

HIP-67/HIP-97

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6. What program(s) would you add to this pac?

7. In the list below, select up to three application areas for which you purchased this pac. Please indicate the order of importance by 1, 2, 3, (1 represents the most important area).

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| ___ 03 Electrical/Electronic | ___ 53 Insurance |
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| ___ 06 Surveying | ___ 56 Securities |
| ___ 10 Other (Specify) _____ | ___ 57 Sales |
| Science | ___ 58 Marketing |
| ___ 31 Biology | ___ 59 Other (Specify) _____ |
| ___ 32 Chemistry | Other |
| ___ 33 Earth Sciences | ___ 71 Architecture |
| ___ 34 Mathematics | ___ 72 Aviation |
| ___ 35 Medical Sciences | ___ 73 Computer Science |
| ___ 36 Physics | ___ 74 Education |
| ___ 37 Statistics | ___ 75 Navigation |
| ___ 39 Other (Specify) _____ | ___ 79 Other (Specify) _____ |

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ATTENTION: APPLICATIONS

Introduction

The 23 programs of ME Pac I have been drawn from the fields of statics, dynamics, stress analysis, machine design, and thermodynamics.

Each program in this pac is represented by one or more magnetic cards and a section in this manual. The manual provides a description of the program with relevant equations, a set of instructions for using the program, and one or more example problems, each of which includes a list of the actual keystrokes required for its solution. Program listings for all the programs in the pac appear at the back of this manual. Explanatory comments have been incorporated in the listings to facilitate your understanding of the actual working of each program. Thorough study of a commented listing can help you to expand your programming repertoire since interesting techniques can often be found in this way.

On the face of each magnetic card are various mnemonic symbols which provide shorthand instructions to the use of the program. You should first familiarize yourself with a program by running it once or twice while following the complete User Instructions in the manual. Thereafter, the mnemonics on the cards themselves should provide the necessary instructions, including what variables are to be input, which user-definable keys are to be pressed, and what values will be output. A full explanation of the mnemonic symbols for magnetic cards may be found in appendix A.

If you have already worked through a few programs in Standard Pac, you will understand how to load a program and how to interpret the User Instructions form. If these procedures are not clear to you, take a few minutes to review the sections, Loading a Program and Format of User Instructions, in your Standard Pac.

We hope that ME Pac I will assist you in the solution of numerous problems in your discipline. We would very much appreciate knowing your reactions to the programs in this pac, and to this end we have provided a questionnaire inside the front cover of this manual. Would you please take a few minutes to give us your comments on these programs? It is in the comments we receive from you that we learn how best to increase the usefulness of programs like these.

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A WORD ABOUT PROGRAM USAGE

This application pac has been designed for both the HP-97 Programmable Printing Calculator and the HP-67 Programmable Pocket Calculator. The most significant difference between the HP-67 and the HP-97 calculators is the printing capability of the HP-97. The two calculators also differ in a few minor ways. The purpose of this section is to discuss the ways that the programs in this pac are affected by the difference in the two machines and to suggest how you can make optimal use of your machine, be it an HP-67 or an HP-97.

Many of the computed results in this pac are output by PRINT statements; on the HP-97 these results will be output on the printer. On the HP-67 each PRINT command will be interpreted as a PAUSE: the program will halt, display the result for about five seconds, then continue execution. The term “PRINT/PAUSE” is used to describe this output condition.

If you own an HP-67, you may want more time to copy down the number displayed by a PRINT/PAUSE. All you need to do is press any key on the keyboard. If the command being executed is PRINTx (eight rapid blinks of the decimal point), pressing a key will cause the program to halt. Execution of the halted program may be re-initiated by pressing **R/S**.

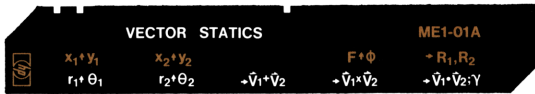
HP-97 users may also want to keep a permanent record of the values input to a certain program. A convenient way to do this is to set the Print Mode switch to NORMAL before running the program. In this mode all input values and their corresponding user-definable keys will be listed on the printer, thus providing a record of the entire operation of the program.

Another area that could reflect differences between the HP-67 and the HP-97 is in the keystroke solutions to example problems. It is sometimes necessary in these solutions to include operations that involve prefix keys, namely, **f** on the HP-97 and **f**, **g**, and **h** on the HP-67. For example, the operation **10^x** is performed on the HP-97 as **f** **10^x** and on the HP-67 as **g** **10^x**. In such cases, the keystroke solution omits the prefix key and indicates only the operation (as here, **10^x**). As you work through the example problems, take care to press the appropriate prefix keys (if any) for your calculator.

Also in keystroke solutions, those values that are output by the PRINT command will be followed by three asterisks (***)

Notes

VECTOR STATICS



Part I of this program performs the basic two dimensional vector operations of addition, cross product and dot, scalar, or inner product. In addition, the angle between vectors may be found. Vectors may be input in polar form (r, θ) or rectangular form (x_1, y_1) .

Equations:

for addition: $\vec{V}_1 + \vec{V}_2 = (x_1 + x_2)\vec{i} + (y_1 + y_2)\vec{j}$

for cross products: $\vec{V}_1 \times \vec{V}_2 = (x_1y_2 - x_2y_1)\vec{k}$

for dot, scalar, or inner product: $\vec{V}_1 \cdot \vec{V}_2 = x_1x_2 + y_1y_2$

for the angle between vectors: $\gamma = \cos^{-1} \frac{\vec{V}_1 \cdot \vec{V}_2}{|\vec{V}_1||\vec{V}_2|}$

where:

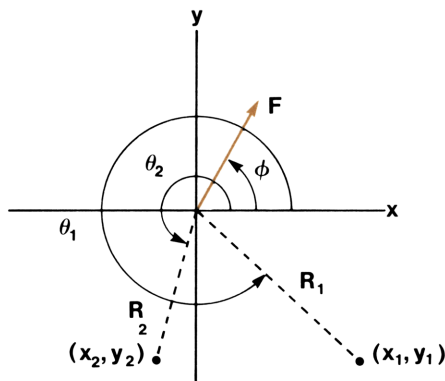
x_1 is the x component of \vec{V}_1 ($x_1 = r_1 \cos \theta_1$);

x_2 is the x component of \vec{V}_2 ($x_2 = r_2 \cos \theta_2$);

y_1 is the y component of \vec{V}_1 ($y_1 = r_1 \sin \theta_1$);

y_2 is the y component of \vec{V}_2 ($y_2 = r_2 \sin \theta_2$);

Part II of this program calculates the two reaction forces necessary to balance a given two-dimensional force vector. The direction of the reaction forces may be specified as a vector of arbitrary length or by Cartesian coordinates using the point of force application as the origin.



Equations:

$$R_1 \cos \theta_1 + R_2 \cos \theta_2 = F \cos \phi$$

$$R_1 \sin \theta_1 + R_2 \sin \theta_2 = F \sin \phi$$

where:

F is the known force;

ϕ is the direction of the known force;

R_1 is one reaction force;

θ_1 is the direction of R_1 ;

R_2 is the second reaction force;

θ_2 is the direction of R_2 .

The coordinates x_1 and y_1 are referenced from the point where F is applied to the end of the member along which R_1 acts; x_2 and y_2 are the coordinates referenced from the point where F is applied to the end of the member along which R_2 acts.

Remarks:

Registers $R_0 - R_3$; $R_{S0} - R_{S9}$ and I are available for user storage.

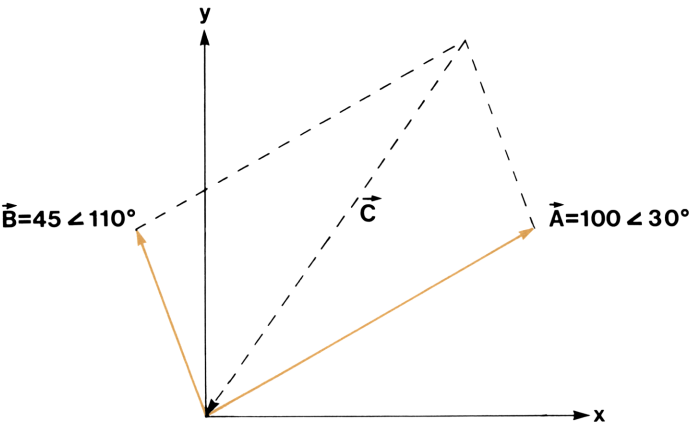
STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	To resolve a force in two known directions, go to step 6.			
	For vector addition, cross product, or dot product continue with step 3.			
3	Input \vec{V}_1 and \vec{V}_2 :			
	\vec{V}_1 in polar form	r_1	ENTER	r_1
		θ_1	A	y_1
	or			
	\vec{V}_1 in rectangular form	x_1	ENTER	x_1
		y_1	f A	y_1
	and			
	\vec{V}_2 in polar form	r_2	ENTER	r_2
		θ_2	B	y_2
	or			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	\vec{V}_2 in rectangular form.	x_2	ENTER➤	x_2
		y_2	I B	y_2
4	Perform vector operation:			
	add vectors		C	r, θ
	or			
	take cross product		D	$\vec{V}_1 \times \vec{V}_2$
	or			
	take dot (or scalar) product.		E	$\vec{V}_1 \cdot \vec{V}_2$
	(Optionally, calculate angle			
	between vectors after dot			
	product.)		R/S	γ
5	For a new case, go to step 3			
	and change \vec{V}_1 and/or \vec{V}_2 .			
6	Define reaction directions as			
	Cartesian coordinates or as			
	vectors of arbitrary magnitude.			
	(Use the point of force appli-			
	cations as the origin):			
	define direction one in polar			
	form	1	ENTER➤	1.00
		θ_1	A	$\sin \theta_1$
	or			
	in rectangular form	x_1	ENTER➤	x_1
		y_1	I A	y_1
	and			
	define direction two in polar			
	form	1	ENTER➤	1.00
		θ_2	B	$\sin \theta_2$
	or			
	in rectangular form.	x_2	ENTER➤	x_2
		y_2	I B	y_2

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	Input known force:			
	magnitude	F	ENTER	F
	then direction.	ϕ	f D	$F \sin \phi$
8	Compute reactions		f E	R_1, R_2
9	To change force, go to step 7.			
	To change either or both			
	directions, go to step 6.			

Example 1:

Forces A and B are shown below. If static equilibrium exists, what is force C.



Keystrokes:

Outputs:

To obtain \vec{C} , add \vec{A} and \vec{B} using negative magnitudes for both.

45 **CHS** **ENTER** 110 **A** 100 **CHS**

ENTER 30 **B** **C** \longrightarrow

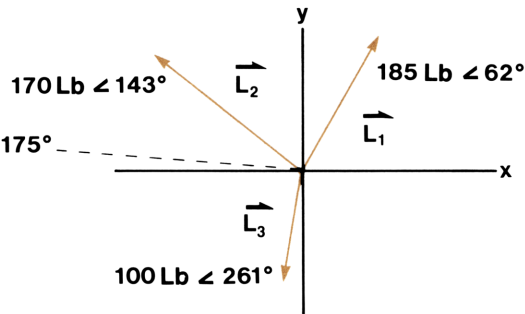
116.57 ***

-127.66 ***

$\vec{C} = 116.57 \angle -127.66^\circ$

Example 2:

Resolve the following three loads along a 175 degree line.



Keystrokes:

First add \vec{L}_1 and \vec{L}_2 .

185 **ENTER** 62 **A** 170 **ENTER**
143 **B C** \longrightarrow

Define the result as \vec{V}_1 and add \vec{L}_3 .
A 100 **ENTER** 261 **B C** \longrightarrow

To resolve the vector, just calculated
along the 175° line.

A 1 **ENTER** 175 **B E** \longrightarrow

What is the angle between the
vector and the line?

R/S \longrightarrow

Outputs:

270.12 *** (lb)
100.43 *** (deg)

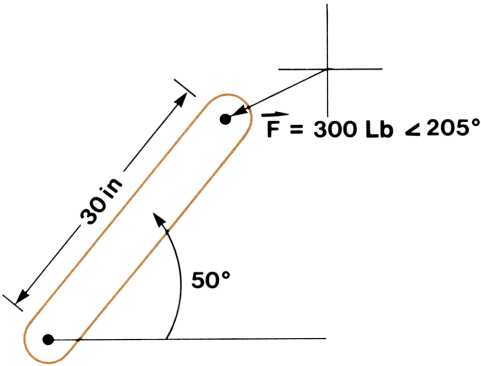
178.94 *** (lb)
111.15 *** (deg)

78.86 *** (lb)

63.85 *** (deg)

Example 3:

What is the moment at the shaft of the crank pictured below? What is the reaction force transmitted along the member?



Keystrokes:

Moment by cross product ($\vec{r}_1 \times \vec{F}$).

30 **ENTER** 50 **A** 300 **ENTER**
205 **B D** \longrightarrow

Resolution along crank

1 **ENTER** 50 **A E** \longrightarrow

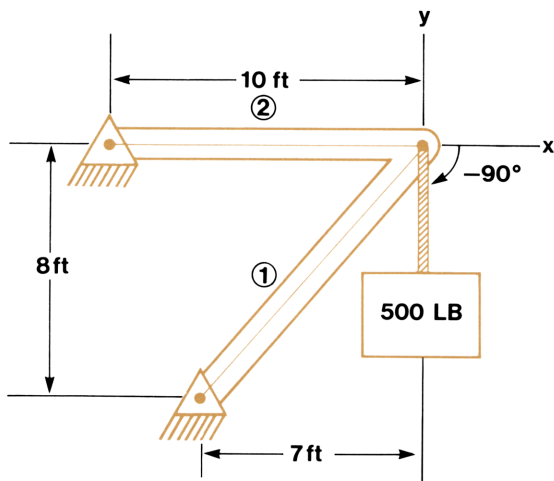
Outputs:

3803.56 in-lb

-271.89 lb

Example 4:

Find the reaction forces in the pin-jointed structure shown below.



Keystrokes:

7 CHS ENTER + 8 CHS f A →
10 CHS ENTER + 0 f B →
500 ENTER + 90 CHS f D →
f E →

Outputs:

-8.00
0.00
-500.00
-664.38 *** (R₁)
437.50 *** (R₂)

Notes

SECTION PROPERTIES

SECTION PROPERTIES - INPUT

ME1-02A1

START

$(x_i + y_i + 1)x_{i+1} + y_{i+1}$

$x_0 + y_0 + 2d$

SECTION PROPERTIES - OUTPUT

ME1-02A2

\bar{x}, \bar{y}, A

I_x, I_y, I_{xy}

$I_{\bar{x}}, I_{\bar{y}}, I_{\bar{xy}}$

$\Phi, I_{x\Phi}, I_{y\Phi}$

The properties of polygonal sections (see figure 1) may be calculated using this program. The (x, y) coordinates of the vertices of the polygon (which must be located entirely within the first quadrant) are input sequentially for a complete, clockwise path around the polygon. Holes in the cross section, which do not intersect the boundary, may be deleted by following a counter-clockwise path.

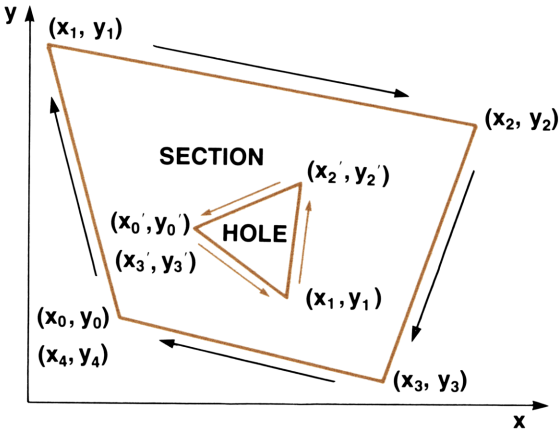


Figure 1 — Polygonal Sections

A special feature allows addition or deletion of circular areas. After the point by point traverse of the section has been completed, circular deletions or additions are specified by the (x,y) coordinates of the circle centers and by the circle diameters. If the diameter is specified as a positive number, the circular areas are added. A negative diameter causes circular areas to be deleted. Example 4 shows an application of this feature.

After all values have been input, the coordinates of the centroid (\bar{x}, \bar{y}) and the area (A) of the section may be output using card 2, key **A**. The moment of inertia about the x axis (I_x), about the y axis (I_y) and the product of inertia (I_{xy}) are output using **B**. Similar moments, $I_{\bar{x}}$, $I_{\bar{y}}$ and $I_{\bar{xy}}$, about an axis translated to the centroid of the section are calculated when **C** is pressed.

Pressing **D** calculates the moments of inertia, $I_{\bar{x}\phi}$ and $I_{\bar{y}\phi}$, about the principal axis. The rotation angle (ϕ) between the principal axis and the axis which was translated to the centroid is also calculated. The moments of inertia I_x' , I_y' , the polar moment of inertia J and the product of inertia I_{xy}' may be calculated about any arbitrary axis by specifying its location and rotation with respect to the original axis and pressing **f D**.

Equations:

$$A = - \sum_{i=0}^n (y_{i+1} - y_i)(x_{i+1} + x_i)/2$$

$$\bar{x} = \frac{-1}{A} \sum_{i=0}^n [(y_{i+1} - y_i)/8] [(x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2/3]$$

$$\bar{y} = \frac{1}{A} \sum_{i=0}^n [(x_{i+1} - x_i)/8] [(y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2/3]$$

$$I_x = \sum_{i=0}^n [(x_{i+1} - x_i)(y_{i+1} + y_i)/24] [(y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2]$$

$$I_y = - \sum_{i=0}^n [(y_{i+1} - y_i)(x_{i+1} + x_i)/24] [(x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2]$$

$$I_{xy} = \sum_{i=0}^n \frac{1}{(x_{i+1} - x_i)} \left[\frac{1}{8} (y_{i+1} - y_i)^2 (x_{i+1} + x_i) (x_{i+1}^2 + x_i^2) \right. \\ \left. + \frac{1}{3} (y_{i+1} - y_i) (x_{i+1} y_i - x_i y_{i+1}) (x_{i+1}^2 + x_{i+1} x_i + x_i^2) \right. \\ \left. + \frac{1}{4} (x_{i+1} y_i - x_i y_{i+1})^2 (x_{i+1} + x_i) \right]$$

$$I_{\bar{x}} = I_x - A\bar{y}^2$$

$$I_{\bar{y}} = I_y - A\bar{x}^2$$

$$I_{\bar{x}\bar{y}} = I_{xy} - A\bar{x}\bar{y}$$

$$\phi = \frac{1}{2} \tan^{-1} \left(\frac{-2I_{\bar{x}\bar{y}}}{I_{\bar{x}} - I_{\bar{y}}} \right)$$

$$I_x' = I_{\bar{x}} \cos^2 \theta + I_{\bar{y}} \sin^2 \theta - I_{\bar{x}\bar{y}} \sin 2\theta$$

$$I_y' = I_{\bar{y}} \cos^2 \theta + I_{\bar{x}} \sin^2 \theta + I_{\bar{x}\bar{y}} \sin 2\theta$$

$$J = I_x' + I_y'$$

$$I_{xy}' = \frac{(I_{\bar{x}} - I_{\bar{y}})}{2} \sin 2\theta + I_{\bar{x}\bar{y}} \cos 2\theta$$

$$A_{\text{circle}} = \frac{\pi d^2}{4}$$

$$I_{\text{circle}} = \frac{\pi d^4}{64}$$

where:

x_{i+1} is the x coordinate of the current vertex point;

y_{i+1} is the y coordinate of the current vertex point;

x_i is the x coordinate of the previous vertex point;

y_i is the y coordinate of the previous vertex point;

A is the area;

\bar{x} is the x coordinate of the centroid;

\bar{y} is the y coordinate of the centroid;

I_x is the moment of inertia about the x-axis;

I_y is the moment of inertia about the y-axis;

I_{xy} is the product of inertia;

$I_{\bar{x}}$ is the moment of inertia about the x-axis translated to the centroid;

$I_{\bar{y}}$ is the moment of inertia about the y-axis translated to the centroid;

$I_{\bar{x}\bar{y}}$ is the product of inertia about the translated axis;

ϕ is the angle between the translated axis and the principal axis;

$I_{\bar{x}\phi}$ is the moment of inertia about the translated, rotated, principal x-axis;

$I_{\bar{y}\phi}$ is the moment of inertia about the translated, rotated, principal y-axis;

θ is the angle between the original axis and an arbitrary axis.

I_x' is the x moment of inertia about the arbitrary axis;

I_y' is the y moment of inertia about the arbitrary axis;

J is the polar moment of inertia about the arbitrary axis;

I_{xy}' is the product of inertia about the arbitrary axis;

d is the diameter of a circular area.

Reference:

Wojciechowski, Felix; *Properties of Plane Cross Sections; Machine Design*; P. 105, Jan. 22, 1976.







Remarks:

Registers $R_{S0} - R_{S9}$ are available for user storage.

The polygon must be entirely contained in the first quadrant.

Rounding errors will accumulate if the centroid of the section is a large distance from the origin of the coordinate system.

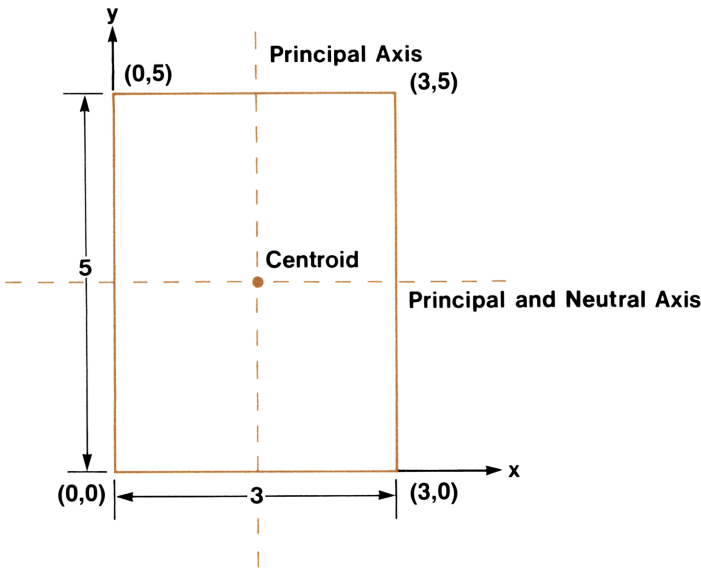
Curved boundaries may be approximated by straight line segments.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2 of card 1.			
2	Initialize.		 	
3	Key in (x, y) coordinates of first vertex.	x_i		y_i
		y_i		y_i
4	Key in (x, y) coordinates of next clockwise vertex.	x_{i+1}		x_{i+1}
		y_{i+1}		y_{i+1}
5	Wait for execution to end, then repeat step 4 for next point. Go to step 6 after you have reinput the starting point.			
6	To delete subsections within the section just traversed, return to step 3, but traverse in a counter-clockwise direction.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	Optional: Add circular areas,	x	ENTER +	x
		y	ENTER +	y
		d	C	0.00
	or delete circular areas.	x	ENTER +	x
		y	ENTER +	y
		d	CHS C	0.00
8	Load side 1 and side 2 of card 2.			
9	Calculate any or all of the following:			
	Centroid and area;		A	\bar{x}, \bar{y}, A
	Properties about original axis;		B	I_x, I_y, I_{xy}
	Properties about axis trans- lated to centroid;		C	$I_{\bar{x}}, I_{\bar{y}}, I_{\bar{xy}}$
	Angular orientation of principal axis and properties about principal axis;		D	$\phi, I_{\bar{x}\phi}, I_{\bar{y}\phi}$
	or			
	Specify arbitrary axis and rotation and calculate properties.	x'	ENTER +	
		y'	ENTER +	
		θ	f D	$I_{x'}, I_{y'}, J, I_{xy}'$
10	To modify the section, go to step 1, but skip step 2. For a new case, go to step 1.			

Example 1:

What is the moment of inertia about the x-axis (I_x) for the rectangular section shown? What is the moment of inertia about the neutral axis through the centroid of the section ($I_{\bar{x}\phi}$)?



Keystrokes:

Load side 1 and side 2 of card 1.

f A 0 ENTER 0 ENTER
0 ENTER 5 A →
3 ENTER 5 A →
3 ENTER 0 A →
0 ENTER 0 A →

Load side 1 and side 2 of card 2.

B →

D →

Outputs:

5.00
5.00
0.00
0.00

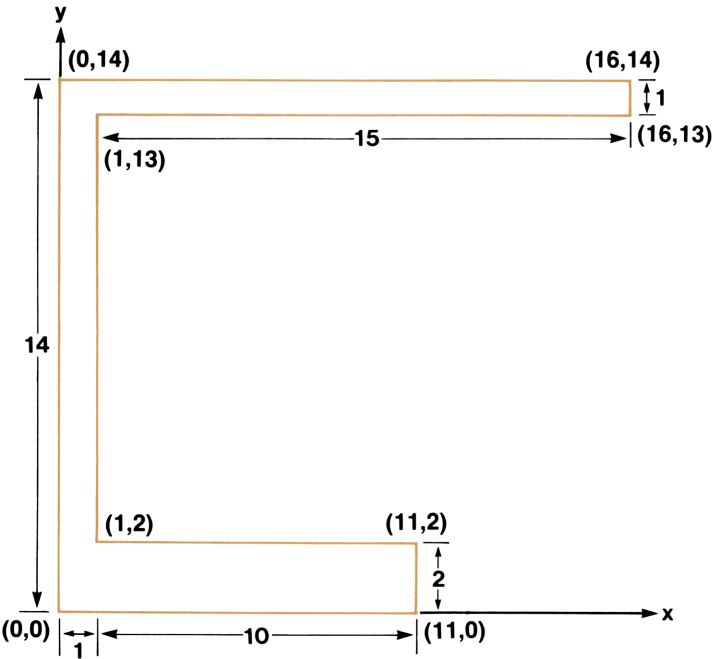
125.00 *** (I_x)
45.00 *** (I_y)
56.25 *** (I_{xy})
0.00 *** (ϕ)
31.25 *** ($I_{\bar{x}\phi}$)
11.25 *** ($I_{\bar{y}\phi}$)

Since $\phi = 0$ we would expect $I_{\bar{x}\phi}$ to equal $I_{\bar{x}}$. Press **C** to calculate $I_{\bar{x}}$, $I_{\bar{y}}$ and $I_{\bar{x}\bar{y}}$ and you will see that this prediction is correct. Also, $I_{\bar{x}\bar{y}}$ is zero about the principal axis.

C →	31.25 *** ($I_{\bar{x}}$)
	11.25 *** ($I_{\bar{y}}$)
	0.00 *** ($I_{\bar{x}\bar{y}}$)

Example 2:

Calculate the section properties for the beam shown below.



Keystrokes:

Load side 1 and side 2 of card 1.

f A 0 ENTER 0 ENTER	
0 ENTER 14 A →	
16 ENTER 14 A →	
16 ENTER 13 A →	
1 ENTER 13 A →	
1 ENTER 2 A →	
11 ENTER 2 A →	
11 ENTER 0 A →	

Outputs:

14.00
14.00
13.00
13.00
2.00
2.00
0.00

0 **ENTER** 0 **A** \longrightarrow

0.00

Load side 1 and side 2 of card 2.

A \longrightarrow

5.19 *** (\bar{x})

6.54 *** (\bar{y})

49.00 *** (A)

B \longrightarrow

3676.33 *** (I_x)

2256.33 *** (I_y)

1890.25 *** (I_{xy})

C \longrightarrow

1580.00 *** ($I_{\bar{x}}$)

934.49 *** ($I_{\bar{y}}$)

225.61 *** ($I_{\bar{x}\bar{y}}$)

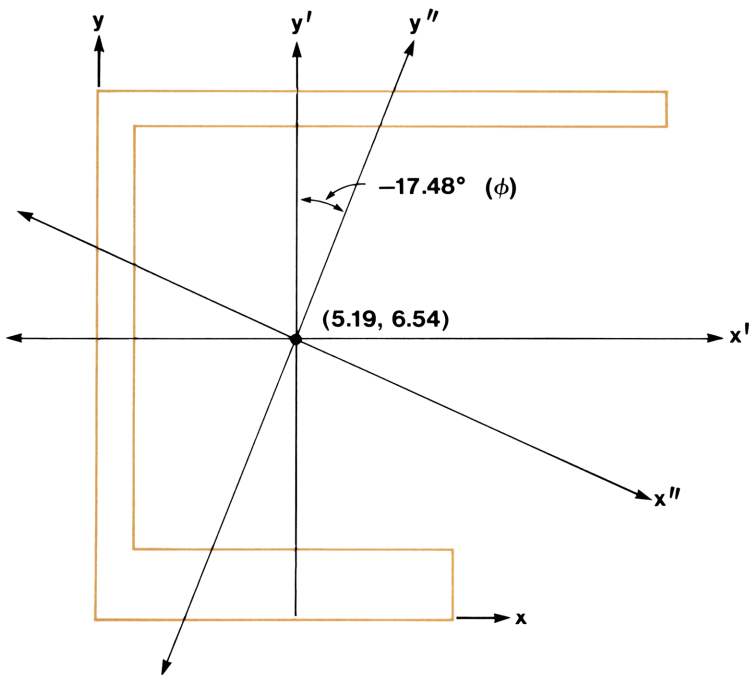
D \longrightarrow

-17.48 *** (ϕ)

1651.04 *** ($I_{\bar{x}\phi}$)

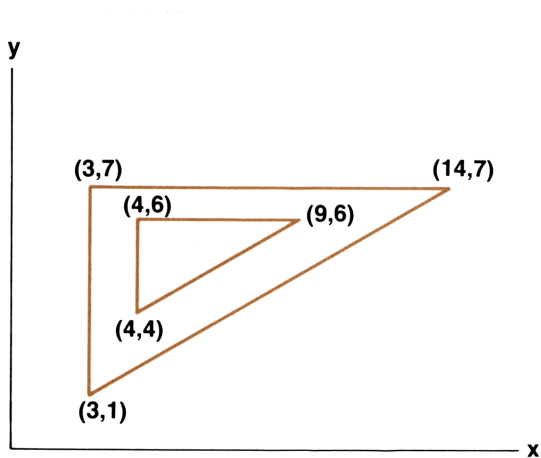
863.46 *** ($I_{\bar{y}\phi}$)

Below is a figure showing the translated axis and the rotated, principal axis of example 2.



Example 3:

What is the centroid of the section below? The inner triangular boundary denotes an area to be deleted.



Keystrokes:

Load side 1 and side 2 of card 1.

f A 3 ENTER 1 ENTER

3 ENTER 7 A →

14 ENTER 7 A →

3 ENTER 1 A →

Delete inner triangle:

4 ENTER 4 ENTER 9 ENTER

6 A →

4 ENTER 6 A →

4 ENTER 4 A →

Load side 1 and side 2 of card 2.

Compute Centroid

A →

Outputs:

7.00

7.00

1.00

6.00

6.00

4.00

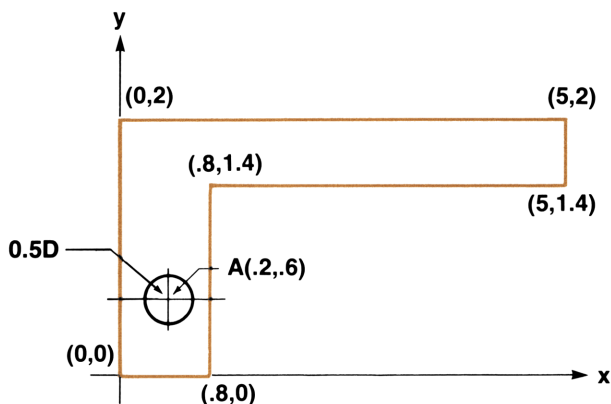
6.85 *** (\bar{x})

4.94 *** (\bar{y})

28.00 *** (A)

Example 4:

For the part below, compute the polar moment of inertia about point A. Point A denotes the center of a hole about which the part rotates. The area of the hole must be deleted from the cross section.

**Keystrokes:**

Load side 1 and side 2 of card 1.

```
f A 0 ENTER 0 ENTER 0 ENTER
2 A 5 ENTER 2 A 5 ENTER
1.4 A .8 ENTER 1.4 A .8 ENTER
0 A 0 ENTER 0 A
```

Delete the hole.

```
.2 ENTER .6 ENTER
.5 CHS C
```

Load side 1 and side 2 of card 2.

Compute J about point (.2, .6) with θ of zero.

```
.2 ENTER .6 ENTER
0 f D
```

Outputs:

0.00

0.00

```
3.91 *** (Ix)
22.22 *** (Iy)
26.13 *** (J)
7.61 *** (Ixy)
```

STRESS ON AN ELEMENT



STRESS ON AN ELEMENT

ME1-03A

E + ν

θ + s, τ

$\epsilon_a + \epsilon_b + \epsilon_c$

$+ \epsilon_1, \epsilon_2, \theta$

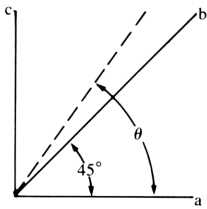
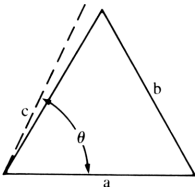
$s_x + s_y + \tau_{xy}$

$+ s_1, s_2, \tau_{max}, \theta$

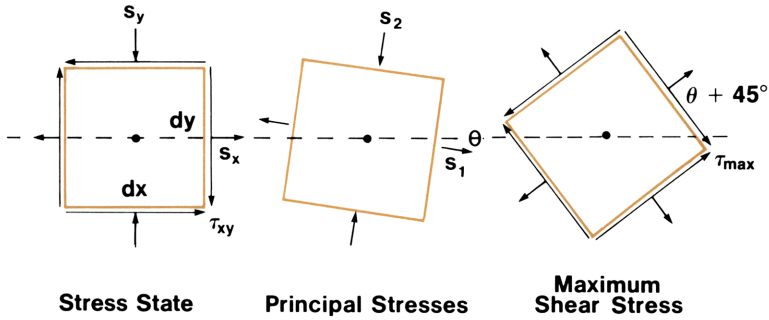
This program reduces data from rosette strain gage measurements and/or performs Mohr circle stress analysis calculations.

Correlations for rectangular and equiangular rosette configurations are included.

Strain Gage Equations:

CONFIGURATION CODE	1	2
TYPE OF ROSETTE	RECTANGULAR	DELTA (EQUIANGULAR)
		
PRINCIPAL STRAINS: ϵ_1, ϵ_2	$\frac{1}{2} \left[\epsilon_a + \epsilon_c \pm \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2} \right]$	$\frac{1}{3} \left[\epsilon_a + \epsilon_b + \epsilon_c \pm \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2 + 2(\epsilon_c - \epsilon_a)^2} \right]$
CENTER OF MOHR CIRCLE: $\frac{s_1 + s_2}{2}$	$\frac{E(\epsilon_a + \epsilon_c)}{2(1 - \nu)}$	$\frac{E(\epsilon_a + \epsilon_b + \epsilon_c)}{3(1 - \nu)}$
MAXIMUM SHEAR STRESS: τ_{max}	$\frac{E}{2(1 + \nu)} \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2}$	$\frac{E}{3(1 + \nu)} \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2 + 2(\epsilon_c - \epsilon_a)^2}$
ORIENTATION OF PRINCIPAL STRESSES	$\tan^{-1} \left[\frac{2\epsilon_b - \epsilon_a - \epsilon_c}{\epsilon_a - \epsilon_c} \right]$	$\tan^{-1} \left[\frac{\sqrt{3}(\epsilon_c - \epsilon_b)}{2(\epsilon_a - \epsilon_b - \epsilon_c)} \right]$

The Mohr circle portion of the program converts an arbitrary stress configuration to principal stresses, maximum shear stress and rotation angle. It is then possible to calculate the state of stress for an arbitrary orientation θ' .



Mohr Circle Equations:

$$\tau_{\max} = \sqrt{\left(\frac{s_x - s_y}{2}\right)^2 + \tau_{xy}^2}$$

$$s_1 = \frac{s_x + s_y}{2} + \tau_{\max}$$

$$s_2 = \frac{s_x + s_y}{2} - \tau_{\max}$$

$$\theta = \frac{1}{2} \tan^{-1} \left(\frac{2\tau_{xy}}{s_x - s_y} \right)$$

$$s = \frac{s_1 + s_2}{2} + \tau_{\max} \cos 2\theta'$$

$$\tau = \tau_{\max} \sin 2\theta'$$

where:

s is the normal stress, and τ is the shear stress.

ϵ_a , ϵ_b , and ϵ_c are the strains measured using rosette gages;

s_x is the stress in the x direction for Mohr circle input;

s_y is the stress in the y direction for Mohr circle input;

τ_{xy} is the shear stress on the element for Mohr circle input;

ϵ_1 and ϵ_2 are the principal strains;

s_1 and s_2 are the principal normal stresses;

τ_{\max} is the maximum shear stress;

θ is the counterclockwise angle of rotation from the specified axis to the principal axis. Note that this is opposite to the normal Mohr circle convention.

θ' is an arbitrary rotation angle from the original (x, y) axis;

E is modulus of elasticity.

Reference:

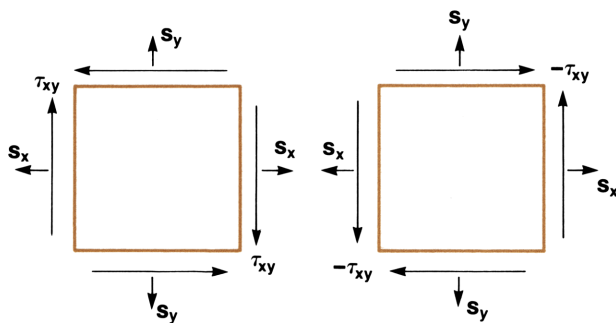
Spotts, M.F., *Design of Machine Elements*, Prentice-Hall, 1971.

Beckwith, T. G., Buck, N. L., *Mechanical Measurements*, Addison-Wesley, 1969

Remarks:

R_0, R_1, R_7, R_8, R_D and $R_{S0}-R_{S9}$ are available for user storage.

Negative stresses and strains indicate compression. Positive and negative shear are represented below:

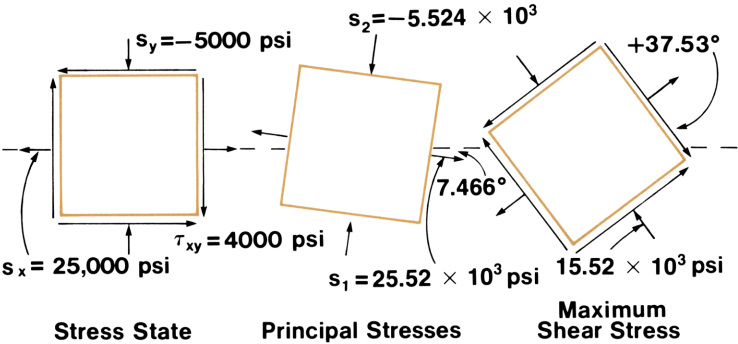


STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	If a stress configuration is known, go to step 8 for Mohr circle evaluation. Continue with step 3 for strain gage data reduction.			
3	Select strain gage configuration:			
	Rectangular		f A	1.000 00
	or Delta.		f B	2.000 00

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
4	Input modulus of elasticity,	E	ENTER	E
	<i>then</i> Poisson's ratio.	ν	D	E
5	Input strains:			
		ϵ_a	ENTER	ϵ_a
		ϵ_b	ENTER	ϵ_b
		ϵ_c	A	ϵ_a
6	Calculate principal strains			
	and rotation angle.		B	$\epsilon_1, \epsilon_2, \theta$
7	Skip to step 9 for Mohr circle			
	applications of calculations			
	just completed.			
8	Input stress on element in x			
	direction	S_x	ENTER	S_x
	<i>then</i> stress in y direction	S_y	ENTER	S_y
	<i>then</i> shear stress.	τ_{xy}	C	0.000 00
9	Calculate principal stresses.		D	$S_1, S_2, \tau_{max},$
				θ
10	Optional: Calculate stress			
	configuration at a specified			
	angle.	θ'	E	S, τ
11	To specify another angle go			
	to step 10. For a new case go			
	to step 2.			

Example 1:

If $s_x = 25000$ psi, $s_y = -5000$ psi, and $\tau_{xy} = 4000$ psi, compute the principal stresses and the maximum shear stress. Compute the normal stresses, where shear stress is maximum ($\theta + 45^\circ$).



Keystrokes:

25000 **ENTER** 5000 **CHS** **ENTER**
4000 **C** **D** \longrightarrow

45 **+** \longrightarrow
E \longrightarrow

Outputs:

25.52 03 *** (s_1)
-5.524 03 *** (s_2)
15.52 03 *** (τ_{\max})
-7.466 00 *** (θ)
37.53 00
10.00 03 *** (s)
15.52 03 *** (τ_1)

Example 2:

A rectangular rosette measures the strains below. What are the principal strains and principal stresses?

$\epsilon_a = 90 \times 10^{-6}$ $\epsilon_b = 137 \times 10^{-6}$ $\epsilon_c = 305 \times 10^{-6}$
 $\nu = 0.3$ $E = 30 \times 10^6 \text{ psi}$

Keystrokes:

f **A** \longrightarrow
30 **EEX** 6 **ENTER** .3 **f** **D** \longrightarrow
90 **EEX** **CHS** 6 **ENTER** 137
EEX **CHS** 6 **ENTER** 305 **EEX** **CHS**
6 **A** \longrightarrow
B \longrightarrow

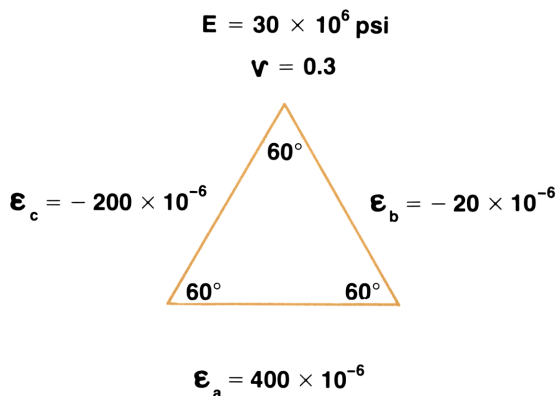
D \longrightarrow

Outputs:

1.000 00
30.00 06
90.00-06
320.9-06 *** (ϵ_1)
74.14-06 *** (ϵ_2)
14.69 00 *** (θ)
11.31 03 *** (s_1)
5.618 03 *** (s_2)
2.847 03 *** (τ_{\max})
14.69 00 *** (θ)

Example 3:

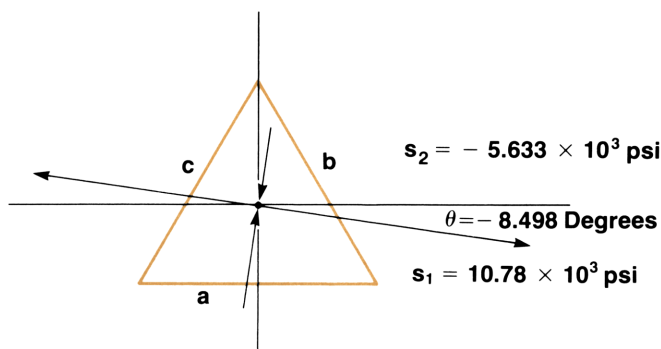
An equiangular rosette measures the strains below. What are the principal strains and stresses?

**Keystrokes:**

f B _____ →
 400 **EEX** **CHS** 6 **ENTER** 20
CHS **EEX** **CHS** 6 **ENTER** 200
CHS **EEX** **CHS** 6 **A** _____ →
B _____ →
D _____ →

Outputs:

2.000 00
 400.0-06
 415.5-06 *** (ϵ_1)
 -295.5-06 *** (ϵ_2)
 -8.498 00 *** (θ)
 10.78 03 *** (s_1)
 -5.633 03 *** (s_2)
 8.204 03 *** (τ_{\max})
 -8.498 00 *** (θ)

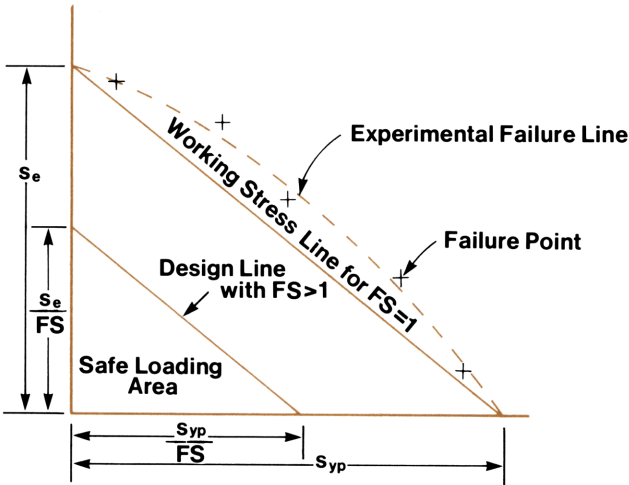


SODERBERG'S EQUATION FOR FATIGUE



This program will calculate the seventh variable from the other six values in Soderberg's equation. It is useful in sizing parts for cyclic loading, calculating factors of safety, choosing materials based on size constraints and estimating the fatigue resistance of available parts. Soderberg's equation is graphically represented in figure 1.

Equations:



Working Stress Diagram
Figure 1

$$\frac{S_{yp}}{FS} = \frac{S_{max} + S_{min}}{2} + K \left(\frac{S_{yp}}{S_e} \right) \left(\frac{S_{max} - S_{min}}{2} \right)$$

$$\frac{S_{max} + S_{min}}{2} = \frac{P_{max} + P_{min}}{2A}$$

$$\frac{S_{max} - S_{min}}{2} = \frac{P_{max} - P_{min}}{2A}$$

where:

S_{yp} is the yield point stress of the material;

S_e is the material endurance stress from reversed bending tests;

K is the stress concentration factor for the part;

FS is the factor of safety ($FS \geq 1.00$)

s_{\max} is the maximum stress;

s_{\min} is the minimum stress;

P_{\max} is the maximum load;

P_{\min} is the minimum load;

A is the cross sectional area of the part.

Reference:

Spotts, M. F., *Design of Machine Elements*; Prentice-Hall, Inc., 1971.

Baumeister, T. *Marks Standard Handbook for Mechanical Engineers*, McGraw-Hill Book Company, 1967.

Remarks:

If s_{\max} and s_{\min} are to be input or calculated instead of P_{\max} or P_{\min} , simply use 1.00 for the value of area.

R_0 – R_7 , R_{S0} – R_{S9} and I are available for storage.

This implementation of Soderberg's equation is for ductile materials only.

Values of stress concentration factors and material endurance limits may be found in the referenced sources.

In the presence of corrosive media, or for rough surfaces, fatigue effects may be much more significant than predicted by this program.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input six of the following seven:			
	Yield point stress	S_{yp}	F A	S_{yp}
	Endurance stress	S_e	F B	S_e
	Cross sectional area	A	A	A
	Stress concentration factor	K	B	K
	Maximum load	P_{\max}	C	P_{\max}
	Minimum load	P_{\min}	D	P_{\min}
	Factor of safety	FS	E	FS

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
3	Calculate the remaining value:			
	Yield point stress		f A	S_{yp}
	Endurance stress		f B	S_e
	Cross sectional area		A	A
	Stress concentration factor		B	K
	Maximum load		C	P_{max}
	Minimum load		D	P_{min}
	Factor of safety		E	FS
4	Optional: Output values in			
	S_{yp} , S_e , A, K, P_{max} , P_{min} ,			
	FS order.		f C	OUTPUT
5	For a new case, go to step 2			
	and change appropriate			
	inputs.			

Example 1:

What is the maximum permissible cyclic load for a part if the minimum load is 2000 pounds and the area is 0.5 square inches?

$S_{yp} = 70000 \text{ psi}$

$S_e = 25000 \text{ psi}$

$K = 1.25$

$FS = 2.0$

Keystrokes:

70000 **f** **A** 25000 **f** **B** .5 **A**
1.25 **B** 2000 **D** 2 **E** **C** →

If P_{max} is changed to 10000 pounds
what will S_e have to be?

10000 **C** **f** **B** →

Outputs:

8.889 03 (P_{max})

30.43 03 (S_e)

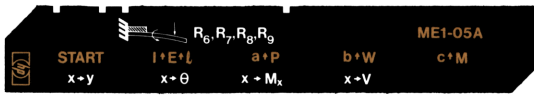
If s_e is changed back to 25000 psi
what will the factor of safety be?

25000 **f** **B** **E** \longrightarrow 1.750 00 (FS)

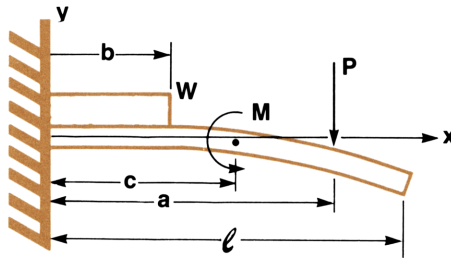
Output values for review:

f **C** \longrightarrow 70.00 03 *** (s_{yp})
25.00 03 *** (s_e)
500.0 -03 *** (A)
1.250 00 *** (K)
10.00 03 *** (P_{max})
2.000 03 *** (P_{min})
1.750 00 *** (FS)

CANTILEVER BEAMS



This program calculates deflection, slope, moment and shear at any specified point along a rigidly fixed, cantilever beam of uniform cross section. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, applied moments and combined distributed loads may be analyzed.

Equations:

$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{PX_1^2}{6EI} (X_1 - 3a) - \frac{Pa^2}{2EI} (x-a)(x>a)^* \quad (\text{deflection due to point load})$$

$$y_2 = \frac{-WX_2^2}{6EI} \left[X_2 \left(\frac{X_2}{4} - b \right) + 1.5 b^2 \right] - \frac{Wb^3}{6EI} (x-b)(x>b) \quad (\text{distributed load})$$

$$y_3 = \frac{MX_3^2}{2EI} + \frac{Mc}{EI} (x-c)(x>c) \quad (\text{applied moment})$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{PX_1}{2EI} (X_1 - 2a) \quad (\text{slope due to point load})$$

$$\theta_2 = \frac{WX_2}{EI} \left[X_2 \left(\frac{X_2}{6} - \frac{b}{2} \right) + \frac{b^2}{2} \right] \quad (\text{distributed load})$$

$$\theta_3 = \frac{MX_3}{EI} \quad (\text{applied moment})$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = P(X_1 - a) \quad (\text{moment due to point load})$$

$$M_{x2} = -W (X_2 (X_2/2 - b) + b^2/2) \quad (\text{distributed load})$$

$$M_{x3} = M (x \leq c) \quad (\text{applied moment})$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = P (x \leq a) \quad (\text{shear due to point load})$$

$$V_2 = W (b - X_2) \quad (\text{distributed load})$$

$$V_3 = 0 \quad (\text{applied moment})$$

where:

y is the deflection at a distance x from the wall;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

ℓ is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length.

M is an applied moment;

a is the distance from the foundation to the point load;

b is the distance to the end of the distributed load;

c is the distance to the applied moment;

$X_1 = x$ if $x \leq a$ or a if $x > a$;

$X_2 = x$ if $x \leq b$ or b if $x > b$

$X_3 = x$ if $x \leq c$ or c if $x > c$.







*The notation $(x > a)$ is interpreted as 1.00 if x is greater than a and as 0.00 if x is less than or equal to a .

Remarks:











Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

Registers R_{S0}–R_{S9} are available for user storage.

SIGN CONVENTIONS FOR BEAMS

NAME	VARIABLE	SENSE	SIGN
DEFLECTION	y		+
SLOPE	θ		+
INTERNAL MOMENT	M _x		+
SHEAR	V		+
EXTERNAL FORCE OR LOAD	P or W		+
EXTERNAL MOMENT	M		+

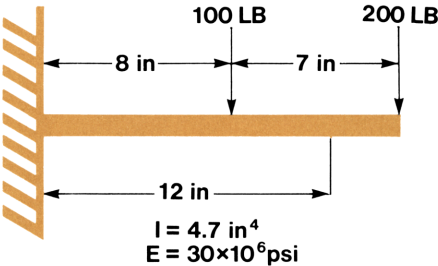
Sums of y, θ , M_x and V may be stored in R₆, R₇, R₈, and R₉, respectively. Note that these registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Initialize.		 A	0.000 00
3	Input moment of inertia	I	ENTER 	I
	then modulus of elasticity	E	ENTER 	E
	then beam length.	l	 B	EI
4	Input load(s):			
	Location of point load	a	ENTER 	a
	Point load	P	 C	a
	Length of distributed load	b	ENTER 	b
	Distributed load (force/length)	W	 D	b
	Location of applied moment	c	ENTER 	c
	Applied moment	M	 E	c
5	Key in x to specify the point of interest and calculate			
	deflection	x	A	y
	or slope	x	B	θ

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	or moment	x	C	M_x
	or shear.	x	D	V
6	For a new calculation with the same loading, go to step 5.			
	For new loads, go to step 4.			
	Be sure to set obsolete loadings to zero. For new beam properties, go to step 3.			
	To restart, go to step 2.			

Example 1:

What is the deflection at $x = 12$? Neglect the weight of the beam.



Keystrokes:

Outputs:

f **A** 4.7 **ENTER** 30 **EEX**

6 **ENTER** 15 **f** **B** 141.0 06

Compute deflection at 12 inches due to 100 lb weight:

8 **ENTER** 100 **f** **C** 12 **A** -211.8 -06

Store deflection due to 100 lb load for addition to deflection due to 200 lb load:

STO **9** -211.8-06

Compute deflection at 12 inches due to 200 lb load:

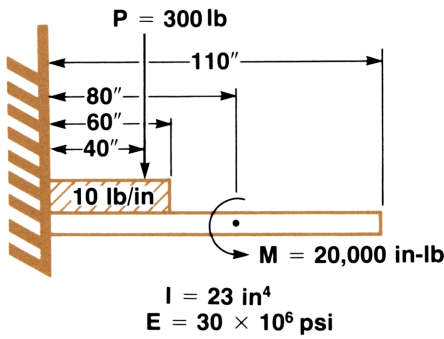
15 **ENTER** 200 **f** **C** 12 **A** -1.123 -03

Compute total deflection:

RCL **9** **+** -1.335 -03

Example 2:

For the beam below, compute deflection, slope, moment and shear at 0, 50, and 90 inches. Neglect the weight of the beam.



Keystrokes:

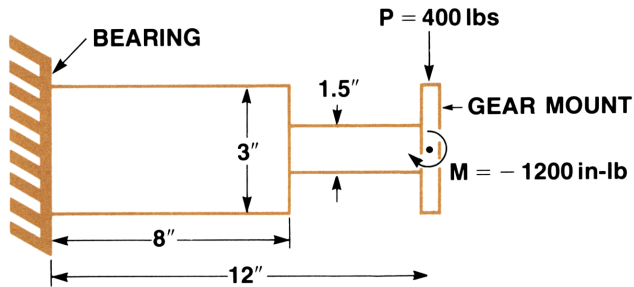
f A 23 ENTER 30 EEX
6 ENTER 110 f B 40 ENTER
300 f C 60 ENTER 10 f D
80 ENTER 20000 f E
0 A _____>
0 B _____>
0 C _____>
0 D _____>
50 A _____>
50 B _____>
50 C _____>
50 D _____>
90 A _____>
90 B _____>
90 C _____>
90 D _____>

Outputs:

0.000 00 (y)
0.000 00 (θ)
-10.00 03 (M_x)
900.00 00 (V)
5.211 -03
582.1 -06
19.50 03
100.0 00
50.14 -03
1.449 -03
0.000 00
0.000 00

Example 3:

The axle for a gear has the cross sectional shape and properties below. Assuming that the shaft may be modeled as a cantilever, calculate the deflection and slope at the gear mount and the moment and shear at the bearing. Neglect the weight of the axle.



$$E = 30 \times 10^6 \text{ psi}$$

$$I_{0-8} = 3.98 \text{ in}^4$$

$$I_{8-12} = 0.25 \text{ in}^4$$

Keystrokes:

Outputs:

First compute the deflection and slope from 0 to 8 inches based on larger cross section.

f **A** 3.98 **ENTER** 30 **EEX**

6 **ENTER** 12 **f** **B** 12 **ENTER**

400 **f** **C** 12 **ENTER** 1200

CHS **f** **E** 8 **A** **STO** **[6]** \longrightarrow -1.322 -03 (y_8)

8 **B** **STO** **[7]** \longrightarrow -294.8 -06 (θ_8)

Compute the deflection at 12 inches assuming no bending occurs from 8 to 12 inches.

4 **x** **RCL** **[6]** **+** **STO** **[6]** \longrightarrow -2.501 -03 (y_{12})

Compute the moment and shear at the bearing.

0 **C** \longrightarrow -6.000 03 (M_0)

0 **D** \longrightarrow 400.0 00 (V_0)

Change to smaller cross section and move origin to shoulder between large and small members.

.25 **ENTER** 30 **EEX** 6 **ENTER**

4 **f** **B** \longrightarrow 7.500 06

Add deflection and slope at 12 inches based on smaller cross section to values previously stored for large cross section.

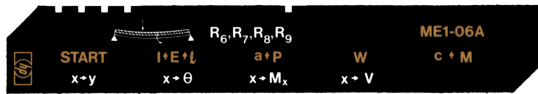
4 **A** \longrightarrow -5.831 -03

STO **+** **[6]** **RCL** **[6]** \longrightarrow -8.333 -03 (y_{12})

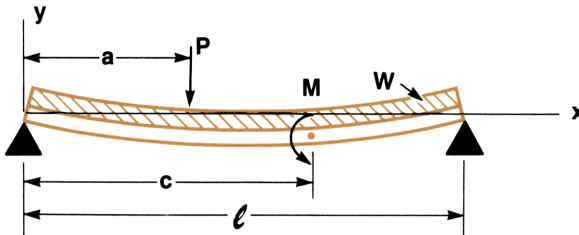
4 **B** \longrightarrow -2.773 -03

STO **+** **[7]** **RCL** **[7]** \longrightarrow -3.068 -03 (θ_{12})

SIMPLY SUPPORTED BEAMS



This program calculates deflection, slope, moment and shear at any specified point along a simply supported beam of uniform cross section. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, and multiple applied moments can be analyzed.

Equations:

$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{P(\ell - a)x}{6EI} [x^2 + (\ell - a)^2 - \ell^2]^* \quad (\text{deflection due to point load})$$

$$y_2 = \frac{-Wx}{24EI} [\ell^3 + x^2(x - 2\ell)] \quad (\text{distributed load})$$

$$y_3 = \frac{-Mx}{EI} \left[c - \frac{x^2}{6\ell} - \frac{1}{3} - \frac{c^2}{2\ell} \right]^{**} \quad (\text{applied moment})$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total moment})$$

$$\theta_1 = \frac{P(\ell - a)}{6EI} [3x^2 + (\ell - a)^2 - \ell^2]^* \quad (\text{slope due to point load})$$

$$\theta_2 = -\frac{W}{24EI} [\ell^3 + x^2(4x - 6\ell)] \quad (\text{distributed load})$$

$$\theta_3 = \frac{-M}{EI} \left[c - \frac{x^2}{2\ell} - \frac{\ell}{3} - \frac{c^2}{2\ell} \right]^{**} \quad (\text{applied moment})$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = \frac{P(\ell - a)x}{\ell}^* \quad (\text{moment due to point load})$$

$$M_{x2} = -\frac{Wx}{2} [x - \ell] \quad (\text{distributed load})$$

$$M_{x3} = \frac{Mx}{\ell}^{**} \quad (\text{applied moment})$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = \frac{P(\ell - a)}{\ell}^* \quad (\text{shear due to point load})$$

$$V_2 = W \left(\frac{\ell}{2} - x \right) \quad (\text{distributed load})$$

$$V_3 = \frac{M}{\ell} \quad (\text{applied moment})$$

where:

y is the deflection at a distance x from the left support;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

ℓ is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length;

M is an applied moment;

a is the distance from the left support to the point load;

c is the distance to the applied moment.

*If x is greater than a , $(\ell - a)$ is replaced by $-a$ and x is replaced by $(x - \ell)$.










**If x is greater than c , x is replaced by $(x - \ell)$ and c is replaced by $(\ell - c)$.

Remarks:

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

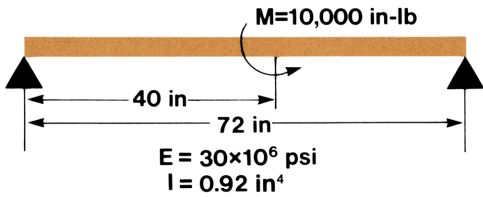
Registers R_{S0} – R_{S9} are available for user storage.

Sums of y , θ , M_x and V may be stored in R_6 , R_7 , R_8 , and R_9 , respectively. Note that these registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Initialize.		 A	0.000 00
3	Input moment of inertia	I	ENTER 	I
	then modulus of elasticity	E	ENTER 	E
	then beam length.	l	 B	EI
4	Input load(s):			
	Location of point load	a	ENTER 	a
	Point load	P	 C	a
	Distributed load (force/length)	W	 D	W
	Location of applied moment	c	ENTER 	c
	Applied moment	M	 E	c
5	Key in x to specify the point of interest and calculate			
	deflection	x	A	y
	or slope	x	B	θ
	or moment	x	C	M_x
	or shear.	x	D	V
6	For a new calculation with the same loading, go to step 5.			
	For new loads, go to step 4. Be sure to set obsolete loadings to zero. For new beam properties, go to step 3. To restart, go to step 2.			

Example 1:

Find the deflection, slope, internal moment and shear at distances of 0, 24 and 60 inches for the beam below. Neglect the weight of the beam.



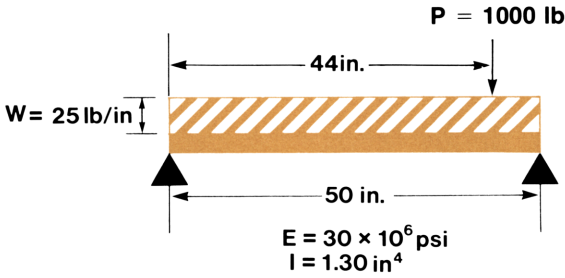
Keystrokes:

Outputs:

f A .92 ENTER 30 EE			
6 ENTER 72 f B	→	27.60 06	
40 ENTER 10000 f E	→	40.00 00	
0 A	→	0.000 00	(y_0)
0 B	→	-1.771 -03	(θ_0)
0 C	→	0.000 00	(M_0)
0 D	→	138.9 00	(V_0)
24 A	→	-30.92 -03	(y_{24})
24 B	→	-322.1 -06	(θ_{24})
24 C	→	3.333 03	(M_{24})
24 D	→	138.9 00	(V_{24})
60 A	→	2.415 -03	(y_{60})
60 B	→	40.26 -06	(θ_{60})
60 C	→	-1.667 03	(M_{60})
60 D	→	138.9 00	(V_{60})

Example 2:

What is the slope of the beam below at $x = 38$ inches?



Keystrokes:

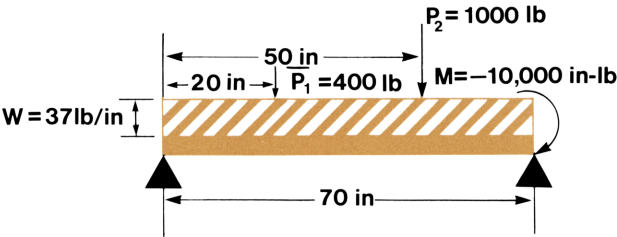
f A 1.30 ENTER 30 EEX
6 ENTER 50 f B
44 ENTER 1000 f C
25 f D
38 B

Outputs:

39.00 06
44.00 00
25.00 00
3.327 -03 (in/in)

Example 3:

What is the total moment at the center of the beam below? (It is not necessary to know the values of E or I to solve the problem. Simply key in 70 and press f B.)



First solve for the effect of the distributed load, P_1 , and M .

Keystrokes:

f A 70 f B 20 ENTER
400 f C
37 f D 70 ENTER
10000 CHS f E
70 ENTER 2 ÷ C

Outputs:

20.00 00
70.00 00
21.66 03

Store values in R_6 .

STO 6

21.66 03 (in-lb)

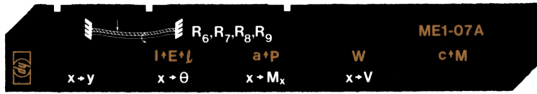
Now solve for the effect of P_2 and add it to the content of R_6 . This is the final answer assuming superposition is valid.

f A 50 ENTER 1000 f C
35 C
RCL 6 +

50.00 00
10.00 03 (in-lb)
31.66 03 (in-lb)

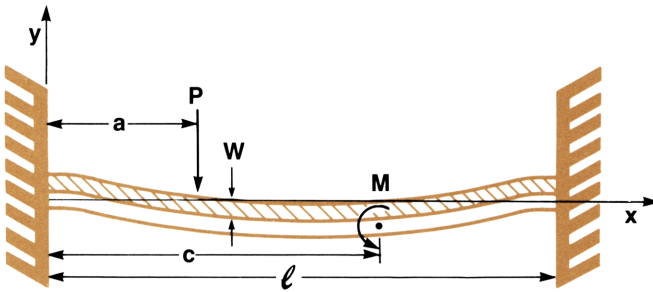
Notes

BEAMS FIXED AT BOTH ENDS



This program calculates deflection, slope, moment and shear at any specified point along a beam of uniform cross section, fixed at both ends. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, and multiple applied moments can be analyzed.

Equations:



$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{P(\ell - a)^2 x^2}{6EI^3} [x(\ell + 2a) - 3a\ell]^* \quad (\text{deflection due to point load})$$

$$y_2 = \frac{Wx^2}{24EI} [x(2\ell - x) - \ell^2] \quad (\text{distributed load})$$

$$y_3 = \frac{M(\ell - c)x^2}{\ell^2 EI} \left[\frac{cx}{\ell} + \frac{\ell - 3c}{2} \right]^{**} \quad (\text{applied moment})$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{P(\ell - a)^2 x}{2EI^3} [x(\ell + 2a) - 2a\ell]^* \quad (\text{slope due to point load})$$

$$\theta_2 = \frac{Wx}{12EI} [x(3\ell - 2x) - \ell^2] \quad (\text{distributed load})$$

$$\theta_3 = \frac{M(\ell - c)x}{\ell^2 EI} \left[\frac{3cx}{\ell} + \ell - 3c \right]^{**} \quad (\text{applied moment})$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = \frac{P(\ell - a)^2}{\ell^3} [x(\ell + 2a) - a\ell]^* \quad (\text{moment due to point load})$$

$$M_{x2} = \frac{W}{12} [6x(\ell - x) - \ell^2] \quad (\text{distributed load})$$

$$M_{x3} = \frac{M(\ell - c)}{\ell^2} \left[\frac{6cx}{\ell} + \ell - 3c \right]** \quad (\text{applied moment})$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = \frac{P(\ell - a)^2}{\ell^3} (\ell + 2a) \quad (\text{shear due to point load})$$

$$V_2 = \frac{-W}{2} (2x - \ell) \quad (\text{distributed load})$$

$$V_3 = \frac{-6M(\ell - c)c}{\ell^3} \quad (\text{applied moment})$$

where:

y is the deflection at a distance x from the left support;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

ℓ is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length;

M is an applied moment;

a is the distance from the left support to the point load;

c is the distance to the applied moment.

*If x is greater than a , a is replaced by $(\ell - a)$ and x is replaced by $(\ell - x)$. The signs of θ_1 and V_1 are also changed.

**If x is greater than c , x is replaced by $(\ell - x)$ and c is replaced by $(\ell - c)$. The signs of y_3 and M_{x3} are also changed.

Remarks:

This card differs from other beam cards. The “start” function is not included on **LBL** **f** **A**. You must manually perform the “start” function by storing zero when P, W or M are not included in the problem.

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

Registers R_{S0} – R_{S9} are available for user storage.

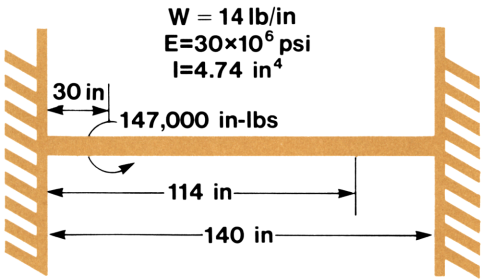
Sums of y , θ , M_x and V may be stored in R_6 , R_7 , R_8 , R_9 , respectively. Note that these registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input moment of inertia	I	ENTER +	I
	<i>then</i> modulus of elasticity	E	ENTER +	E
	<i>then</i> beam length.	<i>l</i>	f B	EI
3	Input load(s):*			
	Location of point load	a	ENTER +	a
	Point load	P	f C	a
	Distributed load (force/length)	W	f D	W
	Location of applied moment	c	ENTER +	c
	Applied moment	M	f E	c
4	Key in x to specify the point			
	of interest and calculate			
	deflection	x	A	y
	<i>or</i> slope	x	B	θ
	<i>or</i> moment	x	C	M_x
	<i>or</i> shear.	x	D	V

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
5	For a new calculation with the			
	same loading, go to step 4. For			
	new loads, go to step 3. Be			
	sure to set obsolete loadings to			
	zero. For new beam properties,			
	go to step 2.			
	*Loads must be input, even if			
	zero.			

Example 1:

For the beam below, what are the values of deflection, slope, moment, and shear at an x of 114 inches?



Keystrokes:

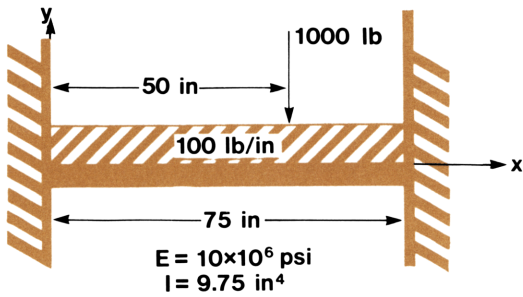
4.74 **ENTER** 30 **EEX** 6 **ENTER**
140 **f** **B** →
0 **f** **C** 30 **ENTER** 147000 **f** **E**
14 **f** **D** →
114 **A** →
RCL **O** **B** →
RCL **O** **C** →
RCL **O** **D** →

Outputs:

142.2 06
14.00 00
43.72 -03 (y)
-3.155-03 (θ)
13.05 03 (M_x)
444.7 00 (V)

Example 2:

Find the internal moment at $x = 0$ for the configuration below.



Keystrokes:

9.75 **ENTER** 10 **EEX** 6 **ENTER**
75 **f B** →
0 **f E** 100 **f D** 50 **ENTER**
1000 **f C** →
0 **C** →

Outputs:

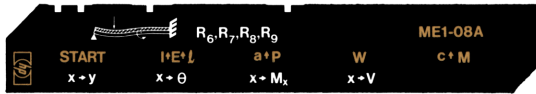
97.50 06
50.00 00
-52.43 03 (M_0)

Also, find the deflection at $x = 40$.

40 **A** → -101.0 -03 (Y_{40})

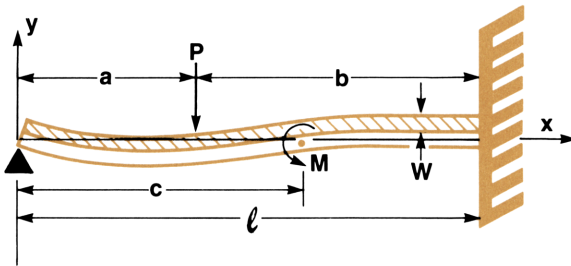
Notes

PROPPED CANTILEVER BEAMS



This program calculates deflection, slope, moment and shear at any specified point along a propped cantilever beam of uniform cross section. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, and multiple applied moments can be analyzed.

Equations:



$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{P}{6EI} [F(x^3 - 3\ell^2 x) + 3b^2 x]; \quad x \leq a \quad (\text{deflection due to point load})$$

$$y_2 = \frac{W}{48EI} (3\ell x^3 - 2x^4 - \ell^3 x) \quad (\text{distributed load})$$

$$y_3 = \frac{M}{EI} G(x^3 - 3\ell^2 x) + \ell x - cx; \quad x \leq c \quad (\text{applied moment})$$

$$y_3 = \frac{M}{EI} G(x^3 - 3\ell^2 x) + \ell x - \frac{1}{2} (x^2 + c^2); \quad x > c$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{P}{6EI} [F(3x^2 - 3\ell^2) + 3b^2]; \quad x \leq a \quad (\text{slope due to point load})$$

$$\theta_1 = \frac{P}{6EI} [F(3x^2 - 3\ell^2) - 3(x - a)^2]; \quad x > a$$

$$\theta_2 = \frac{W}{48EI} (9x^2 - 8x^3 - \ell^3) \quad (\text{distributed load})$$

$$\theta_3 = \frac{M}{EI} [G(3x^2 - 3\ell^2) + \ell - c]; \quad x \leq c \quad (\text{applied moment})$$

$$\theta_3 = \frac{M}{EI} [G(3x^2 - 3\ell^2) + \ell - x]; \quad x > c$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = PFx; \quad x \leq a \quad (\text{moment due to point load})$$

$$M_{x1} = PFx - P(x - b); \quad x > a$$

$$M_{x2} = W (3/8x \ell - x^2/2) \quad (\text{distributed load})$$

$$M_{x3} = 6MGx; \quad x \leq c \quad (\text{applied moment})$$

$$M_{x3} = 6MGx - M; \quad x > c$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = PF; \quad x \leq a \quad (\text{shear due to point load})$$

$$V_1 = PF - P; \quad x > a$$

$$V_2 = W \left(\frac{3}{8} \ell - x \right) \quad (\text{distributed load})$$

$$V_3 = 6MG \quad (\text{applied moment})$$

$$F = \left[\frac{3b^2 \ell - b^3}{2\ell^3} \right]$$

$$b = (\ell - a)$$

$$G = \frac{\ell^2 - c^2}{4\ell^3}$$

where:

- y is the deflection at a distance x from the left support;
- θ is the slope (change in y per change in x) at x;
- M_x is the moment at x;
- V is the shear at x;
- I is the moment of inertia of the beam;
- E is the modulus of elasticity of the beam;
- ℓ is the length of the beam;
- P is a concentrated load;
- W is a uniformly distributed load with dimensions of force per unit length;
- M is an applied moment;
- a is the distance from the left support to the point load;
- c is the distance to the applied moment.

Remarks;

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

Registers R_{S0} – R_{S9} and R_B are available for user storage.

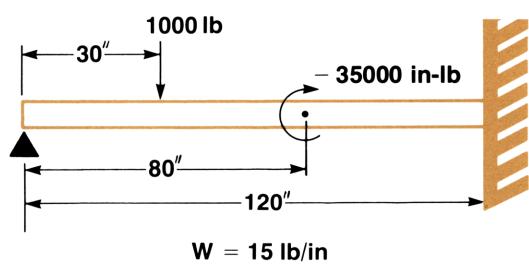
Sums of y, θ , M_x and V may be stored in R_6 , R_7 , R_8 and R_9 , respectively. Note that those registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Initialize.		A	0.000 00
3	Input moment of inertia	I	ENTER	I
	then modulus of elasticity	E	ENTER	E
	then beam length.	ℓ	B	E ℓ
4	Input load(s):			
	Location of point load	a	ENTER	a
	Point load	P	C	a
	Distributed load (force/length)	W	D	W
	Location of applied moment	c	ENTER	c
	Applied moment.	M	E	c

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
5	Key in x to specify the point of interest and calculate			
	deflection	x	A	y
	or slope	x	B	θ
	or moment	x	C	M_x
	or shear.	x	D	V
6	For a new calculation with the same loading, go to step 5.			
	For new loads, go to step 4.			
	Be sure to set obsolete loadings to zero. For new beam properties, go to step 3.			
	To restart, go to step 2.			

Example 1:

What are the values of moment and shear at both ends of the beam below? (It is not necessary to know the values of E or I since deflection and slope are not required.)



Keystrokes:

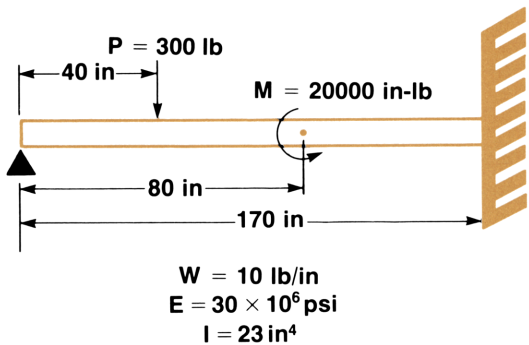
f A 120 **f B** 30 **ENTER**
 1000 **f C** \longrightarrow
 80 **ENTER** 35000 **CHS** **f E**
 15 **f D** \longrightarrow
 0 **C** \longrightarrow
 0 **D** \longrightarrow
 120 **C** \longrightarrow
 120 **D** \longrightarrow

Outputs:

30.00 00
 15.00 00
 0.000 00 (in-lb)
 1.065 03 (lb)
 -35.23 03 (in-lb)
 -1.735 03 (lb)

Example 2:

Calculate the deflection, slope, moment and shear at $x = 90$ for the beam below.



Keystrokes:

f **A** 23 **ENTER** 30 **EEX** 6 **ENTER**
170 **f** **B** \longrightarrow
40 **ENTER** 300 **f** **C** 10 **f** **D**
80 **ENTER** 20000 **f** **E** \longrightarrow
90 **A** \longrightarrow
90 **B** \longrightarrow
90 **C** \longrightarrow
90 **D** \longrightarrow

Outputs:

690.0 06
80.00 00
-75.73 -03 (in)
920.8 -06 (in/in)
11.89 03 (in-lb)
-229.0 00 (lb)

Notes

HELICAL SPRING DESIGN



This program performs one or two point design for helical compression springs, of round wire, with ends square and ground.

After a tentative spring design has been found, a check can be run to determine whether stresses are acceptable, and whether sufficient clearance between coils is available at the point of highest operating load.

Equations:

$$k = \frac{P_2 - P_1}{L_1 - L_2}$$

$$s_2 = \frac{8 P_2 D_H}{\pi d^3}$$

$$D = D_H f_0 - d$$

$$N = \frac{G d^4}{8 D^3 k}$$

$$L_s = (N + 2) d$$

$$L_f = \frac{P_1}{k} + L_1$$

$$s_s = \frac{8 D k (L_f - L_s) W}{\pi d^3}$$

$$W = \frac{4 (D/d) - 1}{4 (D/d) - 4} + \frac{0.615}{(D/d)}$$

$$s_{\max} = \begin{cases} .45 \text{ TS for ferrous materials.} \\ .35 \text{ TS for non-ferrous materials.} \end{cases}$$

$$YS = \begin{cases} .65 \text{ TS for ferrous materials.} \\ .55 \text{ TS for non-ferrous materials.} \end{cases}$$

$$TS = \beta \ln d + \alpha$$

Design checking logic:

If $(L_2 - L_s) < 0.1 (L_f - L_2)$ and $s_s > s_{\max}$, the spring lacks sufficient clearance between coils and stresses are too high; code = 1.

If $(L_2 - L_s) < 0.1 (L_f - L_2)$ and $s_s \leq s_{\max}$, clearance between coils is insufficient; code = 2.

If $(L_2 - L_s) \geq 0.1 (L_f - L_2)$ and $s_s > YS$, stress is too high; code = 3.

If $(L_2 - L_s) \geq 0.1 (L_f - L_2)$ and $s_s \leq YS$, design is satisfactory. If $s_s \leq 0.3 TS$, stresses are quite conservative and code = 4. If $s_s > 0.3 TS$, design is acceptable and code = 5.

where:

G is the torsional modulus of rigidity;

α and β are tensile strength regression coefficients from table 1 (metric) or table 2 (English);

P_1 is the spring load at most extended operating point (see figure 1);

L_1 is spring length, at the most extended operating point;

P_2 is spring load at most compressed operating point;

L_2 is the spring length, at the most compressed operating point;

k is the spring constant;

d is the wire diameter;

f_0 is the clearance factor for the spring and the hole (possibly imaginary) in which the spring is designed to work:

$$f_0 = \begin{cases} 0.95 & \text{if } D_H \geq 12.70 \text{ mm (0.5 in)} \\ 0.90 & \text{if } D_H < 12.70 \text{ mm (0.5 in);} \end{cases}$$

D_H is the diameter of the hole (possibly imaginary) into which the spring must fit;

s_2 is the uncorrected stress at operating point 2;

N is the number of active coils;

s_s is the Wahl corrected stress when the spring is fully compressed to solid (coils touching);

L_f is the free length of the spring;

L_s is the fully compressed or solid spring length;

D is the mean spring diameter;
OD is the outside spring diameter;
Code is a digit from 1-5, explained in program User Instructions;
W is the Wahl factor which corrects stresses for curvature;
 s_{\max} is the maximum allowable working stress for the material;
YS is the yield strength of the material;
TS is the tensile strength of the material.

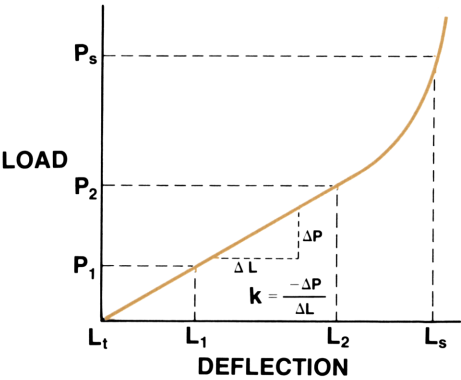


Figure 1-Spring Deflection

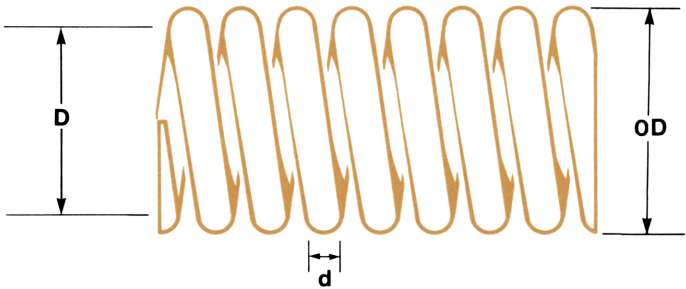


Figure 2-Helical Compression Spring

Table 1
MINIMUM TENSILE STRENGTH REGRESSION COEFFICIENTS
(Metric Units)

MATERIAL	MODULUS OF RIGIDITY G,N/(mm) ²	WIRE DIAMETER RANGE— MILLIMETERS	TENSILE STRENGTH COEF.	
			α ,N/(mm) ²	β ,N/(mm) ²
Music Wire ASTM-A228	7.93 × 10 ⁴	0.41–6.35	2205	–346.1
Alloy Steel ASTM-A232	7.93 × 10 ⁴	0.64–7.62	1921	–249.7
Stainless Steel ASTM-A313	6.90 × 10 ⁴	0.41–1.91	1851	–209.6
		1.91–5.08	1950	–393.6
		5.08–9.40	2221	–560.4
Oil Tempered ASTM-A229	7.93 × 10 ⁴	0.51–6.86	1827	–304.7
Hard Drawn ASTM-A227	7.93 × 10 ⁴	0.51–3.56	1773	–283.4
		3.56–12.7	1757	–270.8
Tempered Value Spring ASTM-A230	7.93 × 10 ⁴	2.36–5.08	1586	–153.1
Phosphor Bronze ASTM-B159	4.07 × 10 ⁴	0.64–9.40	957	– 63.97

Table 2
MINIMUM TENSILE STRENGTH REGRESSION COEFFICIENTS
(English Units)

MATERIAL	MODULUS OF RIGIDITY G,psi	WIRE DIAMETER RANGE— INCHES	TENSILE STRENGTH COEF.	
			α ,psi	β ,psi
Music Wire ASTM-A228	11.5×10^6	0.016–0.25	157400	–50200
Alloy Steel ASTM-A232	11.5×10^6	0.025–0.30	161400	–36220
Stainless Steel ASTM-A313	10.0×10^6	0.016–0.075	170200	–30400
		0.075–0.20	98110	–57090
		0.20 –0.37	59190	–81280
Oil Tempered ASTM-A229	11.5×10^6	0.020–0.27	122100	–44190
Hard Drawn ASTM-A227	11.5×10^6	0.020–0.14	124200	–41110
		0.14 –0.50	127800	–39280
Tempered Valve Spring ASTM-A230	11.5×10^6	0.093–0.20	158300	–22200
Phosphor Bronze ASTM-B159	5.9×10^6	0.025–0.37	108800	–9278

Reference:

Design Handbook—Springs, Custom Metal Parts, Associated Spring Corporation, Bristol, Connecticut, 1970.

Remarks:

Registers R_{s0} – R_{s9} are available for user storage.

The assumptions implicit to this program are based on engineering practice and experience. Generally, designs found by this program will be conservative, however, caution must be exercised when high or low temperatures, corrosive media or other adverse environmental circumstances exist.

For one point design, specify the free length (L_1) and a corresponding zero load (P_1), then specify the length (L_2) and corresponding load (P_2).

Some designs achieved by this program may require coiling the spring wire in such a small radius that the spring material would fail in the manufacturing process. No program check is made for this condition.

If code = 2, then s_2 has no intelligent meaning.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Toggle ferrous (1) or non-ferrous (0) material mode (consider stainless steel non-ferrous).		A	1.00/0.00
3	Specify material properties from table 1 (Metric) or table 2 (English):			
	Modulus of rigidity	G	ENTER ↕	G
	Tensile strength Alpha	α	ENTER ↕	α
	Tensile strength Beta	β	B	G
4	Input load point 1:			
	Force 1	P_1	ENTER ↕	P_1
	Corresponding spring length 1	L_1	C	P_1
5	Input load Point 2 and calculate spring constant:			
	Force 2	P_2	ENTER ↕	P_2
	Corresponding spring length 2	L_2	D	k
6	Input wire diameter, and clearance factor ($f_0 = 0.90$ if spring diameter < 12.70mm (0.5 in); otherwise, $f = 0.95$)., and maximum outside spring diameter.	d	ENTER ↕	d
		f_0	ENTER ↕	f_0
		D_H	E	s_2

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	If s_2 is a reasonable value			
	(not extremely high or low for			
	your application), proceed to			
	step 8. Otherwise, you may wish			
	to modify the design specifica-			
	tions in steps 4, 5 or 6.			
8	Compute number of coils.		A	N
9	Compute stress at solid			
	(maximum).		B	s_s
10	Check design.		C	Code
11	If code = 1, the design is			
	over constrained. The specified			
	conditions cannot be met. Try			
	another material, larger D_H ,			
	new load points or another type			
	of spring.			
	If code = 2, clearance between			
	coils is not sufficient. Press			
	R+ to see current wire			
	diameter.		R+	d
	Key in a smaller wire diameter			
	and calculate a new N. Go			
	back to instruction step 9.	d	R/S	N

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	If code = 3, stress at solid			
	is too high. Press R+ to			
	see the current wire diameter.		R+	d
	Key in a larger wire dia-			
	meter and calculate a new N.	d	R/S	N
	Go back to instruction			
	step 9.			
	If code = 4, design is			
	acceptable but smaller wire			
	might also work. Press R+			
	to see current wire diameter.		R+	d
	Key in a new smaller wire			
	diameter and calculate N.	d	R/S	N
	Go back to instruction			
	step 9.			
	If code 5, design is			
	acceptable but not necessarily			
	optimal. Try manipulating			
	design parameters to obtain a			
	more economical design.			
12	Display free length, solid			
	length, mean diameter, and			
	outside diameter.		E	L_f, L_s, D, OD
13	Go to steps 2 through 6 for			
	a new case.			

Example 1:

Using Oil Tempered Wire (ASTM-A229), design a spring which supports a load of 270 newtons at a length of 62 millimeters and a load of 470 newtons at 50 millimeters. Wire is available in 0.5 mm increments. Try 4.0 mm wire first. Space available limits the spring diameter to 40.00 mm.

Variables:

$$P_1 = 270 \text{ N}$$
$$L_1 = 62 \text{ mm}$$
$$P_2 = 470 \text{ N}$$
$$L_2 = 50 \text{ mm}$$
$$d = 4.0 \text{ mm}$$
$$D_H = 40.0 \text{ mm}$$
$$f_0 = 0.95 \text{ (since } D_H > 12.70 \text{ mm)}$$
$$G = 7.93 \times 10^4 \text{ N/mm}^2$$
$$\alpha = 1827 \text{ N/mm}^2$$
$$\beta = -304.7$$

}

From table 1

Keystrokes:

Select iron wire (press **f** **A** until 1.00 is displayed.)

f **A** _____→
7.93 **EE** 4 **ENTER** 1827 **ENTER**
304.7 **CHS** **f** **B** _____→
270 **ENTER** 62 **f** **C** 470 **ENTER**
50 **f** **D** _____→
4 **ENTER** .95 **ENTER** 40 **f** **E** ►
A _____→
B _____→
C _____→

Outputs:

1.00 00
79.30 03
16.67 00 *** (k)
748.0 00 *** (N/mm², s₂)
3.874 00 *** (Coils)
1.446 03 *** (N/mm², s_s)
3.000 00 (Code)

Since Code = 3, select a larger wire. 4.5 mm wire is the next largest, so give it a try.

4.5 **R/S** _____→
B _____→
C _____→

6.487 00 *** (Coils)
748.4 00 *** (s_s)
5.000 00 (Code)

Since code = 5, design is acceptable. Output free length, solid length, mean diameter and outside diameter.

E →	78.20 00 *** (L_f)
	38.19 00 *** (L_s)
	33.50 00 *** (D)
	38.00 00 *** (OD)

Example 2:

Using music wire (ASTM-A228), design a spring which will work in a 0.25 inch hole, for the loading below:

$P_1 = 1$ lb	$L_1 = 1.5$ in	
$P_2 = 10$ lb	$L_2 = 1.0$ in	
$G = 11.5 \times 10^6$ psi	} From table 2	
$\alpha = 157.4 \times 10^3$ psi		
$\beta = -50.20 \times 10^3$ psi		
$d = 0.035$ or 0.040		
$f_0 = 0.90$ (from User Instructions)		

Keystrokes:

Outputs:

Since music wire is a ferrous material, press **f A** until 1.00 is displayed.

f A →	1.000 00
11.5 EEX 6 ENTER 157.4 EEX	
3 ENTER 50.20 CHS EEX	
3 f B →	11.50 06
1 ENTER 1.5 f C 10 ENTER	
1.0 f D →	18.00 00 *** (k)
.035 ENTER .9 ENTER	
.25 f E →	148.5 03 *** (s_2 , psi)
A →	17.47 00 *** (Coils)
B →	227.7 03 *** (s_s , psi)
C →	3.000 00 (Code)

Try the larger wire.

.04 R/S →	32.29 00 *** (Coils)
B →	32.66 03 *** (s_s , psi)
C →	2.000 00 (Code)

Since neither available wire will meet these specifications the specifications must be modified. After due consideration, it is decided that P_2 could be lowered to 9 pounds.

9	ENTER	1	f	D	→	16.00	00	***	(k)
.04	ENTER	.9	ENTER						
.25	f	E	→			89.52	03	***	(s ₂ , psi)
A	→					36.33	00	***	(Coils)
B	→					4.651	03	***	(s _s , psi)

Interestingly, and unfortunately, $s_s < s_2$ indicates that this spring cannot be compressed to s_2 .

C	→					2.000	00		
---	---	--	--	--	--	-------	----	--	--

Sure enough, insufficient clearance. Try the smaller wire.

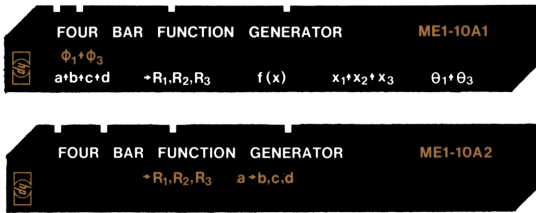
.035	R/S	→				21.29	00	***	(Coils)
B	→					169.6	03	***	(s _s , psi)
C	→					5.000	00		(Code)

Since the design checks out, calculate the dimensions:

E	→					1.563	00	***	(L _f)
						815.3	-03	***	(L _s)
						185.0	-03	***	(D)
						220.0	-03	***	(OD)

Notes

FOUR BAR FUNCTION GENERATOR



These cards may be used to design a four bar linkage which will approximate an arbitrary function of one variable. Freudenstein's approach is used in the solution. Cramer's rule is used to solve the 3×3 system of linear equations.

Equations:

Three precision points are used in the solution.

Freudenstein's equations

$$R_1 \cos \theta_1 - R_2 \cos \phi_1 + R_3 = \cos (\theta_1 - \phi_1)$$

$$R_1 \cos \theta_2 - R_2 \cos \phi_2 + R_3 = \cos (\theta_2 - \phi_2)$$

$$R_1 \cos \theta_3 - R_2 \cos \phi_3 + R_3 = \cos (\theta_3 - \phi_3)$$

are solved simultaneously for R_1 , R_2 and R_3 which are defined as follows:

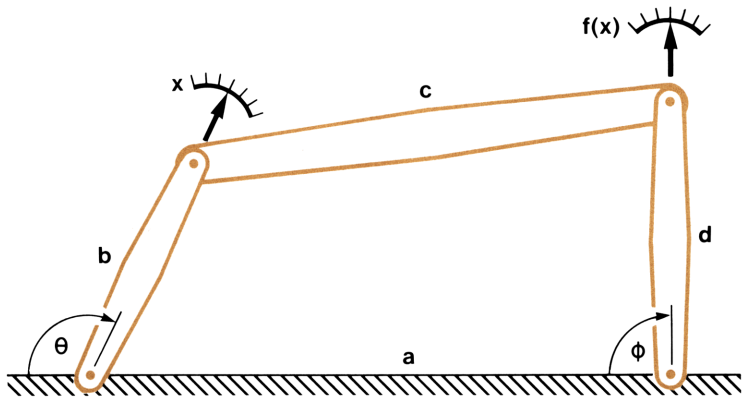
$$R_1 = a/d, \quad R_2 = a/b, \quad R_3 = \frac{a^2 + b^2 + d^2 - c^2}{2bd}$$

where a is the distance between fixed pivots, b is the length of the input link, c is the length of the coupler and d is the length of the output link. θ_1 refers to the angle of the input link at the first precision point, θ_2 the angle at the second point, and θ_3 the angle at the third. ϕ_1 is the angle of the output link at the first precision point, ϕ_2 is the angle at the second point, and ϕ_3 is the angle at the third precision point.

$$\theta_2 = \theta_1 + \frac{x_2 - x_1}{x_3 - x_1} (\theta_3 - \theta_1)$$

$$\phi_2 = \phi_1 + \frac{f(x_2) - f(x_1)}{f(x_3) - f(x_1)} (\phi_3 - \phi_1)$$

x_1 , x_2 and x_3 are the precision points or the three points at which the mechanism will yield kinematically exact solutions to the function ($f(x)$) which is to be generated.

**Reference:**

Martin, G. H., *Kinematics and Dynamics of Machines* McGraw-Hill, 1969.

Remarks:

$f(x)$ must be stated in 119 or less steps.

$$\left(\cos \phi_2 - \frac{\cos \phi_1 \cos \theta_2}{\cos \theta_1} \right) \left(\frac{\cos \theta_3}{\cos \theta_1} - 1 \right) \\ \neq \left(\frac{\cos \theta_2}{\cos \theta_1} - 1 \right) \left(\cos \phi_3 - \frac{\cos \phi_1 \cos \theta_3}{\cos \theta_1} \right)$$

θ_1 may not be equal to 90° or 270° .

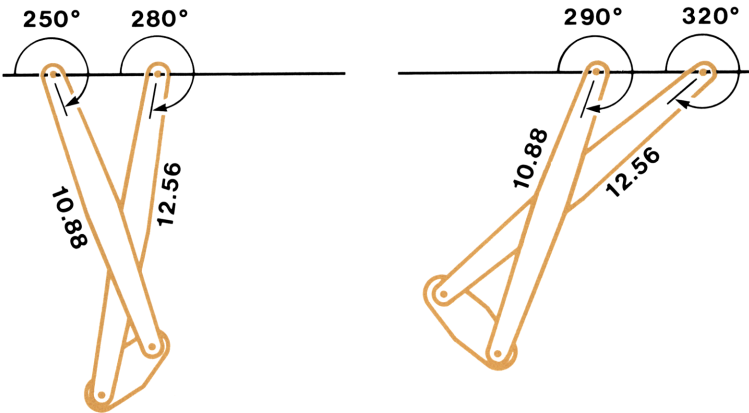
All registers are used.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2 of card 1.			
2	To calculate link ratios, go to step 4.			
3	For function generator, go to step 7.			
4	Input the link lengths.	a	ENTER	a
		b	ENTER	b
		c	ENTER	c
		d	A	a
5	Calculate the link ratios.		B	R_1, R_2, R_3
6	For a new case, go to step 2.			
7	Key the function into memory:			
	i. Go to label C.		GTO C	
	ii. Switch to PRGM mode.			
	iii. Key in the function.*	$f(x)$		
	iv. Switch to RUN mode.			
	(The argument of the function is in X when the routine is called.)			
8	Input 3 precision points	x_1	ENTER	x_1
		x_2	ENTER	x_2
		x_3	D	x_1
9	Input starting input angle and final input angle ($\theta_1 \neq 90 \neq 270$)	θ_1	ENTER	θ_1
		θ_3	E	θ_2
10	Input starting output angle and final output angle.	ϕ_1	ENTER	ϕ_1
		ϕ_3	f A	ϕ_2
11	Load side 1 and side 2 of card 2.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
12	Calculate R_1 , R_2 and R_3 .		f B	R_1 , R_2 , R_3
13	Input a to calculate b, c, and d.	a	f C	b, c, d
14	For a new case, go to step 1.			
	*119 steps are allowed.			

Example 1:

Suppose the output of a linkage is to be the square root of the input. The input link is to move from 70° to 110° while the output moves from 100° to 140° . Precision points are $x_1 = 3(70^\circ)$, $x_2 = 5$, and $x_3 = 9(110^\circ)$. The distance between foundation pivots is 3.75. What are the remaining link lengths?



Data for input:

$$f(x) = \sqrt{x}$$

$$x_1 = 3, x_2 = 5, x_3 = 9$$

$$\theta_1 = 70^\circ, \theta_3 = 110^\circ, \phi_1 = 100^\circ, \phi_3 = 140^\circ$$

$$a = 3.75$$

Keystrokes:

Load side 1 and side 2 of Card 1.

GTO **C**

Switch to PRGM mode.

√x

Switch to RUN mode.

3 **ENTER** 5 **ENTER** 9 **D** 70 **ENTER**

110 **E** →

100 **ENTER** 140 **f** **A** →

Load side 1 and side 2 of card 2.

f **B** →

3.75 **f** **C** →

Outputs:

83.33 (θ_2)

115.90 (ϕ_2)

-0.30 *** (R_1)

-0.34 *** (R_2)

1.03 *** (R_3)

-10.88 *** (b)

3.04 *** (c)

-12.56 *** (d)

Note that should you decide to run the program ‘‘PROGRESSION OF FOUR BAR SYSTEM’’ for the same linkage, then input of a, b, c and d is not necessary since a, b, c and d are already stored in the corresponding registers from this program.

b = -10.88, c = 3.04, d = -12.56 (The negative signs indicate that the links are opposite to the assumed direction i.e., $\theta = 250^\circ$ and $\phi = 280^\circ$).

Example 2:

Compute the link ratios for the following link lengths:

- a = 1.0
- b = 1.371
- c = 2.12
- d = 1.502

Keystrokes:

Load side 1 and side 2 of Card 1

DSP **4**

1 **ENTER** 1.371 **ENTER**

2.12 **ENTER** 1.502 **A** **B** →

Outputs:

0.6658 *** (R_1)

0.7294 *** (R_2)

0.1557 *** (R_3)

Notes

PROGRESSION OF FOUR BAR SYSTEM



PROGRESSION OF A FOUR BAR SYSTEM

$a \cdot b \cdot c \cdot d$
 $\theta \cdot \phi(\alpha)$

connector?

$\dot{\theta} \cdot \dot{\phi}(\dot{\alpha})$

ME1-11A

$\theta_0 \cdot n \cdot \Delta\theta \cdot \text{RPM} \cdot P$
 $\ddot{\theta} \cdot \ddot{\phi}(\ddot{\alpha})$

This program calculates angular displacement, velocity and acceleration for the output link of a four bar system (figure 1). (Either the “connecting link” (c) or the “output link” (d) may be selected as the program’s output link.)

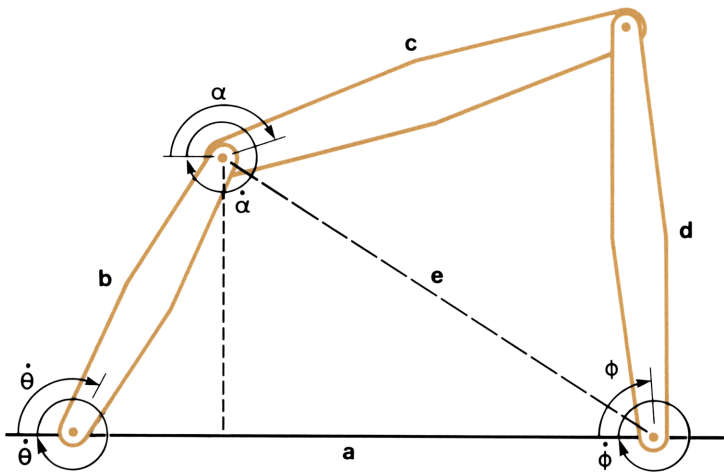


FIGURE 1-FOUR BAR SYSTEM SHOWING POSITIVE ANGULAR CONVENTIONS

Automatic and manual modes of operation are available. In manual mode, the output angle is calculated by keying in the input angle and pressing **A**. The angular output velocity may then be found by keying in the angular input velocity and pressing **C**. After angular velocity is calculated, the output link acceleration is found by keying in the input link acceleration and pressing **E**. In automatic mode, a starting input link angle θ_0 , the number of increments n , the angular increment $\Delta\theta$, and the constant input link RPM are input using **f E**. The program automatically progresses from θ_0 through n increments of $\Delta\theta$. RPM is output once, followed by groups of four values. The first value, of these four-value groups, is input angle, the second value is output angle, the third value is angular output velocity and the fourth value is angular output acceleration. Example problem 1 demonstrates manual operation while example 2 demonstrates automatic operation.

Equations:

Output Link

$$\phi = \sin^{-1} \left(\frac{b}{e} \sin \theta \right) + \cos^{-1} \left(\frac{d^2 + e^2 - c^2}{2de} \right)$$

Connecting Link

$$\alpha = \sin^{-1} \left(\frac{b}{e} \sin \theta \right) + \cos^{-1} \left(\frac{c^2 + e^2 - d^2}{-2ce} \right)$$

where:

$$e = \sqrt{a^2 + b^2 + 2ab \cos \theta}$$

$$\frac{d\phi}{d\theta} = \frac{R_1 \sin \theta - \sin (\theta - \phi)}{R_2 \sin \phi - \sin (\theta - \phi)}$$

$$R_1 = \frac{a}{d} \quad R_2 = \frac{a}{b}$$

$$\frac{d\alpha}{d\theta} = \frac{S_1 \sin \theta - \sin (\theta - \alpha)}{S_2 \sin \alpha - \sin (\theta - \alpha)}$$

$$S_1 = -\frac{a}{c} \quad S_2 = \frac{a}{b}$$

$$\frac{d^2\phi}{d\theta^2} = \frac{R_1 \cos \theta - R_2 \cos \phi \left(\frac{d\phi}{d\theta} \right)^2 - \left(1 - \frac{d\phi}{d\theta} \right)^2 \cos (\theta - \phi)}{R_2 \sin \phi - \sin (\theta - \phi)}$$

$$\frac{d^2\alpha}{d\theta^2} = \frac{S_1 \cos \theta - S_2 \cos \alpha \left(\frac{d\alpha}{d\theta} \right)^2 - \left(1 - \frac{d\alpha}{d\theta} \right)^2 \cos (\theta - \alpha)}{S_2 \sin \alpha - \sin (\theta - \alpha)}$$

$$\dot{\phi} = \frac{d\phi}{d\theta} \dot{\theta} \quad \dot{\alpha} = \frac{d\alpha}{d\theta} \dot{\theta}$$

$$\ddot{\phi} = \frac{d^2\phi}{dt^2} = \frac{d^2\phi}{d\theta^2} \left(\frac{d\theta}{dt} \right)^2 + \frac{d^2\theta}{dt^2} \frac{d\phi}{d\theta}$$

$$= \dot{\theta}^2 \frac{d^2\phi}{d\theta^2} + \ddot{\theta} \frac{d\phi}{d\theta} \quad \alpha = \dot{\theta}^2 \frac{d^2\alpha}{d\theta^2} + \ddot{\theta} \frac{d\alpha}{d\theta}$$

Remarks:

$\dot{\phi}$ has the units of θ , since $\frac{d\phi}{d\theta}$ is dimensionless.

$\frac{d^2\phi}{d\theta^2}$ has units of rad^{-1} . So that the dimensions making up $\ddot{\phi}$ agree, the program assumes $\frac{d^2\theta}{dt^2}$ is given in RPM^2 , and $\frac{d^2\phi}{d\theta^2}$ is multiplied by $2\pi \frac{\text{rad}}{\text{rev}}$:

$$\ddot{\phi} \frac{\text{rev}}{\text{min}^2} = \dot{\theta}^2 \frac{\text{rev}^2}{\text{min}^2} \frac{d^2\phi}{d\theta^2} \text{rad}^{-1} \left[\frac{2\pi \text{ rad}}{\text{rev}} \right] + \ddot{\theta} \frac{\text{rev}}{\text{min}^2} \frac{d\phi}{d\theta}$$

The program could be altered by the appropriate constant change if $\dot{\theta}$ and $\ddot{\theta}$ are in units other than revolutions/time (e.g. for degrees/ time change 2π to $\pi/180$ (radians/degree), or for radians/time, no constant necessary).

These same remarks apply to $\dot{\alpha}$ and $\ddot{\alpha}$.

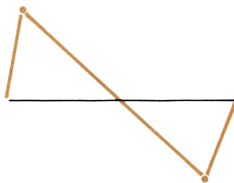
An error during calculation of ϕ or α may indicate the linkage may not physically assume the specified position.

The sign of RPM determines the direction of rotation in automatic mode.

Two possible configurations exist for a given set of links:







Configuration A



Configuration B

Configuration A is assumed by the program. To obtain configuration B change step 87 from + to -.

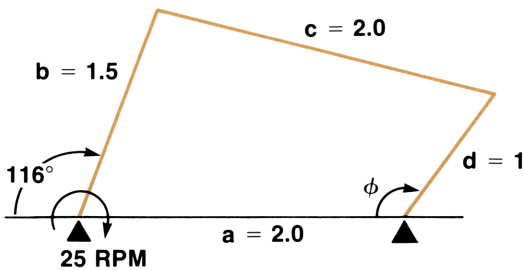
Registers R_{s0} - R_{s9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input link lengths:			
	fixed link	a	ENTER↵	a
	input link	b	ENTER↵	b
	connecting link	c	ENTER↵	c
	output link	d	 A	a
3	If connecting link output values (α , $\dot{\alpha}$, $\ddot{\alpha}$) are desired, rather than output link values (ϕ , $\dot{\phi}$, $\ddot{\phi}$), set connecting link mode by pressing  C. A 1.00 appears in the display indicating connecting link mode is on. Pressing  C repeatedly toggles connecting link mode off and on.			
			 C	1.00/0.00
4	For automatic progression of input link, go to step 9.			
5	Key in input link angle and calculate output angle.	θ	A	ϕ (α)
6	Key in input RPM and calculate output RPM.	$\dot{\theta}$ (RPM)	C	$\dot{\phi}$ ($\dot{\alpha}$)
7	Key in input link acceleration and calculate output acceleration.	$\ddot{\theta}$ (RPM ²)	E	$\ddot{\phi}$ ($\ddot{\alpha}$)
8	For a new input link angle, go to step 5. For the alternate output member (connector, or output link), go to step 3. For a new case, go to step 2.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
9	Key in starting input link angle	θ_0	ENTER	θ_0
	then number of increments	n	ENTER	n
	then angular increment	$\Delta\theta$	ENTER	$\Delta\theta$
	then RPM (+ or -) and			
	calculate the output $\theta(\alpha)$, $\dot{\phi}(\dot{\alpha})$,			
	and $\ddot{\phi}(\ddot{\alpha})$ for constant input			
	RPM between θ_0 and θ_r	RPM	I E	output
10	For another set of inputs, go			
	to step 9. For the alternate			
	output member (connector or			
	output link) go to step 3. For a			
	new case go to step 2.			

Example 1:

The input link of the four bar linkage below is instantaneously rotating at 25 RPM with an angular acceleration of 2.3 RPM². The input link is at 116°. What are the values of position, velocity, and acceleration of link d? Link c?



Keystrokes:

2 **ENTER** 1.5 **ENTER** 2 **ENTER**
1 **I** **A** _____
116 **A** _____
25 **C** _____
2.3 **E** _____

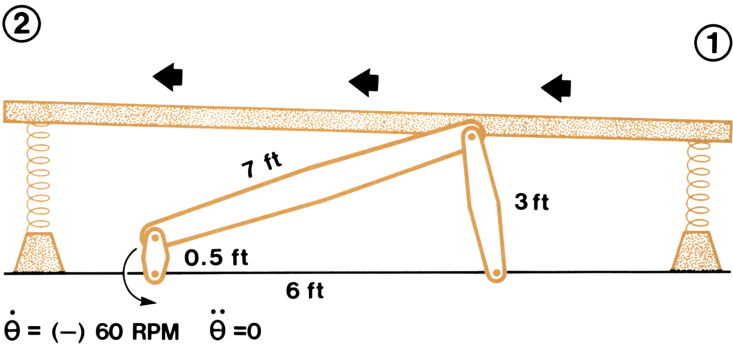
Outputs:

2.00
125.75 (ϕ)
39.29 ($\dot{\phi}$)
2279.89 ($\ddot{\phi}$)

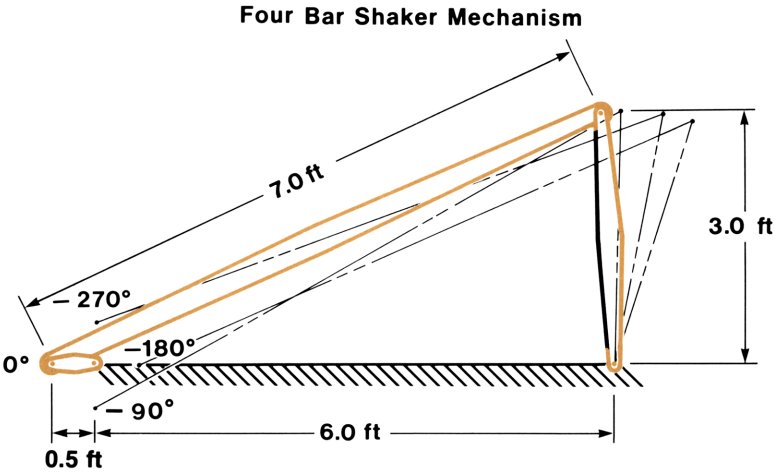
f C	—————→	1.00	(connecting link selected)
116 A	—————→	195.56	(α)
25 C	—————→	3.38	($\dot{\alpha}$)
2.3 E	—————→	2049.01	($\ddot{\alpha}$)

Example 2:

A four bar linkage is to be used to convert rotary motion from an electric motor to the reciprocating motion necessary to activate a shaking conveyor system which moves fruit between two process stations.



For the geometry shown above, what is the motion of the output link? Start at $\theta = 0^\circ$ and go to -330° by 12, 30° increments. Find the corresponding connecting link motion.



11-07

Solution:

θ^0	ϕ^0	$\dot{\phi}(\text{RPM})$	$\ddot{\phi}(\text{RPM}^2)$	α^0	$\alpha(\text{RPM})$	$\alpha(\text{RPM}^2)$
0	86.69	-4.62	3392.91	154.67	-4.62	-92.82
-30	85.63	0.46	3816.90	152.42	-4.20	713.38
-60	87.18	5.70	3615.33	150.67	-2.60	1594.02
-90	91.19	10.12	2592.67	150.01	0.10	2210.83
-120	96.94	12.38	449.28	150.84	3.19	2062.19
-150	102.95	10.93	-2597.20	153.04	5.34	887.00
-180	107.18	5.45	-4998.56	155.83	5.45	-693.75
-210	108.09	-1.86	-5112.85	158.18	3.73	-1628.64
-240	105.56	-7.86	-3351.37	159.45	1.32	-1738.45
-270	100.72	-10.95	-1099.60	159.53	-0.93	-1481.44
-300	95.11	-11.05	887.85	158.59	-2.75	-1133.46
-330	90.08	-8.70	2404.65	156.87	-4.04	-698.86

Keystrokes:

6 **ENTER** .5 **ENTER** 7 **ENTER**
3 **f** **A** \longrightarrow
Select output link.
f **C** \longrightarrow
0 **ENTER** 12 **ENTER** 30 **ENTER**
60 **CHS** **f** **E** \longrightarrow

Outputs:

6.00
0.00 (Press **f** **C** again if 1.00 is displayed)
-60.00 *** (RPM)
0.00 *** (θ_0)
86.69 *** (ϕ)
-4.62 *** ($\dot{\phi}$)
3392.91 *** ($\ddot{\phi}$)
-30.00 *** (θ_1)
85.63 *** (ϕ_1)
0.46 *** ($\dot{\phi}_1$)
3816.90 *** ($\ddot{\phi}_1$)
etc.
:
:
-330.00 *** (θ_f)
90.08 *** (ϕ_f)
-8.70 *** ($\dot{\phi}_f$)
2404.65 *** ($\ddot{\phi}_f$)

f C →
0 ENTER 12 ENTER 30 ENTER
60 CHS f E →

1.00
-60.00 *** (RPM)
0.00 *** (θ_0)
154.67 *** (α_0)
-4.62 *** ($\dot{\alpha}_0$)
-92.82 *** ($\ddot{\alpha}_0$)
-30.00 *** (θ_1)
152.42 *** (α_1)
-4.20 *** ($\dot{\alpha}_1$)
713.38 *** ($\ddot{\alpha}_1$)
etc.
:
:
:

PROGRESSION OF SLIDER CRANK



In a slider crank mechanism (e.g., the piston, wrist pin and connecting rod in an internal combustion engine), for given crank radius, connecting rod length, slider offset, crankshaft speed (RPM) and crank position, this program calculates the following: the displacement, velocity, and acceleration of the slider; the connecting rod angle, velocity and acceleration; the maximum and minimum displacements, and the maximum and minimum angular values for ϕ .

Equations:

$$\omega = \frac{\pi N}{30}$$

$$x = R \cos \theta + L \cos \phi$$

$$x_{\max} = (R + L) \cos \left[\sin^{-1} \left(\frac{E}{R + L} \right) \right]$$

$$x_{\min} = (L - R) \cos \left[\sin^{-1} \left(\frac{E}{L - R} \right) \right]$$

$$\Delta x = x_{\max} - x_{\min}$$

$$\phi = \sin^{-1} \left(\frac{E + R \sin \theta}{L} \right)$$

$$v = \frac{dx}{dt} = R\omega \left(\frac{-\sin(\theta + \phi)}{\cos \phi} \right)$$

$$a = \frac{d^2x}{dt^2} = R\omega^2 \left(\frac{-\cos(\theta + \phi)}{\cos \phi} - \frac{R \cos^2 \theta}{L \cos^3 \phi} \right)$$

$$\phi_{\max} = \sin^{-1} \left(\frac{E + R}{L} \right)$$

$$\phi_{\min} = \sin^{-1} \left(\frac{E - R}{L} \right)$$

$$\Delta\phi = \phi_{\max} - \phi_{\min}$$

$$\dot{\phi} = \frac{d\phi}{dt} = \omega \frac{R \cos \theta}{L \cos \phi}$$

$$\ddot{\phi} = \frac{d^2\phi}{dt^2} = \omega^2 \left[\left(\frac{d\phi}{d\theta} \right)^2 \tan \phi - \frac{R \sin \theta}{L \cos \phi} \right]$$

where:

N is crankshaft speed in RPM;

E is slider offset;

L is connecting rod length;

R is crank radius;

ω is crank angular velocity in radians/sec;

θ is crank angle;

x is slider displacement;

x_{\max} is maximum slider displacement;

x_{\min} is minimum slider displacement;

Δx is stroke;

v is slider velocity;

a is slider acceleration;

ϕ is connecting rod angular displacement;

ϕ_{\max} is maximum connecting rod angular displacement;

ϕ_{\min} is minimum connecting rod angular displacement;

$\Delta\phi$ is total angular throw of connecting rod;

$\dot{\phi}$ is angular velocity of connecting rod;

$\ddot{\phi}$ is angular acceleration of connecting rod.

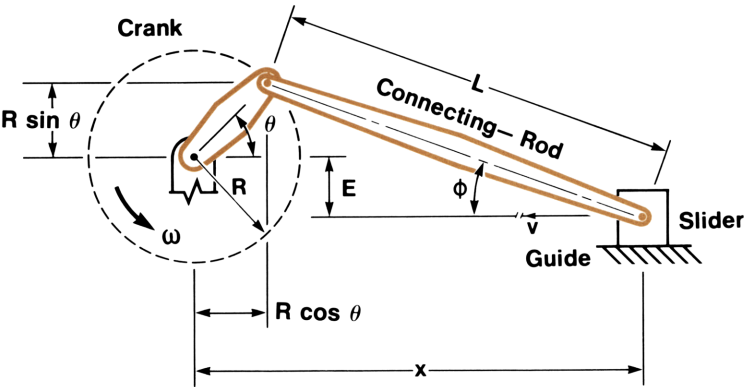
References:

H. A. Rothbart, *Mechanical Design and Systems Handbook*, McGraw-Hill, 1964.

V. M. Faires, *Kinematics*, McGraw-Hill, 1959.

Remarks:

Registers R_{S0}–R_{S9} are available for user storage.



STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the data for the mechanism.	N	ENTER	
		E	ENTER	
		L	ENTER	
		R	A	ω
3	Calculate maximum displacement and minimum displacement of slider.		f A	x _{max} x _{min}
4	Calculate maximum and minimum angular displacements for connecting rod.		f B	φ _{max} φ _{min}
5	Input crank angle to calculate slider displacement and connecting rod angle.	θ	B	x, φ
6	Calculate slider velocity and connecting rod angular velocity.		C	v, φ̇

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	Calculate slider acceleration and connecting rod angular acceleration.		D	$a, \ddot{\phi}$
8	Repeat steps 5-7 for a different θ .			
9	To calculate $x, \phi, v, \dot{\phi}, a,$ and $\ddot{\phi}$ for crank angles between θ_1 and θ_2 with n intervals.	θ_1	ENTER	
		θ_2	ENTER	
		n	E	$\theta, x, \phi, v, \dot{\phi}, a, \ddot{\phi}$
10	For a new mechanism, go to step 2.			

Example 1:

For an in-line slider crank mechanism ($E = 0$), turning at 4800 RPM having a crank radius of 2.0 inches and connecting rod length of 7.0 inches, Find:

- (1) x_{\max}, x_{\min} and ϕ_{\max}, ϕ_{\min}
 - (2) $x, v,$ and a of the wrist pin in the slider
 - (3) $\phi, \dot{\phi},$ and $\ddot{\phi}$ of the connecting rod
- for $\theta = 0^\circ, 15^\circ, 45^\circ, 90^\circ, 135^\circ, 180^\circ, 225^\circ$.

θ°	$x(\text{in})$	ϕ°	$v(\text{in/sec})$	$\dot{\phi}(\text{rad/sec})$	$a(\text{in/sec}^2)$	$\ddot{\phi}(\text{rad/sec}^2)$
0	9.00	0.00	0.00	143.62	-649701.96	0.00
15	8.91	4.24	-332.20	139.10	-614226.44	-17300.41
45	8.27	11.66	-857.50	103.69	-360454.40	-49902.29
90	6.71	16.60	-1005.31	0.00	150658.43	-75329.22
135	5.44	11.66	-564.22	-103.69	354181.29	-49902.29
180	5.00	0.00	0.00	-143.62	360945.53	0.00
225	5.44	-11.66	564.22	-103.69	354181.29	49902.29

Keystrokes:

4800 **ENTER** 0 **ENTER**
7 **ENTER** 2 **A** →
f **A** →
f **B** →
0 **B** →
C →
D →
15 **B** →
C →
D →
45 **B** →
C →
D →
:
225 **B** →
C →
D →

Outputs:

502.65 *** (ω)
9.00 *** (x_{\max})
5.00 *** (x_{\min})
16.60 *** (ϕ_{\max})
-16.60 *** (ϕ_{\min})
9.00 *** (x)
0.00 *** (ϕ)
0.00 *** (v)
143.62 *** ($\dot{\phi}$)
-649701.96 *** (a)
0.00 *** ($\ddot{\phi}$)
8.91 *** (x)
4.24 *** (ϕ)
-332.20 *** (v)
139.10 *** ($\dot{\phi}$)
-614226.44 *** (a)
-17300.41 *** ($\ddot{\phi}$)
8.27 *** (x)
11.66 *** (ϕ)
-857.50 *** (v)
103.69 *** ($\dot{\phi}$)
-360454.40 *** (a)
-49902.29 *** ($\ddot{\phi}$)
5.44 ***
-11.66 ***
564.22 ***
-103.69 ***
354181.29 ***
49902.29 ***

Alternatively, the values may be generated automatically.

0 **ENTER** 225 **ENTER** 5 **E** \longrightarrow

0.00 ***	(θ)
9.00 ***	(x)
0.00 ***	(ϕ)
0.00 ***	(v)
143.62 ***	($\dot{\phi}$)
-649701.96 ***	(a)
0.00 ***	($\ddot{\phi}$)
45.00 ***	
8.27 ***	
11.66 ***	
-857.58 ***	
103.69 ***	
-360454.40 ***	
-49902.29 ***	
90.00 ***	
6.71 ***	
16.60 ***	
-1005.31 ***	
0.00 ***	
150658.43 ***	
-75329.22 ***	
\vdots	
225.00 ***	
5.44 ***	
-11.66 ***	
564.22 ***	
-103.69 ***	
354181.29 ***	
49902.29 ***	

Example 2:

Determine the same values as in example 1 for a slider crank with offset of 1.5 inches (E = 1.5 inches).

Keystrokes:

4800 **ENTER** 1.5 **ENTER**
7 **ENTER** 2 **A** →
f **A** →
f **B** →
0 **B** →
C →
D →
15 **B** →
C →
D →
⋮
225 **B** →
C →
D →

Outputs:

502.65 *** (ω)
8.87 *** (x_{\max})
4.77 *** (x_{\min})
30.00 *** (ϕ_{\max})
-4.10 *** (ϕ_{\min})
8.84 *** (x)
12.37 *** (ϕ)
-220.55 *** (v)
147.03 *** ($\dot{\phi}$)
-660249.41 *** (a)
4742.62 *** ($\ddot{\phi}$)
8.63 *** (x)
16.75 *** (ϕ)
-552.49 *** (v)
144.87 *** ($\dot{\phi}$)
-602160.36 *** (a)
-13194.60 *** ($\ddot{\phi}$)
5.59 ***
0.70 ***
719.57 ***
-101.56 ***
280733.14 ***
51175.65 ***

θ°	x(in)	ϕ°	v(in/sec)	$\dot{\phi}(\text{rad/sec})$	a(in/sec ²)	$\ddot{\phi}(\text{rad/sec}^2)$
0	8.84	12.37	-220.55	147.03	-660249.41	4742.62
15	8.63	16.75	-552.49	144.87	-602160.36	-13194.60
45	7.78	24.60	-1036.35	111.69	-289750.94	-50429.96
90	6.06	30.00	-1005.31	0.00	291748.80	-83356.80
135	4.95	24.60	-385.37	-111.69	424884.76	-50429.96
180	4.84	12.37	220.55	-147.03	350398.08	4742.62
225	5.59	0.70	719.57	-101.56	280733.14	51175.65

0 **ENTER** 360 **ENTER** 8 **E** \longrightarrow

0.00 *** (θ)

8.84 *** (x)

12.37 *** (ϕ)

-220.55 *** (v)

147.03 *** ($\dot{\phi}$)

-660249.41 *** (a)

4742.62 *** ($\ddot{\phi}$)

45.00 ***

7.78 ***

24.60 ***

-1036.35 ***

111.69 ***

-289750.94 ***

-50429.96 ***

⋮

360.00 ***

8.84 ***

12.37 ***

-220.55 ***

147.03 ***

-660249.41 ***

4742.62 ***

CIRCULAR CAMS



This program computes the parameters necessary for the design of a harmonic or cycloidal circular cam with a roller, point or flat follower.

Equations:

Harmonic cams:

$$y = \frac{h}{2} \left(1 - \cos \frac{180\theta}{\beta} \right)$$

$$\frac{dy}{d\theta} = \frac{\pi h}{2\beta} \sin \frac{180\theta}{\beta} \quad \left[\frac{dy}{dt} = \omega \frac{dy}{d\theta} \right]$$

$$\frac{d^2y}{d\theta^2} = \frac{\pi^2 h}{2\beta^2} \cos \frac{180\theta}{\beta} \quad \left[\frac{d^2y}{dt^2} = \omega^2 \frac{d^2y}{d\theta^2} \right]$$

Cycloidal cams:

$$y = h \left[\frac{\theta}{\beta} - \frac{1}{2\pi} \sin \frac{2\pi\theta}{\beta} \right]$$

$$\frac{dy}{d\theta} = \frac{h}{\beta} \left[1 - \cos \frac{2\pi\theta}{\beta} \right] \quad \left[\frac{dy}{dt} = \omega \frac{dy}{d\theta} \right]$$

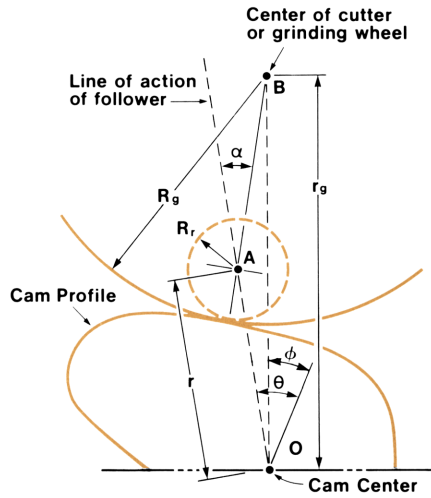
$$\frac{d^2y}{d\theta^2} = \frac{2\pi h}{\beta^2} \sin \frac{2\pi\theta}{\beta} \quad \left[\frac{d^2y}{dt^2} = \omega^2 \frac{d^2y}{d\theta^2} \right]$$

Both cycloidal and harmonic cams:

$$\alpha = \tan^{-1} \left(\frac{180}{\pi r} \frac{dy}{d\theta} \right)$$

$$r = R_b + y$$

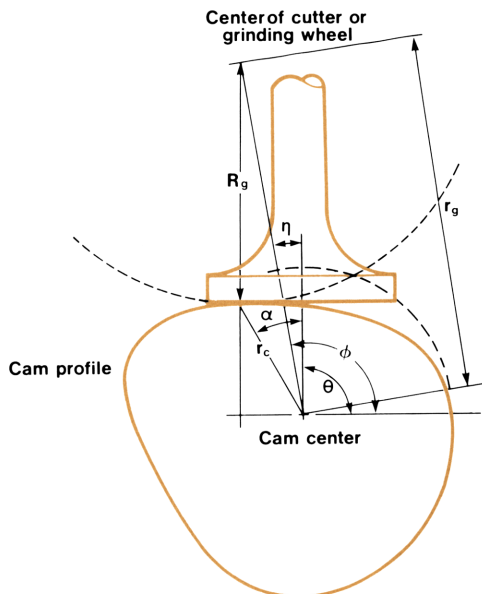
Roller followers:



$$r_g = (r^2 + (R_g - R_r)^2 - 2r(R_g - R_r) \cos \alpha)^{1/2}$$

$$\phi = \sin^{-1} \frac{R_g - R_r}{r_g} + \theta$$

Flat followers:



$$r_c = \left(r^2 + \left(\frac{180}{\pi} \frac{dy}{d\theta} \right)^2 \right)^{1/2}$$

$$r_g = (R_g^2 + r_c^2 + 2R_g r_c \cos \alpha)^{1/2}$$

$$\phi = \cos^{-1} \left(\frac{r_c + R_g \cos \alpha}{r_g} \right) - \alpha + \theta$$

where:

β is duration of lift h ;

$\Delta\theta$ is angular increment of calculation;

h is total cam lift over angle β ;

R_b is base circle radius;

R_g is grinder radius (set to zero for cam profile);

R_r is roller radius (set to zero for point follower);

θ is cam angle;

y is follower lift;

$\frac{dy}{d\theta}$ is follower velocity;

$\frac{d^2y}{d\theta^2}$ is follower acceleration;

α is pressure angle;

ϕ is angle from zero to grinder center;

r_g is center to center distance of grinder and cam.

Reference:

M.F. Spotts, *Design of Machine Elements*, Prentice-Hall 1971.

Remarks:

A flat follower will not properly follow a cam profile with any concave sections, e.g., see figure 1.

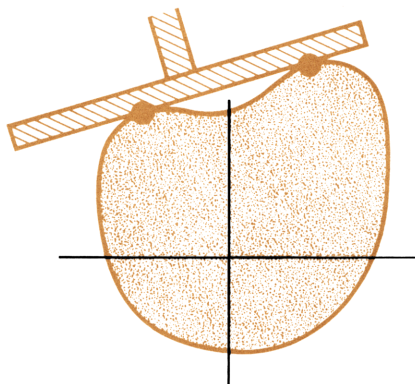


Figure 1
Note two points of contact

A roller follower will not properly follow a cam profile with concave section whose radius is less than the roller radius, e.g., see figure 2.

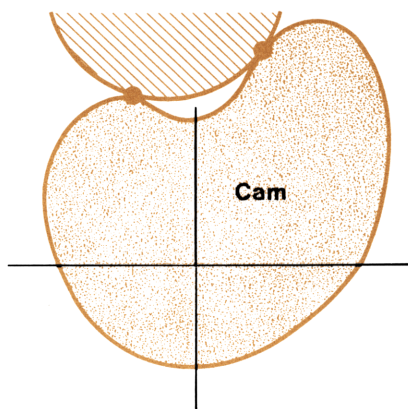


Figure 2
Note two points of contact

When the program is loaded, roller follower and harmonic profile modes are automatically selected.

Profiles other than harmonic and cycloidal may be generated by substituting them instead of label 1 or label 2. Example 3 demonstrates this.

13-05

Registers R_8 and $R_{S0}-R_{S9}$ are available for user storage.

For a parabolic profile, substitute the LBL 3 subroutine of ME1-14A for LBL 1 or LBL 2 of ME1-13A.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Select flat or roller follower			
	(1 = flat, 0 = roller. Roller			
	follower is set when card is			
	loaded).		F A	1/0
3	Select cam function type:			
	Harmonic (set when card			
	was loaded)	1	F B	1.000 00
	or cycloidal.	2	F B	2.000 00
4	Input starting angle.	θ_0	ENTER +	θ_0
5	Input duration of lift.	β	ENTER +	β
6	Input increment of θ .	$\Delta\theta$	F C	0.000 00
7	Input lift.	h	F D	h
8	Input radius of roller (skip for			
	flat followers).	R_r	ENTER +	R_r
9	Input radius of grinder (use			
	zero if cam profile is desired).	R_g	ENTER +	R_g
10	Input base radius.	R_b	F E	$(R_r - R_g)$
11	For automatic output, go to			
	step 15.			
12	Output angle and lift.		B	θ, y
13	Optional: Output other			
	quantities of velocity and			
	acceleration		C	$dy/d\theta, d^2y/d\theta^2$
	and/or pressure angle		D	α
	and/or grinder radius and			
	angle.		E	r_g, ϕ

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
14	For next increment, go to			
	step 12. For a new lift, go to			
	step 4. For a new case, go to			
	step 2.			
15	Automatic output of θ , y , $dy/d\theta$,			
	$d^2y/d\theta^2$, α , r_g , and ϕ with			
	increments of $\Delta\theta$ from θ_0			
	through $\theta_0 + \beta$.		A	θ , y , $dy/d\theta$
16	For next lift, go to step 4. For			
	a new case, go to step 2.			

Example 1:

Design a harmonic cam with a 1.0 inch roller follower, which develops harmonic motion, dropping from a base radius of 12.0 inches to 7.5 inches in 130° of rotation. From 130° to 170° , increase the lift to the original base radius. Using 10° increments, generate the cam profile by letting $R_g = 0$.

θ°	y (in)	$dy/d\theta$ (in/deg)	$d^2y/d\theta^2$ (in/deg ²)	α°	r_g (in)	ϕ
0.000 00	0.000 00	0.000 00	-1.314-03	0.000 00	11.00 00	0.000 00
10.00 00	-65.38-03	-13.01-03	-1.276-03	-3.575 00	10.94 00	9.673 00
20.00 00	-257.7-03	-25.27-03	-1.163-03	-7.029 00	10.75 00	19.35 00
30.00 00	-565.9-03	-36.06-03	-983.5-06	-10.24 00	10.45 00	29.03 00
40.00 00	-971.9-03	-44.75-03	-746.4-06	-13.09 00	10.06 00	38.71 00
50.00 00	-1.452 00	-50.84-03	-466.0-06	-15.44 00	9.588 00	48.41 00
60.00 00	-1.979 00	-53.98-03	-158.4-06	-17.15 00	9.070 00	58.14 00
70.00 00	-2.521 00	-53.98-03	158.4-06	-18.07 00	8.534 00	67.92 00
80.00 00	-3.048 00	-50.84-03	466.0-06	-18.02 00	8.007 00	77.79 00
90.00 00	-3.528 00	-44.75-03	746.4-06	-16.84 00	7.520 00	87.79 00
100.0 00	-3.934 00	-36.06-03	983.5-06	-14.37 00	7.101 00	98.00 00
110.0 00	-4.242 00	-25.27-03	1.163 03	-10.57 00	6.777 00	108.4 00
120.0 00	-4.435 00	-13.01-03	1.276-03	-5.628 00	6.571 00	119.1 00
130.0 00	-4.500 00	0.000 00	1.314-03	0.000 00	6.500 00	130.0 00
130.0 00	0.000 00	0.000 00	13.88-03	0.000 00	6.500 00	130.0 00
140.0 00	659.0-03	125.0-03	9.814-03	41.27 00	7.437 00	145.1 00
150.0 00	2.250 00	176.7-03	0.000 00	46.08 00	9.085 00	154.5 00
160.0 00	3.841 00	125.0-03	-9.814-03	32.26 00	10.51 00	162.9 00
170.0 00	4.500 00	0.000 00	-13.88-03	0.000 00	11.00 00	170.0 00

Keystrokes:

Select roller follower by pressing **f A** until zero is displayed.

f A →

Select harmonic cam:

1 **f B** →

0 **ENTER** 130 **ENTER**

10 **f C** →

7.5 **ENTER** 12 **- f D** →

1 **ENTER** 0 **ENTER** 12 **f E** →

A →

Outputs:

0.000 00

1.000 00

0.000 00

-4.500 00

1.000 00

0.000 00 *** (θ)

0.000 00 *** (y)

0.000 00 *** ($dy/d\theta$)

-1.314-03 *** ($d^2y/d\theta^2$)

0.000 00 *** (α)

11.00 00 *** (r_g)

0.000 00 *** (ϕ)

10.00 00 ***

-65.38-03 ***

-13.01-03 ***

-1.276-03 ***

-3.575 00 ***

10.94 00 ***

9.673 00 ***

⋮

etc.

For the lift back to the original base radius, input β ($170^\circ - 130^\circ = 40^\circ$) and $\Delta\theta$. The start of this lift ($\theta_0 = 130^\circ$) is already displayed and does not need to be keyed in again (unless you hit **R/S** and stopped the calculation prematurely).

Keystrokes:

40 **ENTER** 10 **f C** →

Key in new lift:

4.5 **f D** →

Key in previous roller and grinder radii and new base radius of 7.5:

1 **ENTER** 0 **ENTER** 7.5 **f E** →

A →

Outputs:

0.000 00

4.500 00

1.000 00

130.0 00 ***

0.000 00 ***
0.000 00 ***
13.88-03 ***
0.000 00 ***
6.500 00 ***
130.0 00 ***
140.0 00 ***
659.0-03 ***
125.0-03 ***
9.814-03 ***
41.27 00 ***
7.437 00 ***
145.1 00
:
etc.

Example 2:

Design a cycloidal, flat-faced cam with a lift of 50 millimeters in 40 degrees. The base radius is 500 millimeters and a 200 millimeter cutter is to be used for manufacture. Calculate θ , y , r_g and ϕ at 10 degree increments and calculate dy/dt ($dy/dt = \omega dy/d\theta$) at 20 degrees for a speed of 600 RPM.

Keystrokes:

Press **f A** until 1.000 00 is displayed:
f A →
Select cycloidal subroutine:
2 **f B** →
Input θ_0 , β , $\Delta\theta$.
0 **ENTER** 40 **ENTER**
10 **f C** →
Input h:
50 **f D** →
Input R_g and R_b :
200 **ENTER** 500 **f E** →
B →

Outputs:

1.000 00
2.000 00
0.000 00
50.00 00
200.0 00
0.000 00 *** (θ)
0.000 00 *** (y)

E →	700.0 00 *** (r_g) 0.000 00 *** (ϕ)
B →	10.00 00 *** 4.542 00 ***
E →	708.2 00 *** 15.80 00 ***
B →	20.00 00 *** 25.00 00 ***
E →	739.0 00 *** 31.18 00 ***
Compute dy/dt at 20 degrees:	
C →	2.500 00 *** ($dy/d\theta$) 0.000 00 *** ($d^2y/d\theta^2$)
X↔Y →	2.500 00 ($dy/d\theta$)
600 ENTER 10 ÷ 360 × × →	54.00 03 (dy/dt ; mm/sec)
B →	30.00 00 *** 45.46 00 ***
E →	748.9 00 *** 35.49 00 ***
B →	40.00 00 *** 50.00 00 ***
E →	750.0 00 *** 40.00 00 ***

Example 3:

A cam with a flat-faced follower is to convert an angular input to a linear output according to the following equation and its derivatives:

$$y = (\theta/\beta)^2$$
$$y' = 2 (\theta/\beta)$$
$$y'' = 2$$

Let $\beta = 90^\circ$ and $h = 1$ inch. Generate the cam profile from 0° to 90° in increments of 15° by setting $R_g = 0$.

$$R_b = 3.0 \text{ inches}$$
$$h = 1.0 \text{ inches}$$

The first step is to write a cam function subroutine incorporating the function and the derivatives. The subroutine can access (θ/β) in R_E and must store y' in R_4 , and y'' in R_3 , before returning to the main program with y in the X-register. One such subroutine is shown below:

```

LBL 3
  2
  STO 3 (y''calculated and stored)
  RCL E
  x
  STO 4 (y'calculated and stored)
  RCL E
  x2
  RTN (y calculated)

```

Now, load this sequence into program memory in place of LBL 1 (steps 168-188) or LBL 2 (steps 189-214). After this, the following keystrokes will generate the cam data:

Keystrokes:

Outputs:

Select flat-faced follower by pressing **f** **A** until 1.000 00 appears:

f **A** → 1.000 00

Select subroutine 3 (since the new subroutine is LBL 3):

3 **f** **B** → 3.000 00

0 **ENTER** 90 **ENTER**

15 **f** **C** → 0.000 00

1 **f** **D** → 1.000 00

0 **ENTER** 3.0 **f** **E** → 0.00 00

A → 0.000+00 ***

0.000+00 ***

0.000+00 ***

246.9-06 ***

0.000+00 ***

3.000+00 ***

0.000+00 ***

15.00+00 ***

27.78-03 ***

3.704-03 ***

246.9-06 ***

4.009+00 ***

3.035+00 ***

19.01+00 ***

30.00+00 ***

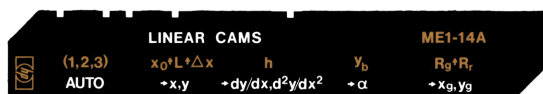
111.1-03 ***
7.407-03 ***
246.9-06 ***
7.768+00 ***
3.140+00 ***
37.77+00 ***
45.00+00 ***
250.0-03 ***
11.11-03 ***
246.9-06 ***
11.08+00 ***
3.312+00 ***
56.08+00 ***
60.00+00 ***
444.4-03 ***
14.81-03 ***
246.9-06 ***
13.84+00 ***
3.547+00 ***
73.84+00 ***
75.00+00 ***
694.4-03 ***
18.52-03 ***
246.9-06 ***
16.02+00 ***
3.844+00 ***
91.02+00 ***
90.00+00 ***
1.000+00 ***
22.22-03 ***
246.9-06 ***
17.66+00 ***
4.198+00 ***
107.7-00 ***

CAM DATA SUMMARY

θ	θ/β	y	r_g	ϕ
0°	0	0	3.000	0
15°	0.167	27.78-03	3.035	19.01
30°	0.333	111.1-03	3.140	37.77
45°	0.500	250.0-03	3.312	56.08
60°	0.667	444.4-03	3.547	73.84
75°	0.833	694.4-03	3.844	91.02
90°	1.000	1.000-00	4.198	107.7

Note that $y = (\theta/\beta)^2$ as specified by the original equation.

LINEAR CAMS



This program computes parameters necessary for the design of harmonic, cycloidal or parabolic profiles for linear cams with roller followers.

Equations:

$$y = hf(x/L) + R_b$$

$$x_g = x - (R_g - R_r) \sin \alpha \quad y_g = y + (R_g - R_r) \cos \alpha$$

$$\alpha = \tan^{-1} \left(\frac{dy}{dx} \right)$$

$$= \tan^{-1} \left(\frac{h}{L} f'(x/L) \right)$$

$$\frac{dy}{dx} = \frac{h}{L} f'(x/L)$$

$$\frac{d^2y}{dx^2} = \frac{h}{L^2} f''(x/L)$$

For harmonic profiles:

$$f(x/L) = \left(1 - \cos \left(\frac{180x}{L} \right) \right)$$

For cycloidal profiles:

$$f(x/L) = \left(\frac{x}{L} - \frac{1}{2\pi} \sin \frac{180x}{L} \right)$$

For parabolic profiles:

$$f(x/L) = \begin{cases} 2h \left(\frac{x}{L} \right)^2 & \frac{x}{L} < .5 \\ \left[1 - 2 \left(1 - \frac{x}{L} \right)^2 \right] & \frac{x}{L} \geq .5 \end{cases}$$

where:

L is the duration of lift h ;

Δx is the linear increment of calculation;

h is the total follower lift over length L ;

y_b is the base height from reference datum to roller center;

R_r is the roller radius (zero for point follower);

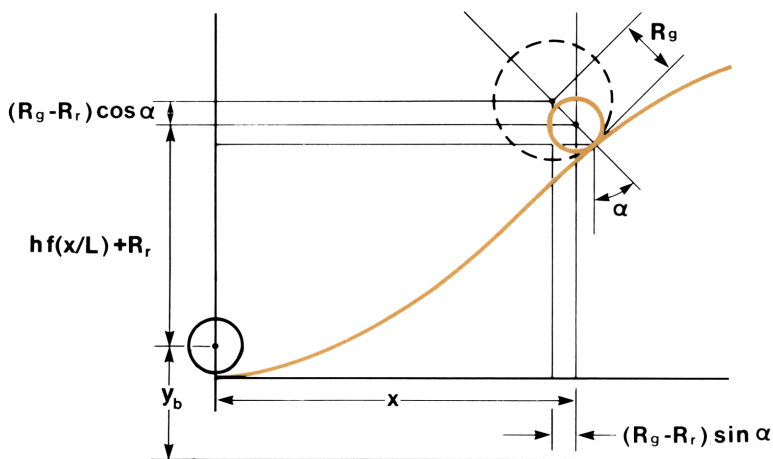
R_g is the grinder radius;

x is the linear displacement of cam;

y is the roller center height above datum;

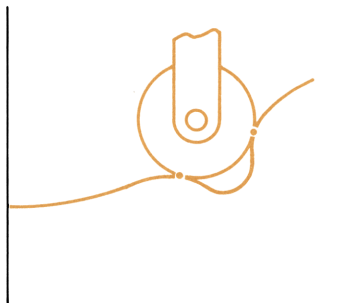
(x_g, y_g) is the grinder center for displacement x ;

α is the pressure angle.



Remarks:

The roller follower will not properly follow a cam profile with concave sections whose radius is less than the roller radius.



Note two points of contact

14-03

When the program is loaded, the harmonic profile mode is assumed. You may change to cycloidal by keying 2 and pressing **f A**. Parabolic is selected by keying 3 and pressing **f A**. Keying 1 and pressing **f A** returns the program to original status.

Arbitrary functions of (x/L) may be substituted in a manner analogous to that of example 3, ME1-13A.

Registers R_{S0}–R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Select cam function type:			
	Harmonic (set when card			
	was loaded)	1	f A	1
	or cycloidal	2	f A	2
	or parabolic	3	f A	3
3	Input starting x.	x ₀	ENTER	x ₀
4	Input duration of lift.	L	ENTER	L
5	Input increment of x.	Δx	f B	0.000 00
6	Input lift.	h	f C	h
7	Input height of follower center			
	above reference datum at x ₀ .	y _b	f D	y _b
8	Input grinder radius.	R _g	ENTER	R _g
9	Input roller radius.	R _r	f E	R _g –R _r
10	For automatic output, go to			
	step 14.			
11	Output x, y coordinates of			
	roller.		B	x, y
12	Optional: output other			
	quantities:			
	Follower velocity and			
	acceleration,		C	dy/dx, d ² y/dx ²
	and/or pressure angle,		D	α
	and/or grinder coordinates.		E	x _g , y _g

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
13	For next increment, go to			
	step 11. For a new case, go to			
	step 2.			
14	Automatic output of x , y , dy/dx ,			
	d^2y/dx^2 , α , x_g , and y_g with			
	increments of Δx from x_0			
	through $x + L$.		A	$x, y, dy/dx \dots$
15	For a new case, go to step 2.			

Example:

Design a harmonic, linear profile which has a base follower displacement of 4 cm, and a 3 cm lift over a distance of 7 cm. After the harmonic profile, a cycloidal lift of 2 cm occurs over a distance of 8 cm. Then a parabolic profile returns the follower to its original height (a drop of 5 cm) over a distance of 10 cm.

The follower and the grinder both have a radius of 1 cm. Therefore, the grinder and follower paths are equivalent. Instead of generating redundant grinder data, generate the surface profile by setting $R_g = 0$.

Use 1 cm step size.

Keystrokes:

Harmonic segment from 0 cm to 7 cm.

1 **f A** _____→
0 **ENTER↑** 7 **ENTER↑** 1 **f B** _____→
3 **f C** _____→
4 **f D** _____→
0 **ENTER↑** 1 **f E** _____→
A _____→

Outputs:

1.000 00 (harmonic profile)
0.000 00
3.000 00
4.000 00
-1.000 00
0.000 00 *** (x)
4.000 00 *** (y)
0.000 00 *** (dy/dx)
302.1-03 *** (d^2y/dx^2)
0.000 00 *** (α)
0.000 00 *** (x_g)

3.000 00 *** (y_g)
1.000 00 ***
4.149 00 ***
292.1-03 ***
272.2-03 ***
16.28 00 ***
1.280 00 ***
3.189 00 ***
:
:
:
7.000 00 ***
7.000 00 ***
0.000 00 ***
-302.1-03 ***
0.000 00 ***
7.000 00 ***
6.000 00 ***

Cycloidal segment from 7 cm to 15 cm.

2 **f** **A** →
7 **ENTER** 8 **ENTER** 1 **f** **B** →
2 **f** **C** →
7 **f** **D** →
A →

2.000 00
0.000 00
2.000 00
7.000 00
7.000 00 *** (x)
7.000 00 *** (y)
0.000 00 *** (dy/dx)
0.000 00 *** (d²y/dx²)
0.000 00 *** (α)
7.000 00 *** (x_g)
6.000 00 *** (y_g)
8.000 00 ***
7.025 00 ***
73.22-03 ***
138.8-03 ***
4.188 00 ***
8.073 00 ***
6.028 00 ***

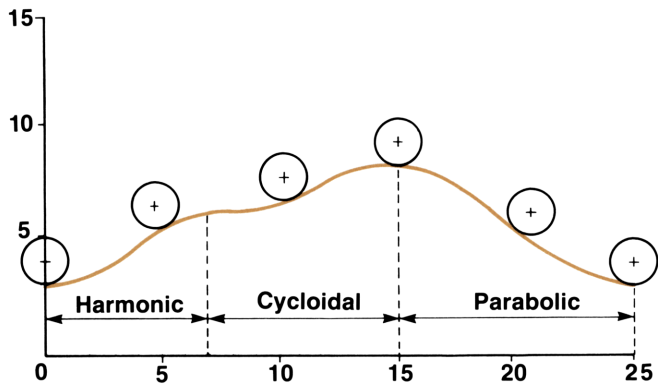
⋮
14.00 00 ***
8.975 00 ***
73.22-03 ***
-138.8-03 ***
4.188 00 ***
14.07 00 ***
7.978 00 ***
15.00 00 ***
9.000 00 ***
0.000 00 ***
0.000 00 ***
0.000 00 ***
15.00 00 ***
8.000 00 ***

Parabolic segment from 15 cm to 25 cm.

3 **f** **A** →
15 **ENTER** 10 **ENTER** 1 **f** **B**
5 **CHS** **f** **C** 9 **f** **D** →
A →

3.000 00
9.000 00
15.00 00 *** (x)
9.000 00 *** (y)
0.000 00 *** (dy/dx)
-200.0-03 *** (d²y/dx²)
0.000 00 *** (α)
15.00 00 *** (x_g)
8.000 00 *** (y_g)
16.00 00 ***
8.900 00 ***
-200.00-03 ***
-200.00-03 ***
-11.31 00 ***
15.80 00 ***
7.919 00 ***
⋮

24.00 00 ***
4.100 00 ***
-200.0-03 ***
200.0-03 ***
-11.31 00 ***
23.80 00 ***
3.119 00 ***
25.00 00 ***
4.000 00 ***
0.000 00 ***
200.0-03 ***
0.000 00 ***
25.00 00 ***
3.000 00 ***



Notes

GEAR FORCES



This program computes three mutually perpendicular forces, resulting from input torque, on helical, bevel or worm gears.

Helical gear equations:

$$F_t = \frac{T}{r}$$

$$F_{gs} = F_t \tan \phi$$

$$F_{gax} = F_t \tan \alpha$$

$$\tan \phi = \frac{\tan \phi_n}{\cos \alpha}$$

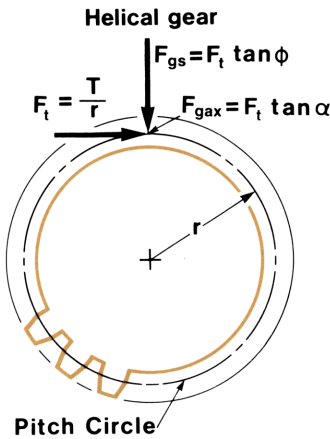


Figure 1-Helical Gear

where:

- T is the input torque;
- r is the pitch radius of the input gear;
- F_t is the tangential force;
- α is the helix angle measured from the axis of the gear (for spur gears α = 0);
- φ_n is the pressure angle measured perpendicular to the gear tooth;

ϕ is the pressure angle measured perpendicular to the gear axis;

F_{gs} is the radial force trying to separate the gears;

F_{gax} is the force parallel to the gear axis.

Bevel gear equations:

$$F_t = \frac{T}{r}$$

$$F_{bpax} = F_t \left(\frac{\tan \phi_n \sin (\text{cone} \angle)}{\cos \alpha} + \tan \alpha \cos (\text{cone} \angle) \right)$$

$$F_{bgax} = F_t \left(\frac{\tan \phi_n \cos (\text{cone} \angle)}{\cos \alpha} - \tan \alpha \sin (\text{cone} \angle) \right)$$

$$\tan \phi = \frac{\tan \phi_n}{\cos \alpha}$$

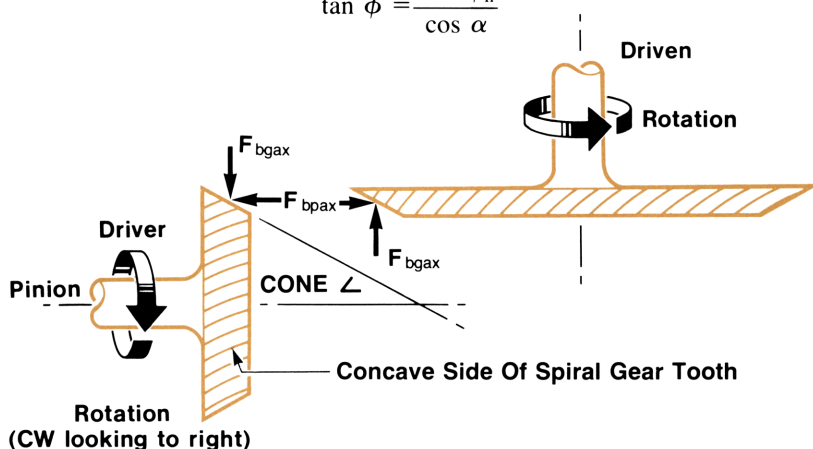


Figure 2—Spiral Bevel Gears

where:

T is the input (pinion) torque;

r is the pitch radius of the pinion gear;

F_t is the tangential force;

α is the pinion spiral angle (zero for straight tooth bevel gears);

ϕ_n is the pressure angle measured perpendicular to the gear tooth;

ϕ is the pressure angle measured perpendicular to the gear axis;

Cone \angle is the pitch cone angle of the pinion;

F_{bpax} is the force along the axis of the bevel pinion;

F_{bgax} is the force along the axis of the bevel gear.

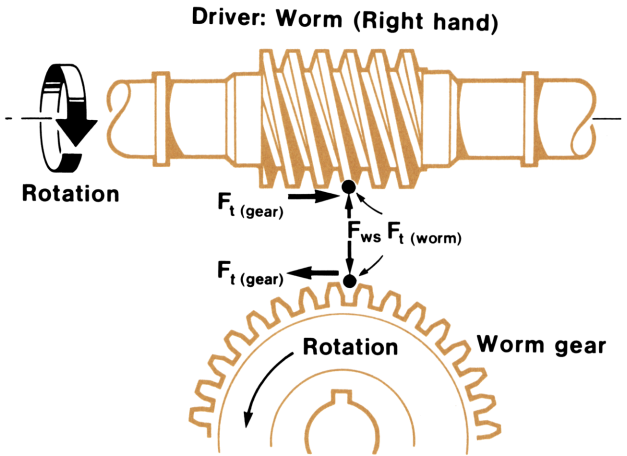
Worm gear equations:

$$F_t = \frac{T}{r}$$

$$F_{ws} = F_t \left(\frac{\sin \phi_n}{\cos \phi_n \sin \alpha + f \cos \alpha} \right)$$

$$F_{gax} = F_t \frac{1 - \frac{f \tan \alpha}{\cos \phi_n}}{\tan \alpha + \frac{f}{\cos \phi_n}}$$

$$\tan \phi = \frac{\tan \phi_n}{\cos \alpha}$$



where:

T is the input (worm) torque;

n is the pitch radius of the worm;

F_t is the tangential force on the worm;

α is the lead angle of the worm ($\alpha = \tan^{-1} (L/2\pi r)$, where L is the lead of the worm);

ϕ_n is the pressure angle measured perpendicular to the worm teeth;

ϕ is the pressure angle measured parallel to the worm axis;

f is the coefficient of friction;

F_{ws} is the separating force between the worm and gear;

F_{gax} is the force parallel to the gear axis.

Remarks:

For bevel gears, the spiral angle (α) is positive if the concave face of the pinion teeth are facing the direction of rotation (see figure 2). α is negative if the convex surface of the pinion teeth face the direction of rotation.

Registers R_0 – R_3 , R_7 – R_{S9} and R_c – R_l are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1.			
2	Input torque.	T	ENTER	T
3	Input pitch radius and calculate tangential force.	r	A	F_t
4	Input helix angle for helical gears, or spiral angle for spiral bevel gears, or lead angle for worm gears.	α	B	α
5	Input normal pressure angle or input pressure angle.	ϕ_n ϕ	C D	ϕ_n ϕ_n
6	For helical gears, go to step 7, for bevel gears, go to step 9, for worm gears, go to step 12.			
7	Calculate separating force and axial force.		E	F_{gs}, F_{gax}
8	For a new case, return to step 2 and modify inputs as necessary.			
9	Input bevel cone angle.	cone \angle	f A	cone \angle
10	Calculate pinion axial force and gear axial force.		f B	F_{bpax}, F_{bgax}

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
11	For a new case, return to			
	step 2 and modify inputs as			
	necessary.			
12	Input coefficient of friction.	f	f D	f
13	Calculate separating force			
	and gear axial force.		f E	F_{ws}, F_{gax}
14	For a new case, go to step 2			
	and modify inputs as			
	necessary.			

Example 1:

A helical gear with pitch radius 12 cm has a torque applied to it of 450,000 dyne-cm. The helix angle is 30°, and the normal pressure angle, measured perpendicular to a tooth, is 17.5°. Find the tangential, separating, and thrust forces.

Keystrokes:

450000 **ENTER** 12 **A** →
30 **B** 17.5 **C E** →

Outputs:

37500.00 (F_t)
13652.84 *** (F_{gs})
21650.64 *** (F_{gax})

Example 2:

A spiral pinion with mean radius 1.73 inches is subjected to a torque of 745 in-lb. The pinion is cut with a normal pressure angle of 20°, a spiral angle of 35°, with a pitch cone of 18°. Find the forces acting on the pinion. Rotation is in the direction of the concave side of the pinion teeth, so α is positive 35°.

Keystrokes:

745 **ENTER** 1.73 **A** →
35 **B** 20 **C** 18 **f A f B** →

Outputs:

430.64 (F_t)
345.90 *** (F_{bpax})
88.80 *** (F_{bgax})

If the rotation were reversed, leaving all other input values unchanged, what would the forces be?

$$35 \text{ CHS } \mathbf{B} \text{ f } \mathbf{B} \longrightarrow \begin{array}{l} -227.65 \text{ *** } (F_{\text{bpax}}) \\ 275.16 \text{ *** } (F_{\text{bgax}}) \end{array}$$

Example 3:

A torque of 512 in-lb is applied to a worm gear having a pitch diameter of 2.92 inches and a lead of 2.20 inches. The normal pressure angle is 20° , and the coefficient of friction is 0.10. Find the lead angle and the forces on the worm and worm gear.

Keystrokes:

512 **ENTER** 2.92 **ENTER**

2 **÷** **A** \longrightarrow

Calculate lead angle ($\alpha = \tan^{-1}(\text{lead}/2\pi r)$).

2.2 **ENTER** 2 **÷** **π** **÷**

2.92 **ENTER** 2 **÷** **÷** **TAN⁻¹** \longrightarrow

B 20 **C** .1 **f** **D** **f** **E** \longrightarrow

Outputs:

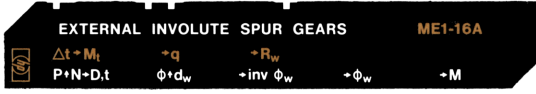
350.68 (F_t)

13.49 (α)

379.10 *** (F_{ws})

986.99 *** (F_{gax})

STANDARD EXTERNAL INVOLUTE SPUR GEARS



This program calculates various parameters for standard external involute spur gears. Given the diametral pitch P , number of teeth N , pressure angle ϕ , and pin diameter d_w , the program will calculate the pitch diameter D , tooth thickness t , and the involute and corresponding flank angle $\text{inv } \phi_w$ and ϕ_w . The flank angle ϕ_w is calculated from the involute by a Newton's method iterative solution for the equation $f(\phi_w) = 0$,

where:

$$f(\phi_w) = \tan \phi_w - \phi_w - \text{inv } \phi_w$$

In this solution, an initial guess is made for ϕ_w :

$$\phi_w^{(0)} = (3 \text{ inv } \phi_w)^{.3}$$

Newton's method then provides refinements of the initial guess by

$$\begin{aligned} \phi_w^{(n+1)} &= \phi_w^{(n)} - \frac{f(\phi_w^{(n)})}{f'(\phi_w^{(n)})} \\ &= \phi_w^{(n)} - \frac{\tan \phi_w^{(n)} - \phi_w^{(n)} - \text{inv } \phi_w}{\tan^2 \phi_w^{(n)}} \end{aligned}$$

The program also calculates various measurements over pins, namely, the theoretical values of the measurement over pins, M ; the radius to the center of the pin, 1 ; and the measurement over one pin, R_w . In addition, given the value of the tooth thinning Δt , the program will return the measurement over pins with tooth thinning, M_t .

Equations:

$$D = \frac{N}{P}$$

$$t = \frac{\pi}{2P}$$

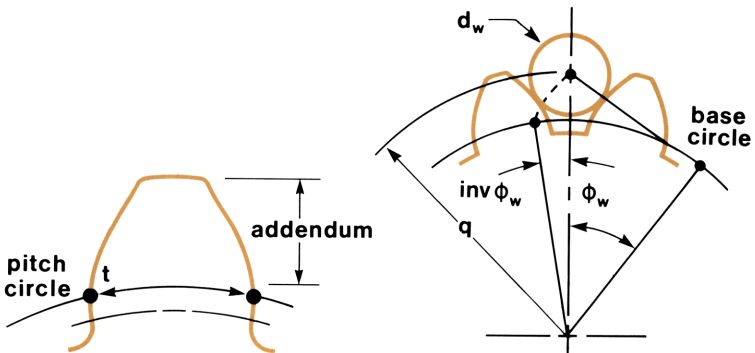
$$\text{inv } \phi_w \text{ (radians)} = \frac{t}{D} + \tan \phi - \frac{\pi \phi}{180} + \frac{d_w}{D \cos \phi} - \frac{\pi}{N}$$

$$M = \begin{cases} d_w + 2q & (N \text{ even}) \\ d_w + 2q \cos \left(\frac{90}{N} \right) & (N \text{ odd}) \end{cases}$$

$$q = \frac{D \cos \phi}{2 \cos \phi_w}$$

$$R_w = q + \frac{d_w}{2}$$

$$M_t = M - \Delta t \frac{\cos \phi}{\sin \phi_w}$$



Reference:

Adapted from a program submitted to the HP-65 Users's Library by Mr. John Nemcovich, Los Angeles, CA.

Dudley, D.W., *Gear Handbook*, McGraw-Hill, 1962.

Remarks:

Registers R_0 , R_{S0} – R_c and I are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input diametral pitch P	P	ENTER	P
	and number of teeth N to			
	calculate the pitch diameter			
	and tooth thickness t.	N	A	D, t
3	Input pressure angle ϕ	ϕ	ENTER	ϕ
	and pin diameter d_w .	d_w	B	ϕ
4	Calculate the involute $\text{inv } \phi_w$.		C	$\text{inv } \phi_w$ (deg.)
5	Calculate the corresponding			
	flank angle.		D	ϕ_w (deg.)
6	Calculate the measurement			
	over pins (theoretical).		E	M
7	Input tooth thinning and			
	calculate measurement over			
	pins with tooth thinning.	Δt	f A	M_t
8	Calculate radius to the center			
	of pin.		f B	q
9	Calculate measurement over			
	one pin.		f C	R_w
10	To change tooth thinning, go			
	to step 7. To change any other			
	input, go to step 2.			
	Note: If d_w is not known, it may			
	be calculated from the pin			
	constant k and pitch P:	k	ENTER	
	$d_w = k/P$	P	\div	d_w
11	To calculate ϕ_w directly from			
	$\text{inv } \phi_w$: store $\text{inv } \phi_w$ in register 6	$\text{inv } \phi_w$	STO 6	
	and calculate ϕ_w .		D	ϕ_w (deg.)

Example:

A 27-tooth gear with pitch 8 is cut with a 20° pressure angle. The pin diameter is 0.24 inches, and tooth thinning is reckoned at 0.002 inches. Calculate the unknown parameters.

Keystrokes:

8 **ENTER** 27 **A** →

20 **ENTER** 0.24 **B C** →

D →

E →

0.002 **f A** →

f B →

f C →

Outputs:

3.3750 *** (D)

0.1963 *** (t)

1.8565 *** ($\text{inv } \phi_w$)

25.6215 *** (ϕ_w)

3.7514 *** (M)

3.7470 *** (M_t)

1.7587 *** (q)

1.8787 *** (R_w)

BELT LENGTH



This program computes the belt length around an arbitrary set of pulleys. It may also be used to compute the total length between any connected set of coordinates. The program assumes the coordinates of the first pulley to be (0,0). Optionally the x, y coordinates of the intersections of the belt and pulleys may be output.

$(x_i, y_i, R_i) = x, y$ coordinates and radius of pulley i

R_1 = Radius of first pulley

C.D. = Center to center distance of consecutive pulleys

L = Total length of belt

Equations:

$$L_{12} = \sqrt{C.D._{12}^2 - (R_2 - R_1)^2}$$

$$\text{Arc Length}_2 = R_2 (\pi - \alpha - \beta - \gamma_2)$$

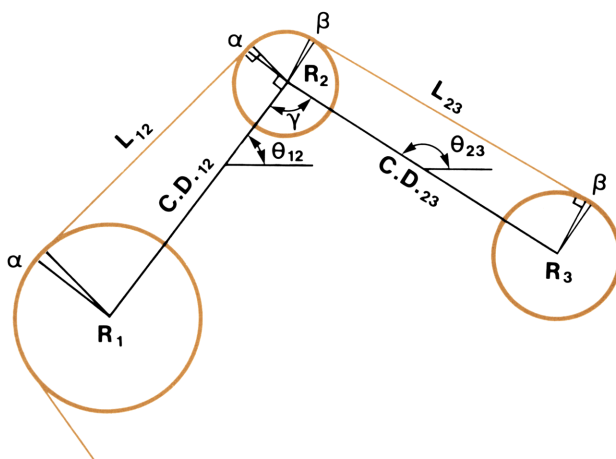
$$\alpha = \tan^{-1} \left(\frac{R_1 - R_2}{L_{12}} \right)$$

$$\beta = \tan^{-1} \left(\frac{R_3 - R_2}{L_{23}} \right)$$

$$\gamma = \theta_{12} - \theta_{23}$$

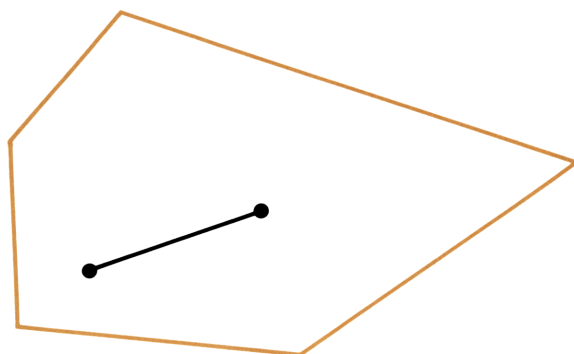
$$\theta_{12} = \tan^{-1} \frac{y_2 - y_1}{x_2 - x_1}$$

$$\theta_{23} = \tan^{-1} \frac{y_3 - y_2}{x_3 - x_2}$$

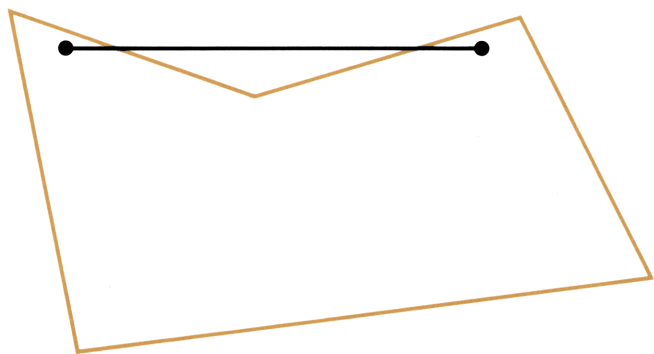


This program generates accurate results for any convex polygon, i.e., a line between any two points within the region bounded by the center-to-center line segments is entirely contained within the region.

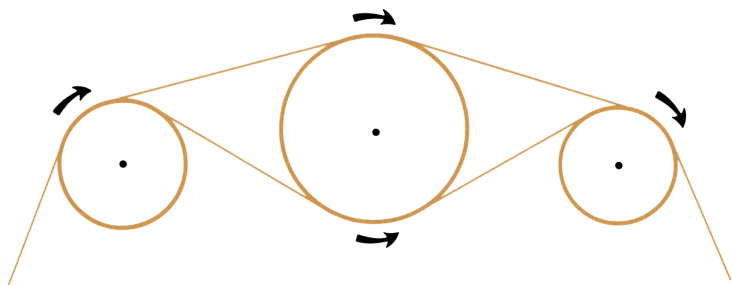
Convex



Concave

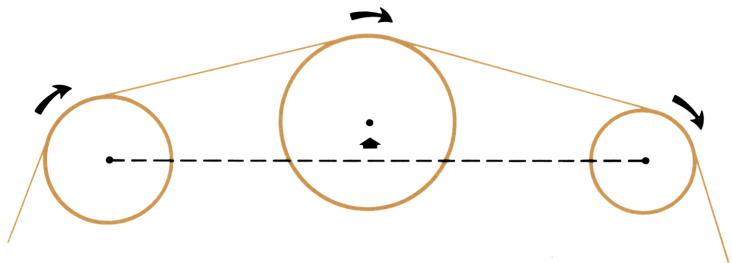


In some cases, there are two physically possible directions for the belt to take:



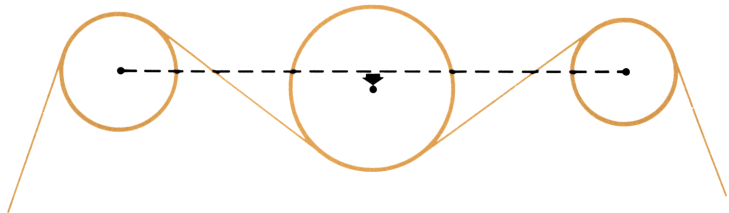
The program chooses the upper side if the middle pulley center lies above the line connecting the previous and following pulleys.

Case 1



The program chooses the lower side if the middle pulley center lies below the line connecting the previous and following pulleys.

Case 2



The program generates inaccurate answers in the second case. Note the figure bounded by the center-to-center line segments for the second case is not convex.

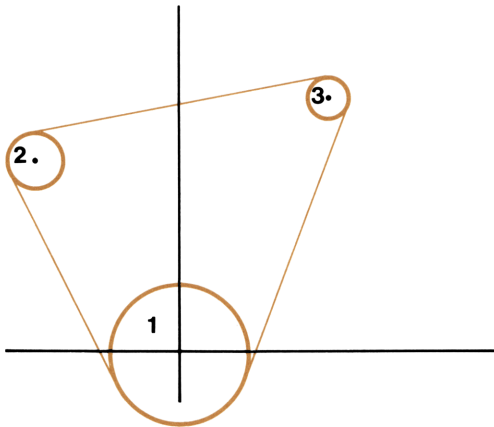
STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Optional: Toggle for printing belt tangent points for each pulley.*		F A	1.00
3	Input the coordinates (x_1 , y_1) and radius of the first pulley.	x_1	ENTER	x_1
		y_1	ENTER	y_1
		R_1	A	R_1
4	Input the next pulley coordinates (x_i , y_i) and radius (R_i).	x_i	ENTER	x_i
		y_i	ENTER	y_i
		R_i	B	R_i
5	Repeat step 4 for all remaining pulleys.			
6	Calculate the belt length.		C	L
7	For a new case, go to step 2.			
	*Note: Pulley coordinates have to be entered in the clockwise sense.			

Example 1:

Assume three pulleys are positioned as shown below with the following coordinates and radii:

- Pulley 1 (0, 0, 4 inches)
- Pulley 2 (-8, 15, 1.5 inches)
- Pulley 3 (9, 16, 1 inches).

Find the belt length around the three pulleys.



Keystrokes:	Outputs:
0 ENTER 0 ENTER 4 A →	4.00 (R ₁)
8 CHS ENTER 15 ENTER	
1.5 B →	1.50 (R ₂)
9 ENTER 16 ENTER 1 B →	1.00 (R ₃)
C →	66.53 (L)

Example 2:

Find the length of line connecting the points (0, 0), (1.5, 7), (3.2, -6), (0, 0.5), (0, 0). (28.01). Let the radius of each “pulley” be 0.

Keystrokes:	Outputs:
0 ENTER 0 ENTER 0 A →	0.00
1.5 ENTER 7 ENTER 0 B →	0.00
3.2 ENTER 6 CHS ENTER	
0 B →	0.00

0 **ENTER** 0.5 **ENTER** 0 **B** →

0.00

C →

28.01 (L)

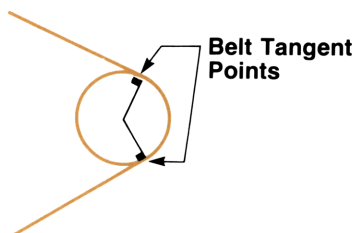
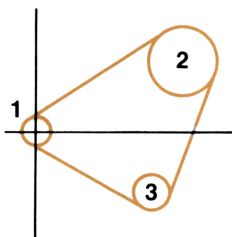
Example 3:

Find the belt length around the following pulley system, also find the belt tangent points on each pulley.

Pulley 1 (0, 0, 2.5)

Pulley 2 (30, 3, 7.5)

Pulley 3 (18, -18, 3.66)



Keystrokes:

f **A** →

0 **ENTER** 0 **ENTER** 2.5 **A** →

30 **ENTER** 3 **ENTER** 7.5 **B** →

18 **ENTER** 18 **CHS** **ENTER** 3.66

B →

C →

Outputs:

1.00

2.5 (R₁)

-0.66 *** (x)

2.41 *** (y) 1st pulley

28.03 *** (x)

10.24 *** (y) 2nd pulley

7.5 (R₂)

35.84 *** (x)

-1.71 *** (y) 2nd pulley

20.85 *** (x)

-20.30 *** (y) 3rd pulley

3.66 (R₃)

15.30 *** (x)

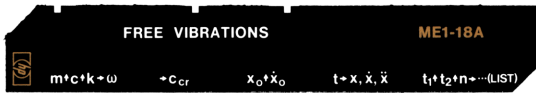
-20.47 *** (y) 3rd pulley

-1.85 *** (x)

-1.69 *** (y) 1st pulley

109.33 (L)

FREE VIBRATIONS



This program provides an exact solution to the differential equation for a damped oscillator vibrating freely: $m\ddot{x} + c\dot{x} + kx = 0$.

The user inputs the mass m , spring constant k , and damping constant c at **A**. The output will be:

1. ω for an underdamped system, i.e. $c < c_{\text{crit}}$. c_{crit} is calculated by pressing **B**.
2. 0 for a critically damped system, i.e. $c = c_{\text{crit}}$.
3. -1 for an overdamped system, i.e. $c > c_{\text{crit}}$.

The initial conditions are the displacement and velocity at time zero (x_0 and \dot{x}_0).

Equations:

$$c_{\text{crit}} = 2 \sqrt{km}$$

$$\omega = \sqrt{\frac{k}{m} - \left(\frac{c}{2m}\right)^2}$$

$$\ddot{x} = -(c\dot{x} + kx)/m$$

Underdamping

$$(c^2 - 4km < 0)$$

$$x(t) = R e^{-\frac{c}{2m}t} \cos(\omega t - \delta)$$

$$\dot{x}(t) = -R\omega e^{-\frac{c}{2m}t} \sin(\omega t - \delta) - \frac{c}{2m} R e^{-\frac{c}{2m}t} \cos(\omega t - \delta)$$

where:

$$R \cos \delta = x_0$$

$$R \sin \delta = \frac{1}{\omega} \left[\dot{x}_0 + \frac{c}{2m} x_0 \right]$$

Critical damping

$$(c = c_{\text{crit}}, \text{ or } c^2 = 4km)$$

$$x(t) = (A_{cr} + B_{cr}t)e^{-\frac{c}{2m}t}$$

$$\dot{x}(t) = \left[B_{cr} - \frac{c}{2m} (A_{cr} + B_{cr}t) \right] e^{-\frac{c}{2m}t}$$

where:

$$A_{cr} = x_0$$

$$B_{cr} = \dot{x}_0 + \frac{c}{2m} x_0$$

Overdamping

$$(c^2 - 4km > 0)$$

$$\dot{x}(t) = A_{ov}e^{r_1t} + B_{ov}e^{r_2t}$$

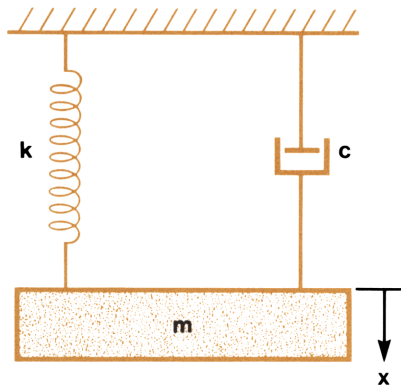
$$x(t) = A_{ov}r_1e^{r_1t} + B_{ov}r_2e^{r_2t}$$

where:

$$r_1, r_2 = -\frac{c}{2m} \pm \sqrt{\left(\frac{c}{2m}\right)^2 - \frac{k}{m}}$$

$$A_{ov} = x_0 - B_{ov}$$

$$B_{ov} = \frac{\dot{x}_0 - r_1 x_0}{r_2 - r_1}$$



Reference:

Boyce, W.E. and DiPrima, R.C., *Elementary Differential Equations*, John Wiley and Sons, 1969.

Remarks:

For overdamping, ω has no meaning and is, in fact, an imaginary number.

For $c = c_{crit}$, $\omega = 0$.

This program sets the angular mode of the calculator to radians. Erroneous answers will occur if degree mode is inadvertently set.

Registers R_{S0} – R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the system parameters	m	ENTER	
	of mass, damping constant,	c	ENTER	
	and spring constant.	k	A	ω or 0 or -1
3	Optional: Calculate c_{crit}		B	c_{crit}
4	Input initial conditions of			
	position	x_0	ENTER	x_0
	and velocity.	\dot{x}_0	C	\dot{x}_0
5	Input t to calculate $x(t)$, $\dot{x}(t)$,			
	and $\ddot{x}(t)$.	t	D	$x(t), \dot{x}(t), \ddot{x}(t)$
6	Repeat step 5 for a different t.			
7	Input t_1 and t_2 and number of			
	intervals (n) to calculate			
	$x(t)$, $\dot{x}(t)$, and $\ddot{x}(t)$ automatically.	t_1	ENTER	t_1
		t_2	ENTER	t_2
		n	E	$x(t), \dot{x}(t), \ddot{x}(t)$
8	For different initial conditions			
	for the same system, go to			
	step 4.			
9	For a different system, go to			
	step 2.			

Example:

A mass of 20 g stretches a spiral spring 10 cm. The mass is pulled down an additional 4 cm, held, and then released. Find the mass displacement and velocity at 0.1 second intervals up to 1 second for the cases in which (a) $c = 50$ dyne-sec/cm (b) $c = c_{\text{crit}}$ and (c) $c = 400$ dyne-sec/cm.

$$k = \frac{F}{x} = \frac{mg}{x} = \frac{20g (980 \text{ cm/s}^2)}{10 \text{ cm}} = \frac{20 \times 980}{10} \text{ dyne/cm}$$

(a) $c = 50$

Keystrokes:

Outputs:

20 **ENTER** 50 **ENTER** 20 **ENTER**

980 **x** 10 **=** **A** \longrightarrow

B \longrightarrow

4 **ENTER** 0 **C** \longrightarrow

0 **D** \longrightarrow

0.1 **D** \longrightarrow

0.2 **D** \longrightarrow

9.820 (ω)

395.980 (c_{crit})

4.000 (x_0)

4.000 *** (x)

1.000000000-09 *** (\dot{x})

-392.00 *** (\ddot{x})

2.334 *** (x)

-29.296 *** (\dot{x})

-155.494 *** (\ddot{x})

-0.827 *** (x)

-28.715 *** (\dot{x})

152.880 *** (\ddot{x})

Or, the same results can be achieved automatically.

0 **ENTER** 1 **ENTER** 10 **E** \longrightarrow

0.000 *** (t)

4.000 *** (x)

1.000000000-09 *** (\dot{x})

-392.000 *** (\ddot{x})

0.100 ***

2.334 ***

-29.296 ***

-155.494 ***

0.200 ***

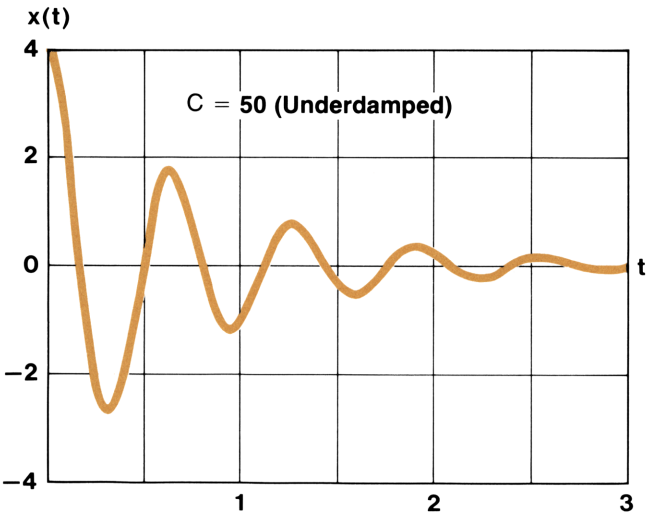
-0.827 ***

-28.715 ***

152.880 ***
0.300 ***
-2.629 ***
-5.330 ***
270.947 ***
0.400 ***
-1.932 ***
17.139 ***
146.511 ***
0.500 ***
0.153 ***
20.950 ***
-67.408 ***
0.600 ***
1.655 ***
7.187 ***
-180.174 ***
0.700 ***
1.503 ***
-9.272 ***
-124.104 ***
0.800 ***
0.184 ***
-14.685 ***
18.677 ***
0.900 ***
-0.990 ***
-7.173 ***
114.959 ***
1.000 ***
-1.114 ***
4.406 ***
98.133 ***

Solution (a) $c = 50$

t s	x cm	\dot{x} cm/s	\ddot{x} cm/s ²
0	4.000	0.00	-392.000
.1	2.334	-29.296	-155.494
.2	-0.827	-28.715	152.880
.3	-2.629	-5.330	270.947
.4	-1.932	17.139	146.511
.5	0.153	20.950	-67.408
.6	1.655	7.187	-180.174
.7	1.503	-9.272	-124.104
.8	0.184	-14.685	18.677
.9	-0.990	-7.173	114.959
1.0	-1.114	4.406	98.133



(b) $c = c_{\text{crit}}$


Keystrokes:

20 **ENTER** 395.98 **ENTER**
20 **ENTER** 980 **x**
10 **÷** **A** \longrightarrow
4 **ENTER** 0 **C** \longrightarrow
0 **D** \longrightarrow

Outputs:

0.000
4.000 (x_0)
4.000 *** (x)
0.000 *** (\dot{x})
-392.000 *** (\ddot{x})

18-07

0.1 **D** 

2.958 ***
-14.567 ***
-1.464 ***

0.2 **D** 

1.646 ***
-10.826 ***
53.041 ***

⋮

Or, automatically:

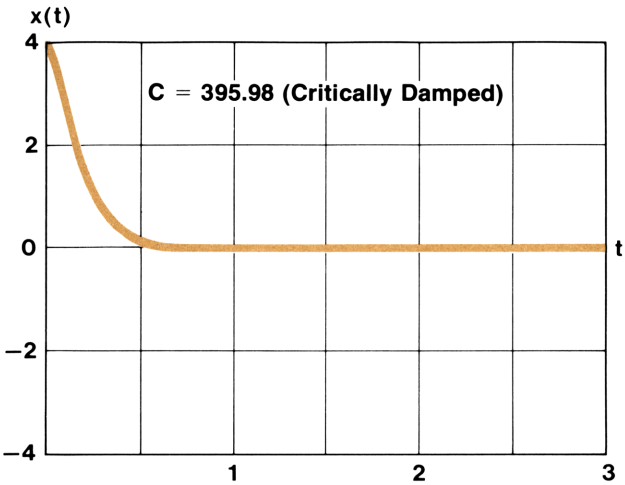
0 **ENTER** 1 **ENTER** 10 **E** 

0.000 ***
4.000 ***
0.000 ***
-392.000 ***
0.100 ***
2.958 ***
-14.567 ***
-1.464 ***
0.200 ***
1.646 ***
-10.826 ***
53.041 ***
0.300 ***
0.815 ***
-6.034 ***
39.622 ***
0.400 ***
0.378 ***
-2.990 ***
22.122 ***
0.500 ***
0.169 ***
-1.389 ***
10.970 ***
0.600 ***
0.073 ***
-0.619 ***
5.098 ***
0.700 ***
0.031 ***

-0.268	***
2.274	***
0.800	***
0.013	***
-0.114	***
0.986	***
0.900	***
0.005	***
-0.048	***
0.419	***
1.000	***
0.002	***
-0.020	***
0.175	***

Solution (b) $c = c_{crit}$

t s	x cm	\dot{x} cm/s	\ddot{x} cm/s ²
0	4.000	0.000	-392.000
.1	2.958	-14.567	-1.464
.2	1.646	-10.826	53.041
.3	0.815	-6.034	39.622
.4	0.378	-2.990	22.122
.5	0.169	-1.389	10.970
.6	0.073	-0.619	5.098
.7	0.031	-0.268	2.274
.8	0.013	-0.114	0.986
.9	0.005	-0.048	0.419
1.0	0.002	-0.020	0.175



(c) $c = 400$

Keystrokes:

20 **ENTER** 400 **ENTER** 20 **ENTER**
980 **x** 10 **÷** **A** \longrightarrow
4 **ENTER** 0 **C** \longrightarrow
0 **D** \longrightarrow

0.1 **D** \longrightarrow

0.2 **D** \longrightarrow

Or, automatically:

0 **ENTER** 1 **ENTER** 10 **E** \longrightarrow

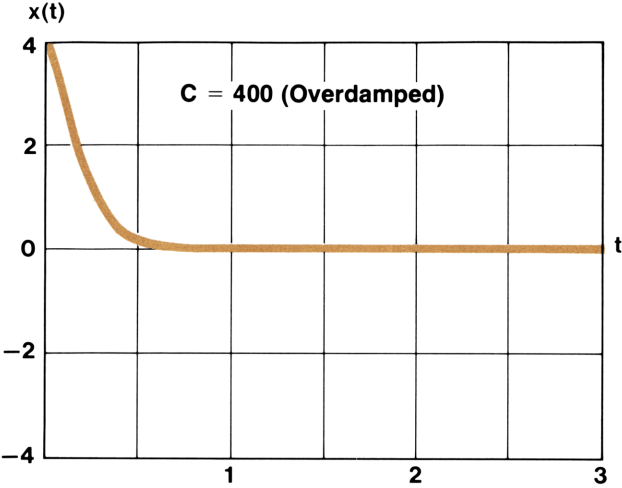
Outputs:

-1.000 ***
4.000 (x₀)
4.000 *** (x)
0.000 *** (\dot{x})
-392.000 *** (\ddot{x})
2.963 *** (x)
-14.469 *** (\dot{x})
-0.963 *** (\ddot{x})
1.660 *** (x)
-10.752 *** (\dot{x})
52.336 *** (\ddot{x})
0.000 ***
4.000 ***
0.000 ***
-392.000 ***
0.100 ***
2.963 ***
-14.469 ***
-0.963 ***
0.200 ***
1.660 ***
-10.752 ***
52.336 ***
0.300 ***
0.833 ***
-6.032 ***
39.022 ***
0.400 ***
0.394 ***
-3.028 ***
21.916 ***
0.500 ***
0.180 ***
-1.433 ***

11.005 ***
0.600 ***
0.081 ***
-0.656 ***
5.212 ***
0.700 ***
0.035 ***
-0.293 ***
2.384 ***
0.800 ***
0.015 ***
-0.129 ***
1.066 ***
0.900 ***
0.007 ***
-0.056 ***
0.470 ***
1.000 ***
0.003 ***
-0.024 ***
0.205 ***

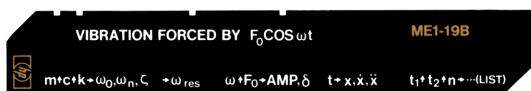
Solution (c) $c = 400$

$t \text{ s}$	$x \text{ cm}$	$\dot{x} \text{ cm/s}$	$\ddot{x} \text{ cm/s}^2$
0	4.000	0.000	-392.000
.1	2.963	-14.469	-0.963
.2	1.660	-10.752	52.336
.3	0.833	-6.032	39.022
.4	0.394	-3.028	21.916
.5	0.180	-1.433	11.005
.6	0.081	-0.656	5.212
.7	0.035	-0.293	2.384
.8	0.015	-0.129	1.066
.9	0.007	-0.056	0.470
1.0	0.003	-0.024	0.205



Notes

VIBRATION FORCED BY $F_0 \cos \omega t$



This program finds the steady-state solution for an object undergoing damped forced oscillations from a periodic external force of the form $F_0 \cos \omega t$. The differential equation to be solved is

$$m\ddot{x} + c\dot{x} + kx = F_0 \cos \omega t$$

The program calculates the following variables: ω_0 , ω_n , ζ , ω_{res} , AMP, δ , $x(t)$, $\dot{x}(t)$, and $\ddot{x}(t)$, which are defined as follows:

Equations:

The steady-state solution ($t \rightarrow \infty$) to this equation is

$$x(t) = \frac{F_0}{\Delta} \cos(\omega t - \delta)$$

$$\dot{x}(t) = -\omega \frac{F_0}{\Delta} \sin(\omega t - \delta)$$

where:

$$\Delta = \sqrt{m^2 (\omega_0^2 - \omega^2)^2 + c^2 \omega^2}$$

$$\omega_0 = \sqrt{\frac{k}{m}} = \text{natural frequency or undamped system}$$

$$\omega_n = \sqrt{\frac{k}{m} - \left(\frac{c}{2m}\right)^2} = \text{damped natural frequency}$$

$$\zeta = \frac{c}{C_{crit}} = \frac{c}{2m \omega_0} = \text{damping ratio}$$

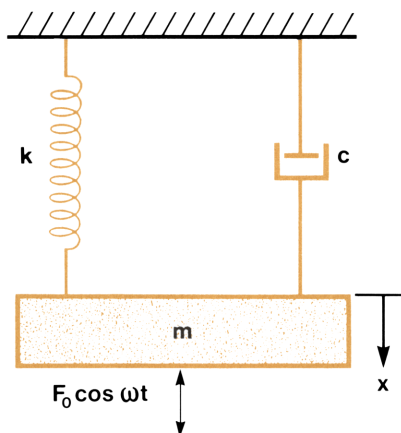
$$\delta = \tan^{-1} \frac{c \omega}{m(\omega_0^2 - \omega^2)}$$

$$AMP = \frac{F_0}{\Delta}$$

ω_{res} is computed from

$$\omega_{res}^2 = \omega_0^2 - \frac{1}{2} \left(\frac{c}{m}\right)^2$$

$$AMP_{max} = \frac{F_0}{\Delta} \quad (\text{where } \omega = \omega_{res})$$



Reference:

Boyce, W.E. and DiPrima, R.C., *Elementary Differential Equations*, John Wiley and Sons, 1969.

Remarks:

The above solution does not take into account the initial conditions ($x(0)$, $\dot{x}(0)$) of the system, consequently values of $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ calculated by this program are for large values of t . However, should you need values of $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ for the system with initial conditions $x(0)$ and $\dot{x}(0)$, use ME1-18A. Calculate the homogeneous solution $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ and add it to the values (the particular solution) calculated by this program.

This program sets the angular mode of the calculator to radians.

Registers R_{S0} — R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the system parameters			
	of mass,	m	ENTER➤	
	damping coefficient	c	ENTER➤	
	and spring constant.	k	A	$\omega_0, \omega_n, \zeta$
3	Optional: Calculate the			
	resonant frequency ω_{res} .		B	ω_{res}
4	Input the frequency of external			
	excitation	ω	ENTER➤	
	and the external excitation			
	force.	F_0	C	AMP, $\delta(\text{deg.})$
5	Input t to calculate $x(t)$, $\dot{x}(t)$,			
	$\ddot{x}(t)$.	t	D	$x, \dot{x}(t) \ddot{x}(t)$
6	Input t_1 and t_2 and number of			
	intervals to calculate $x(t)$, $\dot{x}(t)$,			
	and $\ddot{x}(t)$ automatically.	t_1	ENTER➤	t_1
		t_2	ENTER➤	t_2
		n	E	n + 1 values of
				$x(t), \dot{x}(t),$
				$\ddot{x}(t)$ between
				t_1 and t_2
7	For a different external			
	excitation, applied to the same			
	system, go to step 4.			
8	For a different system, go to			
	step 2.			

Example:

A 400-lb. weight is suspended from a spring and stretches it a distance of 2 inches. The damping constant of the system is 0.5 lb-sec/ft. If the weight is driven by a periodic external force whose greatest value is 5 pounds, find (a) the resonant frequency of the system and (b) the amplitude and phase shift of the oscillation that will result if the mass is driven at the resonant frequency. Calculate the position, velocity, and acceleration for $t = 6.0$ sec. Also calculate the position, velocity, and acceleration for $t_1 = 6$ sec. and $t_2 = 10$ sec. with four intervals ($n = 4$).

$$m = \frac{F}{g} = \frac{400 \text{ lb}}{32.2 \text{ ft/sec}^2} \quad k = \frac{F}{x} = \frac{400 \text{ lb}}{2 \text{ in}} \frac{12 \text{ in}}{1 \text{ ft}}$$

Keystrokes:

400 **ENTER** 32.2 **÷** .5 **ENTER**
 400 **ENTER** 2 **÷** 12 **×** **A** **→**

B **→**

(To drive the system at the resonant frequency, leave ω_{res} in the display and key in the driving force of 5 pounds).

5 **C** **→**

6 **D** **→**

Outputs:

13.900 *** (ω_0)

13.900 *** (ω_n)

0.001 *** (ζ)

13.900 (ω_{res})

0.719 *** (AMP)

89.917 *** (δ in deg.)

0.712 *** (x)

-1.464 *** (\dot{x})

-137.499 *** (\ddot{x})

or automatically:

6 **ENTER** 10 **ENTER** 4 **E** **→**

6.000 ***

0.712 ***

-1.464 ***

-137.499 ***

7.000 ***

0.065 ***

-9.959 ***

-12.582 ***

8.000 ***

-0.681 ***

-3.223 ***

131.577 ***

9.000 ***
-0.386 ***
8.442 ***
74.510 ***
10.000 ***
0.500 ***
7.197 ***
-96.508 ***

Notes

EQUATIONS OF STATE



This card provides both ideal gas and Redlich-Kwong equations of state. Given four of the five state variables, the fifth is calculated. For the Redlich-Kwong solution, the critical pressure and temperature of the gas must be known. They are not needed for ideal gas solutions.

Values of the Universal Gas Constants

Value of R	Units of R	Units of P	Units of V	Units of T
8.314	N - m/g mole - K	N/m ²	m ³ /g mole	K
83.14	cm ³ - bar/g mole - K	bar	cm ³ /g mole	K
82.05	cm ³ - atm/g mole - K	atm	cm ³ /g mole	K
0.7302	atm - ft ³ /lb mole - °R	atm	ft ³ /lb mole	°R
10.73	psi - ft ³ /lb mole - °R	psi	ft ³ /lb mole	°R
1545	psf - ft ³ /lb mole - °R	psf	ft ³ /lb mole	°R

Critical Temperatures and Pressures

Substance	T _c , K	T _c , °R	P _c , ATM
Ammonia	405.6	730.1	112.5
Argon	151	272	48.0
Carbon dioxide	304.2	547.6	72.9
Carbon monoxide	133	239	34.5
Chlorine	417	751	76.1
Helium	5.3	9.5	2.26
Hydrogen	33.3	59.9	12.8
Nitrogen	126.2	227.2	33.5
Oxygen	154.8	278.6	50.1
Water	647.3	1165.1	218.2
Dichlorodifluoromethane	384.7	692.5	39.6
Dichlorofluoromethane	451.7	813.1	51.0
Ethane	305.5	549.9	48.2
Ethanol	516.3	929.3	63
Methanol	513.2	923.8	78.5
n-Butane	425.2	765.4	37.5
n-Hexane	507.9	914.2	29.9
n-Pentane	469.5	845.1	33.3
n-Octane	568.6	1023.5	24.6
Trichlorofluoromethane	471.2	848.1	43.2

Equations:

Ideal gas:

$$PV = nRT$$

Redlich-Kwong:

$$P = \frac{nRT}{(V - b)} - \frac{a}{T^{1/2} V (V + b)}$$

$$a = 4.934 b nRT_c^{1.5}$$

$$b = 0.0867 \frac{nRT_c}{P_c}$$

where:

P is the absolute pressure;

V is the volume;

n is the number of moles present;

R is the universal gas constant;

T is the absolute temperature;

T_c is the critical temperature;

P_c is the critical pressure.

Remarks:

P, V, n and T must have units compatible with R.

At low temperatures or high pressures, the ideal gas law does not represent the behavior of real gases.

No equation of state is valid for all substances nor over an infinite range of conditions. The Redlich-Kwong equation gives moderate to good accuracy for a variety of substances over a wide range of conditions. Results should be used with caution and tempered by experience.

Solutions for V, n, R and T, using the Redlich-Kwong equation, require an iterative technique. Newton's method is employed using the ideal gas law to generate the initial guess. Iteration time is generally a function of the amount of deviation from ideal gas behavior. For extreme cases, the routine may fail to converge entirely, resulting in an "error".

Registers R_0 , R_1 and R_{S0} — R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Select Redlich-Kwong (1.00) or			
	ideal gas (0.00) using mode			
	toggle.		f A	1.00/0.00
3	If you selected ideal gas in			
	step 2, skip to step 5.			
4	Input critical temperature	T_c	f B	T_c
	and critical pressure.	P_c	f C	P_c
5	Input four of the following:			
	Absolute pressure	P	A	P
	Volume	V	B	V
	Number of moles	n	C	n
	Universal gas constant	R	D	R
	Absolute temperature	T	E	T
6	Calculate remaining value:			
	Absolute pressure		A	P
	Volume		B	V
	Number of moles		C	n
	Universal gas constant		D	R
	Absolute temperature		E	T
7	For a new case, go to steps 2,			
	4, or 5 and change values or			
	mode.			

Example 1:

0.63 g moles of air are enclosed in a 25,000 cm³ space at 1200 K. What is the pressure in bars? Assume an ideal gas.

Keystrokes:

Outputs:

Select ideal gas by pressing **f** **A** until 0.00 is displayed.

f **A** **f** **A** →

0.00

25000 **B** .63 **C** 83.14 **D**

1200 **E** **A** →

2.51 (bars)

Example 2:

What is the specific volume (ft³/lb) of a gas at atmospheric pressure and at a temperature of 513°R? The molecular weight is 29. Assume an ideal gas.

Keystrokes:

f **A** \longrightarrow

513 **E** 29 **1/x** **C** 0.7302

D 1 **A** **B** \longrightarrow

What is the density?

1/x \longrightarrow

What is the density at 1.32 atmospheres and 555°R?

1.32 **A** 555 **E** **B** **1/x** \longrightarrow

Outputs:

0.00

12.92 (ft³/lb)

0.08 (lb/ft³)

0.09 (lb/ft³)

Example 3:

The specific volume of a gas in a container is 800 cm³/g mole. The temperature will reach 400 K. What will the pressure be according to the Redlich-Kwong relation?

$$P_c = 48.2 \text{ atm}$$

$$T_c = 305.5 \text{ K}$$

$$R = 82.05 \text{ cm}^3 - \text{atm/g mole-K}$$

Keystrokes:

f **A** \longrightarrow

305.5 **f** **B** 48.2 **f** **C** 82.05

D 1 **C** 400 **E** 800 **B** **A** \longrightarrow

Outputs:

1.00

36.27 (atm)

Example 4:

6 gram moles of carbon dioxide gas are held at a pressure of 50 atmospheres, and at a temperature of 500 K. What is the volume in cubic centimeters? Use the Redlich-Kwong relation.

$$T_c = 304.2 \text{ K}$$

$$P_c = 72.9 \text{ atm}$$

$$R = 82.05 \text{ cm}^3 - \text{atm/g mole} - \text{K}$$

Keystrokes:

f **A** \longrightarrow

72.9 **f** **C** 304.2 **f** **B** 82.05

D 6 **C** 50 **A** 500 **E** **B** \longrightarrow

Outputs:

1.00

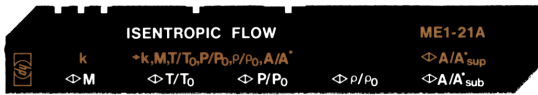
4695.86 (cm³)

How many moles could be contained at this temperature and pressure in 5 liters?

5000 **B** **C** \longrightarrow

6.39 (g moles)

ISENTROPIC FLOW FOR IDEAL GASES



This card replaces isentropic flow tables for a specified specific heat ratio k . Inputs and outputs are interchangeable with the exception of k .

The following values are correlated:

M is the Mach number;

T/T_0 is the ratio of flow temperature T to stagnation or zero velocity temperature T_0 ;

P/P_0 is the ratio of flow pressure P to stagnation pressure P_0 ;

ρ/ρ_0 is the ratio of flow density ρ to stagnation density ρ_0 ;

A/A^*_{sub} and A/A^*_{sup} are the ratios of flow area A to the throat area A^* in converging—diverging passages. A/A^*_{sub} refers to subsonic flow while A/A^*_{sup} refers to supersonic flow.

Equations:

$$T/T_0 = \frac{2}{2 + (k - 1) M^2}$$

$$P/P_0 = (T/T_0)^{k/(k-1)}$$

$$\rho/\rho_0 = (T/T_0)^{1/(k-1)}$$

$$A/A^* = \frac{1}{M} \left[\left(\frac{2}{k + 1} \right) \left(1 + \frac{k - 1}{2} M^2 \right) \right]^{\frac{k + 1}{2(k - 1)}}$$

In the last equation M^2 is determined using Newton's method. The initial guess used is as follows with a positive exponent for supersonic flow:

$$M_0^2 = (\sqrt{\text{Frac}(A/A^*)} + A/A^*)^{\pm 3}$$




Remarks:

After an input of A/A^* , the program begins to iterate to find M^2 for future use. This iteration will normally take less than one minute, but may take longer on occasion. For extreme values of k (1.4 is optimum) the routine may fail to converge at all. An "Error" message will eventually halt the routine if it goes out of control.

A/A* values of 1.00 are illegal inputs. Instead, input an M of 1.00.

The calculator uses flag 3 to decide whether to store or calculate a value. If you use the data input keys (setting flag 3) and then wish to calculate a parameter based on a prior input, clear flag 3 before pressing the appropriate user definable keys.

Registers R₀, R₅ and R_{S0}–R_I are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input specific heat ratio.	k	 A	k
3	Input one of the following:			
	Mach number	M	A	M
	Temperature ratio	T/T ₀	B	M
	Pressure ratio	P/P ₀	C	M
	Density ratio	ρ/ρ ₀	D	M
	Subsonic area ratio	A/A* _{sub}	E	M
	Supersonic area ratio	A/A* _{sup}	 E	M
4	Calculate one of the following:			
	Mach number		A	M
	Temperature ratio		B	T/T ₀
	Pressure ratio		C	P/P ₀
	Density ratio		D	ρ/ρ ₀
	Area ratio (subsonic or supersonic)		E	A/A*
4'	Calculate and output all values automatically.		 B	k, M, T/T ₀ , P/P ₀ ρ/ρ ₀ , A/A*
5	For another calculation based on same input, go to step 4 (or 4'). For a new input, go to step 3. For a new specific heat ratio, go to step 2.			

Example 1:

A pilot is flying at Mach 0.93 and reads on air temperature of 15 degrees Celsius (288 K) on a thermometer that reads stagnation temperature T_0 . What is the true temperature assuming that $k = 1.38$?

Keystrokes:

1.38 **f** **A** →
.93 **A** →
B →
288 **x** →
273 **-** →

Outputs:

1.380
0.930
0.859 (T/T₀)
247.352 (T, K)
-25.648 (T, °C)

If the same pilot reads a stagnation pressure P_0 of 700 millimeters of mercury, what is the true air pressure?

(Since the data input flag was set when 288 was keyed in, we must either clear it, or input 0.93 again.)

.93 **A** **C** →
700 **x** →

0.575 (P/P₀)
402.843 (mm Hg)

Example 2:

A converging, diverging passage has supersonic flow in the diverging section. At an area ratio A/A^* of 1.60, what are the isentropic flow ratios for temperature, pressure and density? What is the Mach number? $k = 1.74$.

Keystrokes:

1.74 **f** **A** →
1.60 **f** **E** →
B →
C →
D →

Outputs:

1.740
2.105 (M)
0.379 (T/T₀)
0.102 (P/P₀)
0.269 (ρ/ρ_0)

or, alternatively, using automatic output.

f **B** →

1.740 *** (k)
2.105 *** (M)
0.379 *** (T/T₀)
0.102 *** (P/P₀)
0.269 *** (ρ/ρ_0)
1.600 *** (A/A*)

Notes

CONDUIT FLOW



This program solves for the average velocity, or the pressure drop for viscous, incompressible flow in conduits.

Equations:

$$v^2 = \frac{\Delta P / \rho}{2 \left(f \frac{L}{D} + \frac{K_T}{4} \right)}$$

For laminar flow ($Re < 2300$)

$$f = 16/Re$$

For turbulent flow ($Re > 2300$)

$$\frac{1}{\sqrt{f}} = 1.737 \ln \frac{D}{\epsilon} + 2.28 - 1.737 \ln \left(4.67 \frac{D}{\epsilon Re \sqrt{f}} + 1 \right)$$

is solved by Newton's method.

$$\frac{1}{\sqrt{f_0}} = 1.737 \ln \frac{D}{\epsilon} + 2.28$$

is used as an initial guess in the iteration.

where:

Re is the Reynolds number, defined as $\rho D v / \mu$;

D is the pipe diameter;

ϵ is the dimension of irregularities in the conduit surface (see table 2);

f is the Fanning friction factor for conduit flow;

ΔP is the pressure drop along the conduit;

ρ is the density of the fluid;

μ is the viscosity of the fluid;

ν is the kinematic viscosity of the fluid;

L is the conduit length;

v is the average fluid velocity;

K_T is the total of the applicable fitting coefficients in table 1.

Table 1
Fitting Coefficients

Fitting	K
Globe valve, wide open	7.5—10
Angle valve, wide open	3.8
Gate valve, wide open	0.15—0.19
Gate valve, $\frac{3}{4}$ open	0.85
Gate valve, $\frac{1}{2}$ open	4.4
Gate valve, $\frac{1}{4}$ open	20
90° elbow	0.4—0.9
Standard 45° elbow	0.35—0.42
Tee, through side outlet	1.5
Tee, straight through	.4
180° bend	1.6
Entrance to circular pipe	0.25—0.50
Sudden expansion	$(1 - A_{up}/A_{dn})^{2*}$
Acceleration from $v = 0$ to $v = V_{entrance}$	1.0

* A_{up} is the upstream area and A_{dn} is the downstream area.

Table 2
Surface Irregularities

Material	ϵ (feet)	ϵ (meters)
Drawn or Smooth Tubing	5.0×10^{-6}	1.5×10^{-6}
Commercial Steel or Wrought Iron	1.5×10^{-4}	4.6×10^{-5}
Asphalted Cast Iron	4.0×10^{-4}	1.2×10^{-4}
Galvanized Iron	5.0×10^{-4}	1.5×10^{-4}
Cast Iron	8.3×10^{-4}	2.5×10^{-4}
Wood Stave	6.0×10^{-4} to 3.0×10^{-3}	1.8×10^{-4} to 9.1×10^{-4}
Concrete	1.0×10^{-3} to 1.0×10^{-2}	3.0×10^{-4} to 3.0×10^{-3}
Riveted Steel	3.0×10^{-3} to 3.0×10^{-2}	9.1×10^{-4} to 9.1×10^{-3}

Reference:

Welty, Wicks, Wilson; *Fundamentals of Momentum, Heat and Mass Transfer*, John Wiley and Sons, Inc., 1969.

Remarks:

The correlation gives meaningless results in the region $2300 < Re < 4000$.

The solution requires an iterative procedure. The time for solution will range from 10 seconds for ΔP , to several minutes for v . The display setting is used to determine when the solution for v is adequately accurate. Time for solution of v is roughly proportional to the number or significant digits in the display setting.

If the conduit is not circular, an equivalent diameter may be calculated using the formula below:

$$D_{eq} = 4 \frac{\text{cross sectional area}}{\text{wetted perimeter}}$$

Unitary consistency must be maintained with the exception of the pressure drop ΔP . If all length units are feet, time is measured in seconds and mass is given in pounds, pressure may be input or output in pounds per square inch, using the **f** **E** keys.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the following in any order			
	(units must be consistent):			
	Viscosity of fluid	μ	f A	
	or			
	Kinematic viscosity of fluid	ν	f B	ν
	Density	ρ	f C	ρ
	Surface irregularity	ϵ	f D	ϵ
	Length of conduit	L	A	L
	Equivalent diameter of			
	passage	D	B	D
	Total fitting coefficient	K_T	C	$K_T/4$
3	Input one of the following:			
	Fluid velocity	v	D	v
	Pressure drop in compatible			
	units	ΔP	E	ΔP
	or			
	Pressure drop in psi	$\Delta P(\text{psi})$	f E	144g ΔP

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
4	Calculate one of the following:			
	Fluid velocity		D	v
	Pressure drop in compatible			
	units		E	ΔP
	or			
	Pressure drop in psi		f E	$\Delta P(\text{psi})$
5	Optional: After calculation of			
	ΔP or v, display Reynolds			
	number		R+	Re
	and Fanning friction factor.		R+	f
6	For a new case, go to step 2 or			
	step 3 and change appropriate			
	inputs.			

Example 1:

A heat exchanger has 20, 3 meter tube passes (60 m of pipe) with 180 degree bends connecting each pair of tubes (from table 1, $K_T = 10 \times 1.6$). The fluid is water ($\nu = 9.3 \times 10^{-7} \text{ m}^2/\text{s}$, $\rho = 10^3 \text{ kg/m}^3$). The surface roughness is $3 \times 10^{-4} \text{ m}$ and the diameter is $2.54 \times 10^{-2} \text{ m}$. If the fluid velocity is 3.05 m/s, what is the pressure loss? What is the Reynolds number? What is the Fanning friction factor?

Keystrokes:

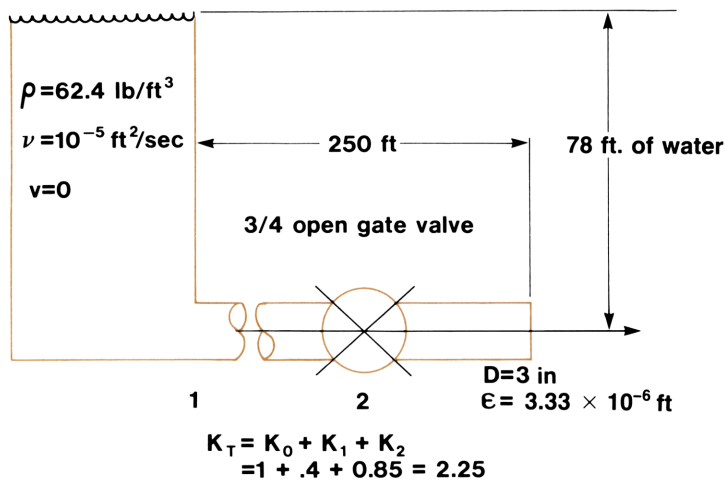
9.3 **EEX** **CHS** 7 **f** **B** **EEX** 3
f **C** 3 **EEX** **CHS** 4 **f** **D** 60
A 2.54 **EEX** **CHS** 2 **B** 16 **C**
3.05 **D** **E** \longrightarrow
R+ \longrightarrow
R+ \longrightarrow

Outputs:

522. 03 ($\Delta P, \text{N/m}^2$)
83.3 03 (Re)
10.2-03 (f)

Example 2:

For the system shown, what is the volume flow rate?



Keystrokes:

Outputs:

First calculate and store ΔP in psi from the given data.

78 **ENTER** 62.4 **×** 144 **÷**
f **E** \longrightarrow 157. 03 (ΔP , psi)

Now store the other values.

EEX **CHS** 5 **f** **B** 62.4 **f**
C 3.33 **EEX** **CHS** 6 **f** **D** 250
A 3 **ENTER** 12 **÷** **B** 2.25
C **D** \longrightarrow 17.8 00 (v , ft/sec)

Calculate volume flow rate ($v \times \text{Area}$).

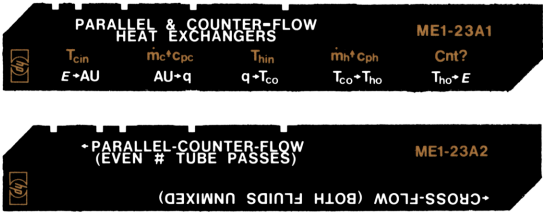
1.5 **ENTER** 12 **÷** **ENTER**
× **π** **×** **×** \longrightarrow 873.-03 (ft^3/sec)

What will the height of the water be when the velocity is 15 ft/sec?

15 **D** **f** **E** \longrightarrow 24.7 00 (ΔP , psi)
144 **×** 62.4 **÷** \longrightarrow 57.0 00 (ft)

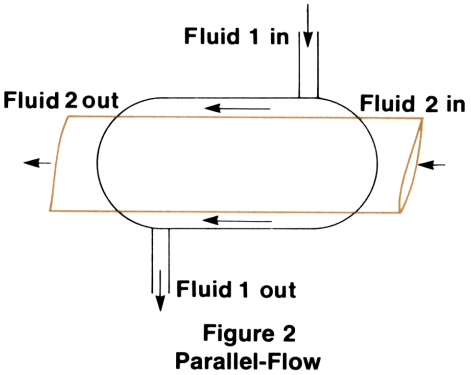
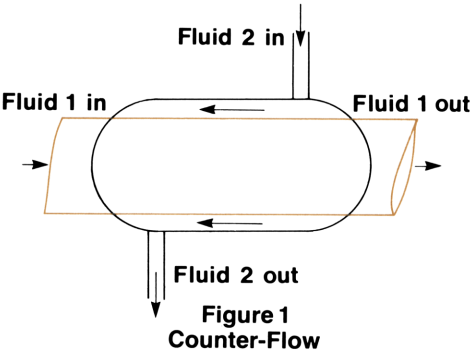
Notes

PARALLEL & COUNTER FLOW HEAT EXCHANGERS

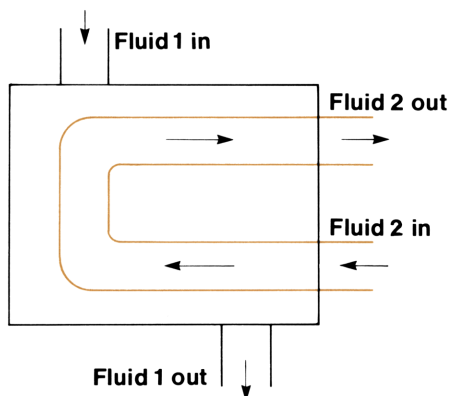


This two card set allows analysis of counter-flow, parallel-flow, parallel-counter flow, and cross-flow (both fluids unmixed) heat exchanges.

The program is organized in four segments. The first side of card 1 performs heat balance calculations and acts as controller for the three slave program segments. Slave program segment one, on side 2 of card 1, is applicable to parallel-flow and counter-flow heat exchanges. Counter-flow is selected by pressing **f E** until 1.00 appears. Parallel-flow is selected by pressing **f E** until 0.00 appears.

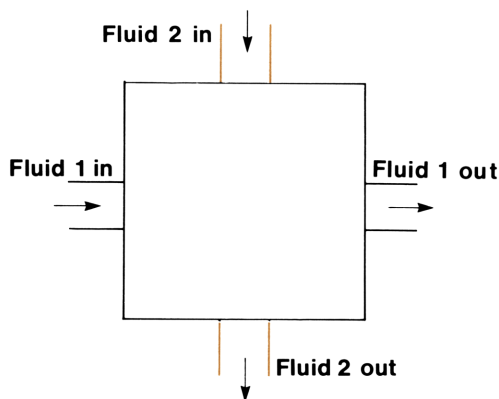


The slave segment for **parallel-counter-flow** configuration (with an even number of tube passes) is on side 1 of card 2.



**Figure 3 Parallel-Counter-Flow
(Even Number Of Tube Passes)**

The slave segment for **cross-flow** (with both fluids unmixed) is on side 2 of card 2.



**Figure 4 Cross Flow
(Both Fluids Unmixed)**

Equations:

Heat exchanger effectiveness E is the ratio of actual heat transfer to maximum possible heat transfer.

$$E = \frac{q}{C_{\min} (T_{\text{hin}} - T_{\text{cin}})} = \frac{C_h (T_{\text{hin}} - T_{\text{ho}})}{C_{\min} (T_{\text{hin}} - T_{\text{cin}})} = \frac{C_c (T_{\text{co}} - T_{\text{cin}})}{C_{\min} (T_{\text{hin}} - T_{\text{cin}})}$$

where:

q is the actual heat transfer;

T_{hin} and T_{cin} are the inlet temperatures of the hot and cold fluids, respectively;

T_{ho} and T_{co} are the outlet temperatures of the hot and cold fluids, respectively;

C_h and C_c are the heat capacities of the hot and cold fluids, respectively, e.g., $C_h = m_h \times c_{ph}$, where m_h is the flow rate and c_{ph} is the specific heat capacity of the hot fluid;

C_{min} and C_{max} (which are used later) are the smaller and larger values of C_h and C_c .

Effectiveness can be related to the product of the surface area of an exchanger and the overall transfer coefficient for specific geometries. This product is designated AU. The geometries considered in this pac have the following correlations:

Counter-Flow (See figure 1)

$$E = \frac{1 - e^{-\frac{AU}{C_{min}} \left(1 - \frac{C_{min}}{C_{max}}\right)}}{1 - (C_{min}/C_{max}) e^{-\frac{AU}{C_{min}} \left(1 - \frac{C_{min}}{C_{max}}\right)}}$$

For $C_{min}/C_{max} = 1$

$$E = \frac{AU/C_{min}}{1 + AU/C_{min}}$$

Parallel-Flow (See figure 2)

$$E = \frac{1 - e^{-\frac{AU}{C_{min}} (1 + C_{min}/C_{max})}}{1 + C_{min}/C_{max}}$$

For $C_{min}/C_{max} = 0$, C_{min} is set to 1.

Parallel-Counter-Flow; Shell Mixed with an Even Number of Tube Passes (See figure 3)

$$E = \frac{2}{\left(1 + \frac{C_{min}}{C_{max}}\right) + \sqrt{1 + \left(\frac{C_{min}}{C_{max}}\right)^2} \left[\frac{1 + e^{-x}}{1 - e^{-x}}\right]}$$

where:

$$x = \frac{AU}{C_{min}} \sqrt{1 + \left(\frac{C_{min}}{C_{max}}\right)^2}$$

Cross-Flow; Both Fluids Unmixed (See figure 4)

No exact expression exists for this case, but the following is a very good approximation. Note that it cannot be stated explicitly in terms of AU and thus requires an iterative solution.

$$E = 1 - e \left(e^{\left(-\frac{AU}{C_{\min}} \frac{C_{\min}}{C_{\max}} y \right)} - 1 \right) \left(\frac{C_{\max}}{C_{\min}} \frac{1}{y} \right)$$

where:

$$y = \left[\frac{C_{\min}}{AU} \right]^{0.22}$$

References:

W.M. Kays and A.L. London, *Compact Heat Exchangers*, National Press, 1955.

Eckert and Drake, *Heat and Mass Transfer*, McGraw-Hill.

Remarks:

Registers R_{S0} - R_{S9} , R_C , R_E , and R_I are available for user storage.

Solution for AU, using the cross-flow slave card takes significantly longer than other solutions because of the iterative technique required.

You should always solve for all values (AU, q, T_{co} , T_{ho} and E). It is quite possible for the heat balance equations to yield meaningless solutions for a particular type of heat exchange. By calculating all results, you are assured that the configuration being used is capable of the performance specified. An error message during calculation of AU or q usually indicates a violation of the second law of thermodynamics.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 of card 1.			
2	Select proper configuration			
	card and side, and load:			
	a. Parallel or counter-flow			
	exchangers → card 1,			
	side 2.			
	b. Parallel-counter-flow			
	(even number of tube			
	passes) → card 2, side 1.			
	c. Cross-flow (both fluids			
	unmixed → card 2, side 2.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
3	If display says "Crd" press CLX .		CLX	0.00
4	If you loaded parallel/			
	counter-flow configurations in			
	step 2, select counter flow			
	(1) or parallel-flow (0) using			
	mode toggle.		f E	1.00/0.00
5	Input the following values			
	Cold fluid inlet temperature	T_{cin}	f A	T_{cin}
	Cold fluid density flow rate	\dot{m}_c	ENTER	m_c
	<i>then</i>			
	Cold fluid heat capacity	c_{pc}	f B	C_c
	<i>and</i>			
	Hot fluid inlet temperature	T_{hin}	f C	T_{hin}
	Hot fluid density flow rate	\dot{m}_h	ENTER	m_h
	<i>then</i>			
	Hot fluid heat capacity	c_{ph}	f D	C_h
6	If the remaining known is			
	effectiveness, go to step 7.			
	If area-conductance product,			
	go to step 8. If heat transfer,			
	go to step 9. If cold fluid outlet			
	temperature, go to step 10.			
	If hot fluid outlet temperature,			
	go to step 11.			
7	With effectiveness displayed,			
	calculate area-conductance			
	product.	E	A	AU
8	With area-conductance			
	product displayed, calculate			
	heat transfer.	AU	B	q

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
9	With heat transfer displayed,			
	calculate cold fluid outlet			
	temperature.	q	C	T_{co}
10	With cold fluid outlet			
	temperature displayed,			
	calculate hot fluid outlet			
	temperature.	T_{co}	D	T_{ho}
11	With hot fluid outlet tempera-			
	ture displayed, calculate			
	effectiveness.	T_{ho}	E	E
12	Go back to step 6 and com-			
	plete calculation of all outputs.			
13	For a new configuration, go to			
	step 2. It is not necessary to			
	repeat the input process if			
	values remain unchanged.			
14	For new input values, go to			
	step 5 and change appropriate			
	variables.			

Example 1:

Water ($c_p = 1 \text{ Btu/lb-}^\circ\text{F}$) is used to cool an oil ($c_p = .53 \text{ Btu/lb-}^\circ\text{F}$) from 200°F to 110°F . The water flow rate is 20,000 pounds per hour while the oil flows at 37,000 pounds per hour. If the water inlet temperature is 55°F and U is $25 \text{ Btu/ft}^2\text{-hr-}^\circ\text{F}$ for the heat exchangers being considered, what are the area requirements for counter-flow, parallel-flow, parallel-counter-flow and cross-flow?

Knowns:

$$\begin{aligned}
 c_{pc} &= 1.0 \text{ Btu/lb-}^\circ\text{F} \\
 \dot{m}_c &= 20,000 \text{ lb/hr} \\
 c_{ph} &= 0.53 \text{ Btu/lb-}^\circ\text{F} \\
 \dot{m}_h &= 37,000 \text{ lb/hr} \\
 T_{cin} &= 55^\circ\text{F}
 \end{aligned}$$

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$T_{hin} = 200^{\circ}\text{F}$
 $T_{ho} = 110^{\circ}\text{F}$
 $U = 25 \text{ Btu/ft}^2\text{-hr-}^{\circ}\text{F}$

Keystrokes:

Load side 1 and side 2 of card 1 and select counter-flow mode.

55 **f** **A** 20000 **ENTER** 1

f **B** 200 **f** **C** 37000 **ENTER**

.53 **f** **D** **f** **E** \longrightarrow

110 **E** \longrightarrow

Since effectiveness is the same for all configurations, store it for later use.

STO **I** \longrightarrow

Calculate AU.

A \longrightarrow

25 **\div** \longrightarrow

Switch to parallel configuration.

f **E** \longrightarrow

RCL **I** \longrightarrow

A \longrightarrow

CLX \longrightarrow

Load parallel-counter flow configuration on side 1 of card 2 and clear display of “Crd.”

CLX \longrightarrow

RCL **I** **A** \longrightarrow

CLX \longrightarrow

Load cross-flow configuration on side 2 of card 2 and clear display of “Crd”.

CLX **RCL** **I** **A** \longrightarrow

25 **\div** \longrightarrow

(Do not alter storage registers if you intend to continue with example 2.)

Outputs:

1.00 (Counter-flow mode on)

0.62 (Effectiveness)

0.62

31587.76 (AU)

1263.51 (ft²)

0.00 (parallel selected)

0.62

Error (Violation of second law)

-0.23

-0.23

Error (Violation of second law)

-0.06

39383.22 (AU)

1575.33 (ft²)

Example 2:

If a counter flow exchanger with an area of 1000 ft² and an overall heat transfer coefficient of 27 Btu/ft²·hr·°F is available, how close will the outlet temperature of the oil be to 110°F? What will the total heat transfer and outlet water temperature be? All unspecified values remain the same as example 1.

Keystrokes:

Outputs:

Load counter-flow routine on side 2 of card 1 and select counter flow mode.

CL x f E →	1.00	
Calculate AU product and calculate q.		
27 ENTER 1000 x →	27000.00	(AU)
B →	1656452.69	(q, Btu/hr)
C →	137.82	(T _{co})
D →	115.53	(T _{ho})
E →	0.58	(E)

Notes

PROGRAM LISTINGS

The following listings are included for your reference. A table of keycodes and keystrokes corresponding to the symbols used in the listings can be found in Appendix E of your Owner's Handbook.

Program	Page
1. Vector Statics	L01-01
2. Section Properties	L02-01
Card 1	
Card 2	
3. Stress on an Element	L03-01
4. Soderberg's Equation for Fatigue	L04-01
5. Cantilever Beams	L05-01
6. Simply Supported Beams	L06-01
7. Beams Fixed at Both Ends	L07-01
8. Propped Cantilever Beams	L08-01
9. Helical Spring Design	L09-01
10. Four Bar Function Generator	L10-01
Card 1	
Card 2	
11. Progression of Four-Bar System	L11-01
12. Progression of Slider Crank	L12-01
13. Circular Cams	L13-01
14. Linear Cams	L14-01
15. Gear Forces	L15-01
16. Standard External Involute Spur Gears	L16-01
17. Belt Length	L17-01
18. Free Vibrations	L18-01
19. Vibration Forced by $F_0 \cos \omega t$	L19-01
20. Equations of State	L20-01
21. Isentropic Flow for Ideal Gases	L21-01
22. Conduit Flow	L22-01
23. Heat Exchangers	L23-01
Card 1	
Card 2	

VECTOR STATICS

TITLE _____

001	#LELA	Convert from polar to	058	RCLB					
002	XZY	rectangular.	059	RCLD					
003	+P		060	x					
004	XZY		061	+					
005	#LBLA	Store x, y components of	062	STOE					
006	STOE	\vec{V}_1 .	063	PRTX					
007	XZY		064	RTN					
008	STOA		065	RCLC					
009	XZY		066	RCLA					
010	RTN		067	RCLB					
011	#LBLB	Convert from polar to	068	+P					
012	XZY	rectangular.	069	XZY		Calculate angle between			
013	+R		070	CLX		vectors.			
014	XZY		071	RCLC					
015	#LBLB		072	RCLD					
016	STOD	Store x, y components of	073	+P					
017	XZY	\vec{V}_2 .	074	XZY					
018	STOC		075	R4					
019	XZY		076	x					
020	RTN		077	÷					
021	#LBLD		078	COS←					
022	XZY	Store F cos φ and F sin φ.	079	RCLC					
023	+R		080	XZY					
024	STOE		081	PRTX					
025	XZY		082	RTN					
026	STOS		083	#LBLC					
027	RTN		084	SPC					
028	#LBLC		085	RCLB					
029	SPC	$\vec{V}_1 + \vec{V}_2$	086	RCLA		Calculate R_1 .			
030	RCLD		087	+P					
031	RCLB		088	CLX					
032	+		089	1					
033	RCLA		090	+R					
034	RCLC		091	STOA					
035	+		092	XZY					
036	+P		093	STOS					
037	PRTX		094	RCLD					
038	XZY		095	RCLC					
039	PRTX		096	+P					
040	RTN		097	CLX					
041	#LBLC		098	1					
042	SPC	$\vec{V}_1 \times \vec{V}_2$	099	+R					
043	RCLA		100	STOE					
044	RCLD		101	XZY					
045	x		102	STO7					
046	RCLC		103	R↑					
047	RCLB		104	x					
048	x		105	R4					
049	-		106	x					
050	PRTX		107	R↑					
051	RTN		108	-					
052	#LBLE		109	STOE					
053	SPC	$\vec{V}_1 \cdot \vec{V}_2$	110	RCL8					
054	RCLA		111	RCL7					
055	RCLC		112	x					
056	x			RCL9					
REGISTERS									
0	1	2	3	4 cos θ ₁	5 sin θ ₁	6 cos θ ₂	7 sin θ ₂	8 F cos φ	9 F sin φ
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	x ₁	B	Y ₁	C	x ₂	D	Y ₂	E	used

SECTION PROPERTIES

TITLE _____

001 #LBLA	Clear registers.	057 ST-1	Sum ΔI_{xy} .
002 CLRG		058 RCLC	
003 RTN		059 RCLB	
004 #LBLA	Store coordinates.	060 x	
005 STOD		061 RCLA	
006 P†		062 RCLD	
007 STOA		063 x	
008 R†		064 -	
009 STOE		065 ENT†	
010 P†		066 ENT†	
011 STOC	Sum ΔA .	067 4	
012 RCLA		068 ÷	
013 +		069 RCLB	
014 STOE		070 x	
015 RCLD		071 RCLA	
016 RCLC		072 RCLC	
017 -		073 x	
018 STO7		074 RCLC	
019 x		075 X²	
020 2		076 STOS	
021 ÷		077 +	
022 ST-0	Sum ΔI_y .	078 RCLA	
023 1		079 X²	
024 2		080 ST+S	
025 ÷		081 +	
026 RCLC		082 RCL7	
027 RCLA		083 x	
028 -		084 3	
029 STOE		085 ÷	
030 X²		086 +	
031 RCLB		087 x	
032 GSB4	Sum ΔI_x .	088 RCLB	
033 ST-4		089 8	
034 RCLB		090 ÷	
035 RCLB		091 RCLB	
036 RCLD		092 x	
037 +		093 RCL7	
038 STOS		094 X²	
039 x		095 x	
040 2		096 +	
041 4		097 RCL6	
042 ÷		098 X≠0?	
043 RCLB		099 ÷	
044 X²		100 ST+S	
045 RCL7		101 RCLC	Recall x_i and y_i for next segment.
046 GSB4	Sum ΔM_x .	102 RCLD	
047 ST+3		103 RTN	
048 RCL6		104 #LBL1	Calculate ΔM_x and ΔM_y .
049 RCLB		105 X²	
050 RCL7		106 3	
051 GSB1		107 ÷	
052 ST+2	Sum ΔM_y .	108 X≠Y	
053 RCL7		109 GSB4	
054 RCLB		110 8	
055 RCL6		111 ÷	
056 GSB1		112 RTN	

REGISTERS									
0 ΣA	1 ΣM_y	2 ΣM_x	3 ΣI_x	4 ΣI_y	5 ΣI_{xy}	6 $(x_{i+1} - x_i)$	7 $(y_{i+1} - y_i)$	8 $(x_{i+1} + x_i)$	9 $(y_{i+1} + y_i)$
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A x_i	B y_i	C x_{i+1}	D y_{i+1}	E	F	G	H	I	J

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113	#LBL4	Calculation subroutine. ----- Add to sums for circular regions.		
114	X ²			
115	+			
116	X			
117	RTN			
118	#LBLC			
119	ENT↑			
120	ABS			
121	X			
122	P↑			
123	X			
124	4			
125	÷			
126	STOA			
127	ST+0			
128	ENT↑			
129	ABS			
130	X			
131	P↑			
132	÷			
133	4			
134	÷			
135	STOB			
136	R↓			
137	STOC			
138	R↓			
139	STOD			
140	R↑			
141	X			
142	RCLA			
143	X			
144	ST+5			
145	RCLB			
146	RCLA			
147	RCLC			
148	X ²			
149	X			
150	+			
151	ST+3			
152	RCLB			
153	RCLA			
154	RCLD			
155	X ²			
156	X			
157	+			
158	ST+4			
159	RCLA			
160	RCLD			
161	X			
162	ST+1			
163	RCLA			
164	RCLC			
165	X			
166	ST+2			
167	CLN			
168	RTN			

LABELS					FLAGS	SET STATUS			
A _{x+1} ↑ y ₊₁	B	C x ↑ y ↑ ± d	D	E	0	FLAGS		TRIG	DISP
a	b	c	d	e	1	ON OFF			
0	1 Calculate	2	3	4 Calculate	2	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>	
						1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>	
						2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>	
5	6	7	8	9	3	3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>2</u>	

(Card 2)

TITLE _____

001 *LELA	Output \bar{x} , \bar{y} and A.	057 RCLA	
002 GSB2		058 X ²	
003 PPTX		059 RCLB	
004 X ² Y		060 X	
005 PRTX		061 CHS	
006 RCL0		062 RCLZ	
007 PPTX		063 +	
008 RTN		064 STOC	
009 *LBL3		065 -	
010 SPC	Calculate \bar{x} and \bar{y} .	066 X ² B ⁰	
011 RCL2		067 ÷	
012 RCL0		068 TAN ⁻¹	
013 +		069 RTN	
014 STOA		070 *LBLD	
015 RCL1		071 GSB3	Calculate $I\bar{x}$, $I\bar{y}$, $I\bar{x}\bar{y}$ and output ϕ .
016 RCL0		072 STOI	
017 +		073 2	
018 STOB		074 +	
019 RTN		075 PRTX	
020 *LBL6	Output Ix , Iy and Ixy .	076 *LBLC	
021 SPC		077 1	
022 RCL3		078 +R	
023 PPTX		079 X ²	
024 RCL4		080 STOA	
025 PRTX		081 RCLC	
026 RCL5		082 X	
027 PPTX		083 X ² Y	
028 RTN		084 X ²	
029 *LBLC		085 STOB	
030 GSB2	Calculate $I\bar{x}$, $I\bar{y}$ and $I\bar{x}\bar{y}$ and ϕ .	086 RCLD	
031 RCLC		087 X	
032 PPTX		088 +	
033 RCLD		089 RCL1	
034 PRTX		090 SIN	
035 RCLC		091 RCLC	
036 PPTX		092 X	
037 RTN		093 -	
038 *LBL3		094 PRTX	
039 GSB2		095 LSTX	
040 RCL5		096 RCLH	
041 RCL0		097 RCLD	
042 RCLA		098 X	
043 RCLB		099 +	
044 X		100 RCLB	
045 X		101 RCLC	
046 -		102 X	
047 STOE		103 +	
048 ENT?		104 PRTX	
049 +		105 RTN	
050 RCL4		106 *LBLD	
051 RCLB		107 ENT?	
052 X ²		108 +	
053 RCL0		109 STOI	
054 X		110 FJ	
055 -		111 STOC	
056 STOC		112 FJ	

REGISTERS								
0 ΣA	1 ΣM_y	2 ΣM_x	3 ΣI_x	4 ΣI_y	5 ΣI_{xy}	6 $(x_{i+1} - x_i)$	7 $(y_{i+1} - y_i)$	8 $(x_{i+1} + x_i)$
S0	S1	S2	S3	S4	S5	S6	S7	S8
A $x_i, \bar{y}, \cos^2 \phi$	B $y_i, \bar{x}, \sin^2 \phi$	C $x_{i+1}, I\bar{y}$	D $y_{i+1}, I\bar{x}$	E $I\bar{x}\bar{y}$	F 2ϕ			

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113	STOD	169	RCLI
114	GSBE	170	SIN
115	x	171	x
116	RCL0	172	RCLC
117	x	173	RCLI
118	CHS	174	COS
119	RCL5	175	x
120	+	176	+
121	RCLD	177	PRTX
122	RCLC	178	RTN
123	-		
124	RCLC		
125	RCLA		
126	-		
127	x		
128	RCL0		
129	x		
130	+		
131	STOE		
132	RCLC		
133	X²		
134	RCLC		
135	RCLA		
136	x		
137	2		
138	x		
139	-		
140	RCL0		
141	x		
142	RCL3		
143	+		
144	STOC		
145	RCLC		
146	X²		
147	RCLD		
148	RCLC		
149	x		
150	2		
151	x		
152	-		
153	RCL0		
154	x		
155	RCL4		
156	+		
157	STOD		
158	RCLI		
159	2		
160	÷		
161	GSBE		
162	+		
163	PRTX		
164	RCLC		
165	RCLD		
166	-		
167	2		
168	÷		

LABELS					FLAGS	SET STATUS		
A →x, y, φ	B →Ix,Iy,Ixy	C →I \bar{x} ,I \bar{y} ,I $\bar{x}\bar{y}$	D →I \bar{x} φ,I \bar{y} φ,I $\bar{x}\bar{y}$ φ	E	0	FLAGS	TRIG	DISP
a	b	c	d →Ix',Iy',Ixy'	e	1	ON OFF 0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
0	1 tan ⁻¹	2 \bar{x}, \bar{y}	3 Ix,Iy,Ixy	4	2	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5	6 Rotate	7	8	9	3	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>2</u>

STRESS ON AN ELEMENT

TITLE _____

001 *LBLA	Store code:	057 ST÷6	-----
002 1	1 = rectangular	058 GSB5	Calculate τ_{\max} and
003 GT00	2 = equiangular	059 RCL5	
004 *LBL6		060 RCL9	$\frac{s_1 + s_2}{2}$ from strains.
005 2		061 1	
006 *LBL0		062 +	
007 ST01	-----	063 ÷	
008 RTN	Store ν and E.	064 ST×5	
009 *LBL4		065 RCL5	
010 ST09		066 1	
011 R4		067 RCL9	
012 ST0E	-----	068 -	
013 RTN	Store ϵ_a , ϵ_b and ϵ_c .	069 ÷	
014 *LBLA		070 ST×6	
015 ST0C		071 RCLC	
016 R4		072 RCL5	
017 ST0B		073 -	
018 R4	-----	074 3	
019 ST0A	Calculate ϵ_1 and ϵ_2 .	075 JX	
020 RTN		076 GT01	
021 *LBLB		077 *LBL1	
022 RCLA		078 2	
023 GT01		079 RCL5	
024 *LBL2		080 x	
025 RCLB		081 RCLA	
026 +		082 -	
027 *LBL1		083 RCLC	
028 RCLC		084 -	
029 +		085 RCLA	
030 ST0E		086 RCLC	
031 0		087 GT04	
032 GT01		088 *LBL2	
033 *LBLC		089 x	
034 RCLC		090 2	
035 RCLA		091 RCLA	
036 -		092 x	
037 *LBL1		093 RCL5	
038 RCL5		094 -	
039 RCLC		095 RCLC	
040 -		096 *LBL4	-----
041 +F		097 -	Output θ .
042 RCLA		098 GSB6	
043 RCLB		099 R4	
044 -		100 PRTX	
045 +P		101 RTN	
046 2		102 *LBLC	-----
047 JX		103 R1	Calculate τ_{\max} and
048 x		104 R1	$(s_1 + s_2)/2$ from s_x , s_y
049 ST05		105 ST03	and τ_{xy} .
050 2		106 ST06	
051 GT01		107 R1	
052 *LBL2		108 ST×6	
053 1		109 -	
054 +		110 ST04	
055 *LBL1		111 2	
056 ST÷5		112 ST÷6	

REGISTERS									
0	1	2 20	3 s_x	4 $s_x - s_y$	5 τ_{\max}	6 $(s_1 + s_2)/2$	7	8	9 ν
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A ϵ_a	B ϵ_b	C ϵ_c	D	E E	I Control				

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<pre> 113 ÷ 114 RT 115 STO2 116 ST+2 117 +P 118 ST05 119 RCL2 120 CHS 121 RCL4 122 #LBL6 123 %θ? 124 ÷ 125 TAN⁻¹ 126 STO2 127 2 128 + 129 0 130 RTN 131 #LBLD 132 GSB5 133 RCL5 134 PRTX 135 RCL2 136 2 137 ÷ 138 PRTX 139 RTN 140 #LBL5 141 SPC 142 ENT↑ 143 + 144 RCL2 145 - 146 RCL5 147 +R 148 RCL5 149 + 150 PRTX 151 %ZY 152 PRTX 153 PTN 154 #LBL5 155 SPC 156 RCL6 157 RCL5 158 + 159 PRTX 160 RCL5 161 RCL5 162 - 163 PRTX 164 RTN </pre>	<p>-----</p> <p>Calculate θ and 2θ.</p> <p>-----</p> <p>Output s_1, s_2 and τ_{\max} and θ.</p> <p>-----</p> <p>Calculate s and t from θ'.</p> <p>-----</p> <p>Calculate ϵ_1 and ϵ_2 or s_1 and s_2.</p> <p>-----</p>		
LABELS			
A $\epsilon_a \uparrow b \uparrow \epsilon_c$	B $\rightarrow \epsilon_1, \epsilon_2, \theta$	C $s_x \uparrow s_y \uparrow \tau_{xy}$	D $\rightarrow s_1, s_2, \tau_{\max}, \theta$
a Rectangular	b Equiangular	c	d $E \uparrow \nu$
0 Store code	1 Rectangular	2 Equiangular	3 Output
5 Calc	6 θ	7	8
FLAGS			
0			
1			
2			
3			
SET STATUS			
ON OFF			
0 <input type="checkbox"/> <input checked="" type="checkbox"/>			
1 <input type="checkbox"/> <input checked="" type="checkbox"/>			
2 <input type="checkbox"/> <input checked="" type="checkbox"/>			
3 <input type="checkbox"/> <input checked="" type="checkbox"/>			
DEG <input checked="" type="checkbox"/>		FIX <input type="checkbox"/>	
GRAD <input type="checkbox"/>		SCI <input type="checkbox"/>	
RAD <input type="checkbox"/>		ENG <input checked="" type="checkbox"/>	
		n <u>3</u>	

SODERBERG'S EQUATION FOR FATIGUE

TIT L E

001	*LBLA					057	*LBLB				
002	STO8					058	STOE				
003	F3?					059	F3?				
004	RTN					060	RTN				
005	GSE1					061	RCL8				
006	GSE2					062	RCL6				
007	RCLB					063	÷				
008	x					064	GSE1				
009	RCL5					065	-				
010	÷					066	GSE2				
011	CHS					067	RCL8				
012	RCL6					068	x				
013	1/X					069	RCL9				
014	+					070	÷				
015	÷					071	÷				
016	STO8					072	STOE				
017	RTN					073	RTN				
018	*LBLC					074	*LBLC				
019	STO9					075	STOC				
020	F3?					076	F3?				
021	RTN					077	RTN				
022	GSE2					078	RCLA				
023	RCL8					079	ENT?				
024	x					080	+				
025	RCLB					081	RCL8				
026	x					082	x				
027	GSE1					083	RCL6				
028	CHS					084	÷				
029	RCL8					085	RCL6				
030	RCL6					086	RCL8				
031	÷					087	x				
032	+					088	RCL9				
033	÷					089	÷				
034	STO9					090	!				
035	RTN					091	-				
036	*LBLA					092	RCLD				
037	STO4					093	x				
038	F3?					094	+				
039	RTN					095	RCL6				
040	!					096	RCL8				
041	STO4					097	x				
042	GSE1					098	RCL9				
043	GSE2					099	÷				
044	RCLB					100	!				
045	x					101	+				
046	RCL8					102	÷				
047	x					103	STOC				
048	RCL9					104	RTN				
049	÷					105	*LBLD				
050	+					106	STOD				
051	RCL8					107	F3?				
052	÷					108	RTN				
053	RCL6					109	RCLA				
054	x					110	ENT?				
055	STO4					111	+				
056	RTN					112	RCL8				

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113 x 114 RCL E 115 ÷ 116 RCL B 117 RCL 8 118 x 119 RCL 9 120 ÷ 121 1 122 + 123 RCL C 124 x 125 - 126 1 127 RCL B 128 RCL 8 129 x 130 RCL 9 131 ÷ 132 - 133 ÷ 134 STOE 135 RTN 136 #LBL E 137 STOE 138 F?? 139 RTN 140 GSB1 141 GSB2 142 RCL B 143 x 144 RCL 8 145 x 146 RCL 9 147 ÷ 148 + 149 RCL 8 150 ÷ 151 1/X 152 STOE 153 RTN 154 #LBL C 155 SPC 156 RCL 8 157 PRTX 158 RCL 9 159 PRTX 160 RCL A 161 PRTX 162 RCL B 163 PRTX 164 RCL C 165 PRTX 166 RCL D 167 PRTX 168 RCL E	169 PRTX 170 RTN 171 #LBL 2 172 RCL C 173 RCL D 174 CHS 175 GT00 176 #LBL 1 177 RCL C 178 RCL D 179 #LBL 0 180 + 181 RCL A 182 ÷ 183 2 184 ÷ 185 RTN	<div style="border-bottom: 1px dashed black; padding-bottom: 5px;"> Q = (P_{max} - P_{min}) </div> <div style="border-bottom: 1px dashed black; padding-bottom: 5px;"> Q = (P_{max} + P_{min}) </div> <div style="border-bottom: 1px dashed black; padding-bottom: 5px;"> Q/2A </div>
<div style="border-bottom: 1px dashed black; padding-bottom: 5px;">Store or calculate FS.</div>		
<div style="border-bottom: 1px dashed black; padding-bottom: 5px;">Output values.</div>		

LABELS					FLAGS	SET STATUS		
A	K	P _{max}	P _{min}	FS	0	FLAGS	TRIG	DISP
a _{typ}	b _{se}	c PRINT	d	e	1	ON OFF 0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input type="checkbox"/>
0+, A, ÷, 2, ÷	1 Save	2 S _r	3	4	2	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5	6	7	8	9	3 Calc	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>

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113	RCL3				169	X ²	
114	x				170	2	
115	RCL1				171	÷	
116	x				172	+	
117	RCLB				173	RCL4	
118	GSB4				174	x	
119	R4				175	-	M ₁ + M ₂
120	RCL1				176	RCLC	
121	6				177	GSB4	
122	÷				178	CLX	M ₃
123	RCLB				179	RCL5	
124	2				180	X ² Y	
125	÷				181	F2?	
126	-				182	+	
127	RCL1				183	RTN	M ₁ + M ₂ + M ₃
128	x				184	*LBLD	
129	RCLB				185	STD0	
130	X ²				186	RCL4	V ₁
131	2				187	GSB4	
132	÷				188	0	
133	+				189	F2?	
134	RCL4				190	RCL3	
135	x				191	RCLB	
136	RCL1				192	GSB4	
137	x				193	CLX	
138	-				194	RCL1	
139	RCLC				195	RCLB	V ₂
140	GSB4				196	-	
141	R4				197	RCL4	
142	RCL5				198	x	
143	RCL1				199	-	
144	x				200	RTN	V
145	+				201	*LBL4	
146	RCLC				202	CF2	
147	÷				203	RCL0	Select smaller of x and a (or b or c) and store as x'.
148	RTN				204	STD1	
149	*LBLC				205	X ² Y	
150	STD0				206	X ² Y?	
151	RCL4				207	STD1	
152	GSB4				208	X ² Y?	
153	RCL1				209	SF2	If x > a set flag.
154	RCL4				210	-	
155	-				211	RTN	
156	RCL3						
157	x						
158	RCLB						
159	GSB4						
160	CLX						
161	RCL1						
162	2						
163	÷						
164	RCLB						
165	-						
166	RCL1						
167	x						
168	RCLB						

LABELS					FLAGS	SET STATUS			
A	x→y	B	x→θ	C	x→M _x	D	x→V	E	
a	Start	b	11E1V	c	a1P	d	b1W	e	c1M
0	1	2	3	4	Store x'	2			
5	6	7	8	9		3			

FLAGS	ON	OFF	TRIG	DISP
0	<input type="checkbox"/>	<input type="checkbox"/>	DEG <input type="checkbox"/>	FIX <input type="checkbox"/>
1	<input type="checkbox"/>	<input type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2	<input type="checkbox"/>	<input type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3	<input type="checkbox"/>	<input type="checkbox"/>		n <u> 3 </u>

SIMPLY SUPPORTED BEAMS

TITLE

[illegible]

DATE _____ AUTHOR _____

113	RTN	-----	169	+	-----
114	*LBL0	Set derivative flag.	170	STO1	-----
115	SF0	-----	171	RCL0	Store x and c.
116	GTO0	-----	172	STO1	-----
117	*LBL0	Clear derivative flag.	173	RCL0	-----
118	CF0	-----	174	STO0	-----
119	*LBL0	-----	175	X>Y?	If c > x GTO 0.
120	STO0	Compute M _{x2}	176	GTO0	-----
121	2	or V ₂	177	RCL0	Otherwise store x - ℓ
122	÷	-----	178	RCL2	for x and ℓ - c for c.
123	RCL2	-----	179	-	-----
124	F0?	-----	180	STO1	-----
125	2	-----	181	RCL2	-----
126	F0?	-----	182	RCL0	-----
127	÷	-----	183	-	-----
128	RCL0	-----	184	STO0	-----
129	-	-----	185	*LBL0	M
130	RCL4	-----	186	RCL5	ℓ
131	x	-----	187	RCL2	-----
132	x	-----	188	÷	-----
133	F0?	-----	189	F0?	-----
134	LSTX	-----	190	RTN	-----
135	GSF1	M _{x1} or V ₁	191	RCL1	M _x
136	GSF2	M _{x3} or V ₃	192	x	ℓ
137	RCL1	M = M _{x1} + M _{x2} + M _{x3}	193	RTN	-----
138	+	or			-----
139	RTN	V = V ₁ + V ₂ + V ₃			-----
140	*LBL1	-----			-----
141	STO1	Store first results.			-----
142	RCL2	Store ℓ - a			-----
143	RCL4	and			-----
144	-	x			-----
145	STO0	-----			-----
146	RCL0	-----			-----
147	STO1	If a > x GTO 0			-----
148	RCL4	-----			-----
149	X>Y?	-----			-----
150	GTO0	-----			-----
151	RCL4	Otherwise store -a for ℓ - a			-----
152	CHS	and x - ℓ for x.			-----
153	STO0	-----			-----
154	RCL2	-----			-----
155	ST-1	-----			-----
156	*LBL0	-----			-----
157	RCL3	$\frac{P(\ell - a)}{\ell}$			-----
158	RCL0	-----			-----
159	x	-----			-----
160	RCL2	-----			-----
161	÷	-----			-----
162	F0?	-----			-----
163	RTN	$\frac{P(\ell - a)x}{\ell}$			-----
164	RCL1	-----			-----
165	x	-----			-----
166	RTN	-----			-----
167	*LBL2	Add first result to second.			-----
168	RCL1	-----			-----

LABELS					FLAGS	SET STATUS		
A x→y	B x→θ	C x→M _x	D x→V	E RCL x	0 Derivative	FLAGS	TRIG	DISP
a Start	b ITETx	c a↑P	d W	e c↑M	1	ON OFF	DEG <input checked="" type="checkbox"/>	FIX <input type="checkbox"/>
0 Used	1 Con	2 Mom	3	4	2	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5	6	7	8	9	3	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>

BEAMS FIXED AT BOTH ENDS

TITLE _____

001 *LBLd	Store W.	057 x							
002 STG4		058 3							
003 RTN		059 X*Y							
004 *LBLk	Store l and EI.	060 x							
005 STG3		061 F0?							
006 F4		062 LSTX							
007 x		063 F0?							
008 STOE		064 -							
009 RTN		065 -							
010 *LBLc	Store P and a.	066 GSE6							
011 STG3		067 e							
012 X*Y		068 ÷							
013 STG4		069 F0?							
014 RTN		070 3							
015 *LBLe	Store M and c.	071 F0?							
016 STG5		072 x							
017 X*Y		073 F0?							
018 STG0		074 GSE3							
019 RTN		075 GSE4							
020 *LBLB	Set derivative flag and start	076 RCLC							
021 SF0	θ_2 calculation.	077 GSE1							
022 STG0		078 F0?							
023 GSE7		079 3							
024 RCL2		080 F0?							
025 3		081 x							
026 x		082 X*Y							
027 RCL0		083 F0?							
028 GSE7		084 GSE7							
029 GT00		085 +							
030 *LBLA	Clear derivative flag and	086 GSE6							
031 CF0	start y_2 calculation.	087 GSE8							
032 STG0		088 RCLC							
033 X²		089 ÷							
034 RCL2		090 RTN							
035 GSE7		091 *LBLD							
036 RCL0		092 SF0							
037 *LBL0		093 STG0							
038 SF1		094 RCL2							
039 -	Complete calculation of θ_2	095 X*Y							
040 RCL0	EI or y_2 EI.	096 GSE7							
041 x		097 GT00							
042 RCL2		098 *LBLC							
043 X²		099 CF0							
044 -		100 STG0							
045 x		101 RCL2							
046 2		102 X*Y							
047 4		103 -							
048 ÷		104 RCL6							
049 RCL4		105 x							
050 x		106 RCL2							
051 RCL4	Calculate y_1 EI or θ_1 EI.	107 X²							
052 GSE1		108 6							
053 RCL1		109 ÷							
054 x		110 *LBL0							
055 RCLD		111 SF1							
056 RCL2		112 -							
REGISTERS									
0 x	1 $x, (l - x)$	2 l	3 P	4 W	5 M	6	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A a	B	C c	D $a, (l - a); c, (l - c)$	E EI	F	SUM			

DATE _____ AUTHOR _____

113	2			169	RCL2		
114	÷			170	RCL0		
115	RCL4			171	-		
116	x			172	STO1		
117	RCLA			173	*LBL0		
118	GSE1			174	RCL5		$P(\ell - a)^2$ or
119	F0?			175	F1?		ℓ^3
120	GTO0			176	RCL3		
121	RCL1	Calculate V_1		177	RCL2		
122	x	or M_1 .		178	RCLD		
123	RCLD			179	-		$M(\ell - a)$
124	RCL2			180	F1?		ℓ^3
125	x			181	X ²		
126	-			182	x		
127	*LBL0			183	RCL2		
128	x			184	3		
129	F0?			185	Y*		
130	GSE3			186	÷		
131	GSE4			187	RCL2		
132	RCLC			188	RCLD		
133	GSE1			189	F1?		
134	F0?	Calculate V_3		190	GTO0		$(\ell - 3a)\ell$
135	R4	or M_3 .		191	3		2
136	F0?			192	x		
137	CLX			193	-		
138	F0?			194	RCL2		
139	RCLD			195	x		
140	6			196	2		
141	x			197	÷		
142	X ² Y			198	RCLD		ax
143	GSE7			199	RCL1		
144	+			200	x		
145	x			201	RTN		
146	*LBL8			202	*LBL0		
147	F0?			203	GSE7		$(\ell + 2a)$
148	GTO4	Sign change?		204	+		
149	GSE3			205	CF1		
150	*LBL4			206	RTN		
151	RCL1			207	*LBL3		
152	+	Calculate sum.		208	F2?		Sign change.
153	RTN			209	CHS		
154	*LBL1			210	RTN		
155	CF2	Store a or c and sum.		211	*LBL6		Calculation subroutine.
156	STOD			212	x		
157	R4			213	RCL1		
158	STO1			214	*LBL5		
159	RCLD			215	X ²		
160	RCL0			216	F0?		
161	STO1			217	JX		
162	X ² Y?			218	x		
163	GTO0	Is x beyond loading point?		219	RTN		
164	SF2			220	*LBL7		
165	RCL2	Yes—set sign change flag		221	ENT1		2X subroutine
166	RCLD	and a = $\ell - a$ or c = $\ell - c$		222	+		
167	-	and x = $\ell - x$.		223	RTN		
168	STOD						

LABELS					FLAGS		SET STATUS		
A x→y	B x→θ	C x→M _x	D x→V	E	0 Derivative	FLAGS	TRIG	DISP	
a	b 11E1 ℓ	c a1P	d W	e c1M	1 P	ON OFF	DEG <input checked="" type="checkbox"/>	FIX <input type="checkbox"/>	
						0 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>	
0 Used	1 Calc.	2	3 Sign	4 sum	2 Sign	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>	
5 Calc.	6 Calc.	7 2x	8	9	3	3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>	

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113	GT00				169	RCL1	or	
114	*LBL6				170	RTN	$V = V_1 + V_2 + V_3$	
115	RCL0				171	*LBL4	Multiply by x if integral	
116	GSB4				172	F0?	flag is set.	
117	*LBL0				173	RCL0		
118	-				174	F0?		
119	GSB8				175	x		
120	RCL6				176	RTN	Finish V_2 , θ_2 , M_2 and	
121	\div				177	*LBL5	V_2 calculations.	
122	RTN				178	RCL4		
123	*LBL0				179	x		
124	CF0				180	GSB4		
125	ST00				181	ε		
126	2				182	\div		
127	x				183	ST01		
128	GT00				184	CF1	Store b.	
129	*LBL0				185	RCL2		
130	SF0				186	RCL4		
131	ST00				187	-		
132	*LBL0				188	ST01		
133	3				189	LST0		
134	RCL2				190	GT00		
135	x				191	*LBL1		
136	X \leftrightarrow Y				192	RCL0	Store c.	
137	4				193	ST01		
138	x				194	*LBL0		
139	-				195	CF2	Set $x \leq$ to a or c flag.	
140	GSB5				196	RCL0		
141	GSB4				197	X \leftrightarrow Y?		
142	F2?				198	SF2		
143	GT00				199	RCL1		
144	1				200	3	Calculate	
145	GSB4				201	x		
146	-				202	F1?	$\frac{3a^2 l - a^3}{2l^3}$	
147	F0?				203	RCL2		
148	RCL4				204	RCL2		
149	F0?				205	x	First pass, then	
150	+				206	RCL1		
151	*LBL0				207	X \leftrightarrow	$\frac{l^2 - c^2}{4l^3}$ on	
152	RCL3				208	-		
153	x				209	2		
154	ST+1				210	F1?		
155	GSB1				211	X \leftrightarrow	Second pass.	
156	ε				212	\div		
157	x				213	RCL2		
158	GSB4				214	3		
159	F2?				215	Y*		
160	GT00				216	\div		
161	F0?				217	F1?		
162	1				218	RTN		
163	F0?				219	SF1		
164	-				220	RCL1		
165	*LBL8				221	x		
166	RCL5				222	RTN		
167	x							
168	ST+1							

LABELS					FLAGS		SET STATUS		
A Start	B 11E1V	C a1P	D W	E c1M	0 Integral	1 Moment	FLAGS	TRIG	DISP
a x \rightarrow y	b x \rightarrow θ	c x \rightarrow M _x	d x \rightarrow V	e	2 x \leq d or c	3	ON OFF 0 <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	DEG <input type="checkbox"/>	FIX <input type="checkbox"/>
0 Used	1 P	2	3	4 x mult			1 <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5 W - P	6 Used	7	8 Mult & Sum	9			2 <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
							3 <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>		n <u>3</u>

DATE _____ AUTHOR _____

113 RTN		169 RCL0	
114 #LBL0	Ferrous/non-ferrous toggle.	170 X≠Y?	
115 F0?		171 GT04	
116 GT00		172 5	Spring is acceptable.
117 SF0		173 RTN	
118 0		174 #LBL4	Spring may be over-
119 RTN		175 RCL6	designed. Try smaller
120 #LBL0		176 4	wire.
121 1		177 RTN	
122 CF0		178 GT05	Smaller wire input.
123 RTN		179 #LBL2	
124 #LBLC		180 RCL8	Compute wire tensile
125 RCL4	If coil-to-coil clearance is	181 LN	strength from α and β.
126 RCL6	adequate, branch to label	182 RCL6	
127 -	zero.	183 x	
128 RCLD		184 RCL0	
129 RCL4		185 +	
130 -		186 ENT1	
131 .		187 ST01	
132 1		188 .	Convert to %max.
133 x		189 3	
134 X≠Y?		190 5	
135 GT00		191 ENT1	
136 GSB2	Check stress with in-	192 .	
137 R4	adequate clearance.	193 1	
138 RCL0		194 F0?	
139 X≠Y?		195 CLX	
140 GT03		196 +	
141 1	Change criteria.	197 x	
142 RTN		198 X≠Y	Convert to YS.
143 #LBL3		199 LSTX	
144 RCL8	Try smaller wire.	200 .	
145 2		201 2	
146 RTN		202 +	
147 ST08	Store smaller wire size and	203 x	
148 GT00	branch.	204 RTN	
149 #LBL0	Check stress with adequate	205 #LBL1	Compute Wahl factor.
150 GSB2	clearance.	206 ST00	
151 RCL0		207 4	
152 X≠Y?		208 x	
153 GT03		209 1	
154 RCL8	Try larger wire.	210 -	
155 3		211 ENT1	
156 RTN		212 ENT1	
157 #LBL5	Store larger wire size and	213 3	
158 RCL8	branch.	214 -	
159 ST+6		215 ÷	
160 R4		216 .	
161 ST08		217 6	
162 ST-6		218 1	
163 GT00		219 5	
164 #LBL3	Check to see if spring is	220 RCL0	
165 RCL1	over-designed.	221 ÷	
166 .		222 +	
167 3		223 RTN	
168 x			

LABELS					FLAGS	SET STATUS		
A → N	B → s _s	C → code	D	E (→ L ₁ L ₂ D O D)	0 Ferrous?	FLAGS	TRIG	DISP
a Fe?	b Gtαβ	c Pt L ₁	d P ₂ ↑ L ₂ → k	e d f f ₀ ↑ D _H → S ₂	1	ON OFF	DEG <input checked="" type="checkbox"/>	FIX <input type="checkbox"/>
						0 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
0 Used	1 Wahl	2 TS	3 code 2,4,5	4 code 4	2	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>
5 Larger d	6	7	8	9	3	3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>

FOUR BAR FUNCTION GENERATOR

TITLE _____

001 *LBLA	Store d, c, b and a.	057 ST03	θ_1 and
002 ST04		058 R4	calculate θ_2 .
003 R4		059 ST01	
004 ST03		060 R1	
005 R4		061 -	
006 ST02		062 RCLA	
007 R4		063 RCLB	
008 ST01		064 -	
009 RTN		065 x	
010 *LBLB	Calculate R_1, R_2 and R_3 .	066 RCLC	
011 RCL1		067 RCLA	
012 RCL4		068 -	
013 ÷		069 ÷	
014 ST0A		070 RCL1	
015 RCL1		071 +	
016 RCL2		072 ST02	
017 ÷		073 F2S	
018 ST0E		074 RTN	
019 RCL1		075 *LBLA	Store ϕ_3 and ϕ_1 and
020 X ²		076 F2S	calculate ϕ_2 .
021 RCL2		077 ST06	
022 X ²		078 R4	
023 +		079 ST04	
024 RCL4		080 R1	
025 X ²		081 -	
026 +		082 CHS	
027 RCL3		083 ST0B	
028 X ²		084 RCLA	
029 -		085 GSEC	
030 RCL2		086 ST01	
031 RCL4		087 ST0E	
032 x		088 RCLC	
033 2		089 GSEC	
034 x		090 RCL1	
035 ÷		091 -	
036 ST0C		092 ST01	
037 DSP4		093 RCLB	
038 RCLA		094 GSBC	
039 SPC		095 RCLE	
040 PRTX		096 -	
041 RCLB		097 RCL1	
042 PRTX		098 ÷	
043 RCLC		099 RCL0	
044 PFTX		100 x	
045 RTN		101 RCL4	
046 *LBLC	f(x) - your function.	102 +	
047 RTN		103 ST05	
048 *LBLD	Store x_3, x_2, x_1 .	104 F2S	
049 ST0C		105 FTH	
050 R4			
051 ST0E			
052 R4			
053 ST0A			
054 RTN			
055 *LBLB	Store θ_3 and		
056 F2S			

REGISTERS									
0 Used	1 a, cos θ_1	2 b, cos θ_2	3 c, cos θ_3	4 d, cos ϕ_1	5 cos ϕ_2	6 cos ϕ_3	7 1	8 1	9 1
S0 Used	S1 θ_1	S2 θ_2	S3 θ_3	S4 ϕ_1	S5 ϕ_2	S6 ϕ_3	S7 R_1	S8 R_2	S9 R_3
A $R_1, x_1, \cos(\theta_1 - \phi_1)$	B $R_2, x_2, \cos(\theta_2 - \phi_2)$		C $R_3, x_3, \cos(\theta_3 - \phi_3)$		D Det		E Used		I Used

(Card 2)

TITLE _____

001 *LBL6	Calculate R_1, R_2 , and R_3 .	057 PRTX	----- Calculate determinant.
002 GSB6		058 X^2	
003 *LBL5		059 RCL0	
004 GSB0		060 RCL7	
005 STOD		061 ÷	
006 RCL4		062 STOD	
007 ST01		063 X^2	
008 RCL6		064 +	
009 ST02		065 RCL0	
010 RCLC		066 X^2	
011 ST03		067 +	
012 GSB0		068 RCL0	
013 RCLD		069 RCL8	
014 ÷		070 ÷	
015 ST01		071 RCL0	
016 PRTX		072 RCL7	
017 GSB6		073 ÷	
018 RCL4		074 x	
019 ST04		075 2	
020 RCL6		076 x	
021 ST05		077 RCL9	
022 RCLC		078 x	
023 ST06		079 -	
024 GSB0		080 JX	
025 RCLD		081 STOD	
026 ÷		082 PRTX	
027 ST0E		083 RCLD	
028 PRTX		084 F2S	
029 GSB6		085 PRTX	
030 RCL4		086 SPC	
031 ST07		087 RTN	
032 RCL6		088 *LBL0	
033 ST08		089 RCL5	
034 RCLC		090 RCL9	
035 ST09		091 x	
036 GSB0		092 RCL8	
037 RCLD		093 RCL6	
038 ÷		094 x	
039 PRTX		095 -	
040 SPC		096 RCL1	
041 F2S		097 x	
042 ST09		098 RCL4	
043 RCL6		099 RCL9	
044 ST08		100 x	
045 RCL1		101 RCL7	
046 ST07		102 RCL6	
047 RCL9		103 x	
048 F2S		104 -	
049 RTN		105 RCL2	
050 *LBL6	----- Calculate b, c, and d.	106 x	
051 ST0A		107 -	
052 F2S		108 RCL4	
053 ST00		109 RCL8	
054 RCL6		110 x	
055 ÷		111 RCL7	
056 ST0E		112 RCL5	

REGISTERS								
0 Used	1 $\cos \theta_1$	2 $\cos \theta_2$	3 $\cos \theta_3$	4 $\cos \phi_1$	5 $\cos \phi_2$	6 $\cos \phi_3$	7 1	8 1
S0 Used	S1 θ_1	S2 θ_2	S3 θ_3	S4 ϕ_1	S5 ϕ_2	S6 ϕ_3	S7 R_1	S8 R_2
A $\cos (\theta_1 - \phi_1), a$	B $\cos (\theta_2 - \phi_2), b$	C $\cos (\theta_3 - \phi_3), c$	D Det, d	E Used	F Used	G Used	H Used	I Used

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113	X		169	R4	
114	-		170	ST03	
115	RCL3		171	1	
116	X		172	ST07	
117	+		173	ST08	
118	RTN		174	ST09	
119	*LBL6		175	RTN	
120	F2S				
121	RCL1				
122	COS				
123	LSTX				
124	RCL4				
125	-				
126	LSTX				
127	COS				
128	CHS				
129	X2Y				
130	COS				
131	ST04				
132	R4				
133	F2S				
134	ST04				
135	R4				
136	ST01				
137	F2S				
138	RCL2				
139	COS				
140	LSTX				
141	RCL5				
142	-				
143	LSTX				
144	COS				
145	CHS				
146	X2Y				
147	COS				
148	ST08				
149	R4				
150	F2S				
151	ST05				
152	R4				
153	ST02				
154	F2S				
155	RCL3				
156	COS				
157	LSTX				
158	RCL6				
159	-				
160	LSTX				
161	COS				
162	CHS				
163	X2Y				
164	COS				
165	ST0C				
166	R4				
167	F2S				
168	ST06				

Calculate the coefficients
for the system of linear
equations.

LABELS					FLAGS	SET STATUS			
A	B	C	D	E		FLAGS		TRIG	DISP
a	^b →R ₁ ,R ₂ ,R ₃	^c a→b, c, d	d	e	1	0	ON OFF	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
⁰ Determinant	1	2	3	4	2	1	<input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
⁵ R ₁ ,R ₂ ,R ₃	⁶ Coefficients	7	8	9	3	2	<input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
						3	<input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>2</u>

PROGRESSION OF SLIDER CRANK

TITLE

001 #LBL0	002 ST00	Store θ , calculate x and ϕ .	057 PTN	058 #LBL0	Output x_{\max} and x_{\min} .		
003 #LBL7	004 SFC		059 SFC	060 CF1			
005 GSB0	006 COS		061 GSB0	062 SF1			
007 ST04	008 RCL0		063 ST04	064 GSB0			
009 x	010 RCL0		065 RTN				
011 COS	012 ST00		066 #LBL6	Calculate ϕ_{\max} and ϕ_{\min} .			
013 RCL0	014 x		067 SFC				
015 +	016 ST01		068 1				
017 PRTX	018 RCL0		069 SIN ⁻¹				
019 GSB2	020 PRTX		070 GSB2				
021 RTN	022 #LBLA		Store R, L, E, and N and calculate ω .	071 ST04		072 PFTX	Subroutine for ϕ .
023 ST00	024 R4			073 1		074 CHS	
025 ST00	026 R4			075 SIN ⁻¹		076 GSB2	
027 ST00	028 R4			077 PRTX		078 RTN	
029 ST0A	030 RCL0			079 #LBL2		080 SIN	
031 P4	032 x			081 RCL0		082 x	
033 0	034 0			083 RCL0		084 +	
035 ÷	036 ST00	085 RCL0		086 ÷			
037 SFC	038 PRTX	087 SIN ⁻¹		088 ST02			
039 RTN	040 #LBL0	089 RTN		090 #LBLC			
041 RCL0	042 RCL0	Calculate x_{\max} or x_{\min} .		091 SFC	Calculate v and ϕ .		
043 RCL0	044 F10			092 RCL0			
045 CHS	046 +			093 RCL2			
047 ÷	048 SIN ⁻¹			094 +			
049 COS	050 RCL0			095 SIN			
051 RCL0	052 F10			096 CHS			
053 CHS	054 +			097 RCL4			
055 x	056 PRTX		098 ÷				
			099 RCL0				
			100 x				
			101 RCL0				
			102 x				
			103 PRTX				
			104 RCL4				
			105 RCL0				
			106 x				
			107 RCL0				
		108 ÷					
		109 1/X					
		110 ST05					
		111 RCL3					
		112 x					

REGISTERS

0 θ	1 x	2 ϕ	3 $\cos \theta$	4 $\cos \phi$	5 $R/(L \cos \phi)$	6 $(\theta_1 - \theta_2)/h$	7 θ_1	8 θ_2	9 n
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A N		B E		C L		D R		E ω	
								I Index	

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113	RCL E		168	-	
114	X		170	CHS	
115	PRTX		171	RCL 9	
116	RTN		172	÷	
117	◀LBLD	-----	173	STO 6	
118	SFC	Calculate a and ϕ .	174	◀LBL 4	
119	RCL 3		175	SFC	
120	X ²		176	SFC	
121	RCL D		177	RCL 7	
122	X		178	PRTX	
123	RCL C		179	STO 8	
124	÷		180	CF 1	
125	RCL 4		181	GSB 7	
126	3		182	GSB C	
127	Y ^x		183	GSB D	
128	÷		184	SF 1	
129	RCL 0		185	DSZ 1	
130	RCL 2		186	GT 0 3	
131	+		187	RTN	
132	COS		188	◀LBL 3	
133	RCL 4		189	RCL 6	
134	÷		190	ST+7	
135	+		191	GT 0 4	
136	CHS		192	RTN	
137	RCL D				
138	X				
139	RCL E				
140	X ²				
141	X				
142	PRTX				
143	RCL 2				
144	TAN				
145	RCL 5				
146	RCL 3				
147	X				
148	X ²				
149	X				
150	RCL 0				
151	SIN				
152	RCL 5				
153	X				
154	-				
155	RCL E				
156	X ²				
157	X				
158	PRTX				
159	RTN				
160	◀LBL E				
161	STO 9				
162	STO 1				
163	ISZ 1				
164	R 4				
165	STO 8				
166	R 4				
167	STO 7				
168	F 1				

LABELS					FLAGS	SET STATUS		
A	B	C	D	E	F	FLAGS	TRIG	DISP
ANTEILTR → ω	θ → x, φ	→ v, φ	→ a, φ	θ ₁ , θ ₂ , 1n → List	0			
a → x _{max} , x _{min}	b → φ _{max} , φ _{min}	c	d	e	1 Max - Min	ON OFF		
0 x _{max}	1	2 φ	3 Used	4 Used	2	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
5	6	7 Used	8	9	3	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
						2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>2</u>

CIRCULAR CAMS

TITLE _____

001 #LBL0	Flat or roller toggle.	057 PRTX	
002 F0?		058 GSB0	
003 GTO0		059 RCL5	
004 1		060 PRTX	
005 SF0		061 RTN	-----
006 PTN		062 #LBL0	Output $dy/d\theta$ and
007 #LBL0		063 SPC	$d^2y/d\theta^2$.
008 0		064 RCL4	
009 CF0		065 PRTX	
010 RTN		066 RCL3	-----
011 #LBL6	Function code store, and	067 PRTX	Output α .
012 CF1	clear flag 1.	068 RTN	-----
013 ST01		069 #LBLD	
014 RTN		070 SPC	
015 #LBL0	Store increment, duration,	071 RCL2	
016 ST00	angle, π (according to	072 PRTX	
017 R4	angular mode of calculator)	073 RTN	
018 ST00	and initialize θ' register.	074 #LBLE	
019 R4		075 SPC	Output r_g and ϕ .
020 ST07		076 RCL0	
021 1		077 PRTX	
022 CHS		078 RCL1	
023 COS+		079 PRTX	
024 ST00		080 RTN	-----
025 0		081 #LBL0	Harmonic if flag 1 is set.
026 ST00		082 1	
027 RTN		083 FI?	
028 #LBL4	Store lift.	084 ST01	-----
029 ST00		085 RCL6	$\theta/\beta \rightarrow R_E$
030 RTN		086 RCL8	
031 #LBLE	Store R_b and R_g or $R_r - R_g$	087 ÷	
032 ST00	for roller cams.	088 ST00	
033 R4		089 GSEI	Lift function.
034 ST0A		090 RCLD	Calculate lift = $h f(\theta/\beta)$.
035 F0?		091 x	
036 RTN		092 ST00	
037 -		093 RCLD	-----
038 ST0A		094 RCL8	Calculate velocity.
039 RTN		095 ÷	
040 #LBLA	Calculate values auto-	096 RCL4	
041 GSB0	matically.	097 x	
042 GSB0		098 ST04	
043 GSB0		099 RCLD	-----
044 GSB0		100 RCL8	Calculate acceleration.
045 RCL8		101 X ²	
046 RCL8	Check for completion and	102 ÷	
047 XZ?	bring θ into display.	103 RCL3	
048 GTOA		104 x	
049 RCL7		105 ST00	
050 RCL0		106 RCL8	
051 -		107 RCL9	-----
052 RTN		108 RCL5	Calculate pressure angle.
053 #LBLE	Output θ and y .	109 +	
054 SPC		110 ST01	
055 SPC		111 ÷	
056 RCL7		112 P;	

REGISTERS									
0 r_g	1 h	2 α	3 y''	4 y'	5 y	6 θ'	7 θ	8	9 R_b
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A R_g or $(R_r - R_g)$	B β	C Inc	D h	E θ'/β	I Control				

LINEAR CAMS

TITLE _____									
001 #LELc	Store function code and	057 PRTX							
002 CF1	clear flag 1.	058 RTN							
003 STG1		059 #LBLE	Output x_g and y_g .						
004 RTN		060 SFC							
005 #LBLE	Store increment, duration	061 RCL0							
006 STGC	angle, and initialize x'	062 PRTX							
007 R4	register.	063 RCL1							
008 STGB		064 PRTX							
009 R4		065 RTN							
010 STG7		066 #LBL0	Harmonic if flag 1 is set.						
011 0		067 1							
012 STGB		068 FI?							
013 RTN		069 STG1							
014 #LBLE	Store lift.	070 RCL6	Store x'/L in R_E .						
015 STGD		071 RCL6							
016 RTN		072 +							
017 #LBLd	Store base lift.	073 STGB							
018 STGB		074 GSBi	Multiply by lift.						
019 RTN		075 RCLD							
020 #LBLE	Store $R_g - R_r$.	076 STX3							
021 STGB		077 STX4							
022 -		078 x							
023 STGB		079 RCL9							
024 RTN		080 +	y						
025 #LBLA	Calculate values auto-	081 STGB							
026 GSBi	matically.	082 RCL6	Divide by L.						
027 GSBi		083 ST+4							
028 GSBi		084 ST+3							
029 GSBi		085 ST+3							
030 RCLB	Check for completion and	086 RCL4	Calculate α .						
031 RCL6	bring x into display.	087 TAN ⁻¹							
032 X=Y?		088 STG2	$(R_g - R_r) \sin \alpha$						
033 STGB		089 RCL4	$(R_g - R_r) \cos \alpha$						
034 RCL7		090 +F							
035 RCLD		091 RCL5	y_g						
036 -		092 +							
037 RTN		093 STG1							
038 #LBLE	Output x and y.	094 X=Y	x_g						
039 SPC		095 CHS							
040 SPC		096 RCL7							
041 RCL7		097 +							
042 PRTX		098 STGB							
043 GSB0		099 RCL0	Increment x.						
044 RCL5		100 ST+6							
045 PRTX		101 ST+7							
046 RTN		102 RTN							
047 #LBLE	Output dy/dx and d^2y/dx^2 .	103 #LBL1	Harmonic function.						
048 SPC		104 DEG							
049 RCL4		105 1							
050 PRTX		106 8							
051 RCL3		107 0							
052 PRTX		108 x							
053 RTN		109 Fi							
054 #LBLD	Output α .	110 2							
055 SPC		111 ÷							
056 RCL2		112 +F							
REGISTERS									
0 x_g	1 y_g	2 α	3 y''	4 y'	5 y	6 x'	7 x	8 R_r	9 y_b
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A $R_g - R_r$	B L	C Δx	D h	E x'/L	F Control				

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113	Fi			169	X²		
114	X			170	2		
115	ST03			171	X		
116	R4			172	FTN		
117	ST04			173	#LBL0	x > .5	
118	1			174	CLX		
119	RCLE			175	4		
120	1			176	CHS		
121	0			177	ST03		
122	0			178	1		
123	X			179	RCLE		
124	COS			180	-		
125	-			181	X		
126	2			182	CHS		
127	÷			183	ST04		
128	RTN			184	LSTN		
129	#LBL2			185	X²		
130	DEG			186	ENT1		
131	ENT1			187	+		
132	+			188	CHS		
133	1			189	1		
134	0			190	+		
135	0			191	FTN		
136	X						
137	1						
138	+F						
139	CHS						
140	1						
141	+						
142	ST04						
143	R4						
144	ST01						
145	ENT1						
146	+						
147	Fi						
148	X						
149	ST03						
150	RCLE						
151	RCL1						
152	2						
153	÷						
154	Fi						
155	÷						
156	-						
157	RTN						
158	#LBL3						
159	.						
160	5						
161	X±Y?						
162	GT00						
163	CLX						
164	4						
165	ST03						
166	X						
167	ST04						
168	RCLE						

LABELS					FLAGS	SET STATUS		
A Auto	B →x, y	C y', y''	D →α	E →xg, yg	0	FLAGS	TRIG	DISP
a (1, 2, 3)	b x₀↑L↑Δx	c h	d yb	e Rg↑Rr	1 Har	ON OFF		
0	1 Harmonic	2 Cycloidal	3 Parabolic	4	2	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input type="checkbox"/>
						1 <input checked="" type="checkbox"/> <input type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
						2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>
5	6	7	8	9	3	3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>

GEAR FORCES

TITLE _____

001 *LBLA	Calculate F_t .	057 R1							
002 ÷		058 +							
003 STOS		059 R4							
004 RTH		060 -							
005 *LBLB	Store α .	061 R1							
006 STOA		062 PRTX							
007 RTN		063 X=Y							
008 *LBLC	Store ϕ_n .	064 PRTX							
009 STOS		065 RTN							
010 RTH		066 *LBLd	Store coefficient of friction.						
011 *LBLE	Convert ϕ to ϕ_n and store.	067 STOA							
012 TAN		068 RTN							
013 RCLA		069 *LBLE	Calculate F_{ws} , F_{gax} .						
014 COS		070 SPC							
015 x		071 RCL5							
016 TAN=		072 SIN							
017 STOS		073 LSTX							
018 RTH		074 COS							
019 *LBLF	Calculate F_{gs} and F_{gax} .	075 RCLA							
020 SPC		076 SIN							
021 RCL6		077 x							
022 RCLA		078 RCLA							
023 TAN		079 COS							
024 x		080 RCL4							
025 RCL5		081 x							
026 TAN		082 +							
027 RCLA		083 ÷							
028 COS		084 RCL6							
029 ÷		085 x							
030 RCL6		086 PRTX							
031 x		087 1							
032 PRTX		088 RCLA							
033 X=Y		089 TAN							
034 PRTX		090 RCL4							
035 RTN	Store bevel gear cone angle.	091 x							
036 *LBLg		092 RCL5							
037 STOB		093 COS							
038 RTN		094 ÷							
039 *LBLh	Calculate F_{bpax} and F_{bgax} .	095 -							
040 SPC		096 RCLA							
041 RCLB		097 TAN							
042 RCL5		098 RCL4							
043 TAN		099 RCL5							
044 RCLA		100 COS							
045 COS		101 ÷							
046 ÷		102 +							
047 RCL6		103 ÷							
048 x		104 RCL6							
049 +P		105 x							
050 RCL6		106 PRTX							
051 RCLA		107 RTN							
052 TAN									
053 x									
054 RCLB									
055 X=Y									
056 +P									
REGISTERS									
0	1	2	3	4 f	5 ϕ_n	6 F_t	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	α	B cone L	C	D	E	F	G	H	I

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LABELS												FLAGS		SET STATUS									
A	$T \uparrow r \rightarrow F_t$	B	α	C	ϕ_n	D	ϕ	E	$\rightarrow F_{gs}, F_{gax}$	0	FLAGS		TRIG		DISP								
a	cone L	D	$\rightarrow F_{bpax}, F_{bgax}$	c		d	f	e	$\rightarrow F_{ws}, F_{gax}$	1	0	<input type="checkbox"/> ON	<input checked="" type="checkbox"/> OFF	DEG	<input checked="" type="checkbox"/>	FIX	<input checked="" type="checkbox"/>						
0	1	2		3		4				2	1	<input type="checkbox"/>	<input checked="" type="checkbox"/>	GRAD	<input type="checkbox"/>	SCI	<input type="checkbox"/>						
5	6	7		8		9				3	2	<input type="checkbox"/>	<input checked="" type="checkbox"/>	RAD	<input type="checkbox"/>	ENG	<input type="checkbox"/>						
											3	<input type="checkbox"/>	<input checked="" type="checkbox"/>			n	<u>2</u>						

TITLE

001	#LBLA					057	3										
002	STO1					058	YK										
003	X \rightarrow Y					059	STO7										
004	STO2					060	#LBL1										
005	÷					061	RCL6										
006	STO5					062	RCL7										
007	SPC					063	+										
008	PRTX					064	RCL7										
009	F; i					065	TAN										
010	2					066	-										
011	÷					067	LSTX										
012	RCL2					068	ENT†										
013	÷					069	x										
014	STO8					070	÷										
015	PRTX					071	ST+7										
016	FTN					072	RCL7										
017	#LBLB					073	÷										
018	STO3					074	ABS										
019	X \rightarrow Y					075	EEX										
020	STO4					076	CHS										
021	RTN					077	6										
022	#LBLC					078	X \leftrightarrow Y?										
023	RCL8					079	GT01										
024	RCL5					080	RCL7										
025	÷					081	SIN										
026	RCL4					082	DEG										
027	TAN					083	SIN ⁻¹										
028	+					084	STO7										
029	RCL4					085	GT09										
030	F; i					086	#LBLB										
031	x					087	RCL5										
032	1					088	2										
033	8					089	÷										
034	0					090	RCL4										
035	÷					091	COS										
036	-					092	x										
037	RCL3					093	RCL7										
038	RCL5					094	COS										
039	÷					095	÷										
040	RCL4					096	STOE										
041	COS					097	2										
042	÷					098	x										
043	+					099	RCL3										
044	F; i					100	RCL1										
045	RCL1					101	2										
046	÷					102	÷										
047	-					103	FRC										
048	STO6					104	X=0?										
049	R \rightarrow D					105	GT03										
050	GT05					106	F4										
051	#LBLE					107	X \rightarrow Y										
052	RAD					108	9										
053	RCL6					109	0										
054	3					110	RCL1										
055	x					111	÷										
056	.					112	COS										
Store P and N and calculate D and t.																	
Store d _w and φ.																	
Calculate inv φ _w .																	
Calculate M.																	
Calculate φ _w .																	
REGISTERS																	
0	1	N	2	P	3	d _w	4	φ	5	D	6 inv φ _w	7	φ _w	8	t	9	Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9								
A	B		C		D	M	E	q		I							

BELT LENGTH

TITLE _____

001 *LBL0	Toggle for printing belt tangent points.	057 RCL1							
002 0		058 RCL4							
003 F2?	059 -								
004 RTN	060 X²								
005 SF2	061 -								
006 1	062 JX								
007 RTN	063 ST+8								
008 *LBLA	064 RCL1								
009 CLR6	065 RCL4								
010 SF1	066 -								
011 ST00	067 X÷Y								
012 ST01	068 GSB1								
013 R4	069 ST07								
014 ST06	070 +								
015 R4	071 RCL1								
016 ST04	072 x								
017 1	073 RCL0								
018 CHS	074 ÷								
019 COS+	075 P;								
020 ST00	076 x								
021 RCL0	077 ST+8								
022 RTN	078 F2?								
023 *LBLB	079 GSB0								
024 ST04	080 RCL4								
025 CLX	081 ST01								
026 RCL3	082 CF1								
027 P±S	083 RTN								
028 ST03	084 *LBLE								
029 P±S	085 -								
030 X÷Y	086 1								
031 ST03	087 +R								
032 X÷Y	088 +P								
033 -	089 x								
034 X÷Y	090 ABS								
035 RCL2	091 RCL7								
036 P±S	092 -								
037 ST02	093 RTN								
038 P±S	094 *LBLC								
039 X÷Y	095 RCL4								
040 ST02	096 RCLB								
041 X÷Y	097 RCL0								
042 -	098 GSB8								
043 +P	099 RCL6								
044 X²	100 RCL5								
045 X÷Y	101 GSB6								
046 X<R?	102 RCL1								
047 GSB0	103 x								
048 F1?	104 RCL0								
049 ST05	105 ÷								
050 F1?	106 P;								
051 ST06	107 x								
052 RCL6	108 ST+8								
053 X÷Y	109 RCL8								
054 ST06	110 RTN								
055 GSB6	111 *LBL0								
056 X÷Y	112 RCL0								

$\theta_i - \alpha_i$									

Calculate the total length.									

REGISTERS									
0 R_i	1 R_{i-1}	2 x_i	3 y_i	4 R_i	5 θ_i	6 θ_i	7 α	8 Σ Length	9 Used
S0	S1	S2 x_{i-1}	S3 y_{i-1}	S4	S5	S6	S7	S8	S9
A x_i		B y_i		C 180°		D $\theta_{i-1}, i + 90^\circ - \alpha$		E	

FREE VIBRATIONS

TITLE _____

001 #LBLA	Store k, c, and m and calculate ω .	057 x	
002 CLF6		058 CHS	
003 ST04		059 e ^x	
004 R4		060 ST00	
005 ST03		061 RCL5	
006 R4		062 X<0?	
007 ST02		063 GT00	
008 RCL4		064 X=0?	
009 GSB0		065 GT01	
010 RTN		066 #LBL0	----- For c > c _{cr} .
011 #LBL0		067 RCL0	
012 RCL2	Calculate $\left[\frac{k}{m} - \left(\frac{c}{2m} \right)^2 \right]^{1/2}$	068 RCL0	
013 +		069 x	
014 ST0E		070 RCL1	
015 RCL3		071 +	
016 RCL2		072 RCL5	
017 2		073 +	
018 x		074 RCL0	
019 ÷		075 +P	
020 ST0D		076 ST0A	
021 X ²		077 R4	
022 -		078 ST0B	
023 RND		079 RCL5	
024 X<0?		080 RCL7	
025 GT01		081 x	
026 X=0?		082 -	
027 RTN		083 CHS	
028 #LBL3		084 ST09	
029 LSTX		085 COS	
030 JX		086 RCL0	
031 ST05		087 x	
032 RTN		088 RCL4	
033 #LBL1		089 x	
034 LSTX		090 ST02	
035 ST05		091 PRTX	
036 1		092 RCL0	
037 CHS		093 x	
038 RTN		094 RCL9	
039 #LBL5		095 SIN	
040 RCL4	Calculate c _{cr} .	096 RCL0	
041 RCL2		097 x	
042 x		098 RCL5	
043 JX		099 x	
044 2		100 RCL4	
045 x		101 x	
046 RTN		102 +	
047 #LBL0		103 CHS	
048 ST01	Store initial displacement and velocity.	104 PRTX	
049 R4		105 GT00	
050 ST0B		106 #LBL6	----- For c = c _{cr} .
051 RTN		107 RCL0	
052 #LBL0		108 RCL0	
053 SPC	Calculate displacement, velocity and acceleration at time t.	109 x	
054 #LBL4		110 RCL1	
055 ST07		111 +	
056 RCL0		112 ST0B	

REGISTERS									
0 x ₀	1 \dot{x}_0	2 m, x(t)	3 c, r ₁	4 k, r ₂	5 $\omega \cdot \sqrt{-\omega^2}$	6 (t ₁ - t ₂)/n	7 t, t ₁	8 $\dot{x}(t)$	9 $\omega t - \delta$
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A R, A _{cr} , A _{ov}	B δ , B _{cr} , B _{ov}	C e ^{-c/2m t}	D c/2m	E k/m	F	G	H	I	J n

113	RCL7			169	x*		
114	x			170	e*		
115	RCL0			171	RCL6		
116	+			172	x		
117	RCLC			173	ST+2		
118	x			174	RCL4		
119	STO2			175	x		
120	PRTX			176	ST+8		
121	RCLD			177	RCL2		
122	x			178	PRTX		
123	CHS			179	RCL6		
124	RCLB			180	PRTX		
125	RCLC			181	*LBL6		
126	x			182	RCLD		
127	+			183	2		
128	PRTX			184	x		
129	STO6			185	x		
130	*LBLc			186	RCL2		
131	CHS			187	RCL		
132	/X			188	x		
133	ENT1			189	+		
134	ENT1			190	CHS		
135	RCLD			191	PRTX		
136	-			192	PTN		
137	STO3			193	*LBL6		
138	XZY			194	STO1		
139	2			195	R4		
140	x			196	XZY		
141	-			197	STO7		
142	STO4			198	-		
143	RCL1			199	RCL1		
144	RCL3			200	÷		
145	RCL0			201	STO6		
146	x			202	ISZ1		
147	-			203	*LBL9		
148	RCL4			204	RCL7		
149	RCL3			205	SFC		
150	-			206	PRTX		
151	÷			207	GSB4		
152	STOE			208	DSZ1		
153	RCL0			209	GT08		
154	x			210	PTN		
155	CHS			211	*LBL8		
156	STO4			212	RCL6		
157	RCL3			213	ST+7		
158	RCL7			214	GT09		
159	x			215	PTN		
160	e*						
161	RCLA						
162	x						
163	STO2						
164	RCL3						
165	x						
166	STO8						
167	RCL4						
168	RCL7						

For $c < c_r$.

Calculate acceleration.

Calculate displacement,
velocity and acceleration
automatically.

LABELS					FLAGS		SET STATUS		
A m t c k → ω	B → c _{cr}	C x ₀ t̄ x ₀	D t → x, ẋ, ẍ	E t ₁ t̄ t ₂ t̄ n → List	0	FLAGS	TRIG	DISP	
a c > c _{cr}	b c = c _{cr}	c c < c _{cr}	d ẍ	e Used	1	ON OFF	DEG <input type="checkbox"/>	FIX <input checked="" type="checkbox"/>	
0 ω	1 c > c _{cr}	2 c = c _{cr}	3 c < c _{cr}	4 Used	2	0 <input type="checkbox"/> ∞ <input type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>	
5	6	7	8 Used	9 t → x	3	1 <input type="checkbox"/> ∞ <input type="checkbox"/>	RAD <input checked="" type="checkbox"/>	ENG <input type="checkbox"/>	
						2 <input type="checkbox"/> ∞ <input type="checkbox"/>	n	3	

VIBRATIONS FORCED BY $F_0 \cos \omega t$

TITLE

001	*LBLA	Store k, c, and m and calculate ω_0 , ω_n and ξ .	057	RCL2	Store F_0 and ω and calculate AMP and δ .	
002	SFC		058	x		
003	CLF6		059	RCL9		
004	SF0		060	RCL3		
005	ST04		061	x		
006	R4		062	X ² /Y		
007	STG3		063	+F		
008	R4		064	STOC		
009	STO2		065	RCL8		
010	RCL4		066	X ² /Y		
011	GSE0		067	÷		
012	PPTX		068	PPTX		
013	RCL3		069	R4		
014	RCL4		070	STOE		
015	RCL2		071	RTN		
016	x		072	*LBLC		Input t and calculate x(t), $\dot{x}(t)$ and $\ddot{x}(t)$.
017	/X		073	SPC		
018	2		074	STOS		
019	x		075	R4		
020	÷		076	STOS		
021	PPTX		077	R1		
022	PTN		078	RCL5		
023	*LBL0		079	RCL9		
024	RCL2		080	GSE4		
025	+		081	F-D		
026	STOE		082	PPTX		
027	/X		083	PTN		
028	PPTX		084	*LBLD		
029	RCL5		085	SPC		
030	RCL3		086	*LBL6		
031	RCL2		087	STOE		
032	2		088	RCL9		
033	x	089	x			
034	÷	090	RCL5			
035	STOD	091	-			
036	X ²	092	COS			
037	-	093	LSTX			
038	RND	094	SIN			
039	X=0?	095	X ² /Y			
040	GT01	096	RCL8			
041	X=0?	097	x			
042	RTN	098	RCLC			
043	*LBL3	099	÷			
044	LSTX	100	PPTX			
045	/X	101	RCL4			
046	STOS	102	x			
047	PTN	103	STOB			
048	*LBL1	104	X ² /Y			
049	LSTX	105	RCL8			
050	STOS	106	x			
051	1	107	RCLC			
052	CHS	108	÷			
053	PTN	109	RCL9			
054	*LBL4	110	x			
055	X ²	111	CHS			
056	-	112	PPTX			

REGISTERS																			
0	k x(t)	1	c x̃(t)	2	m	3	c	4	k	5	$\omega_n \sqrt{-\omega_n^2}$	6	t, t ₁	7	ω_{res}^2	8	F ₀	9	ω
S0		S1		S2		S3		S4		S5		S6		S7		S8		S9	
A	(t ₁ - t ₂)/n			B	δ		C	Δ		D	c/2m		E	k/m		I	0.00		

DATE _____ AUTHOR _____

113	RCL3		169	RCLA	
114	X		170	ST+6	
115	ST01		171	GT07	
116	CHS		172	RTN	
117	RCL0				
118	-				
119	RCL9				
120	RCL6				
121	X				
122	COS				
123	RCL8				
124	X				
125	+				
126	RCL2				
127	+				
128	PRTX				
129	RTN				
130	*LBL6				
131	CF0	Calculate ω_{res} .			
132	RCL5				
133	RCL0				
134	X ²				
135	2				
136	X				
137	-				
138	NO0?				
139	GT05				
140	ABS				
141	FX				
142	ST07				
143	RTN				
144	*LBL5				
145	FX				
146	ST07				
147	DSF9				
148	DSF3				
149	RTN				
150	*LBL4	Calculate $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ and output the values automatically.			
151	ST01				
152	R4				
153	X \leftrightarrow Y				
154	ST06				
155	-				
156	RCL7				
157	+				
158	ST04				
159	ISZ1				
160	*LBL7				
161	SPC				
162	RCL6				
163	PRTX				
164	GSB6				
165	DSZ1				
166	GT08				
167	RTN				
168	*LBL8				

LABELS					FLAGS	SET STATUS		
A m1c1k	B $\rightarrow \omega_{res}$	C $\omega \uparrow F_0 \rightarrow AMP, \delta$	D $t \rightarrow x, \dot{x}, \ddot{x}$	E $t_1 \uparrow t_2 \uparrow n \rightarrow \dots$	0	FLAGS	TRIG	DISP
a	b	c	d	e	1	0 <input type="checkbox"/> ON <input checked="" type="checkbox"/> OFF	DEG <input type="checkbox"/>	FIX <input checked="" type="checkbox"/>
						1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
						2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input checked="" type="checkbox"/>	ENG <input type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>
0 ω_0, ω_n	1 $c > c_{cr}$	2	3 $c < c_{cr}$	4 AMP, δ	2			
5	6 Used	7 $t \rightarrow x_1$	8 $t + \Delta t$	9 ω_{res}	3			

EQUATIONS OF STATE

TITLE

001	*LBL0	Redlich-Kwong; ideal gas	057	*LBL8	Ideal gas solution for n,						
002	FR?	toggle.	058	SF1	R and T.						
003	GTO0		059	*LBL9							
004	0		060	RCL5							
005	SF0		061	RCL6							
006	FTN		062	x							
007	*LBL0		063	RCL7							
008	1		064	÷							
009	CF0		065	RCL8							
010	FTN		066	÷							
011	*LBL6	Store T _c .	067	RCL9							
012	CF3		068	÷							
013	STO0		069	STO1							
014	FTN		070	*LBL0	Stop if ideal gas is desired.						
015	*LBLC	Store P _c .	071	FR?							
016	CF3		072	FTN							
017	STO0		073	GSE1							
018	FTN		074	STO0	Calculate P by Redlich-						
019	*LBLA	P code.	075	*LBL2	Kwong.						
020	5		076	F1?							
021	GTO0		077	GSE1							
022	*LBL0	V code.	078	*LBL0							
023	6		079	RCL6							
024	GTO0		080	RCL9							
025	*LBLC	n code.	081	x							
026	7		082	RCL6							
027	GTO0		083	RCL8							
028	*LELD	R code.	084	-							
029	8		085	STO4							
030	GTO0		086	÷							
031	*LBL0	T code.	087	RCLA							
032	9		088	RCL9							
033	*LBL0	Store input.	089	TX							
034	CF1		090	÷							
035	STO1		091	STO2							
036	R+		092	RCL6							
037	STO1		093	÷							
038	F3?		094	LSTX							
039	FTN		095	RCL6							
040	1		096	+							
041	STO1	Dummy 1.00 for unknown	097	STO3							
042	GTO1	and GTO ideal gas.	098	÷							
043	*LBL5	Ideal gas solution for P	099	RCL5							
044	*LBL7	and V.	100	RCL5	Calculate f(P).						
045	RCL7		101	-							
046	RCL8		102	GSE1	Calculate f'(P).						
047	x		103	÷							
048	RCL9		104	ST-1	Loop again?						
049	x		105	RCL7							
050	RCL5		106	÷							
051	RCL6		107	ABS							
052	x		108	EEY							
053	÷		109	CHS							
054	STO1		110	4							
055	GTO0		111	X=Y?							
056	*LBL7		112	GTO2							
REGISTERS											
0	1	2	3	4	5	6	7	8	9		
		a/T ^{1/2}	(V + b)	(V - b)	P	V	n	R	T		
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9		
A	a	B	b	C	T _c	D	P _c	E	nR	I	Control

ISENTROPIC FLOW FOR IDEAL GASES

TITLE _____

001 *LBL0	Store k, k - 1, 1/(k - 1).	057 SF3	
002 ST02		058 GTOB	
003 1		059 *LBL0	----- Output p/p_0 .
004 -		060 F3?	
005 ST02		061 GTOB	
006 1/X		062 GSEB	
007 ST04		063 RCL4	
008 RCL2		064 Y*	
009 RTN	----- Output M.	065 RTN	
010 *LBL0		066 *LBL0	----- Convert p/p_0 to T/T_0 and GTO B.
011 F3?		067 SF3	
012 GTOB		068 RCL2	
013 RCL1		069 Y*	
014 Y*		070 GTOE	
015 RTN	----- Store M^2 .	071 *LBL0	----- Set -3 in display for subsonic guess.
016 *LBL0		072 2	
017 X ²		073 CHS	
018 ST01		074 X*Y	
019 Y*		075 F3?	
020 RTN	----- Output T/T_0 .	076 GTO1	
021 *LBL0		077 GTO3	
022 F3?		078 *LBL1	
023 GTOB		079 ENT1	----- Make guess of M^2 .
024 2		080 ST06	
025 RCL1		081 FFO	
026 RCL3		082 Y*	
027 X		083 +	
028 2		084 X*Y	
029 +		085 Y*	
030 +		086 ST01	
031 RTN	----- Convert T/T_0 to M^2 .	087 *LBL2	----- Iterate by Newton's method to find M^2 Corresponding to A/A^* .
032 *LBL0		088 RCL6	
033 2		089 GSE3	
034 X*Y		090 ÷	
035 ÷		091 1	
036 2		092 -	
037 -		093 .	
038 RCL3		094 5	
039 ÷		095 RCL8	
040 ST01		096 +	
041 Y*		097 .	
042 RTN	----- Output P/P_0 .	098 5	
043 *LBL0		099 RCL1	
044 F3?		100 ÷	
045 GTOB		101 -	
046 GSEB		102 +	
047 RCL2		103 ST+1	
048 RCL3		104 RCL1	
049 ÷		105 +	
050 Y*		106 ABS	
051 RTN		107 EEN	
052 *LBL0		108 CHS	
053 RCL3	----- Convert P/P_0 to T/T_0 and GTO B.	109 4	
054 RCL2		110 X*Y?	
055 +		111 GTO2	
056 Y*		112 RCL1	

REGISTERS									
0	1 M ²	2 k	3 k - 1	4 1/k - 1	5	6 A/A*	7 (k - 1)/k + 1	8 Used	9 Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J

DATE _____ AUTHOR _____

113 JX		
114 PTH		
115 *LBL6	Set +3 in display for super-	
116 3	sonic guess.	
117 X=Y		
118 F3?		
119 GT01		
120 *LBL3	Convert M ² to A/A*.	
121 2		
122 RCL2		
123 1		
124 +		
125 ÷		
126 RCL7		
127 LSTX		
128 ÷		
129 ST07		
130 RCL1		
131 x		
132 +		
133 ST06		
134 RCL7		
135 2		
136 x		
137 1/X		
138 Y*		
139 RCL1		
140 JX		
141 ÷		
142 FTH		
143 *LBL6	Output values.	
144 SPC		
145 CF3		
146 RCL2		
147 PFTX		
148 SPC		
149 GSBH		
150 PFTX		
151 GSBE		
152 PFTX		
153 GSBG		
154 PFTX		
155 GSED		
156 PFTX		
157 GSBE		
158 PFTX		
159 PTH		

LABELS					FLAGS	SET STATUS			
A M→M	B T/T ₀ →M	C P/P ₀ →M	D ρ/ρ ₀ →M	E A/A* _{sub} →M	0	FLAGS		TRIG	DISP
a k	b→k,M,T/T ₀ ...	c	d	e A/A* _{sup} →M	1	ON OFF			
0 Used	1 M ² guess	2 M ² iter	3 A/A*	4	2	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	SCI <input type="checkbox"/>	FIX <input checked="" type="checkbox"/>
5	6	7	8	9	3 DATA?	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
						2 <input type="checkbox"/> <input checked="" type="checkbox"/>	n <u>3</u>		
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>			

CONDUIT FLOW

TITLE _____

001 *LEL0	Set divide by ρ flag.	057 1/X	Set f and Re in display.
002 SF2	-----	058 X2	-----
003 GT00	-----	059 RCL1	-----
004 *LBL6	Clear divide by ρ flag.	060 RCL4	-----
005 CF2	-----	061 RTN	-----
006 *LBL0	-----	062 *LBLD	Store velocity.
007 ST09	Store μ or ν .	063 ST02	-----
008 GT00	-----	064 F3?	-----
009 *LBL0	-----	065 RTN	-----
010 ST0A	Store ρ .	066 SF0	Guess v.
011 GT00	-----	067 GSE9	-----
012 *LBL0	Store ϵ .	068 *LEL3	Iterate to find v.
013 ST0E	-----	069 RND	-----
014 GT00	-----	070 ST00	-----
015 *LBLA	Store L.	071 GSB8	-----
016 ST03	-----	072 RND.	-----
017 GT00	-----	073 RCL0	-----
018 *LBLB	-----	074 X*Y	-----
019 ST0D	Store D.	075 X*Y?	-----
020 GT00	-----	076 GT03	-----
021 *LBLC	-----	077 RCL5	Set f, Re and v in display.
022 4	Store $K_T/4$.	078 1/X	-----
023 +	-----	079 X2	-----
024 ST00	-----	080 RCL1	-----
025 *LBL0	-----	081 RCL3	Calculate constants.
026 CF2	-----	082 RTN	-----
027 RTN	Clear data input flag.	083 *LEL9	-----
028 *LBL0	-----	084 RCL4	-----
029 4	Convert input psi to lb/ft-sec ² and store.	085 F2?	-----
030 6	-----	086 ST+9	-----
031 3	-----	087 RCLD	-----
032 2	-----	088 RCL5	-----
033 X	-----	089 +	-----
034 ST04	-----	090 ST06	-----
035 F3?	-----	091 LN	-----
036 RTN	-----	092 1	-----
037 GSE6	-----	093 .	-----
038 4	Convert lb/ft-sec ² to psi and display.	094 7	-----
039 6	-----	095 3	-----
040 3	-----	096 7	-----
041 2	-----	097 ST07	-----
042 +	-----	098 X	-----
043 RTN	-----	099 2	-----
044 *LELE	Store pressure.	100 .	-----
045 ST04	-----	101 2	-----
046 F3?	-----	102 8	-----
047 RTN	-----	103 +	-----
048 CF0	-----	104 ST0C	-----
049 GSE9	Compute pressure drop.	105 ST05	-----
050 RCL2	-----	106 F0?	-----
051 X2	-----	107 GT07	-----
052 X	-----	108 *LBL8	is flow turbulent?
053 RCL4	-----	109 1	-----
054 X	-----	110 6	-----
055 ST04	-----	111 RCL2	-----
056 RCL5	-----	112 RCLD	-----

REGISTERS

0 v	1 Re	2 v	3 L	4 ΔP	5 $1/\sqrt{f}$	6 D/ ϵ	7 1.737	8 $K_T/4$	9 ν, μ
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A ρ	B Used	C $1/\sqrt{f_0}$	D D	E ϵ	F	G	H	I	J

DATE _____ AUTHOR _____

113	x				169	GT02		-----
114	RCL9				170	*LBL7		Start calculation of ΔP or v.
115	÷				171	RCL5		
116	ST01				172	1/X		
117	2				173	X²		
118	3				174	RCL3		
119	0				175	x		
120	0				176	RCL0		
121	X↔Y?				177	÷		
122	GT02				178	RCL8		
123	R4				179	+		
124	÷				180	2		
125	7X				181	x		
126	1/X				182	RCL4		
127	GT07				183	RCL4		
128	*LBL2				184	÷		
129	RCL0				185	X↔Y		
130	RCL5				186	F0?		
131	-				187	GT08		
132	4				188	RTN		
133	.				189	*LBL0		
134	€				190	÷		
135	7				191	7X		
136	RCL6				192	ST02		
137	x				193	RTN		
138	RCL1							
139	÷							
140	RCL5							
141	x							
142	1							
143	+							
144	ST05							
145	LN							
146	RCL7							
147	x							
148	-							
149	RCL8							
150	1/X							
151	CHS							
152	1							
153	+							
154	RCL7							
155	x							
156	RCL5							
157	÷							
158	1							
159	+							
160	÷							
161	ST+5							
162	RCL5							
163	÷							
164	ABS							
165	EEX							
166	CHS							
167	7							
168	X↔Y?							
Iterate to find $\frac{1}{\sqrt{f}}$ for turbulent flow.								

LABELS				FLAGS		SET STATUS		
A L	B D	C K _T	D v	E ΔP	F v calc.	ON OFF		
a μ	b ν	c ρ	d €	e ΔP (psi)	f	0	<input type="checkbox"/> <input type="checkbox"/> <input checked="" type="checkbox"/>	
0 Used	1	2 iter. 1/√f	3 iter. v	4	2 ρ divide	1	<input type="checkbox"/> <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>
5	6	7 calc.	8 turb?	9 →f	3	2	<input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>
						3	<input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>

FIX <input type="checkbox"/>	SCI <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>	n <u>2</u>
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HEAT EXCHANGERS (Card 1)

TITLE _____

001 #LBL0	Store T _{cin} .	057 RCL1							
002 ST02		058 -							
003 RTN		059 CHS							
004 #LBL6	Store C _c .	060 RTN							
005 X		061 #LBL5	----- Calculate E from T _{co} .						
006 ST03		062 ST05							
007 RTN		063 GSB1							
008 #LBLc	Store T _{hin} .	064 RCL4							
009 ST01		065 RCL7							
010 RTN		066 ÷							
011 #LBLd	Store C _h .	067 RCL1							
012 X		068 RCL5							
013 ST04		069 -							
014 RTN		070 X							
015 #LBLe	Clear flag 1 for counter flow, set for parallel flow.	071 RCL1							
016 F1?		072 RCL2							
017 GT00		073 -							
018 0		074 ÷							
019 SF1		075 ST05							
020 RTN		076 RTN							
021 #LBL0		077 #LBL0	----- Calculate AU for C _{min} / C _{max} = 0.						
022 J		078 X#0?							
023 CF1		079 GT00							
024 RTN		080 1							
025 #LBLA	Calculate AU from E.	081 RCL5							
026 ST05		082 -							
027 GSB1		083 LN							
028 GSB0		084 CHS							
029 ST08		085 RTN							
030 RTN		086 #LBL2	----- Calculate E for C _{min} / C _{max} = 0.						
031 #LBLe	Calculate q from AU.	087 X#0?							
032 ST08		088 GT02							
033 GSB1		089 1							
034 GSB2		090 RCL8							
035 RCL7		091 CHS							
036 X		092 e*							
037 RCL1		093 -							
038 RCL2		094 RTN							
039 -		095 #LBL1	----- Store C _{min} and C _{min} / C _{max} .						
040 X		096 RCL3							
041 ST06		097 RCL4							
042 RTN		098 X>Y?							
043 #LBLC	Calculate T _{co} from q.	099 X<Y							
044 ST06		100 ST07							
045 RCL3		101 X<Y							
046 ÷		102 ÷							
047 RCL2		103 ST00							
048 +		104 RTN							
049 RTN									
050 #LBLD	Calculate T _{ho} from T _{co} .								
051 RCL2									
052 -									
053 RCL3									
054 X									
055 RCL4									
056 ÷									
REGISTERS									
0 C _{min} /C _{max}	1 T _{hin}	2 T _{cin}	3 C _c	4 C _h	5 E	6 q	7 C _{min}	8 AU	9 C _{max}
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J

(Card 2)
(Side 1: Parallel-Counter-Flow)

TITLE _____

113	*LBL0	Calculate AU for parallel-	168	X ²					
114	GSB6	counter-flow.	170	1					
115	2		171	+					
116	x		172	JX					
117	RCL6		173	ST06					
118	2		174	RTN	-----				
119	RCL5								
120	÷								
121	+								
122	RCL9								
123	-								
124	÷								
125	CHS								
126	1								
127	+								
128	LN								
129	RCL6								
130	÷								
131	CHS								
132	RCL7								
133	÷								
134	LSTX								
135	ENT1								
136	x								
137	x								
138	RTN								
139	*LBL2								
140	GSB6	Calculate E for parallel-c							
141	RCL8	ounter-flow.							
142	RCL7								
143	÷								
144	RCL6								
145	x								
146	CHS								
147	e ^x								
148	1								
149	XZY								
150	+								
151	1								
152	LSTX								
153	-								
154	÷								
155	RCL6								
156	x								
157	RCL9								
158	+								
159	2								
160	XZY								
161	÷								
162	RTN								
163	*LBL6								
164	RCL0								
165	1								
166	+								
167	ST09								
168	RCL0								
REGISTERS									
0 C _{min} /C _{max}	1 T _{hin}	2 T _{cin}	3 C _c	4 C _h	5 E	6 Used	7 C _{min}	8 AU _i	9 Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A AU _{i-1}	B F(AU _i)	C	D F(AU _{i-1})	E	I				

(Side 2: Cross-Flow)

DATE _____ AUTHOR _____

113 *LBL6	Calculate AU for cross-flow.	169 e*	
114 FIX		170 CHS	
115 0		171 1	
116 STOA		172 +	
117 1		173 RTN	-----
118 RCL5			
119 CHS			
120 STOD			
121 +			
122 LN			
123 CHS			
124 STOB			
125 *LBL6			
126 RCL9			
127 GSB2			
128 RCL5			
129 -			
130 STOB			
131 RCL4			
132 RCL8			
133 STOA			
134 -			
135 RCLD			
136 RCL8			
137 STOD			
138 -			
139 ÷			
140 x			
141 ST-8			
142 RCL8			
143 ÷			
144 RND			
145 X#0?			
146 STOB			
147 RCL8			
148 RTN			
149 *LBL2	Calculate E for cross-flow.		
150 RCL8			
151 RCL7			
152 ÷			
153 ENT1			
154 ENT1			
155 .			
156 2			
157 2			
158 Y*			
159 RCL8			
160 ÷			
161 ÷			
162 LSTX			
163 %Y			
164 CHS			
165 e*			
166 1			
167 -			
168 x			

LABELS					FLAGS	SET STATUS			
A	B	C	D	E	0	FLAGS		TRIG	DISP
a	b	c	d	e	1	ON OFF			
0 E→AU	1	2 AU→E	3	4	2	0	<input type="checkbox"/> <input type="checkbox"/>	DEG <input type="checkbox"/>	FIX <input type="checkbox"/>
						1	<input type="checkbox"/> <input type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
						2	<input type="checkbox"/> <input type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
5	6 iterate	7	8	9	3	3	<input type="checkbox"/> <input type="checkbox"/>		n _____

Appendix A
MAGNETIC CARD
SYMBOLS AND CONVENTIONS

SYMBOL OR CONVENTION	INDICATED MEANING
White mnemonic: x A	White mnemonics are associated with the user-definable key they are above when the card is inserted in the calculator's window slot. In this case the value of x could be input by keying it in and pressing A.
Gold mnemonic: y x f E x↑y A	Gold mnemonics are similar to white mnemonics except that the gold f key must be pressed before the user-definable key. In this case y could be input by pressing f E. ↑ is the symbol for ENTER. In this case ENTER is used to separate the input variables x and y. To input both x and y you would key in x, press ENTER, key in y and press A.
X A	The box around the variable x indicates input by pressing STO A.
(x) A	Parentheses indicate an option. In this case, x is not a required input but could be input in special cases.
→x A	→ is the symbol for calculate. This indicates that you may calculate x by pressing key A.
→x, y, z A	This indicates that x, y, and z are calculated by pressing A once. The values would be printed in x, y, z order.
→x; y; z A	The semi-colons indicate that after x has been calculated using A, y and z may be calculated by pressing R/S.
→“x,” y A	The quote marks indicate that the x value will be “paused” or held in the display for one second. The pause will be followed by the display of y.
↔ x A	The two-way arrow ↔ indicates that x may be either output or input when the associated user-definable key is pressed. If numeric keys have been pressed between user-definable keys, x is stored. If numeric keys have not been pressed, the program will calculate x.

<p>P? A</p>	<p>The question mark indicates that this is a mode setting, while the mnemonic indicates the type of mode being set. In this case a print mode is controlled. Mode settings typically have a 1.00 or 0.00 indicator displayed after they are executed. If 1.00 is displayed, the mode is on. If 0.00 is displayed, it is off.</p>
<p>START A</p>	<p>The word START is an example of a command. The start function should be performed to begin or start a program. It is included when initialization is necessary.</p>
<p>DEL A</p>	<p>This special command indicates that the last value or set of values input may be deleted by pressing A.</p>



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A ● C D E