fit an exponential curve to the following set of data and compute  $\hat{y}$  for x = 1.5 and x = 2.

and $x = 2$ .						
_			1.95		3.14	
	y <sub>i</sub> 2.16	1.61	1.16	.85	0.5	
Keystrokes:	•	D	Display	,	•	
XEQ ALPHA EXP ALP	HA		EXP			
.72 ENTER+ 2.16 A			1.00			
1.31 ENTER+ 1.61 A			2.00			
1.95 ENTER+) 1.16 A			3.00			If you don't
2.58 ENTER+ .85 A			4.00			make a mistake
3.15 ENTER+ .05 A			5.00			you can skip
3.15 ENTER+ .05 C			4.00			two steps.
3.14 ENTER+ 0.5 A			5.00			
E			<b>R2</b> =	0.98		
R/S			a=3.	.45		
R/S			b = -	0.58		
1.5 <b>R/S</b>			Y. = 1	.44		
2.0 <b>R/S</b>			Y. = 1	.08		

### Example 3:

Fit a logarithmic curve to the following set of data and compute  $\hat{y}$  for x = 8 and x = 14.5.

and x = 14.5.	1			1			
	Xi	3	4	6	10	12	
	yi	1.5	9.3	23.4	45.8	60.1	
Keystrokes:			I	Display	y:		
		_					
XEQ ALPHA LOG A	lpha	]		LOG			
3 ENTER+ 1.5 A				1.00			
4 ENTER+ 9.3 A				2.00			
6 ENTER+ 23.4 A				3.00			
10 ENTER+ 45.8 A				4.00			
12 ENTER+ 6.01 A				5.00			Another mistake!
12 ENTER+ 6.01 C				4.00			
12 ENTER+ 60.1 A				5.00			
E				<b>R2</b> =	0.98		
R/S				a = -	47.02		
R/S				b = 4	1.39		
8 <b>R/S</b>				<b>Y.</b> = :	39.06		
14.5 <b>R/S</b>				<b>Y.</b> = (	53.67		

# Example 4:

Fit a power curve to the following set of data and compute $\hat{y}$ for $x = 18$ and $x = 22$							
and $x = 23$ . $x_i \mid 10 \mid 12 \mid 15 \mid 17$	20	22	25	27	30	32	35
y <sub>i</sub> 0.95 1.05 1.25 1.4	1 1.73	2.00	2.53	2.98	3.85	4.59	6.02
Keystrokes:	Di	splay			•		
XEQ ALPHA POW ALPHA	P	W					
10 ENTER+ 0.95 A	1	.00					
12 ENTER+ 1.05 A	2	.00					
15 ENTER+ 1.25 A	3	.00					
17 ENTER+ 1.41 A	4	.00					
20 ENTER+ 1.73 A	5	.00					
22 ENTER+ 2.00 A	6	.00					
25 ENTER+ 2.53 A	7	.00					
27 ENTER+ 2.98 A	8	.00					
30 ENTER+ 3.85 A	9	.00					
32 ENTER+ 4.59 A	10	.00					
35 ENTER+) 60.2 A	11	.00					
35 ENTER+ 60.2 C	10	.00			Error	correc	tion again.
35 ENTER+ 6.02 A	11	.00					
E	R	? = 0.9	<del>9</del> 4				
	a	= 0.03	1				
R/S	b	= 1.46	;				
18 <b>R/S</b>	Y.	= 1.7	6				
23 <b>R/S</b>	Y.	= 2.5	2				

# **Programming Highlight**

This program uses a single section of code for most of the calculations it needs to do. Since each of the four types of curve fitting requires the input data to be in a different form, it would seem that a different program should be used for each curve type. Instead, each of the set-up programs, LIN, LOG, EXP, and POW, stores a code in register 00. Then the single function on line 32, XEQ IND 00, takes care of the four different ways of processing the input data by executing the function whose label is stored in register 00.

43 X<>Y 44 RTN R00 = Index R01 = x R02 = y R03 = det R04 = A		93 RCL 05 94 "b" R05 = b R06 = a R07 = used R08 = LIN or EXP o R09 = (Σy) 2/n	r LOG or POW
34 STOP 35+LBL 07 36 LN 37 RTN 38+LBL 08 39 LN 40+LBL 06 41 X<>Y 42 LN	Log. Power and exp.	84 RCL 13 85 RCL 09 86 - 87 / 88 "R2" 89 XEQ 88 90 RCL 06 91 "a" 92 XEQ 88	
28 2- 29 STOP 30+LBL A 31 X<>Y 32 XEQ IND 00 33 2+	Input data.	77 + 78 RCL 12 79 X†2 80 RCL 15 81 / 82 STG 09 83 -	
19 ASTO 08 20 2REG 10 21 CL2 22 BEEP 23 AVIEW 24 STOP 25+LBL C 26 X<>Y 27 XEQ IND 00	Beep, display and set $\Sigma$ registers.	67 RCL 03 68 / 69 STO 05 70+LBL 03 71 RCL 04 72 RCL 12 73 * 74 RCL 05 75 RCL 14 76 *	
13+LBL "POW " 14 8 15 "POW" 16+LBL 13 17 XE0 "INI T" 18 STO 00	Power.	60 XEQ IND 00 61 STO 06 62 RCL 15 63 RCL 14 64 RCL 10 65 RCL 12 66 XEQ 09	
06 6 07 "EXP" 08 GTO 13 09+LBL "LOG" 10 7 11 "LOG" 12 GTO 13	Exponential. Logarithmic.	52 RCL 12 53 RCL 11 54 RCL 10 55 RCL 14 56 XEO 09 57 RCL 03 58 / 59 STO 04	
01+LBL "LIN " 02 5 03 "LIN" 04 GTO 13 05+LBL "EXF "	Linear.	45+LBL E 46 RCL 15 47 RCL 11 48 RCL 10 49 RCL 10 50 XEQ 09 51 STO 03	Calculate A, b and a, b.

95 GT0 01 97+LBL 06 97+LBL 07 100+LBL 07 100+LBL 07 101 RTN 100+LBL 07 101 RTN 101 RTN 102+LBL 09 103 * 103 * 103 * 103 * 103 * 103 * 103 * 104 ST0 07 102+LBL 09 103 * 103 * 104 ST0 07 104 RTN 102+LBL 09 103 * 105 RDN 104 LBL 00 111 * 113 * 114 RCL 27 115 RTN 113 * 114 RCL 27 115 RTN 113 * 114 RCL 27 115 RTN 113 * 114 RCL 27 115 RTN 113 * 115 RTN 114 RCL 27 115 RTN 116 FS7 S5 117 ST0P 118 * 120 RCL 05 120 RDN 120 RDN 120 RDN 120 RDN 120 RDN 121 RCL 05 122 RCL 05 122 RCL 05 122 RCL 05 123 RCL 05 124 RCL 05 125 RCL 05 126 * 127 RCL 05 126 * 127 RCL 06 133 RCL 06 133 RCL 06 133 RCL 06 133 RCL 06 133 RCL 05 135 RCL				
$R12 = \Sigma y$ $R13 = \Sigma y^{2}$ $R14 = \Sigma xy$	96+LBL 06 97+LBL 07 100+LBL 07 100+LBL 07 101 RTN 102+LBL 09 103 * 104 STO 07 105 RDN 106 * 107 RCL 07 108 - 109 RTN 110+LBL 00 111 'Y." 112+LBL 01 113 'H=" 114 ARCL X 115 AVIEW 116 FS? 55 117 STOP 118+LBL 04 119 GTO IND 00 120+LBL 08 121 RCL 05 122 Y†X 123 GTO 09 124+LBL 06 125 RCL 05 126 * 127 E†X 128+LBL 09 129 RCL 06 132 E†X 128 LBL 07 133 LN 134+LBL 05 135 RCL 06 136 * 137 RCL 06 138 + 139 GTO 00 140+LBL 88 141 'H=" 144 RTN R10 = $\Sigma x$	Coefficient of Determination	146 GTO IND 08 147+LBL "INI T" 148 CLRG 149 CF 00 150 CF 01 151 CF 02 152 SF 21 153 SF 27 154 CF 29 155 RTN Important status Size = 016 $\Sigma = 10$ Fix 2 Flags used F00 F01 F02 F21 F27 F29	
	$R11 = \Sigma x^{2}$ $R12 = \Sigma y$ $R13 = \Sigma y^{2}$ $R14 = \Sigma xy$			

Notes

# **VECTOR OPERATIONS**

This program enables you to add, subtract, multiply or divide two vectors. Before executing any of the routines, load the stack with the vector components as shown below.

### Initial Stack Configuration

**Resulting Display** 

 $\mathbf{U} = \mathbf{u} \mathbf{V} = \mathbf{v}$ 

 $T v_1$   $Z u_1$   $Y v_2$   $X u_2$ 

where the two vectors are denoted by:

 $u_1 + iv_1$  and  $u_2 + iv_2$ 

Note that some people prefer the alternate notation of u + vi, u + jv, or ui + vj.

				SIZE: 000
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in the program and choose a convenient display mode. You might wish to assign the routines as shown here CADD + CSUB - CMULT × CDIV +		ASN CADD (+) ASN CSUB (-) ASN CMULT (X) ASN CDIV (+)	
2a	Place the inputs in the operational stack Imaginary part of first vector Real part of first vector	V <sub>1</sub> U <sub>1</sub>	ENTER+) ENTER+)	
2b	Imaginary part of second vector Real part of second vector	V <sub>2</sub> U <sub>2</sub>	ENTER+	
3	Select the desired function Vector addition Vector subtraction Vector multiplication Vector division		CADD CSUB CMULT CDIV	U = (u), V = (v)  U = (u), V = (v)
4	To use this answer as part of another vector calcula- tion, it is not neces- sary to re-input what was just output. Simply continue with subsequent vectors at step 2b.			

# **Example 1**

Add 1 + i3 to 4 + i6.

Keystrokes	Display:	Choose a
FIX 2		convenient display.
6 ENTER+) 4 ENTER+) 3 ENTER+) 1 [XEQ] ALPHA] CADD (ALPHA)	U = 5.00, V = 9.00	Set up the vectors.

# Example 2

Evaluate  $s^2 + 1$  when s = 3 + j2

Keystrokes	Display:	
2 ENTER+ 3 ENTER+		
2 ENTER+) 3 XEQ ALPHA CMULT ALPHA	U = 5.00, V = 12.00	
0 ENTER+) 1 XEQ	0 = 0.00, V = 12.00	Add 1 + j0.
ALPHA CADD ALPHA	U = 6.00, V = 12.00	

# **Programming Highlight**

Many problems require only one number from the user, that is, you need key in only one number before executing the desired function. Vectors, however, are each described by two numbers; and two vectors must be input before the problem can be solved. Many programs can be shortened by judicious use of the stack for input data. The implementation of this program shows how short a program can become when the user is required to be careful with his input.

Notice that if the output section is replaced with LBL "UV" RTN, the four routines can be used as subroutines to any of your programs requiring vector operations. The output values u and  $\nu$  are returned in the X- and Y-registers respectively.

A convenient way to use this program is to assign the various routines to the  $(+, -), (\times)$ , and (+) keys for instant execution of the functions when in USER mode.

01+LBL "CSU B" 02 CHS 03 X<>Y 04 CHS 05 X<>Y 04 CHS 05 X<>Y 06+LBL "CAD D" 07 X<>Y 08 RDN 10 RDN 11 + 12 R† 13 GTO "UV" 14+LBL "CDI V" 15 R-P 16 1/X 17 X<>Y 18 CHS 19 GTO 00 20+LBL "CMU LT" 21 R-P 22 X<>Y 18 CHS 19 GTO 00 20+LBL "CMU LT" 21 R-P 22 X <y 23+LBL 00 24 RDN 25 RDN 26 R-P 27 R† 28 * 29 RDN 30 + 31 R† 32 P-R 33 ARCL X 36 "F,V=" 35 ARCL Y 38 AVIEW 39 RTN 40 -END. Important Status: Size = 000</y 	Subtract. Change sign of second vector, then add. ADD. Divide. Invert second vector, then multiply. Multiply. Display routine.	

Notes

# **BLACKJACK**

This program plays a simple version of the card game blackjack (twenty-one). The calculator deals (without replacement) from a 104-card deck, reshuffling when all but 13 cards have been dealt. The player may bet any amount; if he doesn't place a bet, the value of his previous one will be used.

The player and dealer each receive two cards, one of the dealer's cards being exposed. The player may then either draw additional cards (hit) or not draw (stand). The object of the game is to reach, but not exceed, a score of 21 points, counting 10 for face cards, 1 or 11 for aces, and the face value for the remaining cards. If a player's first two cards count 21, he has *blackjack* and immediately collects  $1\frac{1}{2}$  times his bet unless the dealer also has blackjack.

When hitting, a player who draws a card bringing his score over 21 is said to "bust" or "be busted" and he loses his bet. When the player stands on a score of 21 or less, the dealer must hit his own hand until his score exceeds 16. At that point the higher hand wins and the player's bank is updated. If the player and dealer should have the same score, the bet is a *stand-off* or a *push*.

Options allowed in casino-style blackjack such as splitting pairs, going down for double, and purchasing insurance are not included in this program.

You must have an HP-41C with one additional Memory Module to run this program.

Blackjack 55

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				<b>SIZE:</b> 027
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in program, checks status, and assign DL, HT, and S as desired. A seed ( $0 \le$ seed $< 1$ ) may be placed on $R_{\infty}$ .			
2	Store your initial bank.	bank	STO 21	
3	To shuffle the deck		XEQ SH	SHUFFLING
4	Place your bet	BET	DL	I SHOW c* You have 1 You have 1 2†
5a	Hit, then repeat this step or go to 5b or,		HT	YOU HAVE cards
5b	Stand, and the dealer will show his hand and then hit or stand as appropriate		S	I HAVE cards : :
6	Repeat from step 4 as desired † NOTE: If you get blackjack in step 4, the display will show BLACKJACK, and [S(TAND)] will be executed automatically. * c is any card, cards is a string of cards—the card numbers are linked so a 10 and a 7 will look like 107.			YOUR BANK IS \$ bank

# **Example:**

Shuffle the deck, key in a seed of  $\pi$ , and play Blackjack using a \$2 bet.

# **Keystrokes:**

ASN ALPHA DL ALPHA E+ ASN ALPHA HT ALPHA <sup>1/</sup> x ASN ALPHA S ALPHA T USER XEQ ALPHA SH ALPHA
0 <b>STO</b> 21 π <b>STO</b> 00

2 DL

# Display:

ASN	DL 11
ASN	HT 12
ASN	S 13

# SHUFFLING 104

Only FRC  $(\pi)$  is used.

NOTE: The DL function was assigned to  $\Sigma$ +. Remember, your calculator must be in user mode or you will get  $\Sigma$ +.

	I SHOW 2
	YOU HAVE 107
S	I HAVE 2J
	I HAVE 2JK
	BUST
	YOUR BANK IS \$2
DL	I SHOW 6
	YOU HAVE A5
нт	YOU HAVE A57
НТ	YOU HAVE A575
S	I HAVE 6K
	I HAVE 6K8
	BUST
	YOUR BANK IS \$4

NOTE: The S function was assigned to **F** 

# **Program Highlight**

With the 11 registers left after keying in this program, you can write a program to play blackjack using simple playing and betting schemes. The routine shown checks registers and flags used by the blackjack program to determine whether to hit or stand. If the playing program loses, it doubles its bet, eventually wining. By adding still more memory modules to your HP-41C, more complicated playing strategies may be tried.

Notice that this program requires the data memory size to be increased to 28.

01+LBL "PL" 02 2 03 SF 22 04+LBL 02	Place new bet	18 XEQ "HT" 19 GTO 00 20◆LBL 01 21 FS? 09	lf no blackjack
05 XEQ "DL" 06+LBL 00	Deal	22 XEQ "S" 23 RCL 27	Then stand
07 RCL 24 08 12	check score	24 RCL 21 25 STO 27	Save last bank
09 ENTER† 10 10	Adjustment for Ace	26 - 27 X<0?	If game won,
11 FS? 07 12 CLX 13 -	Clear adjustment	28 GTO "PL" 29 X=0? 30 GTO 02	Place new bet. If game drawn, Use last bet.
13 - 14 X<=Y? 15 GTO 01	lf 12 ≥ score or If blackjack	30 GTO 02 31 2 32 ST* 22	If game lost, Double the bet.
16 FC? 09 17 GTO 01	Then stand Otherwise hit	33 GTO 02 34 END	

01+LBL "CRD " 02 CLA 03 ASTO 19 04 1 05 STO 15 06 RCL 00 07 9821 08 * 09 .211327 10 + 11 FRC 12 STO 00 13 RCL 14 14 * 15 INT 16 1 17 + 18 +LBL 02 19 RCL IND 15 20 X>Y? 21 GTO 03 22 - 23 ISG 15 24+LBL 09 25 GTO 02 26+LBL 03 27 DSE IND 15 28 +LBL 99 29 DSE 14 30 RCL 14 32 X>Y? 33 GTO 04 34 XEQ "SH" 35 ALBL 04 36 RCL 15 37 STO 16 38 10 39 X<=Y? 40 GTO 00 41 X<>Y 42 STO 16 43 1 44 X=Y? 45 GTO A 46 CLA	Routine to get a card. Random number generator. If only 12 cards remain, then shuffle deck.	47 ARCL Y 48 GTO 01 49 bBL 00 50 STO 16 51 CLX 52 10 53 X=Y? 54 GTO "10" 55 1 56 + 57 X=Y? 58 GTO J 59 1 60 + 61 X=Y? 62 GTO "0" 63 "K" 64 GTO 01 65 LBL A 66 "A" 67 CF 07 68 GTO 01 69 LBL "0" 70 "0" 71 GTO 01 72 LBL J 73 "J" 74 GTO 01 75 LBL 01 75 LBL "10" 77 LBL 01 78 ASTO 19 79 RCL 16 80 RTN 81 LBL "SH" 82 TSHUFFLI NG" 83 AVIEW 84 1.013 85 ENTER↑ 86 8 87 LBL 14 88 STO 14 91 104 93 CLD	Store card alpha. Subroutine to reconstruct deck.
R00 = Random numl R01 = Aces R02 = 2's R03 = 3's R04 = 4's	per	R05 = 5's R06 = 6's R07 = 7's R08 = 8's R09 = 9's	

94 CF 00 95 CF 01 96 CF 02 97 CF 03 98 CF 04 99 RTN 100 ◆LBL "DL" 101 CF 09 102 SF 07 103 ABS 104 INT 105 FS?C 22 106 ST0 22 107 RCL 22 108 ST0 20 109 SF 06 110 CLA 111 AST0 26 112 AST0 25 113 XEQ "CRD " 114 RCL 15 115 ST0 17 116 XEQ "CRD" " 117 ST0 23 118 CF 08 119 FS? 07 120 SF 08 121 CLA 122 ARCL 19 123 ARCL 25 124 AST0 25 124 AST0 25 124 AST0 25 124 AST0 25 125 "I SHOW" " 126 ARCL 25 127 AVIEW 128 SF 07 129 0 130 ST0 24 131 XEQ "CRD" "	Blackjack. No ace. Use old bet or store new bet. Get dealer's first card. Get dealer's second card. Save dealer's A-flag. Dealer's hand. Display dealer's up card. No ace. Get player's card. Get player's 2nd card.	137 FS? 07 138 CLX 139 + 140 21 141 X $\neq$ Y? 142 SF 09 143 FS? 09 144 RTN 145 21.5 146 STO 24 147 1.5 148 ST* 20 149 "BLACKJA CK" 150 AVIEW 151 $\bullet$ LBL "S" 152 CF 06 153 FS? 07 154 GTO 05 155 11 156 RCL 24 157 X>Y? 158 GTO 05 159 10 160 ST+ 24 161 $\bullet$ LBL 05 162 CF 07 163 FS? 08 164 SF 07 165 RCL 17 165 RCL 07 173 X $\neq$ Y? 174 GTO 07 175 21.5 176 STO 23 177 HAVE BLACKJAC" 178 "HK"	If no blackjack, then set Flag 9. Blackjack. Go directly to "STAND". Player not busted. If not blackjack, skip to 05. Reinstate Dealer's Ace-flag. Recover Dealer's hole card. Display Dealer's hand. If no dealer ace, skip to LBL 07.
133 XEQ "CRD " 134 XEQ "PH" 135 RCL 24 136 10	Get player's 2nd card. Display player's hand.	178 "⊢K" 179 AVIEW 180 GTO 07 181♦LBL 06	

R10 = 10's

R11 = J's

- R12 = Q's
- R13 = K's
- R14 = # cards left in deck

R15 = counter

R16 = Value of current card

R17 = Dealer's hidden card

R18 = not used

R19 = Current card in ALPHA form

182 XEQ "CRD " 183 XEQ "DH" 1844LBL 07	Dealer hits. Dealer hit or stand? If	227 RCL 24 228 21.5 229 X>Y? 230 RTN 231 "RUST"	Check for bust.
185 FS? 06 186 GT0 09 187 FC? 09 188 GT0 08 189 RCL 23 190 17 191 X<=Y?	player busted, then settle bets. If player blackjack set the black- jack. If dealer's score is above 17, then settle. If no ace, then dealer hits.	231 "BUST" 232 AVIEW 233 GTO Ø5 234◆LBL "DB" 235 "BUST" 236 AVIEW 237 Ø	Dealer bust.
192 GTO 08 193 FS? 07 194 GTO 06		238 RTN 239♦LBL "PH" 240 ST+ 24	Display player's hand.
195 11 196 RCL 23 197 X>Y? 198 GTO 06 199 7 200 Y>Y2	If ace and score is between 7 and 11, then dealer hits.	241 CLA 242 ARCL 26 243 ARCL 19 244 ASTO 26 245 "YOU HAV	
200 X>Y? 201 GTO 06 202 10 203 ST+ 23 204+LBL 08	Add 10 for ace.	246 ARCL 26 247 AVIEW 248 RTN 249◆LBL "DH"	Display dealer's hand.
205 21.5 206 RCL 23 207 X>Y? 208 XEQ "DB" 209 RCL 24	Check for dealer bust.	250 ST+ 23 251 CLA 252 ARCL 25 253 ARCL 19 254 ASTO 25	
210 - 211 X=0? 212 XEQ "P" 213 X>0? 214 SF 06	Check for push. Set bust flag if player loses settle bets.	255 "I HAVE " 256 ARCL 25 257 AVIEW 258 RTN	
215+LBL 09 216 RCL 20 217 FS? 06 218 CHS 219 ST+ 21	lf player loses subtract payoff.	259+LBL "P" 260 "A PUSH" 261 AVIEW 262 ST* 20	Take care of push.
220 "YOUR BA NK IS \$" 221 ARCL 21 222 AVIEW 223 RTN	Display new bank.	Important status Size = 028 Fix 00 CF 29	
224+LBL "HT" 225 XEQ "CRD	Player hits. Get a new card.	Flag 21 Should match Flag 55	
226 XEQ "PH"	Display new hand.		
R20 = Payoff R21 = Player's bank R22 = R23 = Dealer's score R24 = Player's score R25 = Dealer's hand R26 = Player's hand		F09 Set = no blackja F29 Clear to suppres	Ace Clear = dealer Ace ck Clear = blackjack



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