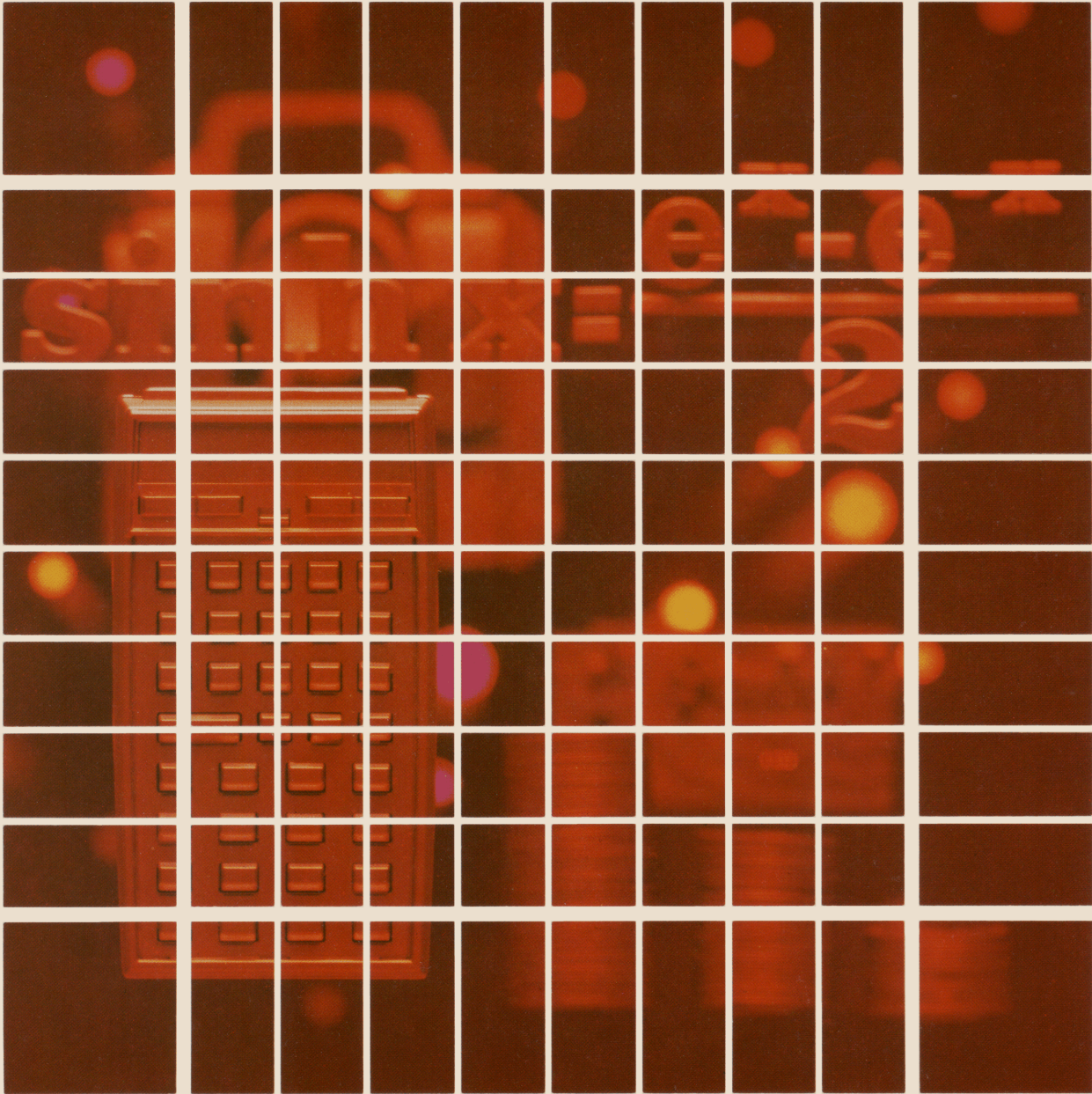


Includes barcode for easy software entry.

HEWLETT-PACKARD

HP-41

USERS' LIBRARY SOLUTIONS  
Chemical Engineering



## **NOTICE**

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## INTRODUCTION

This HP-41C Solutions book was written to help you get the most from your calculator. The programs were chosen to provide useful calculations for many of the common problems encountered.

They will provide you with immediate capabilities in your everyday calculations and you will find them useful as guides to programming techniques for writing your own customized software. The comments on each program listing describe the approach used to reach the solution and help you follow the programmer's logic as you become an expert on your HP calculator.

## KEYING A PROGRAM INTO THE HP-41C

There are several things that you should keep in mind while you are keying in programs from the program listings provided in this book. The output from the HP 82143A printer provides a convenient way of listing and an easily understood method of keying in programs without showing every keystroke. This type of output is what appears in this handbook. Once you understand the procedure for keying programs in from the printed listings, you will find this method simple and fast. Here is the procedure:

- At the end of each program listing is a listing of status information required to properly execute that program. Included is the SIZE allocation required. Before you begin keying in the program, press **XEQ** **ALPHA** **SIZE** **ALPHA** and specify the allocation (three digits; e.g., 10 should be specified as 010).

Also included in the status information is the display format and status of flags important to the program. To ensure proper execution, check to see that the display status of the HP-41C is set as specified and check to see that all applicable flags are set or clear as specified.

- Set the HP-41C to PRGM mode (press the **PRGM** key) and press **■** **GTO** **□** **□** to prepare the calculator for the new program.
- Begin keying in the program. Following is a list of hints that will help you when you key in your programs from the program listings in this handbook.
  - When you see " (quote marks) around a character or group of characters in the program listing, those characters are ALPHA. To key them in, simply press **ALPHA**, key in the characters, then press **ALPHA** again. So "SAMPLE" would be keyed in as **ALPHA** "SAMPLE" **ALPHA**.
  - The diamond in front of each LBL instruction is only a visual aid to help you locate labels in the program listings. When you key in a program, ignore the diamond.
  - The printer indication of divide sign is /. When you see / in the program listing, press **+**.
  - The printer indication of the multiply sign is  $\times$ . When you see  $\times$  in the program listing, press **x**.
  - The  $\vdash$  character in the program listing is an indication of the **APPEND** function. When you see  $\vdash$ , press **■** **APPEND** in ALPHA mode (press **■** and the K key).
  - All operations requiring register addresses accept those addresses in these forms:
    - nn (a two-digit number)
    - IND nn (INDIRECT: **■**, followed by a two-digit number)
    - X, Y, Z, T, or L (a STACK address: **□** followed by X, Y, Z, T, or L)
    - IND X, Y, Z, T or L (INDIRECT stack: **■** **□** followed by X, Y, Z, T, or L)

Indirect addresses are specified by pressing **■** and then the indirect address. Stack addresses are specified by pressing **□** followed by X, Y, Z, T, or L. Indirect stack addresses are specified by pressing **■** **□** and X, Y, Z, T, or L.

### Printer Listing

```

01  $\diamond$ LBL "SAM
PLE"
02 "THIS IS
A "
03  $\vdash$ SAMPLE
"
04 AVIEW
05 6
06 ENTER $\uparrow$ 
07 -2
08 /
09 ABS
10 STO IND
L
11 "R3="
12 ARCL 03
13 AVIEW
14 RTN

```

### Keystrokes

```

 $\diamond$  LBL ALPHA SAMPLE ALPHA
ALPHA THIS IS A ALPHA
ALPHA  $\vdash$  APPEND SAMPLE
 $\vdash$  AVIEW ALPHA
6
ENTER $\uparrow$ 
2 CHS
+
XEQ ALPHA ABS ALPHA
STO  $\square$  L
ALPHA R3=  $\square$  ARCL 03
 $\vdash$  AVIEW
ALPHA
RTN

```

### Display

```

01 LBL $\uparrow$  SAMPLE
02 $\uparrow$  THIS IS A
03 $\uparrow$   $\vdash$  SAMPLE
04 AVIEW
05 6
06 ENTER $\uparrow$ 
07 -2
08 /
09 ABS
10 STO IND L
11 $\uparrow$  R3=
12 ARCL 03
13 AVIEW
14 RTN

```

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	Converts between energy, potential energy and pressure - volume work.	
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4.	HEAT TRANSFER THROUGH COMPOSITE CYLINDERS AND WALLS . . . . .	22
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6.	EQUATIONS OF STATE . . . . .	34
	Uses both ideal gas and Redlich-Kwong equations and provides interchangeable solutions.	
7.	REVERSIBLE POLYTROPIC PROCESS FOR AN IDEAL GAS . . . . .	44
	May be used to solve interchangeably between pressure ratio, volume ratio, temperature ratio, and density ratio.	
8.	CONDUIT FLOW . . . . .	49
	Solves a variety of problems involving viscous conduit flow.	
9.	FLUID TRANSPORT NUMBERS . . . . .	58
	4 programs that solve for the different transport numbers.	
*10.	SINGLE STAGE EQUILIBRIUM FLASH CALCULATION . . . . .	76
	Calculates the composition of liquid and vapor streams from a flash vessel.	
*11.	WEAK ACID/BASE TITRATION CURVE . . . . .	85
	Calculates the pH of weak acid or base solutions with up to 4 dissociation constants.	

\*Requires one additional memory module

## STRAIGHT FIN EFFICIENCY

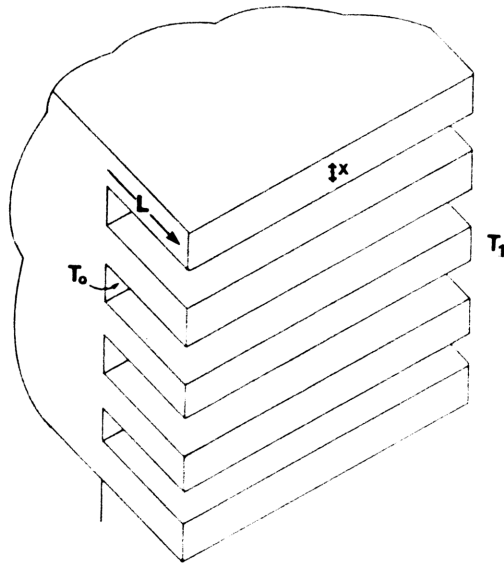
This program evaluates fin efficiency. Given the number of fins per unit of surface length and the temperature difference, the total heat transfer can also be found.

Equations: 
$$\eta_f = \frac{\tanh(y)}{y}$$

$$y = (L + x/2)^{3/2} \sqrt{2h/kxL}$$

$$q = h[(1 - N_{ave}x) + \eta_f N_{ave}(2L + x)] \Delta T$$

$$\Delta T = |T_o - T_1|$$



where  $\eta_f$  is fin efficiency;  
 $L$  is fin length;  
 $x$  is fin thickness;  
 $h$  is the convective coefficient;  
 $k$  is the conductive coefficient;  
 $N_{ave}$  is the average number of fins per unit length of surface area;  
 $q$  is the total heat flux per unit area;  
 $T_o$  is the temperature of the base of the fin;  
 $T_1$  is the fluid temperature.



Remarks:

Dimensional consistency must be maintained.

Example:

The oil pan of a race car is to be cooled by adding aluminum fins ( $k = 133$  Btu/hr - °F - ft). The convective coefficient is about 50 Btu/hr - °F - ft<sup>2</sup>. The fins are to be 0.1 inch thick, 0.5 inches long and average 15 per foot. If  $T_o$  is taken to be 300°F and  $T_1$  is 110°F, what is the total heat transfer? What is the heat transfer without any fins?

Keystrokes:

Display:

[USER]	(set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 008	
[XEQ] [ALPHA] FIN [ALPHA]	H?
50 [R/S]	K?
133 [R/S]	X?
0.1 [ENTER↑] 12 [÷] [R/S]	L?
0.5 [ENTER↑] 12 [÷] [R/S]	NF=0.94
[R/S]	NA?
15 [R/S]	DELTA T?
300 [ENTER↑] 110 [-] [R/S]	Q=20,537.02
[A]	NA?
0 [R/S]	DELTA T?
300 [ENTER↑] 110 [-] [R/S]	Q=9,500.00



# Program Listings

01*LBL "FIN	Initialization	51 +	
02 FIX 2		52 *	
03 DEG		53 1	
04 "H?"		54 X<=Y?	
05 PROMPT		55 0	
06 STO 03		56 /	
07 "K?"		57 "DELTA T	
08 PROMPT		?"	
09 STO 02		58 PROMPT	
10 "X?"		59 RCL 04	
11 PROMPT		60 RCL 01	
12 2		61 +	
13 /		62 ENTER↑	
14 STO 01		63 +	
15 "L?"		64 RCL 06	
16 PROMPT		65 *	
17 STO 04		66 RCL 05	
18 RCL 01		67 *	
19 +		68 RCL 01	
20 SQRT	$\eta_f$	69 ENTER↑	
21 LASTX		70 +	
22 *		71 RCL 06	
23 RCL 03		72 *	
24 RCL 02		73 CHS	
25 /		74 1	
26 RCL 01		75 +	
27 /		76 +	
28 RCL 04		77 *	
29 /		78 RCL 03	
30 SQRT		79 *	
31 *		80 "Q="	
32 STO 07		81*LBL d	
33 E↑X		82 ARCL X	Display
34 ATAN		83 AVIEW	
35 ENTER↑		84 STOP	
36 +		85 RTN	
37 90		86 .END.	
38 -			
39 SIN			
40 RCL 07			
41 /		90	
42 STO 05			
43 "NF="			
44 XEQ d			
45*LBL A			
46 "NA?"	$Q$		
47 PROMPT			
48 STO 06			
49 RCL 01			
50 ENTER↑			
		00	





## STRAIGHT FIN EFFICIENCY

PROGRAM REGISTERS NEEDED: 18

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CHEMICAL ENGINEERING

ROW 1 (1 - 4)



ROW 2 (5 - 13)



ROW 3 (14 - 24)



ROW 4 (25 - 37)



ROW 5 (37 - 44)



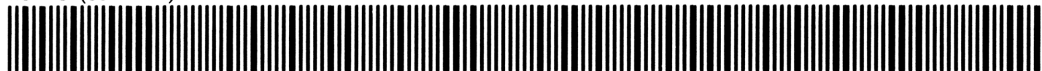
ROW 6 (45 - 53)



ROW 7 (54 - 58)



ROW 8 (59 - 71)



ROW 9 (72 - 81)



ROW 10 (82 - 86)



## CONSERVATION OF ENERGY

This program converts kinetic energy, potential energy and pressure-volume work to energy.

Equation:

$$\frac{V_1^2}{2} + gz_1 + \frac{P_1}{\rho} + \frac{E_1}{\dot{m}} = \frac{V_2^2}{2} + gz_2 + \frac{P_2}{\rho} + \frac{E_2}{\dot{m}}$$

where  $V$  is the fluid velocity;

$z$  is the height above a reference datum;

$P$  is the pressure;

$E$  is an energy term which could represent inputs of work or friction losses (negative value);

$g$  is the acceleration of gravity;

$\rho$  is the fluid density;

$\dot{m}$  is the mass flow rate (assumed to be unity);

subscripts 1 and 2 refer to upstream and downstream values respectively.

Example:

A water tower is 100 feet high. What is the zero flow rate pressure at the base? The density of water is 62.4 lb/ft<sup>3</sup>.

Keystrokes:

Display:

[USER]

(set USER mode)

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] ENG [ALPHA]

DENSITY?

62.4 [R/S]

V?

0 [R/S]

Z?

100 [R/S]

P?

[R/S]

E?

0 [R/S]

[C]

P=43.33



If water is flowing out of the tower at a velocity of 10 ft/sec, what is the static pressure?

Keystrokes:

[XEQ] [ALPHA] ENG [ALPHA]

62.4 [R/S]

10 [CHS] [R/S]

100 [R/S]

[R/S]

0 [R/S]

[C]

Display:

DENSITY?

V?

Z?

P?

E?

P=42.66

# User Instructions

				SIZE: 009
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Load program and set USER mode		[USER]	
2	Begin execution:			
	for English units		[XEQ] ENG	DENSITY?
	for SI units		[XEQ] SI	DENSITY?
3	Input data <sup>†</sup>	$\rho$	[R/S]	V?
		V	[R/S]	Z?
		z	[R/S]	P?
		P	[R/S]	E?
		E	[R/S]	
4	To find: <sup>††</sup>			
	velocity		[A]	V=
	height		[B]	Z=
	pressure		[C]	P=
	energy		[D]	E=
	<sup>†</sup> Downstream values should be input as			
	negatives. However, when an output is			
	called for, the calculator displays the			
	relative value with no regard to upstream			
	or downstream location.			
	<sup>††</sup> "DATA ERROR" will result when the total			
	energy sum stored in register 8 is nega-			
	tive and an attempt is made to calculate			
	velocity.			

# Program Listings

01♦LBL "SI"	SI constants	49 RCL 04	
02 CF 00		50 /	
03 "DENSITY		51 FC? 00	
?"		52 GTO 00	
04 PROMPT		53 RCL 06	
05 STO 04		54 *	
06 CLX		55♦LBL 00	
07 STO 08		56 ST+ 08	
08 9.80665		57 CLX	
09 STO 06		58 "E?"	
10 GTO 00		59 PROMPT	
11♦LBL "ENG		60 ENTER↑	
"	English constants	61 FC? 00	
12 SF 00		62 GTO 00	
13 "DENSITY		63 RCL 05	
?"		64 *	
14 PROMPT		65 RCL 06	
15 STO 04		66 *	
16 CLX		67♦LBL 00	
17 STO 08		68 ST+ 08	
18 778.16		69 STOP	
19 STO 05		70♦LBL A	----- Velocity
20 32.17		71 RCL 08	
21 STO 06		72 2	
22♦LBL 00	Initialization	73 *	
23 CLX		74 SQRT	
24 "V?"		75 "V="	
25 PROMPT		76 GTO d	----- Height
26 ENTER↑		77♦LBL B	
27 ABS		78 RCL 08	
28 *		79 RCL 06	
29 2		80 /	
30 /		81 "Z="	
31 ST+ 08		82 GTO d	----- Pressure
32 CLX		83♦LBL C	
33 "Z?"		84 RCL 08	
34 PROMPT		85 FC? 00	
35 ENTER↑		86 GTO 00	
36 RCL 06		87 RCL 07	
37 *		88 /	
38 ST+ 08		89♦LBL 00	
39 CLX		90 RCL 04	
40 "P?"		91 *	
41 PROMPT		92 "P="	
42 ENTER↑		93 FC? 00	
43 FC? 00		94 GTO d	
44 GTO 00		95 RCL 06	
45 144		96 /	
46 STO 07		97 GTO d	----- Energy
47 *		98♦LBL D	
48♦LBL 00		99 "E="	



	100 RCL 08		51	
	101 FC? 00			
	102 GT0 d			
	103 RCL 05			
	104 /			
	105 RCL 06			
	106 /			
	107 LBL d			
	108 ARCL X			
	109 AVIEW		60	
	110 STOP			
	111 .END.			
20			70	
30			80	
40			90	
50			00	

# REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS			
00		50		SIZE 009	TOT. REG. 038	USER MODE	
				ENG	FIX 2	SCI	ON X OFF
				DEG	RAD	GRAD	
				FLAGS			
05	p 778.16	55		#	INIT S/C	SET INDICATES	CLEAR INDICATES
	g 114			00		ENGLISH	SI
	ΣE						
	temp storage						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION	KEY	FUNCTION	KEY
40		90					
45		95					

## CONSERVATION OF ENERGY

PROGRAM REGISTERS NEEDED: 30

HEWLETT PACKARD  
SOLUTION BOOK:  
CHEMICAL ENGINEERING

ROW 1 (1 - 3)



ROW 2 (3 - 8)



ROW 3 (8 - 12)



ROW 4 (12 - 16)



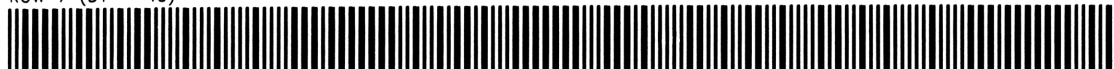
ROW 5 (17 - 20)



ROW 6 (21 - 31)



ROW 7 (31 - 40)



ROW 8 (40 - 47)



ROW 9 (48 - 57)



ROW 10 (58 - 66)



ROW 11 (67 - 75)



ROW 12 (76 - 82)



ROW 13 (82 - 91)



ROW 14 (92 - 97)



ROW 15 (98 - 104)



ROW 16 (105 - 111)



## HYDROCARBON COMBUSTION

Given the atomic composition of a hydrocarbon fuel and the desired amount of excess air, the program calculates the air-fuel ratio on a mass and mole basis. The number of moles of products is also calculated along with the volume percents of sulfur dioxide, carbon dioxide, water vapor, oxygen and nitrogen. Complete combustion is assumed.

Equations:

$$\text{Total combustion air} \quad \text{AIR} = 1 + \frac{\% \text{ Excess Air}}{100}$$

$$\text{Consumed oxygen} \quad \text{O}_2 = \text{C} + \text{S} + \frac{\text{H}}{4} - \frac{\text{O}}{2}$$

$$\text{Air-fuel ratios} \quad \text{AF(mole)} = \text{O}_2(4.762) \text{ AIR}$$

$$\text{AF(mass)} = \frac{1.8094 \text{ AF (mole)}}{0.7507\text{C} + 0.063\text{H} + 2.004\text{S} + 0.875\text{N} + \text{O}}$$

$$\text{Total moles of products} \quad \text{M} = \text{O}_2[4.762 \text{ AIR}] + \frac{\text{H}}{4} + \frac{\text{O}}{2} + \frac{\text{N}}{2}$$

$$\text{Volume percents of products} \quad \text{Volume \%CO}_2 = \frac{100\text{C}}{\text{M}}$$

$$\text{Volume \%SO}_2 = \frac{100\text{S}}{\text{M}}$$

$$\text{Volume \%H}_2\text{O} = \frac{100\text{H}}{2\text{M}}$$

$$\text{Volume \%O}_2 = \frac{100(\text{AIR} - 1) \text{O}_2}{\text{M}}$$

$$\text{Volume \%N}_2 = \frac{(100) \left[ (3.762) \text{ AIR O}_2 + \frac{\text{N}}{2} \right]}{\text{M}}$$

where C, S, N, H and O refer to the number of carbon, sulfur, nitrogen, hydrogen and oxygen atoms respectively per hypothetical fuel molecule;

AF stands for air-fuel ratio;

M stands for total moles of product.

Remarks:

% Excess air  $\geq 0$ .

Complete combustion is assumed.

The volume percent values assume that no water vapor has been condensed out.

Example:

Octane,  $C_8H_{18}$ , is burned in 40% excess air. What is the air-fuel mass ratio and what are the volume percents of the products?

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 010

[XEQ] [ALPHA] HCC [ALPHA]

C?

8 [R/S]

H?

18 [R/S]

O?

0 [R/S]

S?

0 [R/S]

N?

0 [R/S]

%EXCESS AIR?

40 [R/S]

AF,MASS=21.12

[R/S]

AF,MOLES=83.34

[R/S]

PROD MOLES=87.84

[R/S]

%S02=0.00

[R/S]

%C02=9.11

[R/S]

%H2O=10.25

[R/S]

%O2=5.69

[R/S]

%N2=74.95

[illegible]

# Program Listings

01 *LBL "HCC "	Initialization	50 2	
02 FIX 2		51 /	
03 "C?"		52 +	
04 PROMPT		53 STO 07	
05 STO 01		54 RCL 08	AF (mass)
06 "H?"		55 1.8094	
07 PROMPT		56 *	
08 STO 02		57 RCL 01	
09 "O?"		58 .7507	
10 PROMPT		59 *	
11 STO 03		60 RCL 02	
12 "S?"		61 .063	
13 PROMPT		62 *	
14 STO 04		63 +	
15 "N?"		64 RCL 03	
16 PROMPT		65 +	
17 STO 09		66 2.004	
18 "%EXCESS AIR?"		67 RCL 04	
19 PROMPT		68 *	
20 100		69 +	
21 /	Air	70 .875	
22 1		71 RCL 09	
23 +		72 *	
24 STO 05		73 +	
25 RCL 01		74 /	
26 RCL 04		75 "AF, MASS	Outputs
27 +		= "	
28 RCL 02	O <sub>2</sub>	76 XEQ d	
29 4		77 RCL 08	
30 /		78 "AF, MOLE	
31 +		S= "	
32 RCL 03		79 XEQ d	
33 2		80 RCL 07	
34 /		81 "PROD MO	
35 -		LES= "	
36 STO 06		82 XEQ d	
37 *		83 RCL 04	
38 4.762	AF (mole)	84 XEQ E	
39 *		85 "%SO2= "	
40 STO 08		86 XEQ d	
41 RCL 02		87 RCL 01	
42 4	M	88 XEQ E	
43 /		89 "%CO2= "	
44 +		90 XEQ d	
45 RCL 03		91 RCL 02	
46 2		92 2	
47 /		93 /	
48 +		94 XEQ E	
49 RCL 09		95 "%H2O= "	
		96 XEQ d	
		97 RCL 05	

	98	1				51	
	99	-					
	100	RCL 06					
	101	*					
	102	XEQ E					
	103	"%02="					
	104	XEQ d					
	105	RCL 08					
	106	RCL 05					
	107	RCL 06				60	
	108	*					
	109	-					
	110	RCL 09					
	111	2					
	112	/					
	113	+					
	114	XEQ E					
	115	"%N2="					
	116	*LBL d	-- -- -- --				
	117	ARCL X	Display				
	118	AVIEW				70	
	119	STOP					
	120	RTN	-- -- -- --				
	121	*LBL E	Subroutine				
	122	RCL 07					
	123	/					
	124	100	$\frac{100}{M}$	x			
	125	*					
	126	RTN					
	127	.END.				80	
40						90	
50						00	



DATA REGISTERS				STATUS			
00		50		SIZE <u>010</u> TOT. REG. <u>047</u> USER MODE			
	C			ENG _____    FIX <u>2</u> SCI _____    ON _____ OFF <u>X</u>			
	H			DEG _____    RAD _____    GRAD _____			
	O			FLAGS			
	S						
05	AIR	55		#	INIT S/C	SET INDICATES	CLEAR INDICATES
	O <sub>2</sub>					NONE	
	Prod						
	AF(moles)						
	N						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION	KEY	FUNCTION	KEY
40		90					
45		95					

## HYDROCARBON COMBUSTION

PROGRAM REGISTERS NEEDED: 38

HEWLETT PACKARD  
SOLUTIONS BOOK  
CHEMICAL ENGINEERING

ROW 1 (1 : 4)



ROW 2 (5 : 12)



ROW 3 (12 : 18)



ROW 4 (18 : 21)



ROW 5 (22 : 34)



ROW 6 (35 : 43)



ROW 7 (44 : 55)



ROW 8 (55 : 60)



ROW 9 (61 : 66)



ROW 10 (67 : 75)



ROW 11 (75 : 78)



ROW 12 (78 : 81)



ROW 13 (81 : 82)



ROW 14 (82 : 86)



ROW 15 (86 : 90)



ROW 16 (90 : 95)



ROW 17 (96 : 103)



ROW 18 (103 : 111)



## HYDROCARBON COMBUSTION

HEWLETT PACKARD  
SOLUTIONS BOOK  
CHEMICAL ENGINEERING

ROW 19 (112 : 117)



ROW 20 (117 : 126)

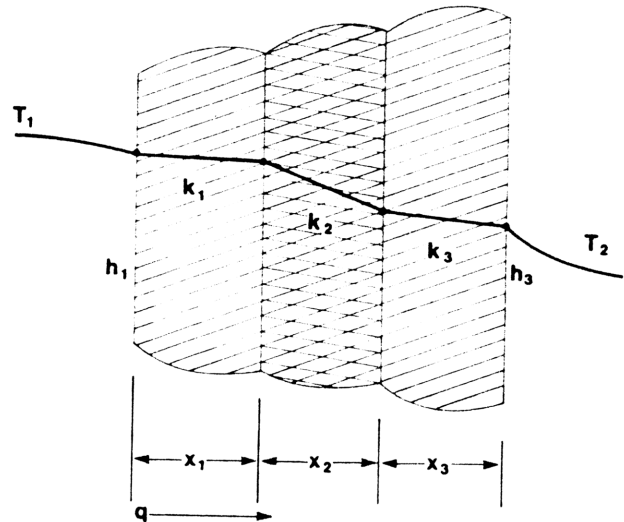
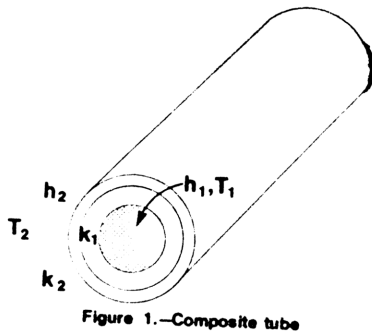


ROW 21 (127 : 127)



## HEAT TRANSFER THROUGH COMPOSITE CYLINDERS AND WALLS

This program can be used to calculate the overall heat transfer coefficient for composite tubes and walls from individual section conductances and surface coefficients.



Equations:

The overall heat transfer coefficient  $U$  is defined by:

$$q/L = U \Delta T$$

or

$$q/A = U \Delta T$$

where  $\Delta T$  is the total temperature difference ( $T_2 - T_1$ ),  $q/L$  is the heat transfer per unit length of pipe, and  $q/A$  is the heat transfer per unit area of wall.

For cylinders

$$U = \frac{2\pi}{\frac{2}{h_1 D_1} + \frac{\ln(D_2/D_1)}{k_1} + \frac{\ln(D_3/D_2)}{k_2} + \dots + \frac{\ln(D_n/D_{n-1})}{k_{n-1}} + \frac{2}{h_n D_n}}$$

For walls

$$U = \frac{1}{\frac{1}{h_1} + \frac{x_1}{k_1} + \frac{x_2}{k_2} + \dots + \frac{x_n}{k_n} + \frac{1}{h_n}}$$

where

- h is the convective surface coefficient;
- $D_n$  is the outside diameter of the annulus;
- k is the conductive coefficient;
- x is the thickness of a wall section.

Remarks:

These equations are for steady state heat transfer through materials with constant properties in all directions.

For composite cylinders, inputs must start with the inside convective coefficient and work out.

Zero is an invalid input for D, k, and h.

Dimensional consistency must be maintained.

Example:

A steel pipe with an inside diameter of 4 inches and a thickness of 0.5 inches has a conductivity of 25 Btu/ft-hr-°F. Two inches of asbestos (k = 0.1 Btu/hr-ft-°F) enclose the pipe bringing the total diameter to 9 inches. If the inside convective coefficient is 1000 Btu/hr-ft<sup>2</sup>-°F and the outside coefficient is 5 Btu/hr-ft<sup>2</sup>-°F, what is the overall heat transfer coefficient? What is the heat loss for 100 feet of pipe if ΔT is 115°F?

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] CYL [ALPHA]

NO. OF SECTS?

2 [R/S]

D?

4 [ENTER↑] 12 [÷] [R/S]

H?

1000 [R/S]

D?

5 [ENTER↑] 12 [÷] [R/S]

K?

25 [R/S]

D?

9 [ENTER↑] 12 [÷] [R/S]

K?

0.1 [R/S]

H?

5 [R/S]

U=0.98 Btu/hr-ft-°F

115 [X]

112.44 Btu/hr-ft

100 [X]

11,244.20 Btu/hr

# User Instructions

				SIZE: 009
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Load program			
2	For walls go to step 3, and for cylinders			
	go to step 9.			
3	Initialize for walls		[XEQ] WALLS	NO. OF SECTS?
4	Key in number of sections	N	[R/S]	H?
5	Key in the first section's			
	convective coefficient	$h_1$	[R/S]	X?
6	Key in thickness of the current section	$x_1$	[R/S]	k?
7	Key in the conductive coefficient for the			
	section of step 6	$k_1$	[R/S]	X? or H?
	(Repeat steps 6 and 7 for each section.			
	The prompt after the last section will be			
	"H?")			
8	Key in the last section's			
	convective coefficient	$h_n$	[R/S]	U=
9	Initialize for cylinders		[XEQ] CYL	NO. OF SECTS?
10	Key in number of sections	N	[R/S]	D?
11	Key in the inside section's inner			
	diameter	$D_1$	[R/S]	H?
12	Key in the inside convective coefficient	$h_1$	[R/S]	D?
13	Key in the outside diameter of the current			
	section	$D_1$	[R/S]	K?
14	Key in the conductive coefficient for the			
	section of step 13	$k_1$	[R/S]	D? or H?
	(Repeat steps 13 and 14 for each section)			
15	Key in the outside convective coefficient	$h_n$	[R/S]	U=



DATA REGISTERS				STATUS							
00	No. of surfaces	50		SIZE	009	TOT. REG.	034	USER MODE			
	outside diameter			ENG		FIX	2	SCI	ON	OFF	X
				DEG		RAD		GRAD			
	U			FLAGS							
05		55									
	l or π			#	INIT S/C	SET INDICATES		CLEAR INDICATES			
	temp. storage			00		Cyl		Walls			
	ΣR										
10		60									
15		65									
20		70									
25		75									
30		80									
35		85									
				ASSIGNMENTS							
				FUNCTION		KEY		FUNCTION		KEY	
40		90									
45		95									



HEAT TRANSFER THROUGH  
COMPOSITE CYLINDERS AND WALLS  
PROGRAM REGISTERS NEEDED: 26

HEWLETT PACKARD  
SOLUTION BOOK:  
CHEMICAL ENGINEERING

ROW 1 (1 - 4)



ROW 2 (4 - 8)



ROW 3 (9 - 16)



ROW 4 (16 - 18)



ROW 5 (19 - 26)



ROW 6 (27 - 32)



ROW 7 (33 - 43)



ROW 8 (44 - 50)



ROW 9 (51 - 53)



ROW 10 (53 - 59)



ROW 11 (60 - 65)



ROW 12 (66 - 72)



ROW 13 (72 - 79)



ROW 14 (79 - 83)



## VON KÁRMÁN ANALOGY FOR HEAT AND MASS TRANSFER

The von Kármán analogy forms a link between momentum, heat, and mass transfer for conduit flow. If any of the transport coefficients  $f$ ,  $h$ , or  $k_c$  are known, the others can be found using this program and the appropriate fluid transport numbers.

Equations:

Heat transfer

$$St = \frac{f/2}{1 + 5 \sqrt{f/2} (Pr - 1 + \ln [1 + 5/6 (Pr - 1)])}$$

Mass transfer

$$\frac{k_c}{v} = \frac{f/2}{1 + 5 \sqrt{f/2} (Sc - 1 + \ln [1 + 5/6 (Sc - 1)])}$$

In both cases, the equation for  $f$  is solved using Newton's method, with the Colburn analogy as the initial guess,  $f_o$ .

$$\frac{f_o}{2} = St (Pr)^{2/3} = \frac{k_c}{v} (Sc)^{2/3}$$

where

$St$  is the Stanton number.

$f$  is the Fanning friction factor.

$Pr$  is the Prandtl number.

$Sc$  is the Schmidt number.

$k_c$  is the convective mass transfer coefficient.

$v$  is the average fluid velocity.

Reference:

Welty, Wicks, Wilson, *Fundamentals of Momentum Heat and Mass Transfer*; John Wiley and Sons, Inc., 1969.

Remarks:

No form drag may be present. Fanning friction factors should be less than 0.02 and greater than 0.0001.

Example:

The Schmidt number for a mild acid flowing through a metal pipe has been found to be 3.7. The Fanning friction factor is 0.011. If the fluid velocity is 15 feet per second, what is the convective mass transfer coefficient?

Keystrokes:

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] ANALOG [ALPHA]

3.7 [R/S]

[R/S]

[R/S]

0.011 [R/S]

[XEQ] [ALPHA] KC/V [ALPHA]

15 [X]

Display:

SC? OR PR?

ST?

KC/V?

F?

KC/V=0.0023

0.0338

[illegible]

# Program Listings

01♦LBL "ANA LOG"	Initialization	49 -	
02 FIX 4		50 RCL 04	
03 "SC? OR PR?"		51 RCL 02	
04 PROMPT		52 -	
05 STO 03		53 RCL 06	
06 "ST?"		54 /	
07 PROMPT		55 2	
08 "KC/V?"		56 /	
09 PROMPT		57 1	
10 STO 02		58 -	
11 "F?"		59 /	
12 PROMPT		60 +	
13 STO 05		61 STO 06	
14 STOP		62 -	
15♦LBL "ST"	----- St	63 ABS	
16 "ST="		64 1 E-8	
17 GTO B		65 X<=Y?	
18♦LBL "KC/ V"	----- k <sub>c</sub> /v	66 GTO 01	
19 "KC/V="		67 RCL 06	
20♦LBL B	----- St & k <sub>c</sub> /v	68 2	
21 0		69 *	
22 RCL 05		70 STO 05	
23 2		71 GTO d	
24 /		72♦LBL D	
25 STO 06		73 RCL 06	
26 XEQ D		74 RCL 03	
27 /		75 1	
28 STO 02		76 -	
29 GTO d		77 ENTER↑	
30♦LBL F	----- f	78 ENTER↑	
31 "F="		79 5	
32 RCL 05		80 *	
33 RCL 02		81 6	
34 RCL 03		82 /	
35 2		83 1	
36 ENTER↑		84 +	
37 3		85 LN	
38 /		86 +	
39 Y↑X		87 STO 08	
40 *		88 X<>Y	
41 STO 06		89 SQRT	
42♦LBL 01		90 *	
43 XEQ D		91 5	
44 RCL 02		92 *	
45 *		93 1	
46 STO 04		94 +	
47 RCL 06		95 RTN	
48 X<>Y		96♦LBL d	----- Display
		97 ARCL X	
		98 AVIEW	
		99 STOP	
		100 .END.	

# REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS					
00		50		SIZE	009	TOT. REG.	33	USER MODE	
				ENG		FIX	4	SCI	
	St			DEG		RAD		GRAD	
	Pr(Sc)							ON	
	temp storage							OFF	X
05	f	55		FLAGS					
	f/2			#	INIT S/C	SET INDICATES	CLEAR INDICATES		
						NONE			
	temp storage								
10		60							
15		65							
20		70							
25		75							
30		80							
35		85							
				ASSIGNMENTS					
				FUNCTION		KEY		FUNCTION	
								KEY	
40		90							
45		95							

VON KARMAN ANALOGY FOR HEAT  
AND MASS TRANSFER  
PROGRAM REGISTERS NEEDED: 25

HEWLETT PACKARD  
SOLUTION BOOK:  
CHEMICAL ENGINEERING

ROW 1 (1 - 3)



ROW 2 (3 - 6)



ROW 3 (6 - 11)



ROW 4 (11 - 16)



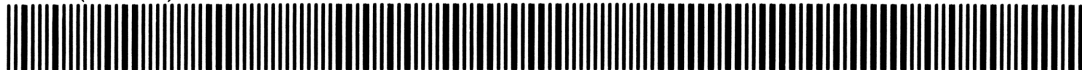
ROW 5 (16 - 18)



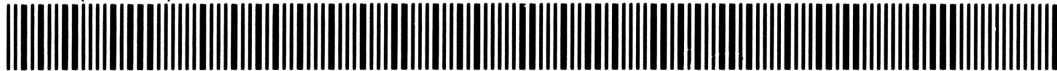
ROW 6 (19 - 25)



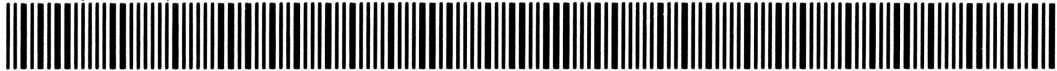
ROW 7 (26 - 31)



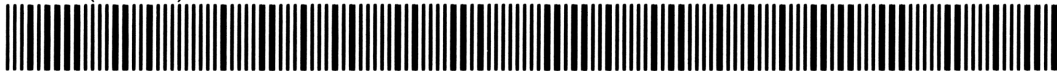
ROW 8 (32 - 43)



ROW 9 (43 - 55)



ROW 10 (56 - 65)



ROW 11 (66 - 74)



ROW 12 (75 - 87)



ROW 13 (88 - 98)



ROW 14 (99 - 100)



## EQUATIONS OF STATE

This program provides both ideal gas and Redlich-Kwong equations of state. Given four of the five state variables, the fifth is calculated. For the Redlich-Kwong solution, the critical pressure and temperature of the gas must be known. They are not needed for ideal gas solutions.

Values of the Universal Gas Constants

Value of R	Units of R	Units of P	Units of V	Units of T
8.314	N-m/g mole-K	N/m <sup>2</sup>	m <sup>3</sup> /g mole	K
83.14	cm <sup>3</sup> -bar/g mole-K	bar	cm <sup>3</sup> /g mole	K
82.05	cm <sup>3</sup> -atm/g mole-K	atm	cm <sup>3</sup> /g mole	K
0.7302	atm-ft <sup>3</sup> /lb mole-°R	atm	ft <sup>3</sup> /lb mole	°R
10.73	psi-ft <sup>3</sup> /lb mole-°R	psi	ft <sup>3</sup> /lb mole	°R
1545	psf-ft <sup>3</sup> /lb mole-°R	psf	ft <sup>3</sup> /lb mole	°R

Critical Temperatures and Pressures

Substance	T <sub>c</sub> , K	T <sub>c</sub> , °R	P <sub>c</sub> , ATM
Ammonia	405.6	730.1	112.5
Argon	151	272	48.0
Carbon dioxide	304.2	547.6	72.9
Carbon monoxide	133	239	34.5
Chlorine	417	751	76.1
Helium	5.3	9.5	2.26
Hydrogen	33.3	59.9	12.8
Nitrogen	126.2	227.2	33.5
Oxygen	154.8	278.6	50.1
Water	647.3	1165.1	218.2
Dichlorodifluoromethane	384.7	692.5	39.6
Dichlorofluoromethane	451.7	813.1	51.0
Ethane	305.5	549.9	48.2
Ethanol	516.3	929.3	63
Methanol	513.2	923.8	78.5
n-Butane	425.2	765.4	37.5
n-Haxane	507.9	914.2	29.9
n-Pentane	469.5	845.1	33.3
n-Octane	568.6	1023.5	24.6
Trichlorofluoromethane	471.2	848.1	43.2



Equations:

Ideal gas:  $PV = nRT$

Redlich-Kwong: 
$$P = \frac{nRT}{(V - b)} - \frac{a}{T^{1/2} V (V + b)}$$

$$a = 4.934 b nRT_c^{1.5}$$

$$b = 0.0867 \frac{nRT_c}{P_c}$$

where:

- P is the absolute pressure;
- V is the volume;
- n is the number of moles present;
- R is the universal gas constant;
- T is the absolute temperature;
- $T_c$  is the critical temperature;
- $P_c$  is the critical pressure.

Remarks:

P, V, n and T must have units compatible with R.

At low temperatures or high pressures, the ideal gas law does not represent the behavior of real gases.

No equation of state is valid for all substances or over an infinite range of conditions. The Redlich-Kwong equation gives moderate to good accuracy for a variety of substances over a wide range of conditions. Results should be used with caution and tempered by experience.

Solutions for V, n, R and T, using the Redlich-Kwong equation, require an iterative technique. Newton's method is employed using the ideal gas law to generate the initial guess. Iteration time is generally a function of the amount of deviation from ideal gas behavior. For extreme cases, the routine may fail to converge entirely, resulting in "DATA ERROR".

## Example 1:

0.63 g moles of air are enclosed in a 25,000 cm<sup>3</sup> space at 1200 K. What is the pressure in bars? Assume ideal gas behavior.

## Keystrokes:

[XEQ] [ALPHA] SIZE [ALPHA] 015

[XEQ] [ALPHA] ID [ALPHA]

0 [R/S]

25000 [R/S]

0.63 [R/S]

83.14 [R/S]

1200 [R/S]

## Display:

P?

V?

N?

R?

T?

P=2.51

## Example 2:

The specific volume of a gas in a container is 800 cm<sup>3</sup>/g mole. The temperature will reach 400 K. What will the pressure be, according to the Redlich-Kwong relation?

$$P_c = 48.2 \text{ atm}$$

$$T_c = 305.5 \text{ K}$$

$$R = 82.05 \text{ cm}^3 - \text{atm/g mole-K}$$

## Keystrokes:

[XEQ] [ALPHA] RK [ALPHA]

305.5 [R/S]

48.2 [R/S]

0 [R/S]

800 [R/S]

1 [R/S]

82.05 [R/S]

400 [R/S]

## Display:

TC?

PC?

P?

V?

N?

R?

T?

P=36.27

[illegible]

# Program Listings

01*LBL "ID"	Initialization	50 FS? 02	
02 0		51 RTN	
03 SF 00		52 GTO IND	
04 GTO 00		10	-----
05*LBL "RK"		53*LBL 05	Calculate
06 1		54 "P="	unknown
07 CF 00		55 GTO 00	
08 "TC?"		56*LBL 06	
09 PROMPT		57 "V="	
10 STO 13		58*LBL 00	
11 "PC?"		59 RCL 07	
12 PROMPT		60 RCL 08	
13 STO 14		61 *	
14*LBL 00		62 RCL 09	
15 SF 02		63 *	
16 CF 01		64 RCL 05	
17 FIX 2		65 RCL 06	
18 "P?"		66 *	
19 PROMPT		67 /	
20 5		68 STO IND	
21 XEQ 00		10	
22 "V?"		69 GTO 00	
23 PROMPT		70*LBL 07	
24 6		71 SF 01	
25 XEQ 00		72 "N="	
26 "N?"		73 GTO 01	
27 PROMPT		74*LBL 08	
28 7		75 SF 01	
29 XEQ 00		76 "R="	
30 "R?"		77 GTO 01	
31 PROMPT		78*LBL 09	
32 8		79 "T="	
33 XEQ 00		80 SF 01	
34 "T?"		81*LBL 01	
35 PROMPT		82 RCL 05	
36 CF 02		83 RCL 06	
37 9		84 *	
38*LBL 00		85 RCL 07	
39 CF 01		86 /	
40 STO 01		87 RCL 08	
41 RDN		88 /	
42 STO IND		89 RCL 09	
01		90 /	
43 X#0?		91 STO IND	
44 GTO 01		10	
45 R↑		92*LBL 00	
46 STO 10		93 FS? 00	
47 1		94 GTO 10	
48 STO IND		95 XEQ 01	
01		96 GTO 00	
49*LBL 01		97*LBL 02	

# Program Listings

```

98 FS? 01
99 XEQ 01
100♦LBL 00
101 RCL 00
102 RCL 09
103 *
104 RCL 06
105 RCL 12
106 -
107 STO 04
108 /
109 RCL 11
110 RCL 09
111 SQRT
112 /
113 STO 02
114 RCL 06
115 /
116 LASTX
117 RCL 12
118 +
119 STO 03
120 /
121 -
122 RCL 05
123 -
124 XEQ IND
10
125 /
126 ST- IND
10
127 RCL IND
10
128 /
129 ABS
130 1 E-4
131 X<=Y?
132 GTO 02
133 RCL IND
10
134 GTO 10
135♦LBL 06
136 RCL 06
137 ENTER↑
138 +
139 RCL 12
140 +
141 RCL 02
142 *
143 RCL 03
144 RCL 06
145 *

```

-----  
 If ideal,  
 display

-----  
 Calculate using  
 Redlich-Kwong  
 equations

-----  
 $\frac{\partial P}{\partial V}$

```

146 X↑2
147 /
148 RCL 00
149 RCL 09
150 *
151 RCL 04
152 X↑2
153 /
154 -
155 RTN
156♦LBL 09
157 RCL 00
158 RCL 04
159 /
160 RCL 02
161 2
162 /
163 RCL 09
164 /
165 RCL 06
166 /
167 RCL 03
168 /
169 +
170 RTN
171♦LBL 07
172♦LBL 08
173 RCL 09
174 RCL 06
175 *
176 RCL 04
177 X↑2
178 /
179 RCL 06
180 ENTER↑
181 +
182 RCL 12
183 +
184 RCL 00
185 /
186 RCL 06
187 /
188 RCL 03
189 X↑2
190 /
191 RCL 02
192 *
193 -
194 RCL 00
195 *
196 RCL IND

```

-----  
 $\frac{\partial P}{\partial T}$

-----  
 $\frac{\partial P}{\partial n}$  or  $\frac{\partial P}{\partial R}$

# Program Listings

10		51	
197 /			
198 RTN			
199♦LBL 05			
200 LASTX			
201 +			
202 STO 05			
203 GTO 10			
204♦LBL 01	-----		
205 RCL 07	Calculate a, b		
206 RCL 08		60	
207 *			
208 STO 00			
209 .0867			
210 RCL 14			
211 /			
212 X<>Y			
213 RCL 13			
214 *			
215 *			
216 STO 12		70	
217 LASTX			
218 *			
219 RCL 13			
220 SQRT			
221 *			
222 4.934			
223 *			
224 STO 11			
225 RTN	-----		
226♦LBL 10	Display	80	
227 ARCL X			
228 AVIEW			
229 STOP			
230 .END.			
40		90	
50		00	

DATA REGISTERS				STATUS			
00	NR	50		SIZE <u>015</u> TOT. REG. <u>61</u> USER MODE ENG _____    FIX <u>2</u> SCI _____    ON _____ OFF <u>X</u> DEG _____    RAD _____    GRAD _____			
	temp storage index			<b>FLAGS</b> <div> <div>#</div> <div>INIT S/C</div> <div>SET INDICATES</div> <div>CLEAR INDICATES</div> </div>			
	$a/T^{1/2}$						
	(V + b)						
	(V - b)						
05	P	55		00		Ideal	Redlich-Kwong
	V			01		Calc a, b	
	n			02		Inputting data	Calculate
	f						
	T						
10	control	60					
	a						
	b						
	$T_c$						
	$P_c$						
15		65					
20		70					
25		75					
30		80					
35		85					
				<b>ASSIGNMENTS</b>			
				FUNCTION		KEY	
40		90					
45		95					

## EQUATIONS OF STATE

PROGRAM REGISTERS NEEDED: 47

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CHEMICAL ENGINEERING

ROW 1 (1 - 5)



ROW 2 (5 - 10)



ROW 3 (11 - 17)



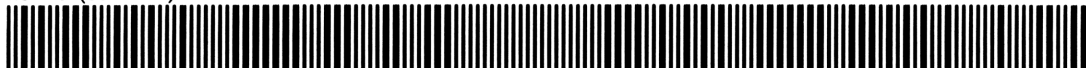
ROW 4 (18 - 24)



ROW 5 (25 - 30)



ROW 6 (30 - 37)



ROW 7 (38 - 47)



ROW 8 (48 - 55)



ROW 9 (55 - 65)



ROW 10 (66 - 73)



ROW 11 (73 - 79)



ROW 12 (80 - 91)



ROW 13 (91 - 98)



ROW 14 (98 - 108)



ROW 15 (109 - 121)



ROW 16 (122 - 130)



ROW 17 (130 - 138)



ROW 18 (139 - 151)





## EQUATIONS OF STATE

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ROW 19 (152 - 164)



ROW 20 (165 - 177)



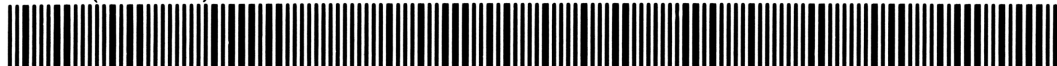
ROW 21 (178 - 190)



ROW 22 (191 - 202)



ROW 23 (203 - 210)



ROW 24 (211 - 222)



ROW 25 (222 - 229)



ROW 26 (230 - 230)



## REVERSIBLE POLYTROPIC PROCESS FOR AN IDEAL GAS

This program may be used to solve interchangeably between pressure ratio, volume ratio, temperature ratio, and density ratio for polytropic processes involving ideal gases. Polytropic processes are defined by the relation

$$pV^n = C.$$

Isentropic processes are special cases of polytropic processes. For isentropic processes,  $k$ , the specific heat ratio, is equal to  $n$ .

Equations:

$$\frac{P_2}{P_1} = \left( \frac{V_2}{V_1} \right)^{-n} = \left( \frac{T_2}{T_1} \right)^{\frac{n}{n-1}} = \left( \frac{\rho_2}{\rho_1} \right)^n$$

where

$P_2/P_1$  is the final pressure divided by the initial pressure;  
 $V_2/V_1$  is the final volume divided by the initial volume;  
 $T_2/T_1$  is the final temperature divided by the initial temperature;  
 $\rho_2/\rho_1$  is the final density divided by the initial density.

Note that in the display " $\rho$ " is indicated by "D".

Example:

A compressor has a compression ratio of 8.5 ( $V_1/V_2$ ). The polytropic constant is 1.43. If inlet air is at 300 K, what is the outlet temperature? What is the outlet pressure in atmospheres if the inlet pressure is one atmosphere?

Keystrokes:	Display:
[XEQ] [ALPHA] SIZE [ALPHA] 006	
[XEQ] [ALPHA] GAS [ALPHA]	N?
1.43 [R/S]	0.00
8.5 [1/x] [XEQ] [ALPHA] V2/V1 [ALPHA]	0.00
[XEQ] [ALPHA] T2/T1 [ALPHA]	T2/T1=2.51
300 [X]	752.96
0 [XEQ] [ALPHA] P2/P1 [ALPHA]	P2/P1=21.33




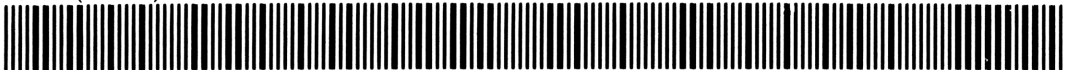











# Program Listings

01♦LBL "GAS "	Initialization	48 STO 05	
02 FIX 2		49 0	
03 "N?"		50 STOP	
04 PROMPT		51♦LBL 01	
05 STO 02		52 RCL 05	
06 1		53 RCL 03	
07 -		54 RCL 02	
08 STO 03		55 /	
09 1/X		56 Y↑X	
10 STO 04		57 "T2/T1="	
11 0		58 GT0 d	
12 STOP		59♦LBL "D2/ D1"	$\rho_2/\rho_1$
13♦LBL "P2/ P1"	$P_2/P_1$	60 X=0?	
14 X=0?		61 GT0 01	
15 GT0 01		62 RCL 02	
16 STO 05		63 Y↑X	
17 0		64 STO 05	
18 STOP		65 0	
19♦LBL 01		66 STOP	
20 RCL 05		67♦LBL 01	
21 "P2/P1="		68 RCL 05	
22 GT0 d		69 RCL 02	
23 STOP		70 1/X	
24♦LBL "V2/ V1"	$V_2/V_1$	71 Y↑X	
25 X=0?		72 "D2/D1="	
26 GT0 01		73♦LBL d	Display
27 RCL 02		74 ARCL X	
28 CHS		75 AVIEW	
29 Y↑X		76 STOP	
30 STO 05		77 .END.	
31 0			
32 STOP			
33♦LBL 01			
34 RCL 05			
35 RCL 02			
36 CHS			
37 1/X			
38 Y↑X		90	
39 "V2/V1="			
40 GT0 d			
41♦LBL "T2/ T1"	$T_2/T_1$		
42 X=0?			
43 GT0 01			
44 RCL 02			
45 RCL 04			
46 *			
47 Y↑X		00	

[illegible]

REVERSIBLE POLYTROPIC PROCESS  
FOR AN IDEAL GAS  
PROGRAM REGISTERS NEEDED: 24

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ROW 1 (1 - 4)	
ROW 2 (5 - 13)	
ROW 3 (13 - 17)	
ROW 4 (18 - 22)	
ROW 5 (23 - 26)	
ROW 6 (27 - 37)	
ROW 7 (38 - 41)	
ROW 8 (41 - 46)	
ROW 9 (47 - 57)	
ROW 10 (57 - 59)	
ROW 11 (59 - 65)	
ROW 12 (65 - 72)	
ROW 13 (72 - 77)	

## CONDUIT FLOW

This program solves for the average velocity, or the pressure drop for viscous, incompressible flow in conduits.

Equations:

$$v^2 = \frac{\Delta P / \rho}{2 \left( f \frac{L}{D} + \frac{K_T}{4} \right)}$$

For laminar flow ( $Re < 2300$ )

$$f = 16/Re.$$

For turbulent flow ( $Re > 2300$ )

$$\frac{1}{\sqrt{f}} = 1.737 \ln \frac{D}{\epsilon} + 2.28 - 1.737 \ln \left( 4.67 \frac{D}{\epsilon Re \sqrt{f}} + 1 \right)$$

is solved by Newton's method.

$$\frac{1}{\sqrt{f_0}} = 1.737 \ln \frac{D}{\epsilon} + 2.28$$

is used as an initial guess in the iteration.

where:  $Re$  is the Reynolds number, defined as  $\rho Dv/\mu$ ;

$D$  is the pipe diameter;

$\epsilon$  is the dimension of irregularities in the conduit surface (see table 2);

$f$  is the Fanning friction factor for conduit flow;

$\Delta P$  is the pressure drop along the conduit;

$\rho$  is the density of the fluid;

$\mu$  is the viscosity of the fluid;

$\nu$  is the kinematic viscosity of the fluid and  $\mu = \rho \nu$ ;

$L$  is the conduit length;

$v$  is the average fluid velocity;

$K_T$  is the total of the applicable fitting coefficients in table 1.

Table 1  
Fitting Coefficients

Fitting	K
Globe valve, wide open	7.5—10
Angle valve, wide open	3.8
Gate valve, wide open	0.15—0.19
Gate valve, 3/4 open	0.85
Gate valve, 1/2 open	4.4
Gate valve, 1/4 open	20
90° elbow	0.4—0.9
Standard 45° elbow	0.35—0.42
Tee, through side outlet	1.5
Tee, straight through	.4
180° bend	1.6
Entrance to circular pipe	0.25—0.50
Sudden expansion	$(1-A_{up}/A_{dn})^{2*}$
Acceleration from $v = 0$ to $v = v_{entrance}$	1.0

\* $A_{up}$  is the upstream area and  $A_{dn}$  is the downstream area.

Table 2  
Surface Irregularities

Material	$\epsilon$ (feet)	$\epsilon$ (meters)
Drawn or Smooth Tubing	$5.0 \times 10^{-6}$	$1.5 \times 10^{-6}$
Commercial Steel or Wrought Iron	$1.5 \times 10^{-4}$	$4.6 \times 10^{-5}$
Asphalted Cast Iron	$4.0 \times 10^{-4}$	$1.2 \times 10^{-4}$
Galvanized Iron	$5.0 \times 10^{-4}$	$1.5 \times 10^{-4}$
Cast Iron	$8.3 \times 10^{-4}$	$2.5 \times 10^{-4}$
Wood Stave	$6.0 \times 10^{-4}$ to $3.0 \times 10^{-3}$	$1.8 \times 10^{-4}$ to $9.1 \times 10^{-4}$
Concrete	$1.0 \times 10^{-3}$ to $1.0 \times 10^{-2}$	$3.0 \times 10^{-4}$ to $3.0 \times 10^{-3}$
Riveted Steel	$3.0 \times 10^{-3}$ to $3.0 \times 10^{-2}$	$9.1 \times 10^{-4}$ to $9.1 \times 10^{-3}$

Reference:

Welty, Wicks, Wilson, *Fundamentals of Momentum, Heat and Mass Transfer*, John Wiley and Sons, Inc., 1969.



### Remarks:

The correlation gives meaningless results in the region  $2300 < Re < 4000$ .

The solution requires an iterative procedure. The time for solution will range from 10 seconds for  $\Delta P$ , to several minutes for  $v$ . The display setting is used to determine when the solution for  $v$  is adequately accurate. Time for solution of  $v$  is roughly proportional to the number or significant digits in the display setting.

If the conduit is not circular, an equivalent diameter may be calculated using the formula below:

$$D_{eq} = 4 \frac{\text{cross sectional area}}{\text{wetted perimeter}}$$

Unitary consistency must be maintained.

### Example:

A heat exchanger has 20, 3 meter tube passes (60 m of pipe) with 180 degrees bends connecting each pair of tubes (from table 1,  $K_T = 10 \times 1.6$ ). The fluid is water ( $\nu = 9.3 \times 10^{-7} \text{ m}^2/\text{s}$ ,  $\rho = 10^3 \text{ kg/m}^3$ ). The surface roughness is  $3 \times 10^{-4} \text{ m}$  and the diameter is  $2.54 \times 10^{-2} \text{ m}$ . If the fluid velocity is 3.05 m/s, what is the pressure loss? What is the Reynolds number? What is the Fanning friction factor?

### Keystrokes:

```
[XEQ] [ALPHA] SIZE [ALPHA] 015
[/[/[/[/ [ENG] 3
[XEQ] [ALPHA] CONDUIT [ALPHA]
9.3 [EEX] [CHS] 7 [ENTER^]
[EEX] 3 [X] [R/S]
[EEX] 3 [R/S]
3 [EEX] [CHS] 4 [R/S]
60 [R/S]
2.54 [EEX] [CHS] 2 [R/S]
16 [R/S]
3.05 [R/S]
[R/S]
[R/S]
[R/S]
```

### Display:

```
U=?
RHO=?
E=?
L=?
D=?
KT=?
V=?
DP=?
DP=521.9E3
Re=83.30E3
F=10.18E-3
```

[illegible]

# Program Listings

<pre> 01♦LBL "CON DUIT" 02 SF 21 03 SF 27 04 "U=?" 05 PROMPT 06 STO 09 07 "RHO=?" 08 PROMPT 09 STO 10 10 ST/ 09 11 "E=?" 12 PROMPT 13 STO 14 14 "L=?" 15 PROMPT 16 STO 03 17 "D=?" 18 PROMPT 19 STO 13 20 "KT=?" 21 PROMPT 22 4 23 / 24 STO 08 25♦LBL C 26 CF 22 27 "V=?" 28 PROMPT 29 SF 00 30 FS? 22 31 CF 00 32 STO 02 33 "DP=?" 34 PROMPT 35 STO 04 36 XEQ 09 37 FS? 00 38 GT0 03 39 RCL 02 40 X↑2 41 * 42 RCL 10 43 * 44 STO 04 45 "DP=" 46 GT0 10 47♦LBL 03 48 RND 49 STO 00 </pre>	Input	<pre> 50 XEQ 08 51 RND 52 RCL 00 53 X&lt;&gt;Y 54 X≠Y? 55 GT0 03 56 "V=?" 57 RCL 02 58 GT0 10 59♦LBL 09 60 RCL 10 61 RCL 13 62 RCL 14 63 / 64 STO 06 65 LN 66 1.737 67 STO 07 68 * 69 2.28 70 + 71 STO 12 72 STO 05 73 FS? 00 74 GT0 07 75♦LBL 08 76 16 77 RCL 02 78 RCL 13 79 * 80 RCL 09 81 / 82 STO 01 83 2300 84 X&lt;=Y? 85 GT0 02 86 RDN 87 / 88 SQRT 89 1/X 90 STO 05 91 GT0 07 92♦LBL 02 93 RCL 12 94 RCL 05 95 - 96 4.67 97 RCL 06 98 * 99 RCL 01 </pre>	<p>-----</p> <p>Calculate constants</p> <p>-----</p> <p>Is flow turbulent?</p> <p>-----</p> <p>Iterate to find <math>\frac{1}{\sqrt{f}}</math></p>
<pre> 35 STO 04 36 XEQ 09 37 FS? 00 38 GT0 03 39 RCL 02 40 X↑2 41 * 42 RCL 10 43 * 44 STO 04 45 "DP=" 46 GT0 10 47♦LBL 03 48 RND 49 STO 00 </pre>	1st V	<pre> 50 XEQ 08 51 RND 52 RCL 00 53 X&lt;&gt;Y 54 X≠Y? 55 GT0 03 56 "V=?" 57 RCL 02 58 GT0 10 59♦LBL 09 60 RCL 10 61 RCL 13 62 RCL 14 63 / 64 STO 06 65 LN 66 1.737 67 STO 07 68 * 69 2.28 70 + 71 STO 12 72 STO 05 73 FS? 00 74 GT0 07 75♦LBL 08 76 16 77 RCL 02 78 RCL 13 79 * 80 RCL 09 81 / 82 STO 01 83 2300 84 X&lt;=Y? 85 GT0 02 86 RDN 87 / 88 SQRT 89 1/X 90 STO 05 91 GT0 07 92♦LBL 02 93 RCL 12 94 RCL 05 95 - 96 4.67 97 RCL 06 98 * 99 RCL 01 </pre>	<p>-----</p> <p>Is flow turbulent?</p> <p>-----</p> <p>Iterate to find <math>\frac{1}{\sqrt{f}}</math></p>
<pre> 40 X↑2 41 * 42 RCL 10 43 * 44 STO 04 45 "DP=" 46 GT0 10 47♦LBL 03 48 RND 49 STO 00 </pre>	Calculate ΔP	<pre> 50 XEQ 08 51 RND 52 RCL 00 53 X&lt;&gt;Y 54 X≠Y? 55 GT0 03 56 "V=?" 57 RCL 02 58 GT0 10 59♦LBL 09 60 RCL 10 61 RCL 13 62 RCL 14 63 / 64 STO 06 65 LN 66 1.737 67 STO 07 68 * 69 2.28 70 + 71 STO 12 72 STO 05 73 FS? 00 74 GT0 07 75♦LBL 08 76 16 77 RCL 02 78 RCL 13 79 * 80 RCL 09 81 / 82 STO 01 83 2300 84 X&lt;=Y? 85 GT0 02 86 RDN 87 / 88 SQRT 89 1/X 90 STO 05 91 GT0 07 92♦LBL 02 93 RCL 12 94 RCL 05 95 - 96 4.67 97 RCL 06 98 * 99 RCL 01 </pre>	<p>-----</p> <p>Is flow turbulent?</p> <p>-----</p> <p>Iterate to find <math>\frac{1}{\sqrt{f}}</math></p>
<pre> 40 X↑2 41 * 42 RCL 10 43 * 44 STO 04 45 "DP=" 46 GT0 10 47♦LBL 03 48 RND 49 STO 00 </pre>	Iterate to find V using 1st V as guess	<pre> 50 XEQ 08 51 RND 52 RCL 00 53 X&lt;&gt;Y 54 X≠Y? 55 GT0 03 56 "V=?" 57 RCL 02 58 GT0 10 59♦LBL 09 60 RCL 10 61 RCL 13 62 RCL 14 63 / 64 STO 06 65 LN 66 1.737 67 STO 07 68 * 69 2.28 70 + 71 STO 12 72 STO 05 73 FS? 00 74 GT0 07 75♦LBL 08 76 16 77 RCL 02 78 RCL 13 79 * 80 RCL 09 81 / 82 STO 01 83 2300 84 X&lt;=Y? 85 GT0 02 86 RDN 87 / 88 SQRT 89 1/X 90 STO 05 91 GT0 07 92♦LBL 02 93 RCL 12 94 RCL 05 95 - 96 4.67 97 RCL 06 98 * 99 RCL 01 </pre>	<p>-----</p> <p>Is flow turbulent?</p> <p>-----</p> <p>Iterate to find <math>\frac{1}{\sqrt{f}}</math></p>

# Program Listings

<pre> 100 / 101 RCL 05 102 * 103 1 104 + 105 STO 11 106 LN 107 RCL 07 108 * 109 - 110 RCL 11 111 1/X 112 CHS 113 1 114 + 115 RCL 07 116 * 117 RCL 05 118 / 119 1 120 + 121 / 122 ST+ 05 123 RCL 05 124 / 125 ABS 126 1 E-3 127 X&lt;=Y? 128 GT0 02 129♦LBL 07 130 RCL 05 131 1/X 132 X↑2 133 RCL 03 134 * 135 RCL 13 136 / 137 RCL 08 138 + 139 2 140 * 141 RCL 04 142 RCL 10 143 / 144 X&lt;&gt;Y 145 FS? 00 146 GT0 00 147 RTN 148♦LBL 00 149 / </pre>		<pre> 150 SQRT 151 STO 02 152 RTN 153♦LBL 10 154 ARCL X 155 AVIEW 156 "Re=" 157 ARCL 01 158 AVIEW 159 "F=" 160 RCL 05 161 1/X 162 X↑2 163 ARCL X 164 AVIEW 165 END </pre>	<hr/> Output
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[illegible]

CONDUIT FLOW

PROGRAM REGISTERS NEEDED: 38

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ROW 1 (1 : 2)	
ROW 2 (3 : 7)	
ROW 3 (7 : 14)	
ROW 4 (14 : 20)	
ROW 5 (20 : 27)	
ROW 6 (27 : 33)	
ROW 7 (33 : 41)	
ROW 8 (42 : 50)	
ROW 9 (50 : 57)	
ROW 10 (58 : 66)	
ROW 11 (66 : 74)	
ROW 12 (74 : 83)	
ROW 13 (83 : 93)	
ROW 14 (94 : 103)	
ROW 15 (104 : 116)	
ROW 16 (117 : 126)	
ROW 17 (126 : 137)	
ROW 18 (138 : 148)	

## CONDUIT FLOW

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ROW 19 (149 : 157)



ROW 20 (157 : 165)



ROW 21 (165 : 165)



## FLUID TRANSPORT NUMBERS

It is common practice in the fields of heat, mass, and momentum transfer to lump the many variables involved into dimensionless groups. These dimensionless groups, or fluid transport numbers, greatly simplify correlating experimental data and handling calculations once correlations have been obtained.

Before you start to solve a problem, pick a consistent unit system. For instance, make the units of length, feet; the units of temperature, degrees Fahrenheit; the units of time, hours; and the units of energy, British thermal units. Once you have a unit system in mind, convert all of your variables to that system before use. To calculate the Nusselt number using the system just outlined, the inputs would have to be in the following units:

$$h: \text{Btu}/^\circ\text{F-hr-ft}^2 \quad x: \text{ft} \quad k: \text{Btu}/^\circ\text{F-hr-ft}.$$

The dimensionless groups provided in these programs are Reynolds number  $Re$ , Nusselt number  $Nu$ , Nusselt number for mass transfer  $Nu_{ab}$ , Lewis number  $Le$ , Schmidt number  $Sc$ , Stanton number  $St$  and Prandtl number  $Pr$ . All of these numbers are correlated using interchangeable solutions.

Table of Equations

Number	Symbol	Formula	Use
Reynolds	$Re$	$\rho \times v/\mu$	Momentum, mass and heat transfer where velocity and viscosity must be considered
Nusselt-heat	$Nu$	$h \times x/k$	Convective heat transfer
Biot	$Bi$	$h \times x/k$	Combinations of convective and conductive transport systems
Nusselt-mass	$Nu_{ab}$	$k_c \times x/D_{ab}$	Convective mass transfer
Stanton	$St$	$h/\rho \times v \times c_p$	Convective heat transfer
Lewis	$Le$	$k_c/\rho \times c_p \times D_{ab}$	Convective mass transfer
Schmidt	$Sc$	$\mu/\rho \times D_{ab}$	Convective mass transfer
Prandtl	$Pr$	$\mu \times c_p/k$	Convective heat transfer



where:

$\rho$  = density ("D" is used in the display)  
 $v$  = velocity  
 $\mu$  = viscosity  
 $x$  = significant dimension  
 $h$  = convective heat transfer coefficient  
 $k$  = conductive heat transfer coefficient  
 $k_c$  = convective mass transfer coefficient  
 $D_{ab}$  = mass diffusivity  
 $c_p$  = constant pressure heat capacity

Example:

At 60°F, the properties of water are:

$\rho = 62.3 \text{ lb/ft}^3$   
 $c_p = 1.00 \text{ Btu/lb}^\circ\text{F}$   
 $\mu = 0.760 \times 10^{-3} \text{ lb/ft sec}$   
 $\nu = 1.22 \times 10^{-5} \text{ ft}^2/\text{sec}$   
 $k = 0.340 \text{ Btu/hr-ft-}^\circ\text{F}$

Assume that fluid velocity is 37 feet per second and that the critical dimension is 6 inches. Calculate the Reynolds number using viscosity  $\mu$  and density  $\rho$

Load "Reynolds number" program (#1)

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] RE [ALPHA]

X

6 [ENTER] 12 [÷] [R/S]

V

37 [R/S]

D

62.3 [R/S]

U

0.76 [EEX] 3 [CHS] [R/S]

Re

[R/S]

Re=1.517E6

[illegible]

# Program Listings

01♦LBL "Re"	Initialization	52♦LBL a	Label output rtn with 1.0
02 ENG 3	-----	53 ASTO 00	
03 CF 00		54 1	
04 CLX		55 RTN	
05 "X"		56 .END.	
06 PROMPT	Input		
07 X=0?			
08 XEQ b			
09 STO 08			
10 CLX		60	
11 "V"			
12 PROMPT			
13 X=0?			
14 XEQ b			
15 STO 07			
16 CLX			
17 "D"			
18 PROMPT			
19 X=0?			
20 XEQ b			
21 STO 04		70	
22 CLX			
23 "U"			
24 PROMPT			
25 X=0?			
26 XEQ a			
27 STO 05			
28 CLX			
29 "Re"			
30 PROMPT			
31 X=0?		80	
32 XEQ a			
33 STO 01			
34 RCL 05			
35 *	$\frac{Reu}{xvp} = 1.0$		
36 RCL 08			
37 RCL 07			
38 *			
39 RCL 04			
40 *			
41 /		90	
42 FC? 00			
43 1/X			
44 CLA			
45 ARCL 00	Display		
46 "f="			
47 ARCL X			
48 AVIEW			
49 STOP			
50♦LBL b	-----		
51 SF 00		00	

# REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS			
00	label for output	50		SIZE <u>009</u> TOT. REG. <u>21</u> USER MODE			
	Re			ENG <u>3</u> FIX <u>    </u> SCI <u>    </u> ON <u>    </u> OFF <u>X</u>			
				DEG <u>    </u> RAD <u>    </u> GRAD <u>    </u>			
	ρ			FLAGS			
05		55					
	μ			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	v			00		INVERT	NO-INVERT
	x						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90		FUNCTION		KEY	
45		95					



# Program Listings

01*LBL "NU"	Initialization	52 1/X	Display
02 "NU"		53 CLA	
03 SF 01		54 ARCL 00	
04 GTO 01		55 "I="	
05*LBL "BI"		56 ARCL X	
06 "BI"		57 AVIEW	
07 SF 01		58 STOP	
08 GTO 01		59*LBL a	Label for unknown
09*LBL "NUa		60 CF 00	
b"		61*LBL b	
10 "NUab"	Input	62 ASTO 00	
11 CF 01		63 1	
12*LBL 01		64 RTN	
13 ASTO 01		65 .END.	
14 SF 00			
15 ENG 3			
16 CLX			
17 "Kc"			
18 FS? 01			
19 "H"			
20 PROMPT		70	
21 X=0?			
22 XEQ a			
23 STO 05			
24 CLX			
25 "X"			
26 PROMPT			
27 X=0?			
28 XEQ a			
29 STO 08			
30 CLX		80	
31 "Dab"			
32 FS? 01			
33 "K"			
34 PROMPT			
35 X=0?			
36 XEQ b			
37 STO 06			
38 CLX			
39 CLA			
40 ARCL 01		90	
41 PROMPT			
42 X=0?			
43 XEQ b			
44 STO 02			
45 RCL 06	Calculation		
46 *			
47 RCL 08			
48 /			
49 RCL 05			
50 /			
51 FS? 00		00	

DATA REGISTERS				STATUS			
00	label for unknown	50		SIZE <u>009</u> TOT. REG. <u>27</u> USER MODE			
	"NU", "BI", or "NUab"			ENG <u>3</u> FIX <u>    </u> SCI <u>    </u> ON <u>    </u> OFF <u>X</u>			
	Nu (Bi)			DEG <u>    </u> RAD <u>    </u> GRAD <u>    </u>			
05	h(kc)	55		FLAGS			
	k(Dab)			#	INIT S/C	SET INDICATES	CLEAR INDICATES
				00		INVERT	NO-INVERT
	x			01		Nu or Bi	Nu <sub>ab</sub>
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90		FUNCTION		KEY	
45		95					

[illegible]



# Program Listings

01*LBL "Le"	Initialization	53 FS? 00	Display
02 SF 01		54 1/X	
03 GTO 01	Input	55 CLA	Label output rtn with 1.0
04*LBL "ST"		56 ARCL 00	
05 CF 01		57 "I="	
06*LBL 01		58 ARCL X	
07 SF 00		59 AVIEW	
08 ENG 3		60 STOP	
09 CLX		61*LBL a	
10 "H"		62 CF 00	
11 FS? 01		63*LBL b	
12 "Kc"		64 ASTO 00	
13 PROMPT		65 1	
14 X=0?		66 RTN	
15 XEQ a		67 .END.	
16 STO 05			
17 CLX			
18 "D"			
19 PROMPT			
20 X=0?			
21 XEQ b		70	
22 STO 04	Calculation		
23 CLX			
24 "V"			
25 FS? 01			
26 "Dab"			
27 PROMPT			
28 X=0?			
29 XEQ b			
30 STO 07			
31 CLX		80	
32 "CP"			
33 PROMPT			
34 X=0?			
35 XEQ b			
36 STO 06			
37 CLX			
38 "ST"			
39 FS? 01			
40 "Le"			
41 PROMPT		90	
42 X=0?			
43 XEQ b			
44 STO 02			
45 RCL 04			
46 *			
47 RCL 07			
48 *			
49 RCL 06			
50 *			
51 RCL 05			
52 /		00	

DATA REGISTERS				STATUS			
00	label for unknown	50		SIZE <u>008</u> TOT. REG. <u>25</u> USER MODE			
				ENG <u>3</u> FIX <u>      </u> SCI <u>      </u> ON <u>      </u> OFF <u>X</u>			
	St (Le)			DEG <u>      </u> RAD <u>      </u> GRAD <u>      </u>			
	P			FLAGS			
05	h(k <sub>C</sub> )	55					
	c <sub>p</sub>			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	v(Dab)			00		INVERT	NON-INVERT
				01		LEWIS	STANTON
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90		FUNCTION		KEY	
45		95					

[illegible]

# Program Listings

01*LBL "PR"	Initialization		52 STOP	----- Label output rtn with 1.0
02 CF 01			53*LBL a	
03 GTO 01			54 CF 00	
04*LBL "SC"			55*LBL b	
05 SF 01			56 ASTO 00	
06*LBL 01			57 1	
07 SF 00			58 RTN	
08 ENG 3			59 .END.	
09 CLX				
10 "U"				
11 PROMPT	Input	60		
12 X=0?				
13 XEQ b				
14 STO 07				
15 CLX				
16 "CP"				
17 FS? 01				
18 "D"				
19 PROMPT				
20 X=0?				
21 XEQ b		70		
22 STO 04				
23 CLX				
24 "K"				
25 FS? 01				
26 "Dab"				
27 PROMPT				
28 X=0?				
29 XEQ a				
30 STO 06				
31 CLX		80		
32 "PR"				
33 FS? 01				
34 "SC"				
35 PROMPT				
36 X=0?				
37 XEQ a				
38 STO 03				
39 RCL 06	Calculate			
40 *				
41 RCL 04		90		
42 RCL 07				
43 *				
44 /				
45 FS? 00				
46 1/X				
47 CLA				
48 ARCL 00	Display			
49 "F="				
50 ARCL X				
51 AVIEW		00		

DATA REGISTERS				STATUS			
00	label for output	50		SIZE 008		TOT. REG. 23	USER MODE
				ENG 3		FIX	SCI
	Pr (Sc)			DEG		RAD	GRAD
	cp						
05		55		FLAGS			
	K(Dab)			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	μ			00		INVERT	NON-INVERT
				01		Schmidt	Prandtl
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	FUNCTION
40		90					KEY
45		95					

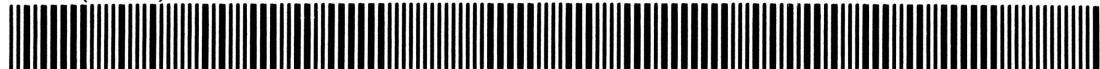
FLUID TRANSPORT NUMBERS  
REYNOLDS NUMBER  
PROGRAM REGISTERS NEEDED: 13

HEWLETT PACKARD  
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CHEMICAL ENGINEERING

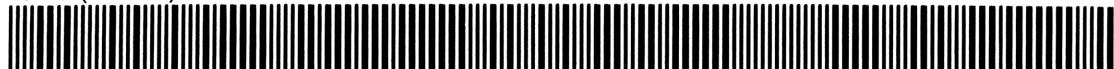
ROW 1 (1 - 5)



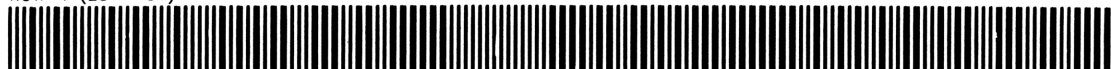
ROW 2 (6 - 14)



ROW 3 (14 - 23)



ROW 4 (23 - 31)



ROW 5 (32 - 42)



ROW 6 (42 - 50)



ROW 7 (50 - 56)



FLUID TRANSPORT NUMBERS  
NUSSELT AND BIOT NUMBERS  
PROGRAM REGISTERS NEEDED: 19

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ROW 1 (1 - 4)



ROW 2 (5 - 8)



ROW 3 (9 - 10)



ROW 4 (11 - 17)



ROW 5 (18 - 25)



ROW 6 (26 - 32)



ROW 7 (33 - 41)



ROW 8 (42 - 51)



ROW 9 (52 - 59)



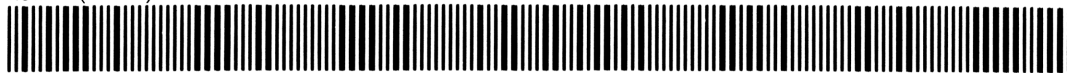
ROW 10 (60 - 65)



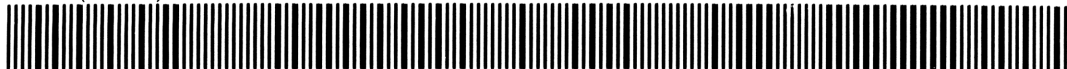
FLUID TRANSPORT NUMBERS  
STANTON AND LEWIS NUMBERS  
PROGRAM REGISTERS NEEDED: 18

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SOLUTION BOOK:  
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ROW 1 (1 - 4)



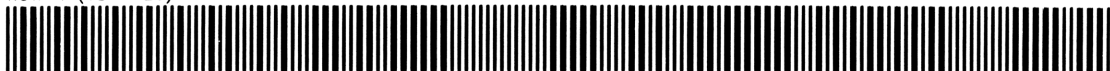
ROW 2 (4 - 10)



ROW 3 (11 - 18)



ROW 4 (18 - 26)



ROW 5 (26 - 32)



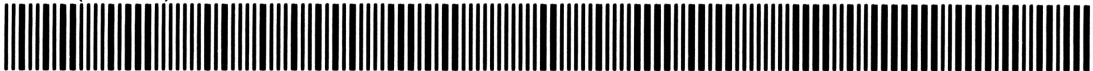
ROW 6 (33 - 40)



ROW 7 (40 - 49)



ROW 8 (50 - 58)



ROW 9 (58 - 66)



ROW 10 (67 - 67)





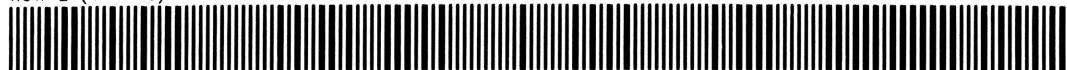
FLUID TRANSPORT NUMBERS  
SCHMIDT AND PRANDTL NUMBERS  
PROGRAM REGISTERS NEEDED: 16

HEWLETT PACKARD  
SOLUTION BOOK:  
CHEMICAL ENGINEERING

ROW 1 (1 - 4)



ROW 2 (4 - 10)



ROW 3 (11 - 18)



ROW 4 (18 - 26)



ROW 5 (26 - 32)



ROW 6 (33 - 40)



ROW 7 (41 - 49)



ROW 8 (50 - 57)



ROW 9 (58 - 59)



# SINGLE STAGE EQUILIBRIUM FLASH CALCULATION

THIS PROGRAM REQUIRES 1 ADDITIONAL MEMORY MODULE

Given the number of components ( $n$ ), the mole fraction ( $z_i$ ), the equilibrium ratio between phases ( $K_i$ ) for each component in the feed and a first guess for the mole ratio ( $V/F$ ), the program will use a second order Newton convergence scheme to converge the Rachford-Rice equation to nearly zero ( $10^{-6}$ ).

$$f(V/F) = \sum_{i=1}^n z_i (K_i - 1) / [(K_i - 1) (V/F) + 1] = 0, \text{ Rachford-Rice Equation}$$

$$(V/F)_{i+1} = (V/F)_i - f[(V/F)_i] / f'[(V/F)_i]$$

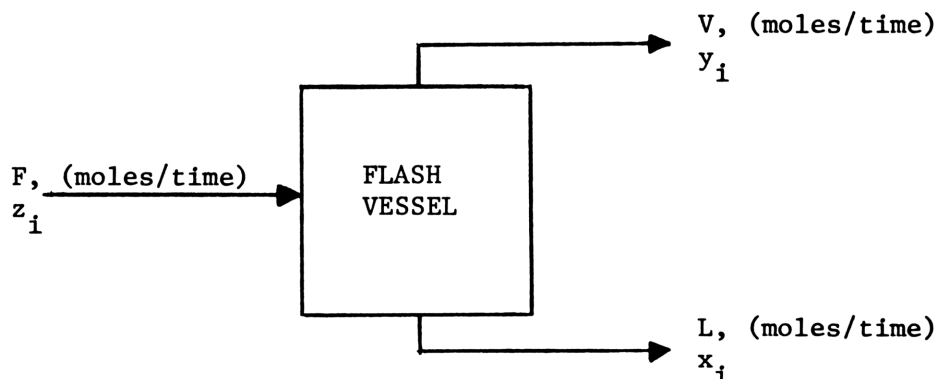
$$f'[(V/F)_i] = - \sum_{i=1}^n z_i (K_i - 1)^2 / [(K_i - 1) (V/F) + 1]^2 \quad \left. \vphantom{\sum_{i=1}^n} \right\} \begin{array}{l} \text{Newton} \\ \text{Convergence} \\ \text{Method} \end{array}$$

Next the program can solve for ( $V/L$ ) and the final compositions of the liquid and the vapor by:  $(V/L) = (V/F) / [1 - (V/F)]$

$$x_i = z_i [1 + (V/L)] / [1 + K_i (V/L)]$$

$$y_i = z_i [1 + (L/V)] / [1 + (1/K_i) (L/V)]$$

Note: Maximum number of components = 10



A five component mixture of hydrocarbons is fed to a steady-state flash vaporization giving product equilibrium at 270°F and 50 psia. The details are given below:

<u>Component</u>	<u><math>K_i</math> @ 270°F &amp; 50 psia</u>	<u><math>z_i</math></u>
$C_3$	12.75	0.15
$C_4$	5.61	0.25
$C_6$	1.40	0.05
$C_7$	0.705	0.30
$C_8$	0.375	0.25

Calculate (V/F) and the composition of both the vapor and the liquid product streams.

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 025

[XEQ] [ALPHA] SSE [ALPHA]

N?

5 [R/S]

K?

12.75 [R/S]

Z?

.15 [R/S]

K?

5.61 [R/S]

Z?

.25 [R/S]

K?

1.4 [R/S]

Z?

.05 [R/S]

K?

.705 [R/S]

Z?

.3 [R/S]

K?

.375 [R/S]

Z?

.25 [R/S]

?

.5 [R/S]

V/F=0.80243

[R/S]

X=0.01438

[R/S]

Y=0.18339

Keystrokes:

[R/S]

[R/S]

[R/S]

[R/S]

[R/S]

[R/S]

[R/S]

[R/S]

Display:

X=0.05320

Y=0.29845

X=0.03785

Y=0.05299

X=0.39304

Y=0.27709

X=0.50153

Y=0.18807

[illegible]

# Program Listings

<pre> 01*LBL "SSE .. 02 CF 02 03 FIX 5 04 "N?" 05 PROMPT 06 1 07 - 08 STO 21 09 STO 23 10*LBL A 11 "K?" 12 PROMPT 13 STO IND 21 14 RCL 21 15 10 16 + 17 "Z?" 18 PROMPT 19 STO IND Y 20 FS? 02 21 GTO C 22 DSE 21 23 GTO A 24 SF 02 25 GTO A 26*LBL c 27 STO 20 28 RCL 23 29 STO 21 30 0 31 STO 24 32*LBL 06 33 XEQ 01 34 DSE 21 35 GTO 06 36 XEQ 01 37 RTN 38*LBL 01 39 RCL 20 40 RCL IND 21 41 1 42 - 43 * 44 1 45 + 46 FS? 00 47 X↑2 </pre>	<p>Initialization</p> <p>-----</p> <p>Prepare for calculation of f(V/F) or f'(V/F)</p> <p>-----</p> <p>Calculate f(V/F)</p> $= \sum_{i=1}^n \frac{Z_i(K_i-1)}{(K_i-1)(V/F)+1}$	<pre> 48 RCL IND 21 49 RCL 21 50 10 51 + 52 RDN 53 RCL IND T 54 X&lt;&gt;Y 55 1 56 - 57 FS? 00 58 X↑2 59 * 60 X&lt;&gt;Y 61 / 62 RCL 24 63 + 64 STO 24 65 RTN 66*LBL 02 67 RCL 20 68 SF 00 69 XEQ c 70 CHS 71 CF 00 72 RTN 73*LBL C 74 "?" 75 FS?C 02 76 PROMPT 77 CF 01 78 STO 20 79 ABS 80 FRC 81 XEQ c 82 STO 22 83 ABS 84 1 E-6 85 X&gt;Y? 86 GTO 04 87 XEQ 02 88 RCL 22 89 X&lt;&gt;Y 90 / 91 RCL 20 92 X&lt;&gt;Y 93 - 94 GTO C 95*LBL 04 96 RCL 20 </pre>	<p>-----</p> <p>set flag 00 so that subroutine c will calc. f'(V/F)</p> <p>-----</p> <p><math>0 \leq (V/F) \leq 1</math></p> <p>-----</p> <p><math> f(V/F)  &lt; 10^{-6}</math></p> <p>-----</p> <p>Adjust by Newtons method</p> <p>-----</p> <p>Display V/F</p>
---	--	--	--

97 "V/F="		144 XEQ d	
98 XEQ d		145 RTN	
99♦LBL D		146♦LBL "V/L	
100 CF 01	Compute the value of Xi then Yi for L = 1 to n	"	Convert V/F to V/L
101 XEQ E		147 SF 01	
102 RCL 23		148♦LBL E	
103 STO 21		149 RCL 20	
104♦LBL 07		150 1	
105 XEQ 05		151 RCL 20	
106 DSE 21		152 -	
107 GTO 07		153 /	
108 XEQ 05		154 STO 24	
109 RTN		155 FC? 01	
110♦LBL 05		156 RTN	
111 RCL IND		157 "V/L="	
21		158 GTO d	
112 RCL 24		159♦LBL "VL"	Compute V and L
113 *		160 "F?"	
114 1		161 PROMPT	
115 +		162 ENTER↑	
116 RCL 24		163 ENTER↑	
117 1		164 RCL 20	
118 +		165 *	
119 X<>Y		166 "V="	
120 /		167 XEQ d	
121 RCL 21		168 -	
122 10		169 "L="	
123 +		170♦LBL d	Display
124 RCL IND		171 ARCL X	
X		172 AVIEW	
125 X<>Y		173 STOP	
126 RDN		174 RTN	
127 *		175 .END.	
128 "X="			
129 XEQ d			
130 RCL IND			
T			
131 1			
132 RCL 24			
133 1/X			
134 +			
135 *	90		
136 RCL 24			
137 1/X			
138 RCL IND			
21			
139 /			
140 1			
141 +			
142 /			
143 "Y="	00		

[illegible]



SINGLE STAGE EQUILIBRIUM  
FLASH CALCULATION  
PROGRAM REGISTERS NEEDED: 46

HEWLETT PACKARD  
SOLUTION BOOK:  
CHEMICAL ENGINEERING

ROW 1 (1 - 4)



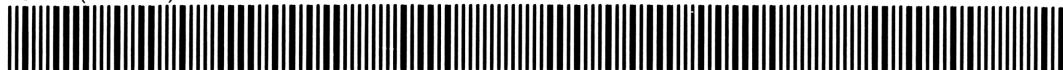
ROW 2 (4 - 11)



ROW 3 (12 - 19)



ROW 4 (19 - 24)



ROW 5 (25 - 31)



ROW 6 (31 - 37)



ROW 7 (38 - 47)



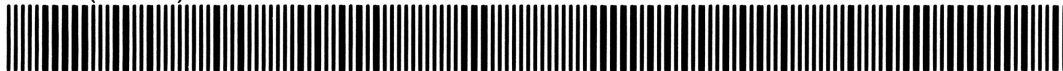
ROW 8 (48 - 56)



ROW 9 (57 - 66)



ROW 10 (67 - 73)



ROW 11 (74 - 81)



ROW 12 (81 - 87)



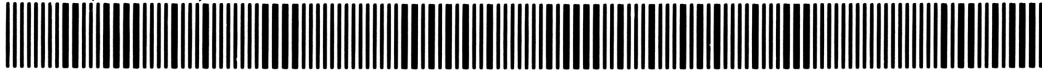
ROW 13 (87 - 95)



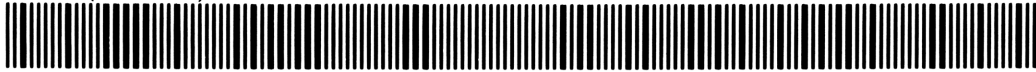
ROW 14 (96 - 100)



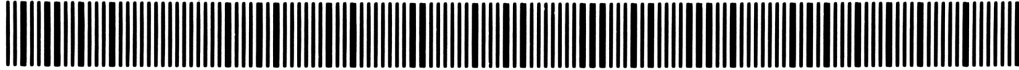
ROW 15 (100 - 106)



ROW 16 (106 - 113)



ROW 17 (114 - 123)



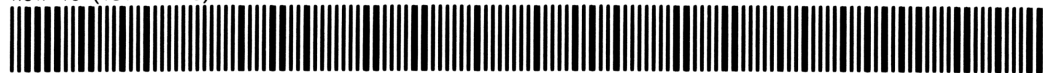
ROW 18 (124 - 130)



SINGLE STAGE EQUILIBRIUM  
FLASH CALCULATION

HEWLETT PACKARD  
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ROW 19 (131 - 140)



ROW 20 (141 - 146)



ROW 21 (146 - 152)



ROW 22 (153 - 158)



ROW 23 (158 - 163)



ROW 24 (164 - 169)



ROW 25 (170 - 175)



## WEAK ACID/BASE TITRATION CURVE

THIS PROGRAM REQUIRES 1 ADDITIONAL MEMORY MODULE

This program concerns the titration of weak acids  $H_4A$ ,  $H_3A$ ,  $H_2A$  and  $HA$ , and weak bases  $A(OH)_4$ ,  $A(OH)_3$ ,  $A(OH)_2$  and  $AOH$ . Given the dissociation constants  $K_n$ , and the beginning volume and molarity ( $V$  and  $M$ ) of the acid or base being titrated, and the normality ( $N$ ) of the titrant, the pH of the solution can be calculated for different volumes of titrant added. Since an iterative technique is being used, an initial guess for pH must be supplied. If it is a base that is being titrated then the main routine calculates pOH; however, pOH is converted to pH for display.

### References:

Breneman, G.L., "A General Acid-Base Titration Curve Computer Program," Journal of Chemical Education; vol. 51, pp. 812-813.

### Example:

For phosphoric acid,  $H_3PO_4$ ,  $K_1 = 7.5 \times 10^{-3}$ ,  $K_2 = 6.2 \times 10^{-8}$  and  $K_3 = 1 \times 10^{-12}$ . Plot a titration curve from 0 to 75 ml of 0.500 N NaOH added to 50.00 ml of 0.200 M  $H_2PO_4$ .

Solution(s): For a complete solution for purposes of a plot, calculations of the pH at approximately 45 different titrant volumes are required. For purposes of illustration the following 15 calculations will suffice:

### Keystrokes:

### Display:

[USER]	(set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 026	
[XEQ] [ALPHA] A/B [ALPHA]	ACID Y/N
Y [R/S]	K?
7.5 [EEX] [CHS] 3 [R/S]	K?
6.2 [EEX] [CHS] 8 [R/S]	K?
[EEX] [CHS] 12 [R/S]	K?
[A]	V?
50 [R/S]	M?
.2 [R/S]	N?
.5 [R/S]	INIT. GUESS
[R/S]	VOLUME ADDED
0 [R/S]	PH=1.454

## Keystrokes:

[R/S]  
10 [R/S]  
[R/S]  
15 [R/S]  
[R/S]  
19.4 [R/S]  
[R/S]  
20 [R/S]  
[R/S]  
20.4 [R/S]  
[R/S]  
21 [R/S]  
[R/S]  
25 [R/S]  
[R/S]  
35 [R/S]  
[R/S]  
39 [R/S]  
[R/S]  
39.8 [R/S]  
[R/S]  
40.1 [R/S]  
[R/S]  
40.8 [R/S]  
[R/S]  
45 [R/S]  
[R/S]  
75 [R/S]

## Display:

VOLUME ADDED  
PH=2.192  
VOLUME ADDED  
PH=2.637  
VOLUME ADDED  
PH=3.654  
VOLUME ADDED  
PH=4.677  
VOLUME ADDED  
PH=5.527  
VOLUME ADDED  
PH=5.930  
VOLUME ADDED  
PH=6.731  
VOLUME ADDED  
PH=7.685  
VOLUME ADDED  
PH=8.483  
VOLUME ADDED  
PH=9.142  
VOLUME ADDED  
PH=9.832  
VOLUME ADDED  
PH=10.584  
VOLUME ADDED  
PH=11.457  
VOLUME ADDED  
PH=12.845

# User Instructions

				SIZE: 026
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Load program and set USER mode		[USER]	
2	Begin execution:		[XEQ] A/B	ACID Y/N
	if acid	Y	[R/S]	K?
	if base	N	[R/S]	K?
3	Input $K_1$ , $K_2$ , $K_3$ and $K_4$ as needed	$K_1$	[R/S]	K?
		$K_2$	[R/S]	K?
		$K_3$	[R/S]	K?
		$K_4$	[R/S]	K?
4	When all K's are input, continue		[A]	V?
		V	[R/S]	M?
		<u>M</u>	[R/S]	N?
		<u>N</u>	[R/S]	INIT. GUESS
5	Begin calculations:			
	input guess for pH*	pHest	[R/S]	VOLUME ADDED
	input volume of titrant added	V	[R/S]	PH =
6	Repeat step 5			
*	A guess for pH need not be entered IF:			
	1) The volume of titrate is going to be			
	zero			
	OR			
	2) The pH in the display left over from			
	the last problem is suitable.			

# Program Listings

<pre> 01♦LBL "A/B " 02 FIX 3 03 "ACID Y/ N" 04 AON 05 PROMPT 06 AOFF 07 ASTO X 08 "Y" 09 ASTO Y 10 CF 00 11 X=Y? 12 SF 00 13 CLRG 14♦LBL E 15 1 16 ST+ 25 17 "K?" 18 PROMPT 19 STO IND 25 20 GTO E 21♦LBL A 22 "V?" 23 PROMPT 24 STO 23 25 "M?" 26 PROMPT 27 * 28 STO 24 29 "N?" 30 PROMPT 31 STO 21 32 RCL 25 33 1 34 + 35 STO 00 36 "INIT. G UESS" 37 PROMPT 38♦LBL B 39 "VOLUME ADDED" 40 PROMPT 41 CF 00 42 X=0? 43 SF 00 44 RCL 21 45 X&lt;&gt;Y 46 * </pre>	<pre> Initialization </pre> <hr/> <pre> Initialize for coefficients </pre>	<pre> 47 LASTX 48 RCL 23 49 + 50 / 51 STO 20 52 RCL 24 53 LASTX 54 / 55 STO 22 56 R↑ 57 STO 08 58 RCL 00 59 STO 07 60♦LBL c 61 RCL 07 62 .5 63 + 64 STO 25 65 ISG 25 66 RCL IND 25 67 RCL 20 68 + 69 .5 70 ST- 25 71 RDN 72 DSE 25 73 RCL 25 74 RCL 22 75 * 76 - 77 RCL IND 25 78 * 79 E-14 80 - 81♦LBL b 82 DSE 25 83 GTO 00 84 RCL 07 85 X&lt;&gt; 25 86 X&lt;&gt;Y 87 RCL 25 88 10 89 + 90 RDN 91 STO IND T 92 DSE 07 93 GTO c 94 RCL 00 </pre>	<pre> ----- [Na<sup>+</sup>] → R<sub>20</sub> ----- c → R<sub>22</sub> pH<sub>est</sub> → R<sub>08</sub> ----- Calculate coefficients </pre>
---	--	--	--

# Program Listings

95 STO 25		144 RCL 14	
96 RCL 01		145 XEQ 07	
97 RCL 20		146 RCL 15	
98 +		147♦LBL 09	
99 STO 10		148 +	
100 RCL 01		149 RCL 16	
101 RCL 22		150 /	
102 *		151 -	
103 SQRT		152 X<0?	
104 FS?C 02		153 GTO a	
105 GTO 01		154 STO 09	
106 GTO B		155 %CH	
107♦LBL 00		156 ABS	
108 RCL IND		157 1	
25		158 X<=Y?	
109 *		159 SF 02	
110 GTO b		160 RCL 09	
111♦LBL a	-----	161 FS?C 02	
112 2	Change pH <sub>est</sub>	162 GTO 01	
113 FS? 00	by ± 2	163 LOG	
114 CHS		164 CHS	
115 ST+ 08		165 XEQ d	-----
116♦LBL B		166 "PH="	Display
117 RCL 08		167 ARCL X	
118 XEQ d		168 AVIEW	
119 CHS		169 STOP	
120 10↑X		170 GTO B	
121♦LBL 01		171♦LBL d	-----
122 ENTER↑		172 FS? 00	Convert to base
123 ENTER↑		173 RTN	
124 GTO IND		174 14	
25		175 X<>Y	
125♦LBL 05	-----	176 -	
126 6	start forming	177 RTN	
127 *	f'([H <sup>+</sup> ])	178♦LBL 06	-----
128 RCL 10		179 *	Common routine
129 5		180♦LBL 07	
130 XEQ 06		181 +	
131 RCL 11		182 *	
132 4		183 RTN	
133 XEQ 06		184♦LBL 08	
134 RCL 12		185 +	
135 3		186 STO 16	
136 XEQ 06		187 CLX	
137 RCL 13		188 RCL 10	
138 2		189 XEQ 07	
139 XEQ 06		190 RCL 11	
140 RCL 14		191 XEQ 07	
141 XEQ 08		192 RCL 12	
142 RCL 13		193 FS?C 02	
143 XEQ 07		194 GTO 09	

# Program Listings

195 GTO 07	----- f' [ (H <sup>+</sup> ) ]	51	
196♦LBL 04			
197 5			
198 *			
199 RCL 10			
200 4			
201 XEQ 06			
202 RCL 11			
203 3			
204 XEQ 06		60	
205 RCL 12			
206 2			
207 XEQ 06			
208 RCL 13			
209 XEQ 08			
210 RCL 13			
211 XEQ 07			
212 RCL 14			
213 GTO 09			
214♦LBL 03		70	
215 4			
216 *			
217 RCL 10			
218 3			
219 XEQ 06			
220 RCL 11			
221 2			
222 XEQ 06			
223 RCL 12			
224 XEQ 08		80	
225 RCL 13			
226 GTO 09			
227♦LBL 02			
228 3			
229 *			
230 RCL 10			
231 2			
232 XEQ 06			
233 RCL 11			
234 SF 02		90	
235 GTO 08			
236 END			
50		00	





## WEAK ACID/BASE TITRATION CURVE

PROGRAM REGISTERS NEEDED: 59

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CHEMICAL ENGINEERING

ROW 1 (1 - 3)



ROW 2 (3 - 9)



ROW 3 (9 - 17)



ROW 4 (17 - 22)



ROW 5 (23 - 29)



ROW 6 (30 - 36)



ROW 7 (36 - 39)



ROW 8 (39 - 41)



ROW 9 (42 - 51)



ROW 10 (51 - 60)



ROW 11 (61 - 68)



ROW 12 (69 - 76)



ROW 13 (77 - 83)



ROW 14 (83 - 91)



ROW 15 (92 - 99)



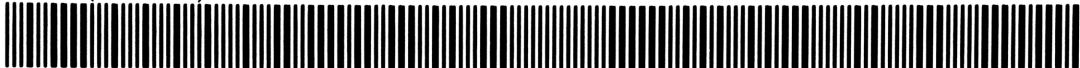
ROW 16 (100 - 107)



ROW 17 (108 - 115)



ROW 18 (115 - 124)



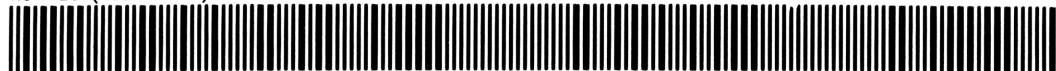
## WEAK ACID/BASE TITRATION CURVE

HEWLETT PACKARD  
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CHEMICAL ENGINEERING

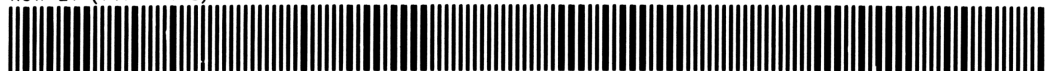
ROW 19 (124 - 133)



ROW 20 (133 - 141)



ROW 21 (141 - 148)



ROW 22 (149 - 158)



ROW 23 (159 - 166)



ROW 24 (166 - 172)



ROW 25 (172 - 183)



ROW 26 (184 - 191)



ROW 27 (192 - 201)



ROW 28 (201 - 208)



ROW 29 (209 - 216)



ROW 30 (217 - 224)



ROW 31 (224 - 233)



ROW 32 (234 - 236)



NOTES

## **Hewlett-Packard Software**

In terms of power and flexibility, the problem-solving potential of the HP-41 programmable calculator is nearly limitless. And in order to see the practical side of this potential, HP has different types of software to help save you time and programming effort. Every one of our software solutions has been carefully selected to effectively increase your problem-solving potential. Chances are, we already have the solutions you're looking for.

## **Application Pacs**

To increase the versatility of your HP-41, HP has an extensive library of "Application Pacs". These programs transform your HP-41 into a specialized calculator in seconds. Included in these pacs are detailed manuals with examples, miniature plug-in Application Modules, and keyboard overlays. Every Application Pac has been designed to extend the capabilities of the HP-41.

You can choose from:

**Aviation (Pre-Flight Only) 00041-15018**  
**Clinical Lab 00041-15024**  
**Circuit Analysis 00041-15024**  
**Financial Decisions 00041-15004**  
**Mathematics 00041-15003**  
**Structural Analysis 00041-15021**  
**Surveying 00041-15005**  
**Securities 00041-15026**

**Statistics 00041-15002**  
**Stress Analysis 00041-15027**  
**Games 00041-15022**  
**Home Management 00041-15023**  
**Machine Design 00041-15020**  
**Navigation 00041-15017**  
**Real Estate 00041-15016**  
**Thermal and Transport Science 00041-15019**  
**Petroleum Fluids 00041-15039**

## **Users' Library**

The Users' Library provides the best programs from contributors and makes them available to you. By subscribing to the HP-41 Users' Library you'll have at your fingertips literally hundreds of different programs from many different application areas.

## **\*Users' Library Solutions Books**

Hewlett-Packard offers a wide selection of Solutions Books complete with user instructions, examples, and listings. These solution books will complement our other software offerings and provide you with a valuable tool for program solutions.

You can choose from:

**Business Stat/Marketing/Sales 00041-90094**  
**Home Construction Estimating 00041-90096**  
**Lending, Saving and Leasing 00041-90086**  
**Real Estate 00041-90136**  
**Small Business 00041-90137**  
**Geometry 00041-90084**  
**High-Level Math 00041-90083**  
**Test Statistics 00041-90082**  
**Antennas 00041-90093**  
**Chemical Engineering 00041-90100**  
**Control Systems 00041-90092**  
**Electrical Engineering 00041-90088**  
**Fluid Dynamics and Hydraulics 00041-90139**  
**Games II 00041-90443**

**Civil Engineering 00041-90089**  
**Heating, Ventilating & Air Conditioning 00041-90140**  
**Mechanical Engineering 00041-90090**  
**Solar Engineering 00041-90138**  
**Calendars 00041-90145**  
**Cardiac/Pulmonary 00041-90097**  
**Chemistry 00041-90102**  
**Games 00041-90099**  
**Optometry I (General) 00041-90143**  
**Optometry II (Contact Lens) 00041-90144**  
**Physics 00041-90142**  
**Surveying 00041-90141**  
**Time Module Solutions 00041-90395**

\*Some books require additional memory modules to accommodate all programs.

## **CHEMICAL ENGINEERING**

STRAIGHT FIN EFFICIENCY  
CONSERVATION OF ENERGY  
HYDROCARBON COMBUSTION  
HEAT TRANSFER THROUGH COMPOSITE CYLINDERS AND WALLS  
VON KÁRMÁN ANALOGY FOR HEAT AND MASS TRANSFER  
EQUATIONS OF STATE  
REVERSIBLE POLYTROPIC PROCESS FOR AN IDEAL GAS  
CONDUIT FLOW  
FLUID TRANSPORT NUMBERS  
SINGLE STAGE EQUILIBRIUM FLASH CALCULATION  
WEAK ACID/BASE TITRATION CURVE



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