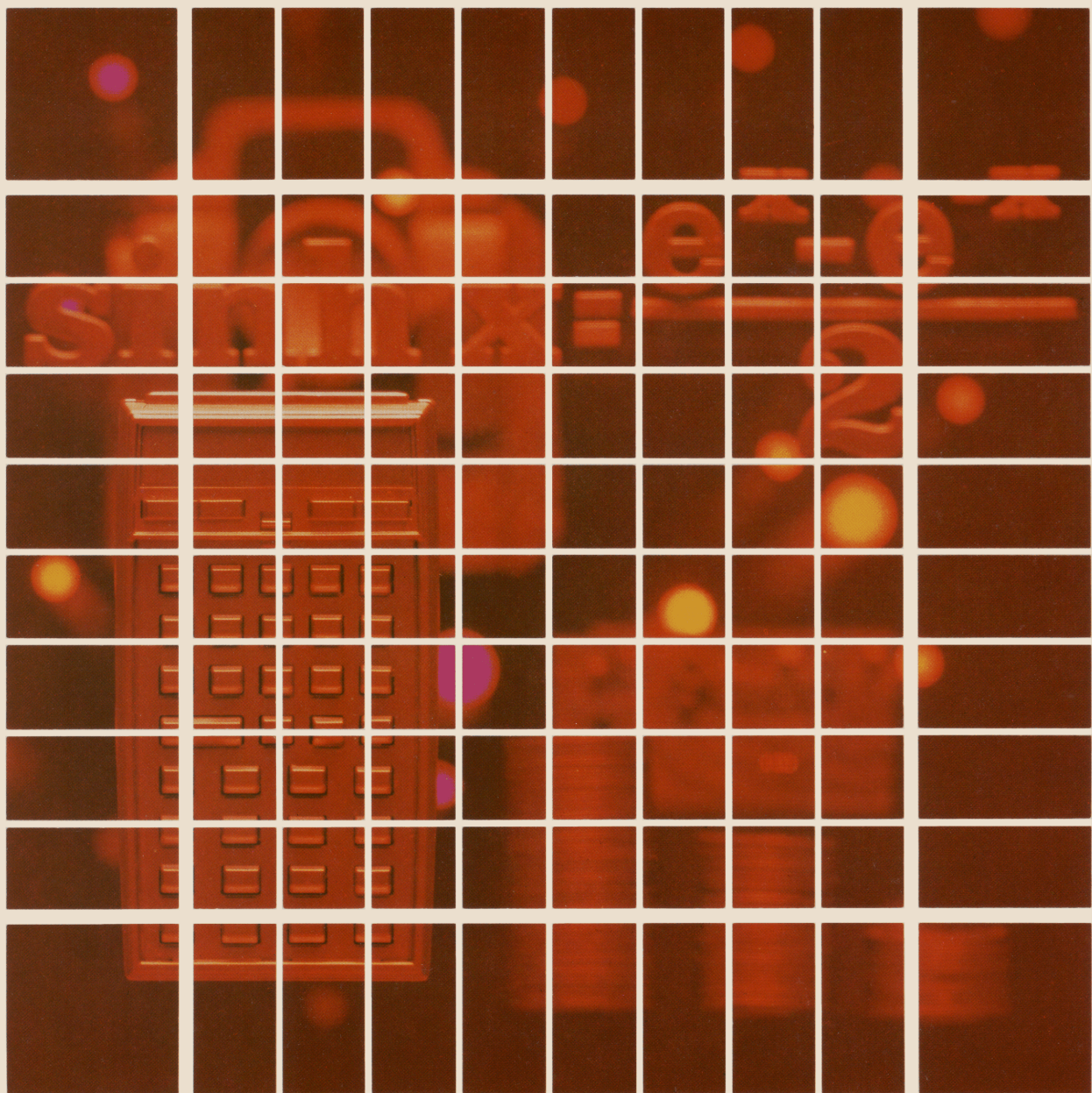


Includes barcode for easy software entry.

HEWLETT-PACKARD

HP-41

USERS' LIBRARY SOLUTIONS
Test Statistics



NOTICE

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INTRODUCTION

This HP-41C Solutions book was written to help you get the most from your calculator. The programs were chosen to provide useful calculations for many of the common problems encountered.

They will provide you with immediate capabilities in your everyday calculations and you will find them useful as guides to programming techniques for writing your own customized software. The comments on each program listing describe the approach used to reach the solution and help you follow the programmer's logic as you become an expert on your HP calculator.

KEYING A PROGRAM INTO THE HP-41C

There are several things that you should keep in mind while you are keying in programs from the program listings provided in this book. The output from the HP 82143A printer provides a convenient way of listing and an easily understood method of keying in programs without showing every keystroke. This type of output is what appears in this handbook. Once you understand the procedure for keying programs in from the printed listings, you will find this method simple and fast. Here is the procedure:

- At the end of each program listing is a listing of status information required to properly execute that program. Included is the SIZE allocation required. Before you begin keying in the program, press **XEQ** **ALPHA** **SIZE** **ALPHA** and specify the allocation (three digits; e.g., 10 should be specified as 010).
Also included in the status information is the display format and status of flags important to the program. To ensure proper execution, check to see that the display status of the HP-41C is set as specified and check to see that all applicable flags are set or clear as specified.
- Set the HP-41C to PRGM mode (press the **PRGM** key) and press **■** **GTO** **■** **■** to prepare the calculator for the new program.
- Begin keying in the program. Following is a list of hints that will help you when you key in your programs from the program listings in this handbook.
 - When you see " (quote marks) around a character or group of characters in the program listing, those characters are ALPHA. To key them in, simply press **ALPHA**, key in the characters, then press **ALPHA** again. So "SAMPLE" would be keyed in as **ALPHA** "SAMPLE" **ALPHA**.
 - The diamond in front of each LBL instruction is only a visual aid to help you locate labels in the program listings. When you key in a program, ignore the diamond.
 - The printer indication of divide sign is /. When you see / in the program listing, press **÷**.
 - The printer indication of the multiply sign is \times . When you see \times in the program listing, press **×**.
 - The \vdash character in the program listing is an indication of the **APPEND** function. When you see \vdash , press **■** **APPEND** in ALPHA mode (press **■** and the K key).
 - All operations requiring register addresses accept those addresses in these forms:
nn (a two-digit number)
IND nn (INDIRECT: **■**, followed by a two-digit number)
X, Y, Z, T, or L (a STACK address: **■** followed by X, Y, Z, T, or L)
IND X, Y, Z, T or L (INDIRECT stack: **■** **■** followed by X, Y, Z, T, or L)

Indirect addresses are specified by pressing **■** and then the indirect address. Stack addresses are specified by pressing **■** followed by X, Y, Z, T, or L. Indirect stack addresses are specified by pressing **■** **■** and X, Y, Z, T, or L.

Printer Listing	Keystrokes	Display
01 ♦ LBL "SAMPLE"	■ LBL ALPHA SAMPLE ALPHA	01 \uparrow LBL \uparrow SAMPLE
02 "THIS IS A"	ALPHA THIS IS A ALPHA	02 \uparrow THIS IS A
03 \vdash SAMPLE	ALPHA ■ APPEND SAMPLE	03 \uparrow \vdash SAMPLE
04 AVIEW	■ AVIEW ALPHA	04 AVIEW
05 6	6	05 6
06 ENTER \uparrow	ENTER \uparrow	06 ENTER \uparrow
07 -2	2 CHS	07 -2
08 /	÷	08 /
09 ABS	XEQ ALPHA ABS ALPHA	09 ABS
10 STO IND L	STO ■ ■ L	10 STO IND L
11 "R3="	ALPHA R3= ■ ARCL 03	11 \uparrow R3=
12 ARCL 03	■ AVIEW	12 ARCL 03
13 AVIEW	ALPHA	13 AVIEW
14 RTN	■ RTN	14 RTN

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1.	ONE SAMPLE TEST STATISTICS FOR THE MEAN	1
	Calculates the z statistic for testing the mean if the variance is known. If the variance is unknown, then the t statistic is calculated.	
2.	TEST STATISTICS FOR THE CORRELATION COEFFICIENT	6
	The t statistic can be used to test if the true correlation coefficient is zero. The z statistic, which can be used to test if the correlation coefficient equals a given number (usually non-zero) is also calculated.	
3.	DIFFERENCES AMONG PROPORTIONS	10
	Calculates the chi-square statistic for testing if several independent binomial distributions have equal means.	
4.	BEHRENS-FISHER STATISTIC	17
	Given random samples from two independent normal populations with unequal variances (unknown), this program calculates the Behren-Fisher statistic for testing the means.	
5.	KRUSKAL-WALLIS STATISTIC	23
	The Kruskal-Wallis statistic can be used to test if the independent random samples come from identical continuous population.	
6.	MEAN-SQUARE SUCCESSIVE DIFFERENCE	29
	The mean-square successive difference is used to test if a given sample is random. Suppose the sample size is large and the population is normal, then a z statistic is used instead.	
7.	THE RUN TEST FOR RANDOMNESS	34
	For a given sequence, the z statistic is calculated for testing the randomness of the sequence.	
8.	INTRAClass CORRELATION COEFFICIENT	40
	Calculates the intraclass correlation coefficient which measures the degree of association among individuals within classes or groups.	
9.	FISHER'S EXACT TEST FOR A 2 X 2 CONTINGENCY TABLE	47
	Fisher's exact probability test is used to analyze a 2 x 2 contingency table when the two independent samples are small in size.	

10. BARTLETT'S CHI-SQUARE STATISTIC 55
This chi-square statistic can be used to test the
homogeneity of variances. Error corrector for erroneous
input data is provided.
11. MANN-WHITNEY STATISTIC 61
Calculates the Mann-Whitney statistic on two independent
samples of equal or unequal sizes. Error corrector for
erroneous input data is provided.
12. KENDALL'S COEFFICIENT OF CONCORDANCE 73
Calculates Kendall's coefficient of concordance to test
agreement between rankings. Error corrector for erroneous
input data is provided.

ONE SAMPLE TEST STATISTICS FOR THE MEAN

Suppose $\{x_1, x_2, \dots, x_n\}$ is a sample from a normal population with a known variance σ^2 and unknown mean μ . A test of the null hypothesis

$$H_0: \mu = \mu_0$$

is based on the z statistic which has a standard normal distribution.

If the variance σ^2 is unknown then the t statistic, which has the t distribution with $n - 1$ degrees of freedom, is used instead.

Equations:

$$z = \frac{\sqrt{n} (\bar{x} - \mu_0)}{\sigma}$$

$$t = \frac{\sqrt{n} (\bar{x} - \mu_0)}{s}$$

where \bar{x} and s are sample mean and sample standard deviation.

Remark: $n > 1$.

Reference: This program is a translation of the HP-65 Stat Pac 2 program.

Example:

Calculate the z and the t statistics for the following set of data if $\mu_0 = 2$ and $\sigma = 1$.

{2.73, 0.45, 2.52, 1.19, 3.51}

Keystrokes:

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] ONEST [ALPHA]

2.73 [Σ+] .45 [Σ+] 2.52 [Σ+]

1.19 [Σ+] 3.51 [Σ+]

[R/S]

2 [R/S]

1 [R/S]

[R/S]

[R/S]

[R/S]

Display:

ONE SAMPLE T.

5.00

MU NAUGHT ?

SIGMA ?

Z=0.18

T=0.14

XBAR=2.08

S=1.24

[illegible]

Program Listings

01*LBL "ONE	Initialize	51	
ST"			
02 FIX 2			
03 CLRG			
04 ΣREG 00			
05 "ONE SAM			
PLE T."			
06 AVIEW			
07 STOP			
08*LBL E			
09 "MU NAUG	Store μ_0 and σ and make calculations	60	
HT ?"			
10 PROMPT			
11 STO 06			
12 "SIGMA ?			
"			
13 PROMPT			
14 STO 07			
15 MEAN			
16 RCL 06			
17 -		70	
18 RCL 05			
19 SQRT			
20 *			
21 STO 08			
22 RCL 07			
23 /			
24 "Z"			
25 XEQ 11			
26 SDEV			
27 RCL 08		80	
28 X<>Y			
29 /			
30 "T"			
31 XEQ 11			
32 MEAN			
33 "XBAR"			
34 XEQ 11			
35 SDEV			
36 "S"			
37 XEQ 11		90	
38 XEQ E			
39*LBL 11	Display subroutine		
40 "F="			
41 ARCL X			
42 AVIEW			
43 STOP			
44 RTN			
45 .END.			
50		00	

ONE SAMPLE TEST
STATISTICS FOR THE MEAN
PROGRAM REGISTERS NEEDED: 16

ROW 1 (1 - 4)



ROW 2 (4 - 5)



ROW 3 (5 - 9)



ROW 4 (9 - 12)



ROW 5 (12 - 23)



ROW 6 (24 - 31)



ROW 7 (31 - 36)



ROW 8 (37 - 42)



ROW 9 (43 - 45)



TEST STATISTICS FOR THE CORRELATION COEFFICIENT

Under the assumptions of normal correlation analysis, the t statistic, which has the t distribution with $n - 2$ degrees of freedom, can be used to test the null hypothesis that the true correlation coefficient $\rho = 0$.

To test the null hypothesis $\rho = \rho_0$, where ρ_0 is a given number, the z statistic is used. z has approximately the standard normal distribution.

Equations:

$$t = \frac{r \sqrt{n-2}}{\sqrt{1-r^2}}$$

$$z = \frac{\sqrt{n-3}}{2} \ln \left[\frac{(1+r)(1-\rho_0)}{(1-r)(1+\rho_0)} \right]$$

where r is an estimate (based on a sample of size n) of the correlation coefficient ρ .

- Remarks:
1. This program requires that $n > 3$, $|r| < 1$ and $|\rho_0| < 1$; otherwise "DATA ERROR" will result.
 2. Usually, the z statistic is used when the sample size is large.

- References:
1. Hogg and Craig, Introduction to Mathematical Statistics, Macmillan and Co., 1970.
 2. J. Freund, Mathematical Statistics, Prentice-Hall, 1971.
 3. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

Given $r = 0.12$, $n = 31$, and $\rho_0 = 0$, find t and z.

Keystrokes:

Display:

[USER]

(set USER mode)

[XEQ] [ALPHA] SIZE [ALPHA] 003

[XEQ] [ALPHA] CORRTS [ALPHA]

COR. COEF. T.S.

N ?

31 [R/S]

R ?

.12 [R/S]

T=0.65

[E]

RHO NAUGHT ?

0 [R/S]


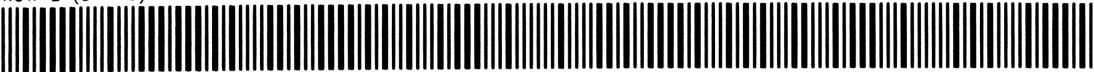

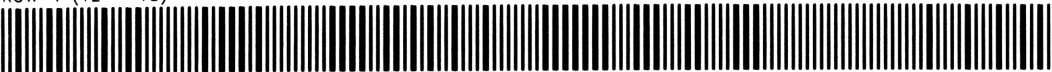







Z=0.64

[illegible]

Line	Code	Comment	Address	Value
01	LBL "COR		49	/
02	RTS"		50	LN
03	FIX 2	Initialize	51	RCL 01
04	"COR. CO		52	3
05	EF. T.S."		53	-
06	AVIEW		54	SQRT
07	PSE		55	*
08	"N ?"		56	2
09	PROMPT		57	/
10	STO 01		58	"Z"
11	3	n	59	LBL 11
12	X<>Y	Test n > 3?	60	"I="
13	X<=Y?		61	ARCL X
14	GTO 09		62	AVIEW
15	"R ?"	r	63	STOP
16	PROMPT	Test r < 1?	64	RTN
17	STO 00		65	LBL 00
18	XEQ 00		66	ABS
19	RCL 01		67	1
20	2		68	X<>Y
21	-		69	X>Y?
22	1		70	GTO 09
23	RCL 00		71	RTN
24	X↑2		72	LBL 09
25	-		73	0
26	/	Calculate t	74	/
27	SQRT		75	.END.
28	RCL 00			
29	*			
30	"T"			
31	GTO 11		80	
32	LBL E			
33	"RHO NAU			
34	GHT ?"			
35	PROMPT			
36	STO 02	Test ρ ₀ < 1		
37	XEQ 00			
38	RCL 00			
39	1			
40	+			
41	1		90	
42	RCL 00			
43	-			
44	/			
45	1			
46	RCL 02	Calculate z		
47	-			
48	*			
49	1			
50	RCL 02			
51	+			
52			00	

DATA REGISTERS				STATUS			
00	r	50		SIZE <u>003</u> TOT. REG. <u>21</u> USER MODE			
	n			ENG _____ FIX <u>2</u> SCI _____ ON <u>X</u> OFF _____			
	ρθ			DEG _____ RAD _____ GRAD _____			
				FLAGS			
05		55		#	INIT S/C	SET INDICATES	CLEAR INDICATES
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90					
45		95					

TEST STATISTICS FOR
THE CORRELATION COEFFICIENT
PROGRAM REGISTERS NEEDED: 19

ROW 1 (1 - 3)	
ROW 2 (3 - 3)	
ROW 3 (3 - 11)	
ROW 4 (12 - 18)	
ROW 5 (19 - 29)	
ROW 6 (30 - 31)	
ROW 7 (31 - 40)	
ROW 8 (41 - 53)	
ROW 9 (54 - 62)	
ROW 10 (63 - 74)	
ROW 11 (75 - 75)	

DIFFERENCES AMONG PROPORTIONS

Suppose x_1, x_2, \dots, x_k are observed values of a set of independent random variables having binomial distributions with parameters n_i and θ_i ($i = 1, 2, \dots, k$).

A chi-square statistic χ^2 can be used to test the null hypothesis $\theta_1 = \theta_1 = \dots = \theta_k$. The χ^2 statistic has the chi-square distribution with $k - 1$ degrees of freedom.

Equations:

$$\chi^2 = \sum_{i=1}^k \frac{(x_i - n_i \hat{\theta})^2}{n_i \hat{\theta} (1 - \hat{\theta})} = \sum_{i=1}^k n_i \left[\frac{1}{\sum_{i=1}^k x_i} \sum_{i=1}^k \frac{x_i^2}{n_i} + \frac{1}{\sum_{i=1}^k (n_i - x_i)} \sum_{i=1}^k \frac{(n_i - x_i)^2}{n_i} - 1 \right]$$

where

$$\hat{\theta} = \sum_{i=1}^k x_i / \sum_{i=1}^k n_i$$

- References:
1. J. Freund, Mathematical Statistics, Prentice-Hall, 1971.
 2. This program is a translation of the HP-65 State Pac 2 program.

Example:

	n_i	x_i
Sample 1	400	232
Sample 2	500	260
Sample 3	400	197

Keystrokes:

[USER]
[XEQ] [ALPHA] SIZE [ALPHA] 010
[XEQ] [ALPHA] DIFF [ALPHA]

400 [R/S]
232 [R/S]
500 [R/S]
260 [R/S]
400 [R/S]
197 [R/S]
[E]
[R/S]
[R/S]

Display:

(set USER mode)

DIFF. A. PROPS
N1 ?
X1 ?
N2 ?
X2 ?
N3 ?
X3 ?
N4 ?
CHI-SQ=6.47
dF=2.00
THETA=0.53

[illegible]

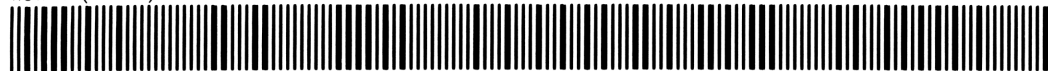
01♦LBL "DIF F"		50 ST+ 06	
02 FIX 2	Initialize	51 FC?C 00	
03 CLRG		52 GT0 A	
04 CF 00		53 1	
05 CF 29		54 ST- 03	
06 "DIFF. A PROPS"		55 GT0 A	
07 AVIEW		56♦LBL E	
08 PSE		57 RCL 05	Calculate y^2
09 GT0 A		58 RCL 01	
10♦LBL C		59 /	
11 SF 00	For corrections	60 RCL 06	
12♦LBL A		61 RCL 02	
13 1		62 /	
14 FS? 00		63 +	
15 CHS		64 1	
16 ST+ 03		65 -	
17 "N"		66 RCL 01	
18 XEQ 12	n_1	67 RCL 02	
19 STO 07		68 +	
20 "X"		69 *	
21 XEQ 12	x_1	70 "CHI-SQ"	
22 STO 08		71 XEQ 11	Calculate df
23 FS? 00		72 RCL 03	
24 CHS		73 2	
25 ST+ 01		74 -	
26 ABS		75 "dF"	
27 -		76 XEQ 11	
28 STO 04		77 RCL 01	
29 FS? 00	accumulate sums	78 RCL 01	Calculate $\hat{\theta}$
30 CHS		79 RCL 02	
31 ST+ 02		80 +	
32 ABS		81 /	
33 RCL 08		82 "THETA"	
34 +		83♦LBL 11	
35 STO 09		84 "f="	
36 RCL 08		85 ARCL X	Display result routine
37 X↑2		86 AVIEW	
38 X<>Y		87 STOP	
39 /		88 RTN	
40 FS? 00		89♦LBL 12	
41 CHS		90 FIX 0	Display input routine
42 ST+ 05		91 "f"	
43 ABS		92 ARCL 03	
44 RCL 04		93 "f ?"	
45 X↑2		94 AVIEW	
46 RCL 09		95 FIX 2	
47 /		96 STOP	
48 FS? 00		97 RTN	
49 CHS		98 .END.	

[illegible]

DIFFERENCES AMONG PROPORTIONS

PROGRAM REGISTERS NEEDED: 26

ROW 1 (1 - 4)



ROW 2 (5 - 6)



ROW 3 (6 - 11)



ROW 4 (12 - 18)



ROW 5 (19 - 26)



ROW 6 (27 - 37)



ROW 7 (38 - 48)



ROW 8 (48 - 55)



ROW 9 (55 - 65)



ROW 10 (66 - 71)



ROW 11 (71 - 79)



ROW 12 (80 - 85)



ROW 13 (85 - 93)



ROW 14 (93 - 98)



BEHRENS-FISHER STATISTIC

Suppose $\{x_1, x_2, \dots, x_{n_1}\}$ and $\{y_1, y_2, \dots, y_{n_2}\}$ are independent random samples from two normal populations having means μ_1, μ_2 (unknown). If the variances σ_1^2, σ_2^2 cannot be assumed equal, then the Behrens-Fisher statistic d is used instead of the t statistic to test the null hypothesis

$$H_0 : \mu_1 - \mu_2 = D$$

Equation:

$$d = \frac{\bar{x} - \bar{y} - D}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

where \bar{x}, \bar{y} and s_1^2, s_2^2 are sample means and variances.

Critical values of this test are tabulated in the Fisher-Yates Tables for various values of n_1, n_2, α and θ , where α is the level of significance and

$$\theta = \tan^{-1} \left(\frac{s_1}{s_2} \sqrt{\frac{n_2}{n_1}} \right)$$

Remark: $n_1 > 1, n_2 > 1$.

- References:
1. Fisher and Yates, Statistical Tables for Biological, Agricultural and Medical Research, Hafner, Publishing Co., 1970.
 2. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

Calculate the Behrens-Fisher statistic for $D = 0$.

x:	79,	84,	108
y:	91,	103,	90, 113, 108

Keystrokes:

[USER]
 [XEQ] [ALPHA] SIZE [ALPHA] 010
 [XEQ] [ALPHA] BEH [ALPHA]
 79 [Σ+] 84 [Σ+] 108 [Σ+]
 [R/S]
 [R/S]
 91 [Σ+] 103 [Σ+] 90 [Σ+] 113 [Σ+]
 108 [Σ+]
 [R/S]
 [R/S]
 [E]
 0 [R/S]
 [R/S]

Display:

(set USER mode)

 BEHRENS-FISH.
 3.00
 XBAR=90.33
 S2/N=80.11

 5.00
 YBAR=101.00
 S2/N=20.90
 D ?
 d=-1.06
 THETA=62.94

[illegible]

DATA REGISTERS				STATUS			
00	used in summations	50		SIZE <u>010</u> TOT. REG. <u>28</u> USER MODE			
	used in summations			ENG <u> </u> FIX <u>2</u> SCI <u> </u> ON <u>X</u> OFF <u> </u>			
	used in summations			DEG <u>X</u> RAD <u> </u> GRAD <u> </u>			
	used in summations			FLAGS			
05	used in summations	55					
	\bar{x}			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	s_1^2/n			01		"YBAR"	"XBAR"
	\bar{y}						
	s_2^2/n						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90		FUNCTION		KEY	
				FUNCTION		KEY	
				FUNCTION		KEY	
				FUNCTION		KEY	
45		95		FUNCTION		KEY	
				FUNCTION		KEY	
				FUNCTION		KEY	

BEHRENS-FISHER STATISTIC

PROGRAM REGISTERS NEEDED: 19

ROW 1 (1 - 5)



ROW 2 (5 - 6)



ROW 3 (6 - 15)



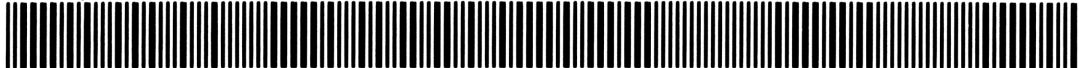
ROW 4 (16 - 19)



ROW 5 (20 - 30)



ROW 6 (30 - 35)



ROW 7 (35 - 40)



ROW 8 (41 - 51)



ROW 9 (51 - 58)



ROW 10 (59 - 65)



KRUSKAL-WALLIS STATISTIC

Suppose we want to test the null hypothesis that k independent random samples of sizes n_1, n_2, \dots, n_k come from identical continuous populations.

Arrange all values from k samples jointly (as if they were one sample) in an increasing order of magnitude. Let R_{ij} ($i = 1, 2, \dots, k, j = 1, 2, \dots, n_i$) be the rank of the j th value in the i th sample.

The Kruskal-Wallis statistic H can be used to test the null hypothesis.

When all sample sizes are large (>5), H is distributed approximately as the chi-square with $k - 1$ degrees of freedom. For small samples, the test is based on special tables.

Equation:

$$H = \frac{12}{N(N+1)} \sum_{i=1}^k \frac{\left(\sum_{j=1}^{n_i} R_{ij} \right)^2}{n_i} - 3(N+1)$$

where

$$N = \sum_{i=1}^k n_i$$

- References:
1. W.J. Conover, Practical Nonparametric Statistics, John Wiley and Sons, 1971.
 2. Table for small samples ($k = 3$):
Alexander and Quade, On the Kruskal-Wallis Three Sample H-statistic, University of North Carolina, Department of Biostatistics, Inst. Statistics Mimeo Ser. 602, 1968.
 3. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

		Ranks R_{ij}									
$i \backslash j$		1	2	3	4	5	6	7	8	9	10
1		29	5	26	10	33	30				
2		11	12	9	7	20	18	19	21		
3		14	28	8	25	17	15	32	4	2	
4		6	27	3	16	24	13	1	31	22	23

Keystrokes:

```

[USER]
[XEQ] [ALPHA] SIZE [ALPHA] 006
[XEQ] [ALPHA] KRU [ALPHA]

29 [R/S]
5 [R/S]
26 [R/S]
⋮
30 [R/S]
[B]
11 [R/S]
12 [R/S]
⋮
21 [R/S]
[B]
14 [R/S]
28 [R/S]
⋮
2 [R/S]
[B]
6 [R/S]
27 [R/S]
⋮
23 [R/S]
[B]
[E]
[R/S]
[R/S]

```

Display:

```

(set USER mode)

KRUSKAL-WALL.
R1,1 ?
R1,2 ?
R1,3 ?
R1,4 ?
⋮
R1,7 ?
R2,1 ?
R2,2 ?
R2,3 ?
⋮
R2,9 ?
R3,1 ?
R3,2 ?
R3,3 ?
⋮
R3,10 ?
R4,1 ?
R4,2 ?
R4,3 ?
⋮
R4,11 ?
R5,1 ?
H=2.29
dF=3.00
N=33.00

```

[illegible]

Program Listings

01♦LBL "KRU "		50 *	
02 CF 29	Initialize	51 RCL 05	Calculate H
03 FIX 0		52 /	
04 CLRG		53 RCL 05	
05 "KRUSKAL -WALL."		54 1	
06 AVIEW		55 +	
07 GTO A		56 /	
08♦LBL C		57 LASTX	
09 1	Correction	58 -	
10 ST- 01		59 3	
11 SF 00		60 *	
12♦LBL A		61 "H"	
13 RCL 01		62 XEQ 11	
14 1		63 RCL 04	
15 +		64 1	
16 RCL 04	Input R_{ij}	65 -	Calculate df and N
17 1		66 "dF"	
18 +		67 XEQ 11	
19 "R"		68 RCL 05	
20 ARCL X		69 "N"	
21 "F,"		70♦LBL 11	
22 ARCL Y		71 "F="	
23 "F ?"		72 ARCL X	Display routine
24 PROMPT		73 AVIEW	
25 FS? 00		74 STOP	
26 CHS		75 RTN	
27 ST+ 02		76 .END.	
28 1			
29 FC?C 00			
30 ST+ 01		80	
31 GTO A			
32♦LBL B			
33 RCL 01			
34 ST+ 05			
35 RCL 02			
36 X↑2	Compute row i partial results		
37 X<>Y			
38 /			
39 ST+ 03		90	
40 1			
41 ST+ 04			
42 0			
43 STO 01			
44 STO 02			
45 GTO A			
46♦LBL E			
47 FIX 2			
48 RCL 03			
49 4		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS			
00		50		SIZE <u>006</u> TOT. REG. <u>25</u> USER MODE ENG _____ FIX <u>2</u> SCI _____ ON <u>X</u> OFF _____ DEG _____ RAD _____ GRAD _____			
	n _i						
	ΣR _{i,j}						
	Σ [(ΣR _{i,j}) ² /n _i]						
	k						
05	N	55		FLAGS			
				#	INIT S/C	SET INDICATES	CLEAR INDICATES
				29		For proper display format	
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	FUNCTION KEY
40		90					
45		95					

KRUSKAL-WALLIS STATISTIC

PROGRAM REGISTERS NEEDED: 20

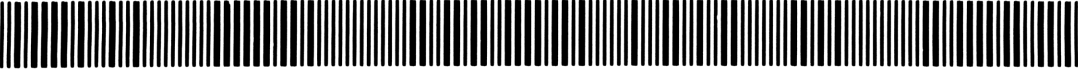
ROW 1 (1 - 5)



ROW 2 (5 - 5)



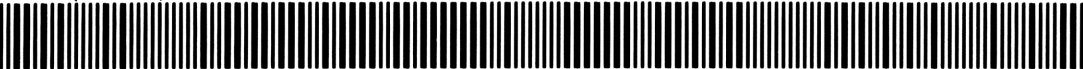
ROW 3 (6 - 12)



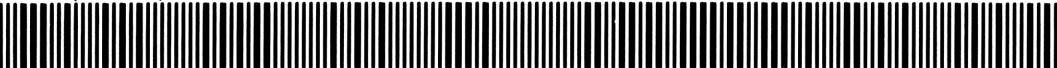
ROW 4 (13 - 21)



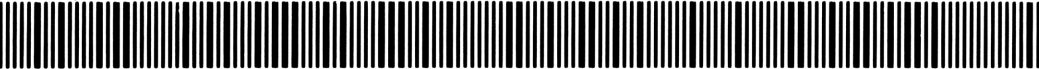
ROW 5 (22 - 28)



ROW 6 (29 - 35)



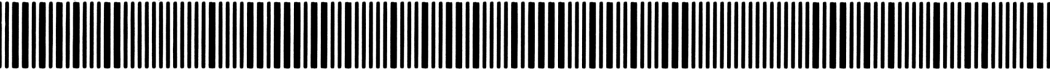
ROW 7 (36 - 45)



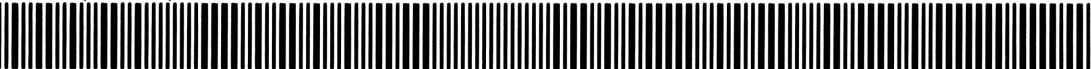
ROW 8 (45 - 55)



ROW 9 (56 - 65)



ROW 10 (66 - 71)



ROW 11 (72 - 76)



MEAN SQUARE SUCCESSIVE DIFFERENCE

When test and estimation techniques are used, the method of drawing the sample from the population is specified to be random in most cases. If observations are chosen in sequence x_1, x_2, \dots, x_n , the mean-square successive difference η can be used to test for randomness.

If the sample size n is large (say, greater than 20) and the population is normal, then a z statistic has approximately the standard normal distribution. Long trends are associated with large positive values of z and short oscillations with large negative values.

Equations:

$$\eta = \sum_{i=2}^n (x_i - x_{i-1})^2 \bigg/ \sum_{i=1}^n (x_i - \bar{x})^2 = \sum_{i=2}^n (x_i - x_{i-1})^2 \bigg/ \left[\sum_{i=1}^n x_i^2 - \frac{\left(\sum_{i=1}^n x_i \right)^2}{n} \right]$$

$$z = \frac{1 - \eta/2}{\sqrt{\frac{n-2}{n^2-1}}}$$

- References:
1. Dixon and Massey, Introduction to Statistical Analysis, McGraw-Hill, 1969.
 2. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

Find the mean-square successive difference for the following set of data:

{0.53, 0.52, 0.39, 0.49, 0.97}

Keystrokes:

Display:

[USER]

(set USER mode)

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] MNSQD [ALPHA]

MEAN SQ DIFF

.53 [A] .52 [A] .39 [A] .49 [A] .97 [A]

5.00

[E]

ETA=1.27

[R/S]

Z=1.03

[illegible]

Program Listings

01*LBL "MNS QD"		50 -	
02 FIX 2		51 /	
03 CLRG		52 SQRT	
04 SF 01		53 /	
05 ΣREG 00	Initialize	54 "Z"	
06 "MEAN SQ DIFF"		55*LBL 11	
07 AVIEW		56 "F="	
08 STOP		57 ARCL X	
09*LBL C		58 AVIEW	
10 RCL 08		59 STOP	
11 STO 07		60 RTN	
12 RCL 06		61 .END.	
13 -			
14 RCL 06			
15 Σ-			
16 STOP			
17*LBL A			
18 STO 06			
19 RCL 07		70	
20 STO 08			
21 -			
22 FS?C 01			
23 0			
24 RCL 06			
25 STO 07			
26 Σ+			
27 STOP			
28*LBL E			
29 RCL 03		80	
30 RCL 01			
31 RCL 00			
32 X↑2			
33 RCL 05			
34 /			
35 -			
36 /			
37 "ETA"			
38 XEQ 11			
39 2		90	
40 /			
41 1			
42 -			
43 CHS			
44 RCL 05			
45 2			
46 -			
47 RCL 05			
48 X↑2			
49 1		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS			
00	Σx_i	50		SIZE <u>009</u>	TOT. REG. <u>23</u>	USER MODE	
	Σx_i^2			ENG _____	FIX <u>2</u>	SCI _____	ON <u>X</u> OFF _____
	$\Sigma (x_i - x_{i-1})^2$			DEG _____	RAD _____	GRAD _____	
05	η	55		FLAGS			
	x_i			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	x_{i-1}			01		for x_1	
	used for corrections						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90					
45		95					

MEAN-SQUARE
SUCCESSIVE DIFFERENCE
PROGRAM REGISTERS NEEDED: 15

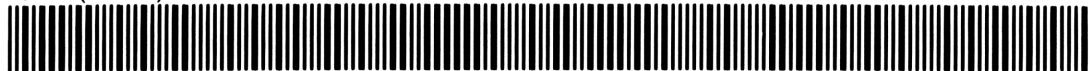
ROW 1 (1 - 4)



ROW 2 (4 - 6)



ROW 3 (6 - 15)



ROW 4 (16 - 26)



ROW 5 (27 - 37)



ROW 6 (37 - 46)



ROW 7 (47 - 56)



ROW 8 (57 - 61)



THE RUN TEST FOR RANDOMNESS

Consider a sequence of symbols such that the symbols are of two types only. A run is a continuous string of identical symbols preceded and followed by a different symbol or no symbol at all. For example, the sequence 1110100011 has five runs.

Let the total number of runs in a given sequence be u , and let n_1 and n_2 represent the number of symbols of type 1 and type 2 respectively. If the sample sizes are large (say, n_1 and n_2 are both greater than 10), then the randomness of the sequence may be tested using a z statistic which has the standard normal distribution.

Equations:

The sample distribution of the run has the mean μ and the standard deviation σ .

$$\mu = \frac{2 n_1 n_2}{n_1 + n_2} + 1$$

$$\sigma = \sqrt{\frac{2 n_1 n_2 (2 n_1 n_2 - n_1 - n_2)}{(n_1 + n_2)^2 (n_1 + n_2 - 1)}}$$

The test is based on the statistic

$$z = \frac{u - \mu}{\sigma}$$

- Remarks:
1. For small samples, the test is based on special tables.
 2. This program can also be used for other tests involving runs. For example, one might want to test runs of scores above and below the median based on the order in which the scores were obtained. In this case, a sequence could be constructed in which each score would be replaced by a 1 if it was above the median or a 0, if below the median. The run test for randomness can then be applied to the sequence of 0's and 1's.

Another use might be for Wald-Wolfowitz run test, which tests the null hypothesis that two random samples have been drawn from identical populations. The data from both groups are combined into one sequence according to magnitude. Each value may be assigned a 0 or 1 depending on which population it came from, and the run test for randomness then performed on the resulting sequence.

- References: 1. Freund and Williams, Dictionary/Outline of Basic Statistics, McGraw-Hill, 1966.
2. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

A statistician sits by the roulette table one night in a Las Vegas casino, suspiciously watching the house rake in stake upon stake. To test the null hypothesis that the sequence of numbers is random, the statistician observes the following sequence of red (R) and black (B) numbers (ignoring 0 and 00):

RRRR B RRR BBBB RR BBB RR BB RRR

In the sequence are 14 R's, 11 B's and a total of 9 runs. Find the mean and standard deviation of the sampling distribution and the z statistic.

Keystrokes:

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] RUNTEST [ALPHA]

9 [R/S]

14 [R/S]

11 [R/S]

[R/S]

[R/S]

Display:

RUN TEST

NO. OF RUNS?

NO. OF TYPE1?

NO. OF TYPE2?

MU=13.32

SIGMA=2.41

Z=-1.79

(His suspicion is not entirely unjustified).

[illegible]

Program Listings

01♦LBL "RUN TEST"	Initialize	47 RCL 04	
02 FIX 2		48 -	
03 "RUN TES T"		49 RCL 05	Calculate z
04 AVIEW		50 /	
05 PSE		51 STO 06	
06 "NO. OF RUNS ?"		52 "Z"	
07 PROMPT		53♦LBL 11	
08 STO 03		54 "F="	
09 "NO. OF TYPE1?"	u	55 ARCL X	Display routine
10 PROMPT		56 AVIEW	
11 STO 01	n ₁	57 STOP	
12 "NO. OF TYPE2?"		58 RTN	
13 PROMPT		59 .END.	
14 STO 02	n ₂		
15 *			
16 2		70	
17 *			
18 STO 07			
19 RCL 01			
20 RCL 02			
21 +			
22 STO 08			
23 /			
24 1			
25 +			
26 STO 04		80	
27 "MU"			
28 XEQ 11			
29 RCL 07			
30 RCL 08			
31 -			
32 RCL 07			
33 *			
34 RCL 08			
35 ENTER↑			
36 *			
37 RCL 08		90	
38 1			
39 -			
40 *			
41 /			
42 SQRT			
43 STO 05			
44 "SIGMA"			
45 XEQ 11			
46 RCL 03		00	

DATA REGISTERS				STATUS			
00		50		SIZE 009 TOT. REG. 28 USER MODE			
	n ₁			ENG FIX 2 SCI ON OFF X			
	n ₂			DEG RAD GRAD			
	u			FLAGS			
	μ						
05	σ	55		#	INIT S/C	SET INDICATES	CLEAR INDICATES
	z						
	2n ₁ n ₂						
	n ₁ +n ₂						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90		FUNCTION		KEY	
45		95					

THE RUN TEST
FOR RANDOMNESS
PROGRAM REGISTERS NEEDED: 20

ROW 1 (1 - 2)



ROW 2 (3 - 6)



ROW 3 (6 - 7)



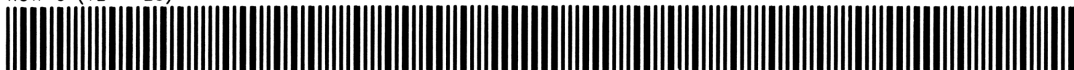
ROW 4 (8 - 9)



ROW 5 (9 - 12)



ROW 6 (12 - 20)



ROW 7 (21 - 29)



ROW 8 (30 - 42)



ROW 9 (43 - 48)



ROW 10 (49 - 57)



ROW 11 (58 - 59)



INTRACLASS CORRELATION COEFFICIENT

The intraclass correlation coefficient r_I measures the degree of association among individuals within classes or groups.

		Observations			
Groups	1	x_{11}	x_{12}	\cdots	x_{1n}
	2	x_{21}	x_{22}	\cdots	x_{2n}

	k	x_{k1}	x_{k2}	\cdots	x_{kn}

The coefficient is most easily calculated using the analysis of variance techniques. r_I is the sample estimate of the population intraclass correlation coefficient ρ_I . If we can assume that the individuals within groups are random samples from normal populations with the same variance, then the hypothesis $\rho_I = 0$ can be tested using the F statistic.

Equations:

1. Sums

Group

$$T_i = \sum_{j=1}^n x_{ij} \quad i = 1, 2, \dots, k$$

Total

$$T = \sum_{i=1}^k T_i$$

2. Sums of squares

Mean

$$MSS = T^2 / k n$$

Among groups

$$ASS = \sum_{i=1}^k T_i^2 / n - MSS$$

Within groups

$$WSS = \sum_{i=1}^k \sum_{j=1}^n x_{ij}^2 - MSS - ASS$$

3. Intraclass correlation coefficient

$$r_I = \left(\frac{ASS}{k-1} - \frac{WSS}{k(n-1)} \right) \div \left(\frac{ASS}{k-1} + \frac{WSS}{k} \right)$$

4. F statistic

$$F = \frac{ASS}{k-1} \div \frac{WSS}{k(n-1)}$$

with $df_1 = k - 1$ and $df_2 = k(n - 1)$ degrees of freedom.

- References:
1. B. Ostle, Statistics, in Research, Iowa State University Press, 1972.
 2. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

		Observations	
Groups	1	71	71
	2	69	72
	3	59	65
	4	65	64
	5	66	60
	6	73	72
	7	68	67
	8	70	68

Keystrokes:

Display:

[USER]	(set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 010	
[XRQ] [ALPHA] INT [ALPHA]	INTRAClass C.
	N ?
2 [R/S]	X1,1 ?
71 [R/S]	X1,2 ?
71 [R/S]	T1=142
[R/S]	X2,1 ?
69 [R/S]	X2,2 ?
72 [R/S]	T2=141
⋮	⋮
70 [R/S]	X8,2 ?
68 [R/S]	T8=138
[E]	RI=0.70
[R/S]	F=5.61
[R/S]	df1=7.00
[R/S]	df2=8.00

[illegible]

Program Listings

01♦LBL "INT "		50 STO 01	
02 FIX 0		51 STO 06	
03 CLRG		52 1	
04 CF 29	Initialize	53 ST+ 02	
05 CF 00		54 RCL 08	
06 "INTRACL		55 "T"	
ASS C."		56 ARCL 02	
07 AVIEW		57 XEQ 11	
08 PSE		58 GTO a	
09 "N ?"		59♦LBL E	
10 PROMPT		60 FIX 2	
11 STO 09		61 RCL 04	
12 GTO a		62 RCL 03	
13♦LBL C	Correction	63 X↑2	
14 SF 00	routine	64 RCL 02	
15 1		65 /	
16 ST- 01		66 -	
17♦LBL a		67 RCL 09	
18 RCL 01		68 STO 01	ASS
19 1		69 /	
20 +		70 RCL 02	Calculate r_I
21 RCL 02	Input prompt	71 1	
22 1	routine	72 -	
23 +		73 /	
24 "X"		74 STO 00	
25 ARCL X		75 RCL 05	
26 "F,"		76 RCL 04	
27 ARCL Y		77 RCL 01	
28 "F ?"		78 /	
29 PROMPT		79 -	
30 FS? 00		80 RCL 02	
31 CHS		81 /	WSS/k
32 ST+ 06		82 STO 08	
33 X↑2		83 RCL 01	
34 FS? 00		84 1	
35 CHS		85 -	
36 ST+ 05		86 STO 01	
37 1		87 /	
38 FC?C 00		88 -	
39 ST+ 01		89 RCL 00	
40 RCL 09	n	90 RCL 08	
41 RCL 01	j	91 +	
42 X≠Y?		92 /	
43 GTO a		93 "RI"	
44 RCL 06		94 XEQ 11	
45 STO 08	Calculate T_i	95 RCL 00	
46 ST+ 03		96 RCL 08	
47 X↑2		97 RCL 01	Calculate F
48 ST+ 04		98 /	
49 0		99 /	
		100 "F"	

Program Listings

101 XEQ 11	Calculate df_i	51	
102 RCL 02			
103 1			
104 -			
105 "dF1"			
106 XEQ 11			
107 RCL 01			
108 RCL 02			
109 *			
110 "dF2"			
111 LBL 11	Display routine	60	
112 "F="			
113 ARCL X			
114 RVIEW			
115 STOP			
116 RTN			
117 .END.			
20		70	
30		80	
40		90	
50		00	

DATA REGISTERS				STATUS			
00	ASS/k-1	50		SIZE	010	TOT. REG.	37
	j → n			ENG		FIX	2
	i → k			DEG		RAD	
	T			SCI		GRAD	
	ΣT_i^2			FLAGS			
05	$\Sigma \Sigma x_{ij}^2$	55		#	INIT S/C	SET INDICATES	CLEAR INDICATES
	Σx_{ij}			00		For corrections	Normal
	temp, WSS/k			29		For proper display format	
	n, n-1						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
40		90		ASSIGNMENTS			
				FUNCTION KEY		FUNCTION KEY	
45		95					

INTRACLAS
CORRELATION COEFFICIENT
PROGRAM REGISTERS NEEDED: 28

ROW 1 (1 - 5)



ROW 2 (5 - 6)



ROW 3 (6 - 12)



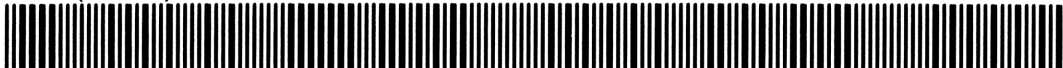
ROW 4 (13 - 21)



ROW 5 (22 - 28)



ROW 6 (28 - 36)



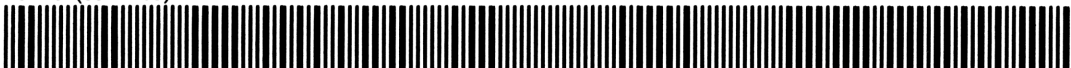
ROW 7 (36 - 44)



ROW 8 (45 - 54)



ROW 9 (55 - 60)



ROW 10 (60 - 72)



ROW 11 (73 - 85)



ROW 12 (86 - 94)



ROW 13 (95 - 104)



ROW 14 (105 - 110)



ROW 15 (110 - 117)



FISHER'S EXACT TEST FOR A 2 x 2 CONTINGENCY TABLE

Fisher's exact probability test is used for analyzing a 2 x 2 contingency table when the two independent samples are small in size.

a	b
c	d

Suppose a, b, c, d are the frequencies and a is the smallest frequency, this program calculates the following:

1. The exact probability p_0 of observing the given frequencies in a 2 x 2 table, when the marginal totals are regarded as fixed.
2. The exact probability p_i ($i = 1, 2, \dots, a$) of each more extreme table having the same marginal totals.
3. The sum S_i of the probabilities of the first $i + 1$ tables.
4. The sum S of the probabilities of all tables with the same margins (i.e., $S = S_a$).

Equations:

$$1. \quad p_0 = \frac{(a+b)!(c+d)!(a+c)!(b+d)!}{N!a!b!c!d!}$$

where

$$N = a + b + c + d.$$

2. For the more extreme table (with the same margins)

$a - i$	$b + i$
$c + i$	$d - i$

$$p_i = \frac{(a+b)!(c+d)!(a+c)!(b+d)!}{N!(a-i)!(b+i)!(c+i)!(d-i)!}$$

where

i can be 1, 2, ... or a .

- 3.

$$S_n = \sum_{i=0}^n p_i$$

where

n can be 1, 2, ..., a.

4.

$$S = \sum_{i=0}^a p_i$$

- Remarks:
1. a must be the smallest among the frequencies. Rearrange the table if necessary.
 2. This program requires $N \leq 69$. However, Fisher's exact test is normally used for $N \leq 30$.
- References:
1. S. Siegel, Nonparametric Statistics, McGraw-Hill, 1956.
 2. Sir R. A. Fisher, Statistical Methods for Research Workers, Oliver and Boyd, 1950.
 3. This program is a translation of the HP-65 Stat Pac 2 program.

Example:

Calculate p_0 , p_1 , p_2 , S_4 and S for the following table

7	10
8	5

Note:

The table must be rearranged as

5	8
10	7

Keystrokes:

[USER]
 [XEQ] [ALPHA] SIZE [ALPHA] 009
 [XEQ] [ALPHA] FIS [ALPHA]

 5 [R/S]
 8 [R/S]
 10 [R/S]
 7 [R/S]
 [A]
 [A]
 [A] [A] [R/S]
 [E]

Display:

(set USER mode)

 FISHERS TEST
 a?
 b?
 c?
 d?
 P0=0.16
 P1=0.06
 P2=0.01
 S4=0.23
 S=0.23

[illegible]

Program Listings

01♦LBL "FIS "		50 RCL 01	
02 FIX 2	Initialize	51 FACT	
03 CF 01		52 /	Loop to calculate P_i
04 CF 29		53 RCL 02	
05 "FISHERS TEST"		54 FACT	
06 AVIEW		55 /	
07 PSE		56 RCL 03	
08 CLRG		57 FACT	
09 "a?"		58 /	
10 PROMPT		59 RCL 04	
11 STO 01		60 FACT	
12 STO 08		61 /	
13 "b?"		62 ST+ 05	
14 PROMPT		63 FS? 01	
15 STO 02		64 RTN	
16 +		65 "P"	
17 STO 05		66 XEQ 11	
18 "c?"		67 RCL 05	
19 PROMPT		68 "S"	Display S_i
20 STO 03		69 XEQ 11	
21 "d?"		70 STOP	
22 PROMPT		71♦LBL A	
23 STO 04		72 1	
24 +		73 ST- 01	
25 STO 06		74 ST+ 02	
26 FACT		75 ST+ 03	
27 RCL 05		76 ST- 04	
28 FACT		77 ST- 08	
29 *		78 ST+ 00	
30 RCL 05		79 RCL 07	
31 RCL 06		80 GTO 00	
32 +		81♦LBL E	
33 FACT		82 SF 01	
34 /		83 RCL 08	
35 RCL 01		84 0	Calculate S
36 RCL 03		85 X=Y?	
37 +		86 XEQ 01	
38 FACT		87 XEQ A	
39 *		88 GTO E	
40 RCL 02		89♦LBL 01	
41 RCL 04		90 CF 01	
42 +		91 RCL 05	
43 FACT		92 "S="	Display S
44 *		93 ARCL X	
45 STO 07		94 AVIEW	
46 0		95 STOP	
47 STO 05		96♦LBL 11	
48 RDN		97 FIX 0	
49♦LBL 00		98 ARCL 00	
		99 "I="	Display routine
		100 FIX 2	

Program Listings

101 ARCL X		51	
102 AVIEW			
103 STOP			
104 RTN			
105 .END.			
10		60	
20		70	
30		80	
40		90	
50		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS			
00	i	50		SIZE <u> 009 </u> TOT. REG. <u> 33 </u> USER MODE			
	a			ENG _____ FIX <u> 2 </u> SCI _____ ON <u> X </u> OFF _____			
	b			DEG _____ RAD _____ GRAD _____			
	c						
	d						
05	a+b, S _n	55		FLAGS			
	c+d			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	numerator of P _j			01		Calculate S	Normal
	a			29		Cleared for proper display format	
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90					
45		95					

FISHER'S EXACT TEST FOR A
2 X 2 CONTINGENCY TABLE
PROGRAM REGISTERS NEEDED: 25

ROW 1 (1 - 4)



ROW 2 (5 - 5)



ROW 3 (6 - 14)



ROW 4 (15 - 23)



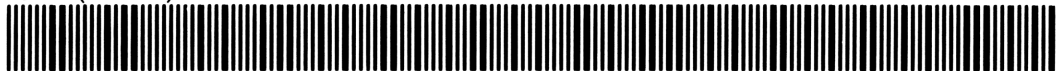
ROW 5 (24 - 36)



ROW 6 (37 - 49)



ROW 7 (50 - 62)



ROW 8 (62 - 69)



ROW 9 (69 - 76)



ROW 10 (76 - 83)



ROW 11 (84 - 90)



ROW 12 (90 - 98)



ROW 13 (98 - 105)



RCW 14 (105 - 105)



BARTLETT'S CHI-SQUARE STATISTIC

$$\chi^2 = \frac{f \ln s^2 - \sum_{i=1}^k f_i \ln s_i^2}{1 + \frac{1}{3(k-1)} \left[\left(\sum_{i=1}^k \frac{1}{f_i} \right) - \frac{1}{f} \right]}$$

where: s_i^2 = sample variance of the i th sample

f_i = degrees of freedom associated s_i^2

i = 1, 2, ..., k

k = number of samples

$$s^2 = \frac{\sum_{i=1}^k f_i s_i^2}{f}$$

$$f = \sum_{i=1}^k f_i$$

This χ^2 has a chi-square distribution (approximately) with $k - 1$ degrees of freedom which can be used to test the null hypothesis that $s_1^2, s_2^2, \dots, s_k^2$ are all estimates of the same population variance σ^2 ; i.e., H_0 : Each of $s_1^2, s_2^2, \dots, s_k^2$ is an estimate of σ^2 .

- References: 1. Statistical Theory with Engineering Applications, A. Hald, John Wiley and Sons, 1960.
2. This program is a translation of the HP-65 Stat Pac 1 program.

Example:

Apply the program to the following data:

i	1	2	3	4	5	6
s_i^2	5.5	5.1	5.2	4.7	4.8	4.3
f_i	10	20	17	18	8	15

Keystrokes:

```
[USER]
[XEQ] [ALPHA] SIZE [ALPHA] 009
[XEQ] [ALPHA] BAR [ALPHA]

10 [R/S]
5.5 [R/S]
:
15 [R/S]
4.3 [R/S]
[E]
[R/S]
```

Display:

```
(set USER mode)

BARTLETTS
F1?
S1 SQ?
F2?
:
S6SQ?
F7?
CHI SQ=0.25
dF=5.00
```

[illegible]

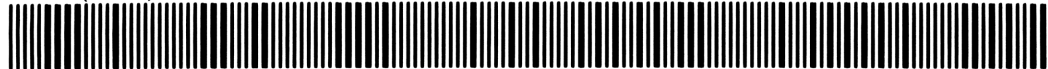
01♦LBL "BAR "		50 CF 01	
02 FIX 0		51 STO 08	
03 CLRG		52 RCL 01	
04 CF 01		53 *	
05 CF 29	Initialize	54 ST+ 00	
06 "BARTLET TS"		55 RCL 08	
07 AVIEW		56 LN	
08 PSE		57 RCL 01	
09 GTO A		58 *	
10♦LBL C	-----	59 ST+ 06	
11 FS? 01		60 1	
12 GTO 01		61 ST+ 05	
13 STO 08	Correct s_1^2	62 GTO A	-----
14 RCL 01		63♦LBL E	
15 *		64 FIX 2	
16 ST- 00		65 RCL 00	
17 RCL 08		66 RCL 03	Calculate χ^2 and df
18 LN		67 /	
19 RCL 01		68 LN	
20 *		69 RCL 03	
21 ST- 06		70 *	
22 1		71 RCL 06	
23 ST- 05		72 -	
24 GTO b	Correct f_1	73 RCL 04	
25♦LBL 01		74 RCL 03	
26 ST- 03		75 1/X	
27 1/X		76 -	
28 ST- 04		77 RCL 05	
29♦LBL A		78 1	
30 "F"		79 -	
31 RCL 05		80 STO 02	
32 1		81 3	
33 +		82 *	
34 ARCL X		83 /	
35 "F?"		84 1	
36 PROMPT		85 +	
37 SF 01		86 /	
38 STO 01		87 "CHI SQ"	
39 ST+ 03		88 XEQ 11	
40 1/X	Accumulate sums	89 RCL 02	
41 ST+ 04		90 "dF"	-----
42♦LBL b		91♦LBL 11	
43 "S"		92 "F="	
44 RCL 05		93 ARCL X	Display routine
45 1		94 AVIEW	
46 +		95 STOP	
47 ARCL X		96 RTN	
48 "F SQ?"		97 .END.	
49 PROMPT			
	00		

DATA REGISTERS				STATUS			
00	$\Sigma f_i s_i^2$	50		SIZE	009	TOT. REG.	32
	f _i			ENG		FIX	2
	df			DEG		SCI	
	Σf_i			RAD		GRAD	
	$\Sigma(1/f_i)$						
05	k	55		FLAGS			
	$\Sigma f_i \ln s_i^2$			#	INIT S/C	SET INDICATES	CLEAR INDICATES
	s _i ²			01		Correct f _i	Correct s _i ²
				29		For proper display format	
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90					
45		95					

BARTLETT'S CHI-SQUARE
STATISTIC

PROGRAM REGISTERS NEEDED: 24

ROW 1 (1 - 5)



ROW 2 (5 - 8)



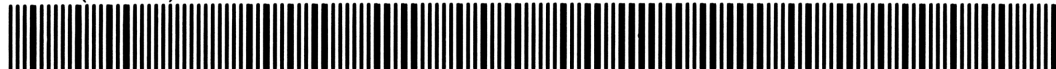
ROW 3 (9 - 16)



ROW 4 (16 - 24)



ROW 5 (25 - 33)



ROW 6 (34 - 41)



ROW 7 (41 - 48)



ROW 8 (48 - 56)



ROW 9 (57 - 64)



ROW 10 (64 - 76)



ROW 11 (77 - 87)



ROW 12 (87 - 92)



ROW 13 (92 - 97)



MANN-WHITNEY STATISTICS

This program calculates the Mann-Whitney test statistic on two independent samples of equal or unequal sizes. This test is designed for testing the null hypothesis of no difference between two populations.

Mann-Whitney test statistic is defined as:

$$U = n_1 n_2 + \frac{n_1 (n_1 + 1)}{2} - \sum_{i=1}^{n_1} R_i$$

where n_1 and n_2 are the sizes of the two samples and R_i ($i = 1, 2, \dots, n$) is the rank assigned to the values of a given sample. All values from both samples should be arranged jointly (as if they were one sample) in an increasing order of magnitude.

When n_1 and n_2 are small, the Mann-Whitney test bases on the exact distribution of U and specially constructed tables. When n_1 and n_2 are both large (i.e., greater than 20) then:

$$Z = \frac{U - \frac{n_1 n_2}{2}}{\sqrt{n_1 n_2 (n_1 + n_2 + 1)/12}}$$

is approximately a random variable having the standard normal distribution.

If the size of neither sample is greater than 20, the user should consult the special U-tables (for example, Handbook of Statistical Tables, D. B. Owens, Addison-Wesley, 1962), using the smaller of the two possible U's (one for each sample). When this occurs, the program automatically determines and displays the approximate U and does not compute Z.

The following program includes two options. Option I assigns and enter ranks based on the number of times a datum occurs in both samples. Rank is determined by:

$$R_n = \frac{F_1 n + F_2 n + 1}{2} + \sum_{i=0}^{n-1} F_1 n + \sum_{i=0}^{n-1} F_2 n$$

Where $F_{10} = F_{20} = 0$

Frequencies are entered sequentially corresponding to increasingly larger data values. There is one error deletion routine for option I.

Option II is used when the ranks for the data values are already known. The inputs are the ranks and the corresponding frequencies for the sample. This option includes two error deletion routines.

- References:
1. Mathematical Statistics, J. E. Freuno, Prentice-Hall, 1962.
 2. Nonparametric Statistics for the Social Sciences, Sidney Siegel, McGraw-Hill, 1956, pp. 115-123; 271-277.

Find U and Z for the following data:

Example:

Sample 1		Sample 2	
Data	Ranks	Data	Ranks
4	4.5	4	4.5
4	4.5	4	4.5
4	4.5	4	4.5
		4	4.5
		4	4.5
6.2	10	6.2	10
6.2	10		
7.1	14.5	7.1	14.5
7.1	14.5	7.1	14.5
7.1	14.5	7.1	14.5
8	22.5	8	22.5
8	22.5	8	22.5
8	22.5	8	22.5
8	22.5	8	22.5
		8	22.5
		8	22.5
10	29	10	29
10	29		
		13	32
		13	32
		13	32
14	35	14	35
		14	35
17	37		

OPTION I (ranks not yet assigned):			
i	Datum Value_i	$F1_i$	$F2_i$
1	4	3	5
2	6.2	2	1
3	7.1	3	3
4	8	4	6
5	10	2	1
6	13	0	3
7	14	1	2
8	17	1	0

OPTION II (ranks already assigned):		
i	F_i	R_{i-}
1	3	4.5
2	2	10
3	3	14.5
4	4	22.5
5	2	29
6	1	35
7	1	37

SOLUTION: Option I

Input	Function	Display	Comments
Load M-W	GTO..	Packing	Load program and set size
Set size 006			Start program
	[XEQ]M-W	Mann-Whitney	
		1:F ₁ ↑ F ₂ ?	Enter the number of times a datum occurs in both samples
3	[ENTER]	3	
5	[R/S]	Rank = 4.5	
		2:F ₁ ↑ F ₂ ?	
2	[ENTER]	2	
1	[R/S]	Rank = 10.0	
		3:F ₁ ↑ F ₂ ?	
3	[ENTER]	3	
	[R/S]	Rank = 14.5	
		4:F ₁ ↑ F ₂ ?	
44	[ENTER]	44	
66	[R/S]	Rank = 72.5	
		5:F ₁ ↑ F ₂ ?	Oops! Need to correct that error.
	[XEQ] "a"	4:F ₁ ↑ F ₂ ?	Input correct values & continue.
4	[ENTER]		
6	[R/S]	Rank = 22.5	
		5:F ₁ ↑ F ₂ ?	
2	[ENTER]		
1	[R/S]	Rank = 29.0	
		6:F ₁ ↑ F ₂ ?	
0	[ENTER]		
3	[R/S]	Rank = 32.0	
		7:F ₁ ↑ F ₂ ?	
2	[R/S]	Rank = 35.0	1 is "entered" by default
		8:F ₁ ↑ F ₂ ?	
0	[R/S]	Rank = 37.0	
		9:F ₁ ↑ F ₂ ?	Last item already entered. Calculate U & Z.
	[XEQ]"c"	u=175.0000	
	[R/S]	z=0.2146	

OPTION II

Input	Function	*Display	Comments
Set size 007			
	[XEQ] "E"	Mann-Whitney	
		$N_1?$	No. data items - sample 1?
16	[R/S]	$N_2?$	No. data items - sample 2?
21	[R/S]	1:F↑R?	Enter frequency & rank
3	[ENTER]	3	
4.5	[R/S]	2:F↑R?	
3	[ENTER]	3	
100	[R/S]	3:F↑R?	Need to correct the last input
	[XEQ] "e"	3 100 deleted	
		2:F↑R?	Enter correct value
2	[ENTER]	2	
10	[R/S]	3:F↑R?	
3	[ENTER]	3	
14.5	[R/S]	4:F↑R?	
5	[ENTER]	5	
225	[R/S]	5:F↑R?	4 was entered incorrectly - to delete
2	[ENTER]	2	
29	[R/S]	6:F↑R?	
5	[ENTER]	5	
225	[XEQ] "d"	5 225 deleted	
		5:F↑R?	Enter correct value
4	[ENTER]	4	
22.5	[R/S]	6:F↑R?	
35	[R/S]	7:F↑R?	
37	[R/S]	U=175.0000	
	[R/S]	Z=0.2146	

* Display shown as appears without a printer - printer output shown on page # 55

PRINTER OUTPUT

Output I

MANN-WHITNEY

F1 = 3
F2 = 5
RANK = 4.5

F1 = 2
F2 = 1
RANK = 10.0

F1 = 3
F2 = 3
RANK = 14.5

F1 = 44
F2 = 66
RANK = 72.5

F1 = 44
F2 = 66

F1 = 4
F2 = 6
RANK = 22.5

F1 = 2
F2 = 1
RANK = 29.0

F1 = 0
F2 = 3
RANK = 32.0

F1 = 1
F2 = 2
RANK = 35.0

F1 = 1
F2 = 0
RANK = 37.0

U=175.0000
Z=0.2146

PRINTER OUTPUT

Output II

MANN-WHITNEY

N1 = 16
N2 = 21

F=3.0 R=4.5
F=3.0 R=100.0
3 100 DELETED
F=2.0 R=10.0
F=3.0 R=14.5
F=5.0 R=225.0
F=2.0 R=29.0
5 225 DELETED
F=4.0 R=22.5
F=1.0 R=35.0
F=1.0 R=37.0

U=175.0000
Z=0.2146

[illegible]

User Instructions

Option II (ranks already assigned)				SIZE: 007
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY **
III1	Load program,* pack, set size 007			
II2	Initialize (Option II)		(GTO) "M-W" [XEQ] E	Mann-Whitney N1?
II3	Input number of data items in sample 1	N1	[R/S]	N2?
II4	Input number of data items in sample 2	N2	[R/S]	1:F↑R?
	Perform steps II5 & II6 for i=1,2...,n, where n is the number of different rank values in sample 1.			
II5	Input the number of times R_i occurs in sample			
	1. If $F_i=1$, this step may be skipped.	F_i	[ENTER]	(F_i)
II6	Input R_i	R_i	[R/S]	(i+1):F↑R?
II7	If a mistake was made in the pair of entries			
	just entered, delete the pair and go to			
	step II5		[XEQ]"e"	$F_i R_i$ deleted (i):F↑R?
II8	If a mistake was made when inputting a			
	different pair of entries (ie, not the most			
	recent) re-enter the incorrect pair, delet,			
	go to step II 5	F_m	[ENTER]	(F_m)
		R_m	[XEQ]"d"	$F_m R_m$ deleted (i):F↑R?
II9	U is calculated (automatically) after the			
	nth input			U=(U)
III10	Z is calculated if either sample size is			
	greater than 20.		[R/S]	Z=(Z)
	*(Note if only Option II is to be used, program lines 02-60 can be deleted.)			
	**If a printer is present - all values will be printed.			

[illegible]

Program Listings

69

01♦LBL "M-W		52 RTN	
"		53 ADV	
02♦LBL A	Begin Option I	54 "F1 = "	
03 XEQ 03		55 ARCL 04	If attached echo
04♦LBL 01		56 AVIEW	print F1 and F2
05 1	Set up counter	57 "F2 = "	
06 ST+ 03		58 ARCL 05	
07 CLA		59 AVIEW	
08 ARCL 03		60 RTN	
09 "F:F1↑F2	Prompt for input	61♦LBL 03	
"		62 SF 12	
10 PROMPT	Store F _{2i}	63 CF 21	Set flag 21 to
11 STO 05		64 FS? 55	match status of
12 X<>Y	Store F _{1i}	65 SF 21	flag 55
13 STO 04		66 "MANN-WH	Output header
14 XEQ 02		ITNEY"	
15 FIX 1		67 AVIEW	
16 "RANK =		68 PSE	
"		69 CF 12	
17 ARCL X		70 0	
18 AVIEW		71 STO 00	Initialize neces-
19 PSE	Display calculated	72 STO 01	sary registers
20 FIX 0	Rank (R _i)	73 STO 02	
21 RCL 04		74 STO 03	
22 ST+ 01	Accumulate	75 SF 27	Set user mode
23 *	F _{1i} (→n ₁)	76 CF 29	
24 ST+ 00	Accumulate R _i	77 FIX 0	
25 RCL 05		78 RTN	
26 ST+ 02	Accumulate F _{2i}	79♦LBL e	Recall F _n & R _n for
27 GTO 01	(→n ₂)	80 RCL 04	deletion (OptionII)
28♦LBL a	Subroutine for	81 RCL 05	Subroutine for
29 RCL 05	deleting F _{1n} and	82♦LBL d	deletion of entries
30 ST- 02	F _{2n}	83 CLA	(Option II)
31 RCL 04		84 ARCL Y	
32 ST- 01	(Option I)	85 "F "	
33 XEQ 02		86 ARCL X	
34 RCL 04		87 "F DELET	
35 *		ED"	
36 ST- 00		88 AVIEW	
37 2		89 X<>Y	
38 ST- 03		90 ST- 06	
39 GTO 01		91 *	
40♦LBL 02	Calculate Rank	92 ST- 00	
41 +		93 2	
42 STO Y		94 ST- 03	
43 1		95 GTO 04	
44 +		96♦LBL E	Begin Option II
45 2		97 XEQ 03	Prompt for and
46 /		98 STO 06	store N1 & N2
47 RCL 01		99 "N1?"	
48 RCL 02		100 PROMPT	
49 +	Printer Attached?	101 STO 01	
50 +	If not return (to	102 "N2?"	
51 FC? 55	line #15)		

Program Listings

103 PROMPT		156 RCL 02	
104 STO 02	If no printer	157 X>Y?	
105 FC? 55	jump to Label 4	158 GTO 05	
106 GTO 04		159 RCL Z	Compute U for
107 ADV	If printer exists	160 STO Y	Sample 2
108 "N1 = "	display input for	161 CHS	
109 ARCL 01	N1 & N2	162 RCL 01	
110 AVIEW		163 RCL 02	
111 "N2 = "		164 *	
112 ARCL 02		165 +	
113 AVIEW		166 X>Y?	Select smaller u
114 ADV		167 X<>Y	& display (Sample
115♦LBL 04		168 GTO 06	<20)
116 1	Set up counter	169♦LBL 07	Subroutine to echo
117 ST+ 03		170 FIX 1	print values of F
118 CLA		171 "F="	& R if printer
119 ARCL 03	Prompt for & store	172 ARCL 04	attached
120 "F: F↑R?"	input (F_i & R_i)	173 "↑ R="	
121 PROMPT		174 ARCL 05	
122 STO 05		175 AVIEW	
123 X<>Y		176 FIX 0	
124 STO 04		177 RTN	
125 FS? 55	Printer exist?	178♦LBL 05	
126 XEQ 07	Jump to Label 7	179 SF 21	
127 ST+ 06	Number of data	180 FS? 55	
128 *	Calculate RI &	181 ADV	Display U
129 ST+ 00	accumulate	182 RCL Z	(Sample >20)
130 RCL 01		183 ARCL X	
131 RCL 06		184 AVIEW	
132 X<Y?		185 RCL 01	Calculate value
133 GTO 04	Any more entries?	186 RCL 02	of Z
134♦LBL C		187 *	
135 SF 29		188 2	
136 FIX 4		189 /	
137 RCL 01	Compute u for	190 -	
138 RCL 02	Sample 1	191 RCL 01	
139 *	(Option I)	192 RCL 02	
140 RCL 01		193 *	
141 1		194 RCL 01	
142 +		195 RCL 02	
143 RCL 01		196 +	
144 *		197 1	
145 2		198 +	
146 /		199 *	
147 +		200 12	
148 RCL 00		201 /	
149 -		202 SQRT	Display final out-
150 "U="	Determine if	203 /	put (U or Z depen-
151 20	sample size >20	204 "Z="	ding on sample
152 RCL 01	If so calculate Z	205♦LBL 06	size)
153 X>Y?		206 ARCL X	
154 GTO 05		207 AVIEW	
155 CLX		208 .END.	

MANN-WHITNEY STATISTIC

PROGRAM REGISTERS NEEDED: 54

ROW 1 (1 : 4)



ROW 2 (5 : 9)



ROW 3 (9 : 16)



ROW 4 (16 : 21)



ROW 5 (22 : 29)



ROW 6 (30 : 37)



ROW 7 (38 : 47)



ROW 8 (48 : 54)



ROW 9 (55 : 60)



ROW 10 (61 : 66)



ROW 11 (66 : 69)



ROW 12 (70 : 79)



ROW 13 (79 : 86)



ROW 14 (86 : 89)



ROW 15 (90 : 97)



ROW 16 (97 : 102)



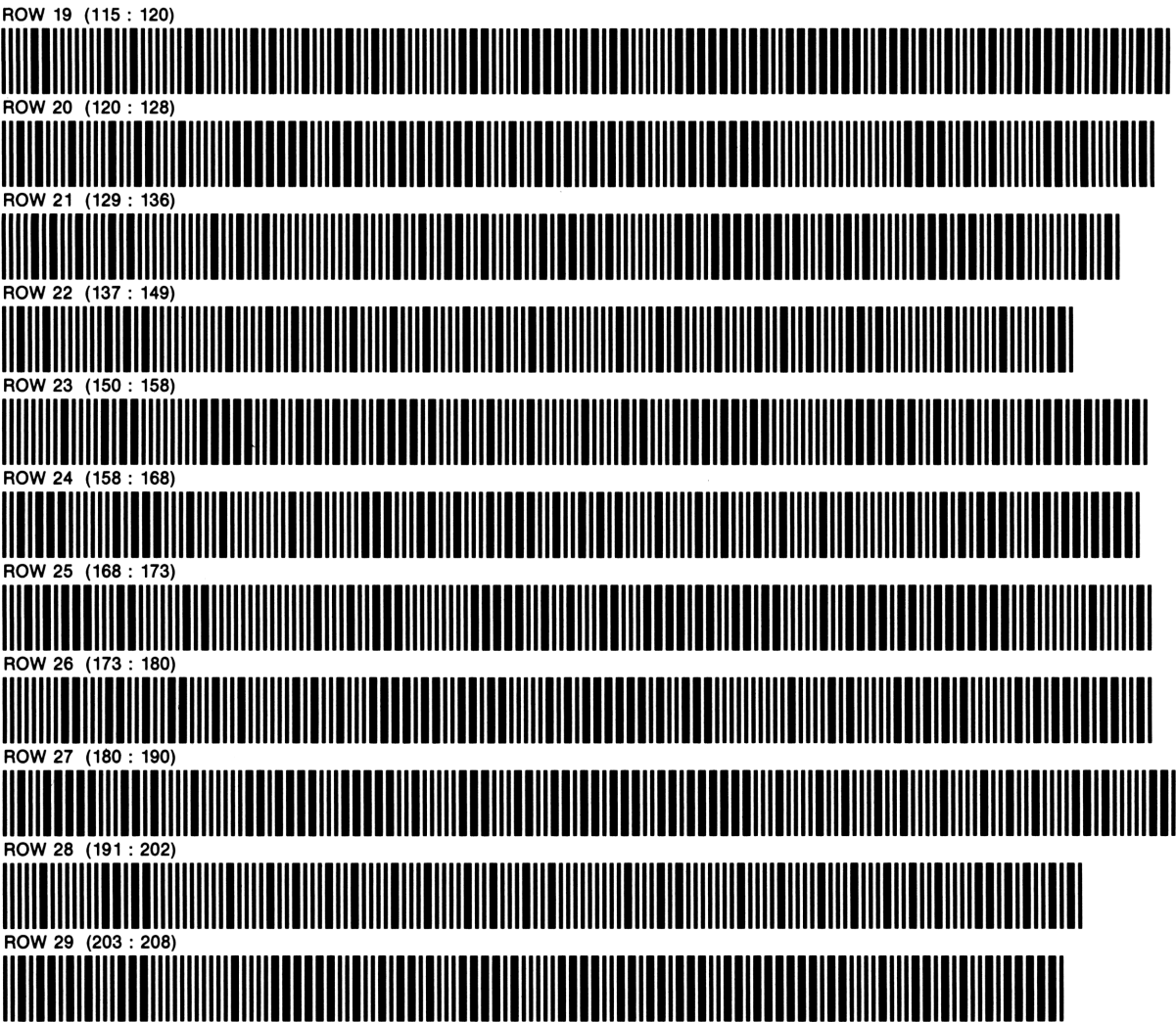
ROW 17 (103 : 108)



ROW 18 (109 : 114)



MANN-WHITNEY STATISTIC



KENDALL'S COEFFICIENT OF CONCORDANCE

Suppose n individuals are ranked from 1 to n according to some specified characteristic by k observers, the coefficient of concordance W measures the agreement between observers (or concordance between rankings).

$$W = \frac{12 \sum_{i=1}^n \left(\sum_{j=1}^k R_{ij} \right)^2}{k^2 n (n^2 - 1)} - \frac{3(n+1)}{n-1}$$

Where R_{ij} is the rank assigned to the i th individual by the j th observer.

W varies from 0 (no community of preference) to 1 (perfect agreement). The null hypothesis that the observers have no community of preference may be tested using special tables, or if $n > 7$, by calculating

$$\chi^2 = k (n - 1) W$$

which has approximately the chi-square distribution with $n - 1$ degrees of freedom (df).

Operating Limits and Warnings:

For small samples (say, less than or equal to 7) the specially constructed tables should be used. For example: Rank Correlation Methods, M.G. Kendall, Hafner Publishing Co., 1962.

- References:
1. Nonparametric Statistical Inference, J. D. Gibbond, McGraw-Hill, 1971.
 2. This program is a translation of the HP-65 Stat Pac 1 program.

Example:

Find W , χ^2 , and df for the following data:

Table for R_{ij} ($n = 4$, $k = 3$)

$i \backslash j$	1	2	3
1	6	7	3
2	1	4	2
3	9	3	5
4	2	6	1

Keystrokes:

```

[USER]
[XEQ] [ALPHA] SIZE [ALPHA] 007
[XEQ] [ALPHA] KEN [ALPHA]

3 [R/S]
6 [R/S]
7 [R/S]
3 [R/S]
[R/S]
1 [R/S]
:
:
1 [R/S]
[E]
[R/S]
[R/S]

```

Display:

```

(set USER mode)

KENDALLS COF.
K?
R1,1 ?
R1,2 ?
R1,3 ?
S1=16
R2,1 ?
R2,2 ?
:
R4,3 ?
S4=9
W=10.00
CHI SQ=90.00
dF=3.00

```

NOTE: Although this example violates the warning ($n < 7$), the amount of data to be entered has been kept small to allow the user to run through the example in short order.

[illegible]

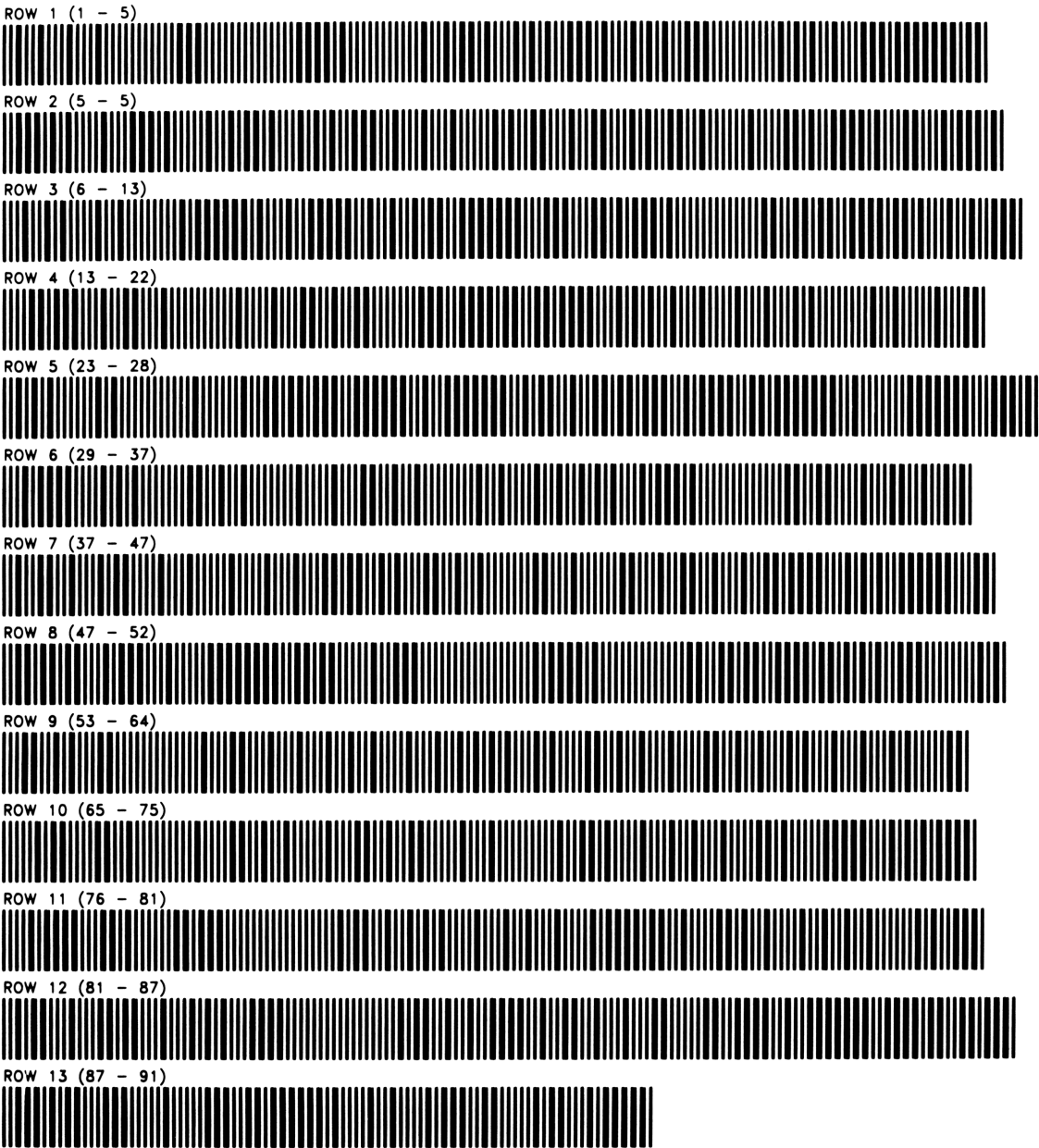
Program Listings

01*LBL "KEN "		50 GTO A	
02 CLRG		51*LBL E	
03 FIX 0		52 FIX 2	
04 CF 29		53 RCL 03	
05 "KENDALL S COF."	Initialize	54 12	
06 AVIEW		55 *	
07 PSE		56 RCL 05	Calculate W
08 "K?"		57 X↑2	
09 PROMPT		58 /	
10 STO 05		59 RCL 04	
11 GTO A		60 /	
12*LBL C		61 RCL 04	
13 ST- 02	Correction	62 X↑2	
14 1	routine	63 1	
15 ST- 01		64 -	
16*LBL A		65 /	
17 "R"		66 RCL 04	
18 RCL 01		67 1	
19 1		68 ST- 04	
20 +		69 +	
21 RCL 04		70 3	
22 1		71 *	
23 +		72 RCL 04	
24 ARCL X		73 /	
25 "F,"	Accumulate sums	74 -	
26 ARCL Y		75 "W"	
27 "F ?"		76 XEQ 11	
28 PROMPT		77 RCL 05	
29 ST+ 02		78 *	
30 1		79 RCL 04	Calculate χ^2
31 ST+ 01		80 *	and df
32 RCL 01		81 "CHI SQ"	
33 RCL 05		82 XEQ 11	
34 X>Y?		83 RCL 04	
35 GTO A		84 "dF"	
36 1		85*LBL 11	
37 ST+ 04		86 "F="	
38 RCL 02		87 ARCL X	Display routine
39 STO 06		88 AVIEW	
40 X↑2		89 STOP	
41 ST+ 03		90 RTN	
42 0		91 .END.	
43 STO 01			
44 STO 02			
45 RCL 06			
46 "S"			
47 "F"			
48 ARCL 04			
49 XEQ 11			
		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS			
00		50		SIZE <u>007</u> TOT. REG. <u>30</u> USER MODE ENG <u> </u> FIX <u>2</u> SCI <u> </u> ON <u>X</u> OFF <u> </u> DEG <u> </u> RAD <u> </u> GRAD <u> </u>			
	j ... k			FLAGS # INIT S/C SET INDICATES CLEAR INDICATES			
	$\sum R_{ij}$						
	$\sum (R_{ij})^2$			29		For proper display format	
	i ... n						
05	K	55					
	$\sum R_{ij}$						
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
				ASSIGNMENTS			
				FUNCTION		KEY	
40		90					
45		95					

KENDALL'S COEFFICIENT
OF CONCORDANCE
PROGRAM REGISTERS NEEDED: 24



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Hewlett-Packard Software

In terms of power and flexibility, the problem-solving potential of the HP-41 programmable calculator is nearly limitless. And in order to see the practical side of this potential, HP has different types of software to help save you time and programming effort. Every one of our software solutions has been carefully selected to effectively increase your problem-solving potential. Chances are, we already have the solutions you're looking for.

Application Pacs

To increase the versatility of your HP-41, HP has an extensive library of "Application Pacs". These programs transform your HP-41 into a specialized calculator in seconds. Included in these pacs are detailed manuals with examples, miniature plug-in Application Modules, and keyboard overlays. Every Application Pac has been designed to extend the capabilities of the HP-41.

You can choose from:

Aviation (Pre-Flight Only) 00041-15018
Clinical Lab 00041-15024
Circuit Analysis 00041-15024
Financial Decisions 00041-15004
Mathematics 00041-15003
Structural Analysis 00041-15021
Surveying 00041-15005
Securities 00041-15026

Statistics 00041-15002
Stress Analysis 00041-15027
Games 00041-15022
Home Management 00041-15023
Machine Design 00041-15020
Navigation 00041-15017
Real Estate 00041-15016
Thermal and Transport Science 00041-15019
Petroleum Fluids 00041-15039

Users' Library

The Users' Library provides the best programs from contributors and makes them available to you. By subscribing to the HP-41 Users' Library you'll have at your fingertips literally hundreds of different programs from many different application areas.

***Users' Library Solutions Books**

Hewlett-Packard offers a wide selection of Solutions Books complete with user instructions, examples, and listings. These solution books will complement our other software offerings and provide you with a valuable tool for program solutions.

You can choose from:

Business Stat/Marketing/Sales 00041-90094
Home Construction Estimating 00041-90096
Lending, Saving and Leasing 00041-90086
Real Estate 00041-90136
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Geometry 00041-90084
High-Level Math 00041-90083
Test Statistics 00041-90082
Antennas 00041-90093
Chemical Engineering 00041-90100
Control Systems 00041-90092
Electrical Engineering 00041-90088
Fluid Dynamics and Hydraulics 00041-90139
Games II 00041-90443

Civil Engineering 00041-90089
Heating, Ventilating & Air Conditioning 00041-90140
Mechanical Engineering 00041-90090
Solar Engineering 00041-90138
Calendars 00041-90145
Cardiac/Pulmonary 00041-90097
Chemistry 00041-90102
Games 00041-90099
Optometry I (General) 00041-90143
Optometry II (Contact Lens) 00041-90144
Physics 00041-90142
Surveying 00041-90141
Time Module Solutions 00041-90395

*Some books require additional memory modules to accommodate all programs.

TEST STATISTICS

ONE SAMPLE TEST STATISTICS FOR THE MEAN
TEST STATISTICS FOR THE CORRELATION COEFFICIENT
DIFFERENCES AMONG PROPORTIONS
BEHRENS-FISHER STATISTIC
KRUSKAL-WALLIS STATISTIC
MEAN-SQUARE SUCCESSIVE DIFFERENCE
THE RUN TEST FOR RANDOMNESS
INTRAClass CORRELATION COEFFICIENT
FISHER'S EXACT TEST FOR A 2×2 CONTINGENCY TABLE
BARTLETT'S CHI-SQUARE STATISTIC
MANN-WHITNEY STATISTIC
KENDALL'S COEFFICIENT OF CONCORDANCE



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