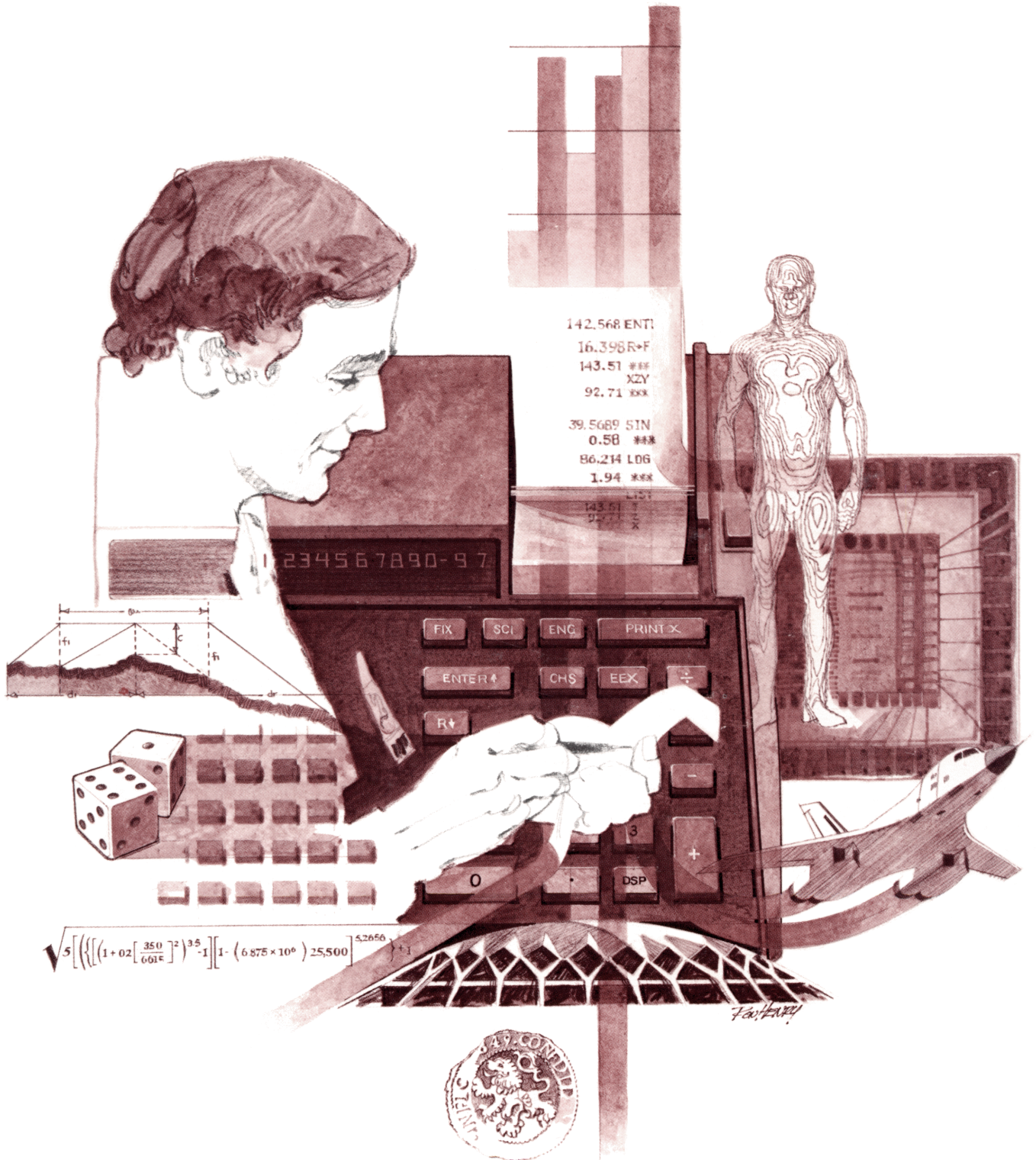


HEWLETT-PACKARD

HP-67/HP-97

Users' Library Solutions
Aeronautical Engineering



INTRODUCTION

In an effort to provide continued value to its customers, Hewlett-Packard is introducing a unique service for the HP fully programmable calculator user. This service is designed to save you time and programming effort. As users are aware, Programmable Calculators are capable of delivering tremendous problem solving potential in terms of power and flexibility, but the real genie in the bottle is program solutions. HP's introduction of the first handheld programmable calculator in 1974 immediately led to a request for program **solutions** — hence the beginning of the HP-65 Users' Library. In order to save HP calculator customers time, users wrote their own programs and sent them to the Library for the benefit of other program users. In a short period of time over 5,000 programs were accepted and made available. This overwhelming response indicated the value of the program library and a Users' Library was then established for the HP-67/97 users.

To extend the value of the Users' Library, Hewlett-Packard is introducing a unique service—a service designed to save you time and money. The Users' Library has collected the best programs in the most popular categories from the HP-67/97 and HP-65 Libraries. These programs have been packaged into a series of low-cost books, resulting in substantial savings for our valued HP-67/97 users.

We feel this new software service will extend the capabilities of our programmable calculators and provide a great benefit to our HP-67/97 users.

A WORD ABOUT PROGRAM USAGE

Each program contained herein is reproduced on the standard forms used by the Users' Library. Magnetic cards are not included. The Program Description I page gives a basic description of the program. The Program Description II page provides a sample problem and the keystrokes used to solve it. The User Instructions page contains a description of the keystrokes used to solve problems in general and the options which are available to the user. The Program Listing I and Program Listing II pages list the program steps necessary to operate the calculator. The comments, listed next to the steps, describe the reason for a step or group of steps. Other pertinent information about data register contents, uses of labels and flags and the initial calculator status mode is also found on these pages. Following the directions in your HP-67 or HP-97 **Owners' Handbook and Programming Guide**, "Loading a Program" (page 134, HP-67; page 119, HP-97), key in the program from the Program Listing I and Program Listing II pages. A number at the top of the Program Listing indicates on which calculator the program was written (HP-67 or HP-97). If the calculator indicated differs from the calculator you will be using, consult Appendix E of your **Owner's Handbook** for the corresponding keycodes and keystrokes converting HP-67 to HP-97 keycodes and vice versa. No program conversion is necessary. The HP-67 and HP-97 are totally compatible, but some differences do occur in the keycodes used to represent some of the functions.

A program loaded into the HP-67 or HP-97 is not permanent—once the calculator is turned off, the program will not be retained. You can, however, permanently save any program by recording it on a blank magnetic card, several of which were provided in the Standard Pac that was shipped with your calculator. Consult your **Owner's Handbook** for full instructions. A few points to remember:

The Set Status section indicates the status of flags, angular mode, and display setting. After keying in your program, review the status section and set the conditions as indicated before using or permanently recording the program.

REMEMBER! To save the program permanently, **clip** the corners of the magnetic card once you have recorded the program. This simple step will protect the magnetic card and keep the program from being inadvertently erased.

As a part of HP's continuing effort to provide value to our customers, we hope you will enjoy our newest concept.

TABLE OF CONTENTS

PROPERTIES OF AIR	1
This program computes the following properties of air at low pressures for a given temperature: specific heat ratio, specific heat at constant pressure, specific heat at constant volume, coefficient of viscosity, and absolute Rankine temperature.	
THEORETICAL U.S. STANDARD ATMOSPHERE TEMPERATURE AND PRESSURE BELOW 35,332 FT.	5
The program computes the theoretical U.S. Standard Atmosphere values for temperature and pressure at any altitude from -16,500 to 35,332 feet or by converting to metric units in the formula, -5,000 to 11,000 meters. Temperature is provided in absolute and thermometer standards. Pressure results are in Hg, psf, psi and mb.	
AIRCRAFT FLYOVER ACOUSTIC TONE DOPPLER SHIFT	9
Computes Doppler shift of an aircraft flyover acoustic source frequency observed on the ground. Also determines the 1/3 octave-band filter, and location within the filter, of the observed frequency. Inputs are flight path speed and angle, air temperature, source frequency, and aircraft elevation angle.	
ISENTROPIC FLOW FOR IDEAL GASES	13
The card replaces isentropic flow tables for a specified specific heat ratio k. Inputs and outputs are interchangeable with the exception of k.	
NORMAL AND OBLIQUE SHOCK PARAMETERS FOR COMPRESSIBLE FLOW	19
Knowing freestream Mach number, shock angle and ratio of specific heats (γ); computes mach number behind shock and the ratios across the shock for: static pressure, total pressure, density and temperature. Assumes adiabatic flow, perfect fluid.	
OBLIQUE SHOCK ANGLE FOR WEDGE	23
Given the upstream Mach number, the flow deflection angle, and the ratio of specific heats the program determines if an oblique shock is possible and finds the shock angle for the weak shock condition if the condition is possible.	
MACH NUMBER AND TRUE AIRSPEED	28
Converts calibrated airspeed and pressure altitude to Mach number and true airspeed.	
TAKE-OFF RUN VS DENSITY ALTITUDE	32
Computes actual take-off run required given sea level run at 15° C at full gross weight, pressure altitude, actual air temperature, and actual take-off weight.	
TRUE AIR TEMPERATURE AND DENSITY ALTITUDE	36
Converts indicated air temperature to true air temperature accounting for the temperature rise associated with high speed flight. Once a true temperature is established the density altitude can be calculated.	
AIRCRAFT CLIMB	40
This program permits one to determine the desirability of climbing from an altitude of high headwinds to an altitude with lower headwinds. Determine the minimum that must remain at the start of the climb to make the climb to higher altitude worthwhile. Program is good for non-supercharged aircraft only.	

Program Description I

1

Program Title	Properties of Air		
Contributor's Name	Hewlett-Packard		
Address	1000 N.E. Circle Blvd.		
City	Corvallis	State	Oregon
		Zip Code	97330

Program Description, Equations, Variables

This program computes properties of air at low pressures for a given temperature * in degrees Fahrenheit or Rankine.

The following properties are computed:

1. Specific heat ratio

$$k = 1/(1 - R/J C_p)$$

where:

R Universal gas constant

J Mechanical equivalent of heat

3. Specific heat at constant volume

$$C_v = C_p/k, \text{ Btu/lb.} - ^\circ\text{R}$$

4. Coefficient of viscosity

$$\mu = 7.4 \times 10^{-7} (T)^{1.5} / (T + 200),$$

lbm./ft. - sec.

2. Specific heat at constant pressure

$$C_p = 0.2478 - 4.2047 \times 10^{-5} T$$
$$+ 5.8 \times 10^{-8} T^2 - 1.49 \times 10^{-11} T^3,$$

Btu/lb. - $^\circ\text{R}$

5. Absolute Rankine temperature

$$T = 459.7 + (T, ^\circ\text{F}), ^\circ\text{R}$$

* If temperature is in degrees Centigrade or Kelvin, use Temperature Conversion program (STD - 08A) from Standard Pac to convert to degrees Fahrenheit or Rankine.

Operating Limits and Warnings

Properties k , C_p , C_v and μ are good for temperature and pressure ranges of 300 - 2000 $^\circ\text{R}$ and 0 - 300 psia respectively.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample Problem(s)

Find the specific heat ratio, specific heat at constant pressure, specific heat at constant volume, coefficient of viscosity, and absolute Rankine temperature for air at a temperature of 300 degrees Fahrenheit.

$$k = 1.3930$$

$$C_p = 0.2428 \text{ Btu/lb. } ^\circ\text{R}$$

$$C_v = 0.1743 \text{ Btu/lb. } ^\circ\text{R}$$

$$\mu = 1.6146 \times 10^{-5} \text{ lbm./ft. } \cdot \text{sec.}$$

$$T = 759.70^\circ\text{R}$$

Solution(s)

Keystrokes:

Outputs:

300[E] [A] -----> 1.3930

300[E] [B] -----> 0.2428

300[E] [C] -----> 0.1743

300[E] [D] -----> 1.6146×10^{-5}

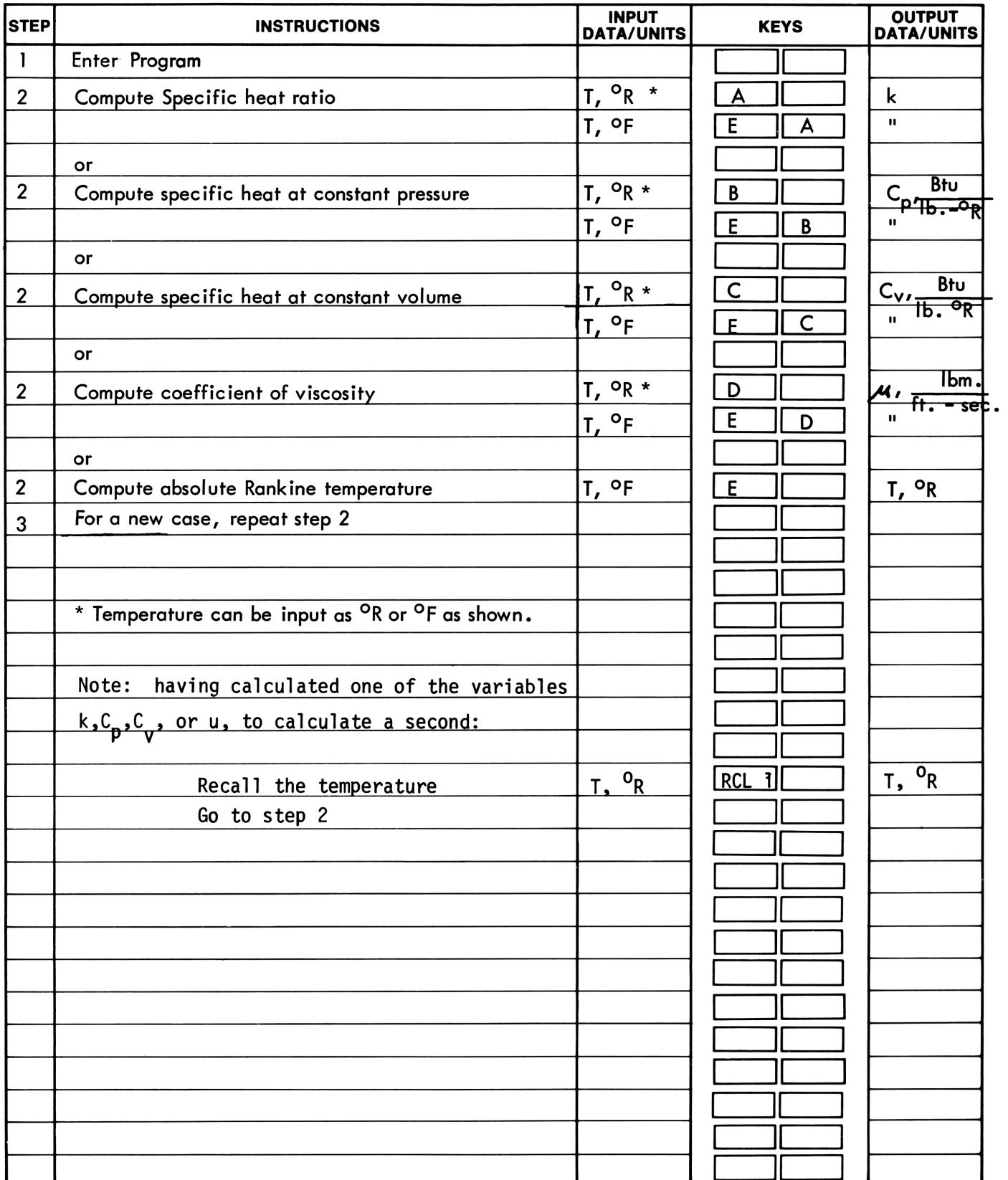
300[E] -----> 759.70

Reference(s)

Keenan and Kay, Gas Tables, fifth printing, John Wiley & Sons, Inc., March, 1956. Hall, Newman A., Thermodynamics of Fluid Flow, Prentice-Hall, Inc., 1951.

This program is a translation of the Users' Library program #01078A submitted by Paul, K. Shumpert.

3



97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11	Compute k T, °R	057	RCL2	36 02	Compute C _v
002	FIX	-11		058	RTN	24	
003	DSP4	-63 04		059	*LBLC	21 13	
004	STO1	35 01		060	GSBA	23 11	
005	ENT↑	-21		061	RCL2	36 02	
006	x	-35		062	X↔Y	-41	
007	5	05		063	=	-24	
008	.	-62		064	RTN	24	
009	8	08		065	*LBLD	21 14	Compute μ
010	EEX	-23		066	STO1	35 01	
011	CHS	-22		067	1	01	
012	8	08		068	.	-62	
013	x	-35		069	5	05	
014	.	-62		070	Y↔X	31	
015	2	02		071	RCL1	36 01	
016	4	04		072	2	02	
017	7	07		073	0	00	
018	8	08		074	0	00	
019	+	-55		075	+	-55	
020	RCL1	36 01	C _p	076	=	-24	
021	2	02		077	7	07	
022	3	03		078	.	-62	
023	7	07		079	4	04	
024	8	08		080	EEX	-23	
025	3	03		081	CHS	-22	
026	=	-24		082	7	07	
027	-	-45		083	x	-35	
028	1	01		084	SCI	-12	
029	4	04		085	RTN	24	
030	9	09		086	*LBLE	21 15	Compute T, °R
031	EEX	-23		087	ENT↑	-21	
032	CHS	-22		088	4	04	
033	1	01		089	5	05	
034	3	03		090	9	09	
035	RCL1	36 01		091	.	-62	
036	3	03		092	7	07	
037	Y↔X	31		093	+	-55	
038	x	-35		094	FIX	-11	
039	-	-45		095	RTN	24	
040	STO2	35 02					SET STATUS
041	1	01					
042	ENT↑	-21					
043	1	01					
044	ENT↑	-21		100			
045	.	-62					
046	0	00					
047	6	06					
048	8	08					
049	5	05					
050	RCL2	36 02	Compute C _p				110
051	÷	-24					
052	-	-45					
053	÷	-24					
054	RTN	24					
055	*LBLB	21 12					
056	GSBA	23 11					

REGISTERS									
0	1	2	3	4	5	6	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

Program Description I

Program Title	Standard Atmosphere Below 35,322 Feet		
Contributor's Name	Hewlett-Packard		
Address	1000 N.E. Circle		
City	Corvallis	State	Oregon
		Zip Code	97330

Program Description, Equations, Variables This program computes the theoretical U.S. Standard Atmosphere temperature and pressure in English and Metric units at altitudes below 35,332 feet and 11,000 meters. Additionally, the actual mean sea level values, at a specific time, can be placed in the program for prediction of altitude temperature and pressure based on the following formulas:

$$P = \frac{P_0}{\left(\frac{T_0}{T_0 - aZ}\right)^n} \quad T = T_0 - aZ \quad t = T - T \text{ abs reference}$$

P = Pressure at altitude above/below mean sea level.

P₀ = Standard air pressure at mean sea level.

T₀ = Standard absolute temperature at mean sea level in Rankine/Kelvin.

a = Temperature lapse rate per foot of altitude in °F/per meter °C.

Z = Altitude above/below mean sea level in feet/meters.

n = Constant G/aR = 5.2561

T = Temperature absolute at altitude in Rankine/Kelvin.

T abs ref. = 459.688 °R/ 273.16 °K.

t = Temperature at altitude in Fahrenheit/Centigrade

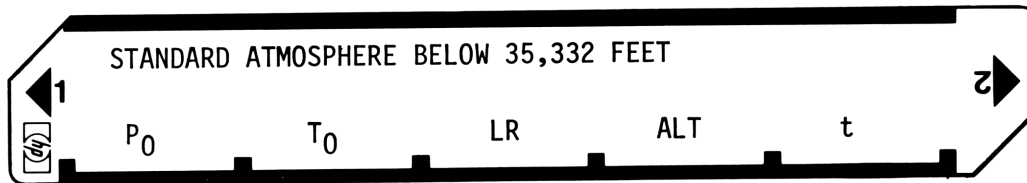
- Operating Limits and Warnings**
1. The program will accurately reproduce the theoretical U.S. Standard Atmosphere tables of temperature and pressure within the limits of -16,500 to 35,332 feet or -5,000 to 11,000 meters.
 2. The correct temperature and pressure cannot be predicted under actual conditions when the temperature gradient is not linear, i.e. the lapse rate is not linear per foot of altitude.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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User Instructions

7



STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Enter Program		<input type="button" value="RTN"/> <input type="button" value="R/S"/>	0.00
2	Initialize		<input type="button" value="GTO"/> <input type="button" value="1"/>	0.000000
3	Automatic input of U.S. Standard Atmosphere mean sea level values of Hg, temperature, lapse rate plus reference temperature absolute.		<input type="button" value="R/S"/> <input type="button" value="D"/>	459.688000
4	Input altitude and compute Hg.	Feet	<input type="button" value="E"/> <input type="button" value="RCL"/> <input type="button" value="6"/>	Hg
5	Compute temperature °F at altitude.		<input type="button" value="RCL"/> <input type="button" value="5"/>	°F
6	Recall °R at altitude.		<input type="button" value="GTO"/> <input type="button" value="2"/>	°R
7	To recall input altitude in step 4		<input type="button" value="R/S"/> <input type="button" value="A"/>	Feet
8	For new case change altitude input in step 4		<input type="button" value="A"/> <input type="button" value="B"/>	
9	Convert program to compute LBS/IN ² at altitude.		<input type="button" value="C"/> <input type="button" value="STO"/> <input type="button" value="7"/>	14.695949
10	Repeat steps 4 thru 8		<input type="button" value="D"/> <input type="button" value="E"/>	
11	Convert program to compute LBS/FT ² at altitude.	2116.216	<input type="button" value="A"/> <input type="button" value="RCL"/> <input type="button" value="6"/>	2116.216
12	Repeat steps 4 thru 8		<input type="button" value="B"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	
13	To compute pressure and temperature based upon other than U.S. Standard Atmosphere, input pressure reference at mean sea level.	Hg	<input type="button" value="A"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	Hg
14	Input temperature reference at MSL.	°R	<input type="button" value="B"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	°R
15	Input temperature lapse rate per foot of altitude in °F.	°F/FT.	<input type="button" value="C"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	°F/FT.
16	Repeat steps 4 thru 8.		<input type="button" value="D"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	
17	To compute the Standard Atmosphere in metric units, input millibars at MSL.	1013.25	<input type="button" value="A"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	1013.25
18	Input temperature reference at MSL in °K.	288.16	<input type="button" value="B"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	288.16
19	Input lapse rate per meter in °C.	.0065	<input type="button" value="C"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	0.0065
20	Input temperature abs reference in °K	273.16	<input type="button" value="STO"/> <input type="button" value="7"/>	273.16
21	Input altitude and compute pressure.	meters	<input type="button" value="D"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	mb
22	Compute temperature °C at altitude.		<input type="button" value="E"/> <input type="button" value="RCL"/> <input type="button" value="5"/>	°C
23	Recall °K at altitude.		<input type="button" value="RCL"/> <input type="button" value="6"/>	°K
24	For new case change altitude input in step 21.		<input type="button" value="RCL"/> <input type="button" value="5"/>	
			<input type="button" value="RCL"/> <input type="button" value="5"/>	
			<input type="button" value="RCL"/> <input type="button" value="5"/>	
			<input type="button" value="RCL"/> <input type="button" value="5"/>	
			<input type="button" value="RCL"/> <input type="button" value="5"/>	

97 Program Listing I

STEP			KEY ENTRY	KEY CODE	COMMENTS	STEP			KEY ENTRY	KEY CODE	COMMENTS		
001	*LBLA	21 16 11			Inputs U.S. Standards in program	057	ST02	35 02			Input MSL ref. temperature		
002	2	02				058	RTN	24					
003	9	09				059	*LBLC	21 13			Input temperature rate.		
004	.	-62				060	ST03	35 03					
005	9	09				061	RTN	24			Input altitude for desired pressure and computes P _A .		
006	2	02				062	*LBLD	21 14					
007	1	01				063	ST05	35 05					
008	2	02				064	RCL2	36 02					
009	6	06				065	ENT↑	-21					
010	ST01	35 01				066	ENT↑	-21					
011	5	05				067	RCL3	36 03					
012	1	01				068	RCL5	36 05					
013	8	08				069	x	-35					
014	.	-62				070	-	-45					
015	6	06				071	ST06	35 06					
016	8	08				072	÷	-24					
017	8	08			073	5	05						
018	ST02	35 02			074	.	-62						
019	.	-62			075	2	02						
020	0	00			076	5	05						
021	0	00			077	6	06						
022	3	03			078	1	01						
023	5	05			079	Y*	31						
024	6	06			080	RCL1	36 01						
025	6	06			081	X*Y	-41						
026	1	01			082	÷	-24						
027	6	06			083	RTN	24						
028	ST03	35 03			084	*LBLE	21 15			Computes °F or °C at altitude.			
029	4	04			085	RCL6	36 06						
030	5	05			086	RCL7	36 07						
031	9	09			087	-	-45						
032	.	-62			088	RTN	24						
033	6	06											
034	8	08											
035	8	08											
036	ST07	35 07											
037	DSP6	-63 06											
038	RTN	24											
039	*LBLB	21 16 12											
040	1	01											
041	4	04											
042	.	-62											
043	6	06											
044	9	09											
045	5	05											
046	9	09											
047	4	04											
048	8	08											
049	6	06											
050	1	01								SET STATUS			
051	ST01	35 01									FLAGS	TRIG	DISP
052	RTN	24											
053	*LBLA	21 11									ON OFF		
054	ST01	35 01									0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
055	RTN	24									1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input checked="" type="checkbox"/>	SCI <input type="checkbox"/>
056	*LBLB	21 12								2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input checked="" type="checkbox"/>	ENG <input type="checkbox"/>	
										3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>4</u>	
REGISTERS													
0	1	2	3	4	5	6	7	8	9				
P ₀ Ref.	T ₀ Ref.	Lapse Rate			Alt.-H	Temp. at H °R/°K	T abs ref.						
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9				
A	B	C	D	E	I								

Program Description I

Program Title Aircraft Flyover Acoustic Tone Doppler Shift
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables Computes doppler shift of an aircraft fly-over acoustic source frequency observed on the ground. Also determines the 1/3 octave-band filter, and location within the filter, of the observed frequency. Inputs are flight path speed and angle, air temperature, source frequency, and aircraft elevation angle. Any input frequency can be located in the A.N.S.I.* 1/3 octave-band filters. Equations: See sketch on next page.

Doppler shift $f_0/f_s = 1/(1-M \cos \beta)$ where $\begin{cases} f_0 & \text{is observed freq.} \\ f_s & \text{is source freq.} \\ M & \text{is Mach Number of source} \end{cases}$
 Source angle $\beta = \theta + \alpha$ $\begin{cases} \beta & \text{= Source angle to observe} \end{cases}$
 Mach number $Mach = V/(29.04\sqrt{t+459})$ $\begin{cases} V & \text{= Flt. path speed, kts} \\ T & \text{= Air temp, } ^\circ\text{F} \end{cases}$

*Mid-frequency of 1/3 oct-band $f_m = 10^{N/10}$, N any integer

*Upper frequency of 1/3 oct-band $f_2 = 1.1225 f_m$
(nominal band edge)

*American National Standards Institute

Operating Limits and Warnings 1/3 octave band filters start at $f_m = 50H_z$ which corresponds to $N=17$, ANSI convention. Minimum input frequency of 45 H_z .

f_m 's are exact preferred frequencies, which are within 0.7% of nominal preferred frequencies.

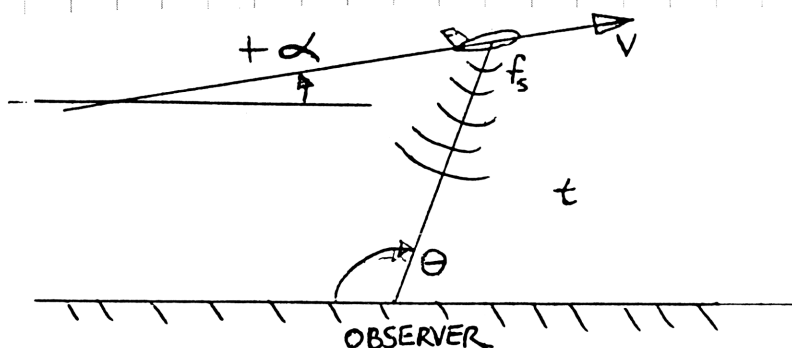
The time required for filter band location is a function of the band no., 3 sec < time < 34 sec for 17 < N < 40.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)



Sample Problem(s) Air temperature $t = 77^\circ\text{F}$

Given: Flight path angle $\alpha = -3^\circ$

Source tone frequency $f_s = 687 \text{ Hz}$

Flight path speed $V = 155 \text{ kts. (re to observer)}$

Calculate the Doppler shift, the observed frequency, the 1/3 oct. band filter position (f_0/f_m), the band number, and the filter mid-frequency for the following aircraft elevation angles.

$\theta_1 = 45 \text{ degrees}$

$\theta_2 = 90 \text{ degrees}$

$\theta_3 = 135 \text{ degrees}$

Aircraft Elev. Angle	$\theta_1 = 45^\circ$	$\theta_2 = 90^\circ$	$\theta_3 = 135^\circ$
f_0/f_s	1.21	1.01	0.87
f_0, Hz	829	695	595
f_0/f_m	1.04	1.10	0.94
Band No.	29	28	28
f_m, Hz	7.9×10^2 (nominal of 800)	6.3×10^2	6.3×10^2

Solutions:

Keystrokes:

Output

77[ENT+] 3[CHS] [A] 687[ENT+] 155[B]

45[C] --->1.21[R/S] --->829.04[D] --->1.04[R/S] 29[R/S] 7.9×10^2

etc.

Reference(s)

1. Wood, A.B., A Textbook of Sound, pages 370B-372, G. Bell & Sons, London, 1957.
2. S1.11-1966, Specification for Octave, Half-Octave, and Third-Octave Band Filter Sets, page 12, American National Standards Institute, New York, 1966.

This program is a translation of the HP-65 Users' Library program #01291A submitted Edgar L. Zwieback.

11

[illegible]

97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS		
001	*LBLA	21 11	Input t,α	057	0	00			
002	ST02	35 02		058	=	-24			
003	X÷Y	-41		059	10×	16 33			
004	ST04	35 04		060	ST07	35 07			
005	X÷Y	-41		061	1	01			
006	RTN	24		062	.	-62			
007	*LBLB	21 12		063	1	01			
008	ST03	35 03		064	2	02			
009	X÷Y	-41		065	2	02			
010	ST06	35 06		066	5	05			
011	RTN	24	Input f _s , V	067	×	-35			
012	*LBLC	21 13		068	RCL5	36 05			
013	FIX	-11		069	X>Y?	16-34			
014	DSP2	-63 02		070	ST01	22 01			
015	ST01	35 01		071	RCL7	36 07			
016	RCL4	36 04		072	RCL5	36 05			
017	4	04		073	X÷Y	-41			
018	5	05		074	÷	-24			
019	9	09		075	R/S	51			
020	+	-55		076	RCLI	36 46			
021	JX	54	f ₀ /f _s	077	CHS	-22	f/f _m		
022	2	02		078	1	01			
023	9	09		079	6	06			
024	.	-62		080	+	-55			
025	0	00		081	R/S	51			
026	4	04		082	RCL7	36 07			
027	×	-35		083	SCI	-12			
028	RCL3	36 03		084	DSP1	-63 01			
029	X÷Y	-41		085	RTN	24			
030	÷	-24						Band no.	
031	RCL1	36 01							
032	RCL2	36 02							
033	+	-55							
034	COS	42							
035	×	-35							
036	CHS	-22							
037	1	01							
038	+	-55							
039	1/X	52	f ₀ /f _s Doppler shift						
040	R/S	51							
041	RCL6	36 06							
042	×	-35							
043	ST05	35 05							
044	RTN	24							
045	*LBLD	21 14							
046	ST05	35 05							
047	0	00							
048	ST01	35 46							
049	*LBL1	21 01	Calc. upper freq. f _z of 1/3 oct- ban filters						
050	DSZI	16 25 46							
051	RCLI	36 46							
052	CHS	-22							
053	1	01							
054	6	06							
055	+	-55							
056	1	01							
REGISTERS									
0	1 θ,deg	2 α,deg	3 V,kts	4 t,°F	5 f ₀ /Hz	6 f _s ,Hz	7 f _m ,Hz	8 N	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A		B		C		D		E	

SET STATUS		
FLAGS	TRIG	DISP
ON OFF		
0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>2</u>

Program Description I

Program Title **ISENTROPIC FLOW FOR IDEAL GASES**

Contributor **HEWLETT-PACKARD**
 Address **1000 N. E. Circle Blvd.**
Corvallis, Oregon 97330
 City _____

State _____ Zip Code _____

Program D

This card replaces isentropic flow tables for a specified specific heat ratio k . Inputs and outputs are interchangeable with the exception of k .

The following values are correlated:

M is the Mach number;

T/T_0 is the ratio of flow temperature T to stagnation or zero velocity temperature T_0 ;

P/P_0 is the ratio of flow pressure P to stagnation pressure P_0 ;

ρ/ρ_0 is the ratio of flow density ρ to stagnation density ρ_0 ;

A/A^*_{sub} and A/A^*_{sup} are the ratios of flow area A to the throat area A^* in converging—diverging passages. A/A^*_{sub} refers to subsonic flow while A/A^*_{sup} refers to supersonic flow.

Equations:

$$T/T_0 = \frac{2}{2 + (k - 1) M^2}$$

$$P/P_0 = (T/T_0)^{k/(k-1)}$$

$$\rho/\rho_0 = (T/T_0)^{1/(k-1)}$$

$$A/A^* = \frac{1}{M} \left[\left(\frac{2}{k+1} \right) \left(1 + \frac{k-1}{2} M^2 \right) \right]^{\frac{k+1}{2(k-1)}}$$

In the last equation M^2 is determined using Newton's method. The initial guess used is as follows with a positive exponent for supersonic flow:

$$M_0^2 = (\sqrt{\text{Frac}(A/A^*)} + A/A^*)^{\pm 3}$$

Operating Limits

Remarks:

After an input of A/A^* , the program begins to iterate to find M^2 for future use. This iteration will normally take less than one minute, but may take longer on occasion. For extreme values of k (1.4 is optimum) the routine may fail to converge at all. An "Error" message will eventually halt the routine if it goes out of control.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description I

Program Title _____

Contributor's Name _____

Address _____

City _____

State _____

Zip Code _____

Program Description, Equations, Variables _____

A/A* values of 1.00 are illegal inputs. Instead, input an M of 1.00.

The calculator uses flag 3 to decide whether to store or calculate a value. If you use the data input keys (setting flag 3) and then wish to calculate a parameter based on a prior input, clear flag 3 before pressing the appropriate user definable keys.

Registers R_0 , R_5 and $R_{S0}-R_1$ are available for user storage.

Operating Limits and Warnings _____

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Example 1:

A pilot is flying at Mach 0.93 and reads on air temperature of 15 degrees Celsius (288 K) on a thermometer that reads stagnation temperature T_0 . What is the true temperature assuming that $k = 1.38$?

Keystrokes:

1.38 **f** **A** →
 .93 **A** →
B →
 288 **x** →
 273 **=** →

Outputs:

1.380
 0.930
 0.859 (T/T_0)
 247.352 (T , K)
 -25.648 (T , °C)

Sample Problem(s)

If the same pilot reads a stagnation pressure P_0 of 700 millimeters of mercury, what is the true air pressure?

(Since the data input flag was set when 288 was keyed in, we must either clear it, or input 0.93 again.)

.93 **A** **C** →
 700 **x** →

0.575 (P/P_0)
 402.843 (mm Hg)

Example 2:

A converging, diverging passage has supersonic flow in the diverging section. At an area ratio A/A^* of 1.60, what are the isentropic flow ratios for temperature, pressure and density? What is the Mach number? $k = 1.74$.

Keystrokes:

1.74 **f** **A** →
 1.60 **f** **E** →
B →
C →
D →

Outputs:

1.740
 2.105 (M)
 0.379 (T/T_0)
 0.102 (P/P_0)
 0.269 (ρ/ρ_0)

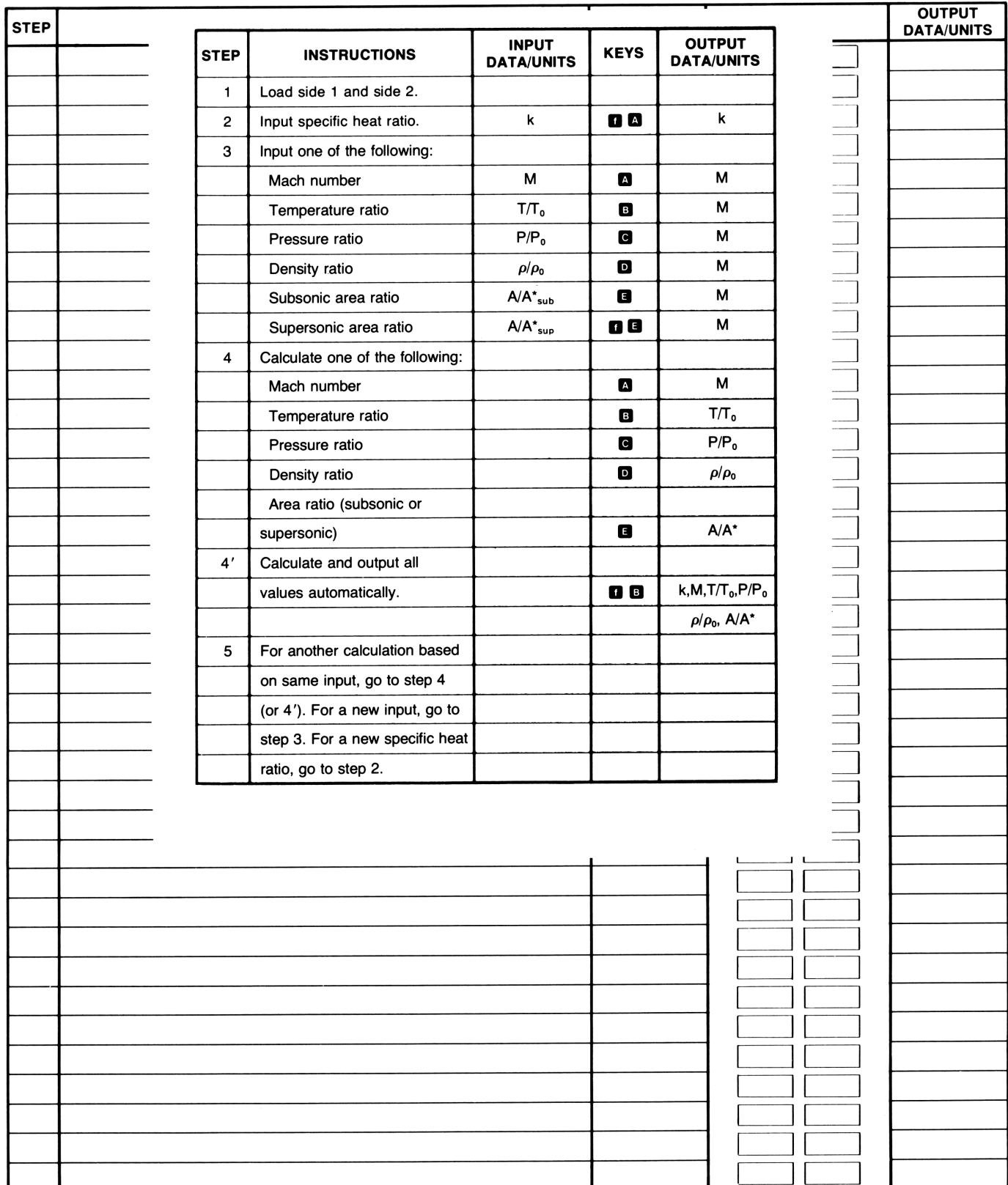
or, alternatively, using automatic output.

f **B** →

1.740 *** (k)
 2.105 *** (M)
 0.379 *** (T/T_0)
 0.102 *** (P/P_0)
 0.269 *** (ρ/ρ_0)
 1.600 *** (A/A^*)

Solution(s)

Reference(s)



97 Program Listing I

17

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 16 11	Store $k-1, 1/(k-1)$	057	SF3	16 21 03	Output ρ/ρ_0 .
002	ST02	35 02		058	GT0B	22 12	
003	1	01		059	*LBLD	21 14	
004	-	-45		060	F3?	16 23 03	
005	ST03	35 03		061	GT00	22 00	
006	1/X	52	Output M.	062	GSBB	23 12	Convert ρ/ρ_0 to T/T_0 and $GT_0 B$.
007	ST04	35 04		063	RCL4	36 04	
008	RCL2	36 02		064	Y*	31	
009	RTN	24		065	RTN	24	
010	*LBLA	21 11		066	*LBL0	21 00	
011	F3?	16 23 03	Store M^2 .	067	SF3	16 21 03	Set -3 in display for subsonic guess.
012	GT00	22 00		068	RCL3	36 03	
013	RCL1	36 01		069	Y*	31	
014	JX	54		070	GT0B	22 12	
015	RTN	24		071	*LBLE	21 15	
016	*LBL0	21 00	Output T/T_0 .	072	3	03	Make guess of M^2 .
017	X ²	53		073	CHS	-22	
018	ST01	35 01		074	X ² Y	-41	
019	JX	54		075	F3?	16 23 03	
020	RTN	24		076	GT01	22 01	Iterate by Newton's method to find M^2 corresponding to A/A^* .
021	*LBLB	21 12	Convert T/T_0 to M^2 .	077	GT03	22 03	
022	F3?	16 23 03		078	*LBL1	21 01	
023	GT00	22 00		079	ENT↑	-21	
024	2	02		080	ST06	35 06	
025	RCL1	36 01	Output P/P_0 .	081	FRC	16 44	
026	RCL3	36 03		082	JX	54	
027	x	-35		083	+	-55	
028	2	02		084	X ² Y	-41	
029	+	-55		085	Y*	31	
030	÷	-24	Convert P/P_0 to T/T_0 and $GT_0 B$.	086	ST01	35 01	
031	RTN	24		087	*LBL2	21 02	
032	*LBL0	21 00		088	RCL6	36 06	
033	2	02		089	GSB3	23 03	
034	X ² Y	-41		090	÷	-24	
035	÷	-24	Output P/P_0 .	091	1	01	
036	2	02		092	-	-45	
037	-	-45		093	.	-62	
038	RCL3	36 03		094	5	05	
039	÷	-24		095	RCL8	36 08	
040	ST01	35 01	Convert P/P_0 to T/T_0 and $GT_0 B$.	096	÷	-24	
041	JX	54		097	.	-62	
042	RTN	24		098	5	05	
043	*LBLC	21 13		099	RCL1	36 01	
044	F3?	16 23 03		100	÷	-24	
045	GT00	22 00	Convert P/P_0 to T/T_0 and $GT_0 B$.	101	-	-45	
046	GSBB	23 12		102	÷	-24	
047	RCL2	36 02		103	ST+1	35-55 01	
048	RCL3	36 03		104	RCL1	36 01	
049	÷	-24		105	÷	-24	
050	Y*	31	Convert P/P_0 to T/T_0 and $GT_0 B$.	106	ABS	16 31	
051	RTN	24		107	EEX	-23	
052	*LBL0	21 00		108	CHS	-22	
053	RCL3	36 03		109	4	04	
054	RCL2	36 02		110	X ² Y?	16-35	
055	÷	-24	Convert P/P_0 to T/T_0 and $GT_0 B$.	111	GT02	22 02	
056	Y*	31		112	RCL1	36 01	

REGISTERS

0	1	2	3	4	5	6	7	8	9
	M^2	k	k-1	1/k-1		A/A*		Used	Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

STEP	KEY ENTRY	KEY CODE	COMMENTS
113	JX	54	
114	RTN	24	
115	*LBL _e 21 16 15		Set +3 in display
116	3	03	for supersonic
117	XZY	-41	guess
118	F3? 16 23 03		
119	GTO1	22 01	
120	*LBL3 21 03		
121	2	02	Convert M ² to A/A*
122	RCL2	36 02	
123	1	01	
124	+	-55	
125	=	-24	
126	RCL3	36 03	
127	LSTX	16-63	
128	=	-24	
129	STO7	35 07	
130	RCL1	36 01	
131	x	-35	
132	+	-55	
133	STO8	35 08	
134	RCL7	36 07	
135	2	02	
136	x	-35	
137	1/X	52	
138	Yx	31	
139	RCL1	36 01	
140	JX	54	
141	=	-24	
142	RTN	24	
143	*LBL _b 21 16 12		Output values
144	SPC	16-11	
145	CF3 16 22 03		
146	RCL2	36 02	
147	PRTX	-14	
148	SPC	16-11	
149	GSBA	23 11	
150	PRTX	-14	
151	GSBB	23 12	
152	PRTX	-14	
153	GSBC	23 13	
154	PRTX	-14	
155	GSBD	23 14	
156	PRTX	-14	
157	GSBE	23 15	
158	PRTX	-14	
159	RTN	24	

Program Description I

Program Title Normal and Oblique Shock Parameters for Compressible Flow
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

Given the values for: free stream Mach number (M_1), the ratio of specific heats (γ), and the shock angle (θ); the program computes:

$$M_2 = \left[\frac{(\gamma+1)^2 M_1^4 \sin^2 \theta - 4(M_1^2 \sin^2 \theta - 1)(\gamma M_1^2 \sin^2 \theta + 1)}{[2\gamma M_1^2 \sin^2 \theta - (\gamma - 1)][(\gamma - 1)M_1^2 \sin^2 \theta + 2]} \right]^{1/2} \quad \text{Mach No. behind shock}$$

$$\frac{P_2}{P_1} = \frac{2\gamma M_1^2 \sin^2 \theta - (\gamma - 1)}{\gamma + 1} \quad \text{Static pressure ratio}$$

$$\frac{\rho_2}{\rho_1} = \frac{(\gamma + 1)M_1^2 \sin^2 \theta}{(\gamma - 1)M_1^2 \sin^2 \theta + 2} \quad \text{Density ratio}$$

$$\frac{T_2}{T_1} = \frac{[2\gamma M_1^2 \sin^2 \theta - (\gamma - 1)][(\gamma - 1)M_1^2 \sin^2 \theta + 2]}{(\gamma + 1)^2 M_1^2 \sin^2 \theta} \quad \text{Temperature ratio}$$

$$\frac{P_{T_2}}{P_{T_1}} = \left[\frac{(\gamma + 1)M_1^2 \sin^2 \theta}{(\gamma - 1)M_1^2 \sin^2 \theta + 2} \right]^{\frac{\gamma}{\gamma - 1}} \left[\frac{\gamma + 1}{2\gamma M_1^2 \sin^2 \theta - (\gamma - 1)} \right]^{\frac{1}{\gamma - 1}} \quad \text{Total pressure ratio}$$

Where the 1 subscript denotes the value upstream of the shock, and the 2 subscript denotes the value downstream of the shock.

Operating Limits and Warnings

Assumes calorically perfect (C_p and C_v are constant) and thermally perfect ($P = \rho RT$) gas, and adiabatic flow. Only solutions where $M_2 < M_1$; $\frac{P_2}{P_1}$, $\frac{\rho_2}{\rho_1}$, $\frac{T_2}{T_1} > 1$ and $\frac{P_{T_2}}{P_{T_1}} < 1$ are valid. If any one of these conditions is satisfied, the other four are satisfied.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample Problem(s)

1. Find the Mach number and static pressure behind an oblique shock where $M_1 = 2.5$, $\theta = 70^\circ$, $\gamma = 1.4$ and $P_1 = 85$ psi. Also find the ratios across the shock for density, temperature and total pressure. (See Fig. 1)
2. Find the temperature, Mach number and total pressure behind a normal shock ($\theta = 90^\circ$) where $M_1 = 6.23$, $\gamma = 1.4$, $P_{T_1} = 64$ psi and $T_1 = 624^\circ R$ (See Fig. 2)

Solution(s)

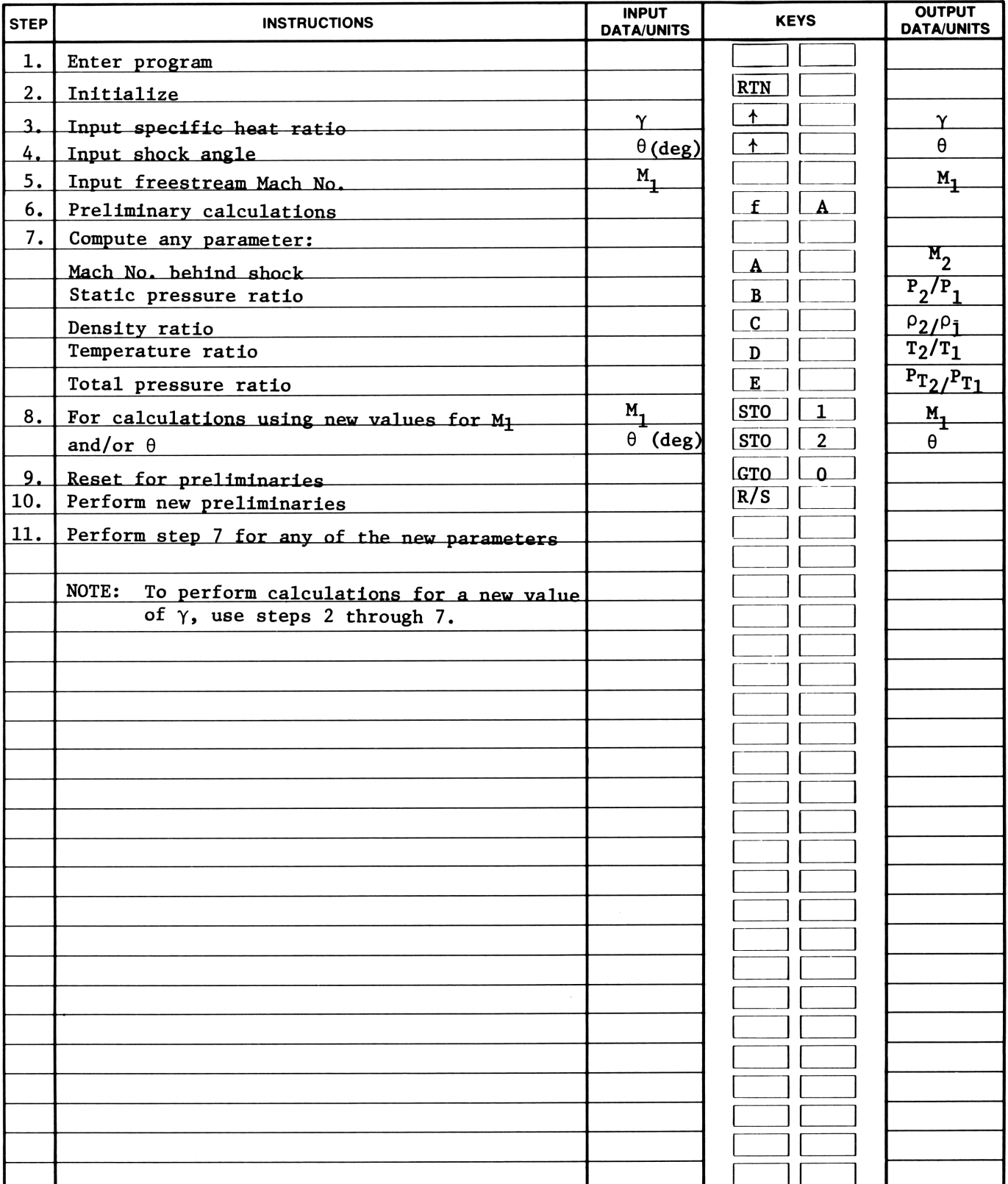
- | | | | | | | | | |
|----|--------------|----------|------------|-------|---------|---------------------|----------------------------------|----------------------------|
| 1. | 1.4 [+] | 70 [+] | 2.5 [f] | [a] | [A] | ----- | 0.80 (M) | |
| | [B] | ----- | | | | | 6.27 (P_2/P_1) | |
| | 85 [X] | ----- | | | | | 533.12 (psi) (P_2) | |
| | [C] | ----- | | | | | 3.15 (P_2/P_1) | |
| | [D] | ----- | | | | | 1.99 (T_2/T_1) | |
| | [E] | ----- | | | | | 0.56 (P_{T_2}/P_{T_1}) | |
| 2. | 6.23 [ST0] | [] | 90 [ST0] | [2] | [GT0] | [0] [R/S] [D] | ----- | 8.49 ($\frac{T_2}{T_1}$) |
| | 624 [X] | ----- | | | | | 5296.40 ($^\circ R$) (T_2) | |
| | [A] | ----- | | | | | 0.40 (M_2) | |
| | [E] | ----- | | | | | .30 (P_{T_2}/P_{T_1}) | |
| | 64 [X] | ----- | | | | | 1.62 (psi) (P_{T_2}) | |

Reference(s)

National Advisory Committee for Aeronautics, Report 1135, Equations, Tables and Charts for Compressible Flow, By Ames Research Staff, pgs. 7,8, U.S. Government Printing Office, 1953.

This program is a translation of the HP-65 Users' Library program #01303A submitted by Glenn D. Rambach.

21



97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBL0	21 16 11		057	*LBLB	21 12	Compute P_2/P_1
002	ST01	35 01		058	RCL3	36 03	
003	R↓	-31	Store M_1 in R_1	059	RCL4	36 04	
004	ST02	35 02	Store θ in R_2	060	x	-35	
005	R↓	-31		061	2	02	
006	ST03	35 03	Store γ in R_3	062	x	-35	
007	1	01		063	RCL7	36 07	
008	-	-45		064	-	-45	
009	ST07	35 07		065	RCL8	36 08	
010	2	02		066	÷	-24	
011	+	-55		067	RTN	24	Display P_2/P_1
012	ST08	35 08		068	*LBLC	21 13	Compute ρ_2/ρ_1
013	*LBL0	21 00	Initial point for repeated operations	069	RCL5	36 05	
014	RCL2	36 02		070	RCL6	36 06	
015	SIN	41		071	2	02	
016	RCL1	36 01		072	+	-55	
017	x	-35		073	÷	-24	
018	X ²	53		074	RTN	24	Display ρ_2/ρ_1
019	ST04	35 04		075	*LBLD	21 14	Compute T_2/T_1
020	RCL8	36 08		076	GSBB	23 12	
021	x	-35		077	GSBC	23 13	
022	ST05	35 05		078	÷	-24	
023	RCL7	36 07		079	RTN	24	
024	RCL4	36 04		080	*LBLE	21 15	Display T_2/T_1
025	x	-35		081	GSBC	23 13	
026	ST06	35 06		082	GSBB	23 12	Compute P_{T_2}/P_{T_1}
027	R/S	51		083	÷	-24	
028	*LBLA	21 11	Compute M_2	084	RCL7	36 07	
029	RCL5	36 05		085	1/X	52	
030	RCL8	36 08		086	Y*	31	
031	x	-35		087	GSBC	23 13	
032	RCL1	36 01		088	x	-35	
033	X ²	53		089	RTN	24	Display P_{T_2}/P_{T_1}
034	x	-35					
035	RCL4	36 04					
036	RCL3	36 03					
037	x	-35					
038	1	01					
039	+	-55					
040	4	04					
041	x	-35					
042	RCL4	36 04					
043	1	01					
044	-	-45					
045	x	-35					
046	-	-45					
047	GSBC	23 13					
048	x	-35					
049	GSBB	23 12					
050	÷	-24					
051	RCL8	36 08					
052	÷	-24					
053	RCL5	36 05					
054	÷	-24					
055	Y*	54					
056	RTN	24	Display M_2				

REGISTERS

0	1 M_1	2 θ	3 γ	4 $M_1^2 \sin^2 \theta$	5 $(\gamma+1)M_1^2$	6 $(\gamma-1)M_1^2$	7 $\gamma-1$	8 $\gamma+1$	9
S0	S1	S2	S3	S4	$\sin^2 \theta$	$\sin^2 \theta$	S7	S8	S9
A	B	C	D	E	I				

SET STATUS

FLAGS	TRIG	DISP
ON OFF		
0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>2</u>

Program Description I

Program Title Oblique Shock Angle for Wedge
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

When the upstream Mach number, the deflection angle and the specific heat ratio are given the compressible flow equation will give at most three values for the shock angle. This program calculates the weak oblique shock angle when it is possible.

The equation which must be solved is

$$\sin^6 \sigma + b \sin^4 \sigma + c \sin^2 \sigma + d = 0$$

where

$$b = - \frac{M_1^2 + 2}{M_1^2} - k \sin^2 \delta$$

$$c = \frac{2M_1^2 + 1}{M_1^4} + \left[\frac{(k+1)^2}{4} + \frac{k-1}{M_1^2} \right] \sin^2 \delta$$

$$d = - \frac{\cos^2 \delta}{M_1^4}$$

M_1 = Upstream Mach number > 1.0

δ = Deflection angle (deg)

k = Specific heat ratio

σ = Shock angle (D.M.S.)

Operating Limits and Warnings

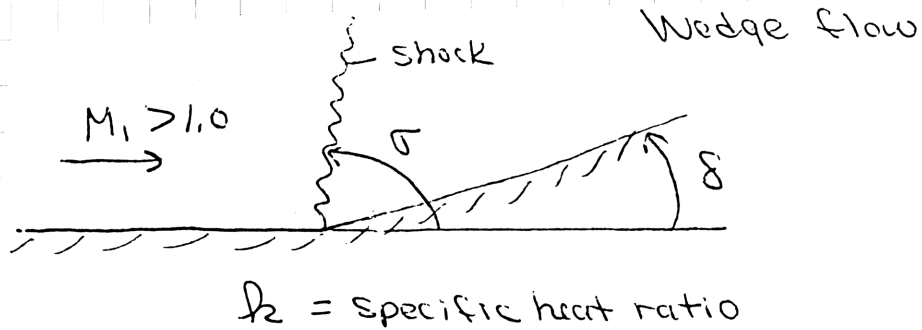
If no shock condition is possible, i.e., if the shock must detach from the corner, then the first program card stops with a blinking display. If δ approaches δ_{\max} for the flow the program takes some time (1 min or so) to converge. I have never had the program fail to converge, although it may be possible. Should convergence not occur, change the calculator to the DEG mode after the iteration is stopped.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)



Sample Problem(s) Given

$$M_1 = 2.0$$

$$\delta = 10^\circ$$

$$k = 1.4$$

$$\sigma = 39.3139 \text{ Deg}$$

Solution(s)

Keystrokes:

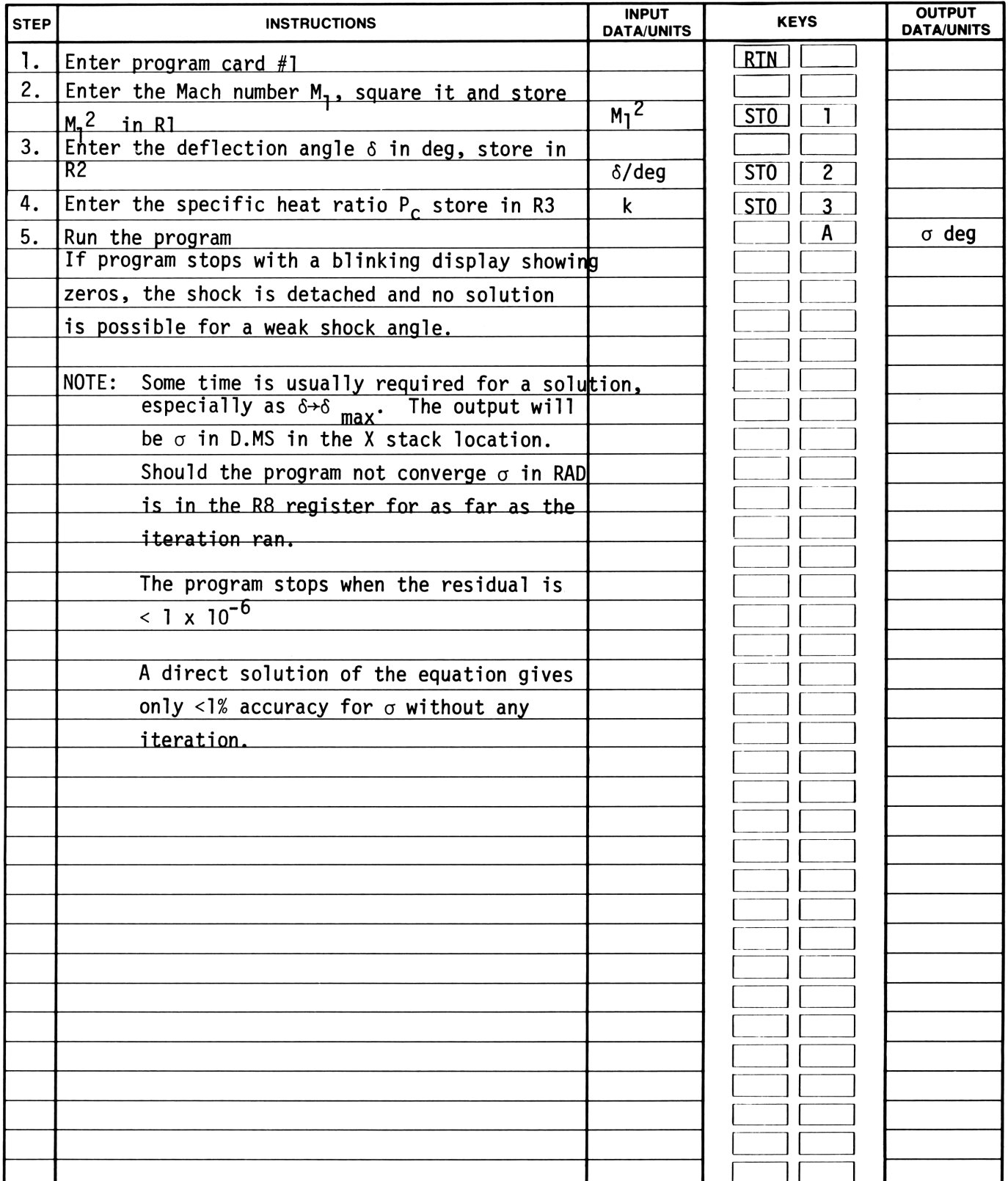
Outputs:

2[x²] [STO] [1] 10 [STO] [2] 1.4 [STO] [3] [A] -----> 39.3139

Reference(s) 1. Introductory Gas Dynamics, A.J. Chapman and W.F. Walker, HRW Series in Mech. Engineering.

This program is a translation of the HP-65 Users' Library program #00630A submitted by Harry W. Townes.

25



97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11		057	ENT↑	-21	
002	RCL2	36 02		058	X	-35	
003	SIN	41		059	-	-45	
004	ENT↑	-21		060	ST07	35 07	
005	X	-35		061	RCL4	36 04	
006	ST07	35 07		062	RCL5	36 05	
007	RCL3	36 03		063	X	-35	
008	X	-35		064	3	03	
009	RCL1	36 01		065	X	-35	
010	2	02		066	RCL6	36 06	
011	+	-55		067	-	-45	
012	RCL1	36 01		068	2	02	
013	÷	-24		069	÷	-24	
014	+	-55		070	RCL4	36 04	
015	CHS	-22		071	ENT↑	-21	
016	3	03		072	ENT↑	-21	
017	÷	-24		073	X	-35	
018	ST04	35 04	b/3 R4	074	X	-35	
019	RCL3	36 03		075	-	-45	
020	1	01		076	ST08	35 08	
021	+	-55		077	RCL7	36 07	
022	ENT↑	-21		078	ENT↑	-21	
023	X	-35		079	ENT↑	-21	
024	4	04		080	X	-35	
025	÷	-24		081	X	-35	
026	RCL3	36 03		082	ST06	35 06	
027	1	01		083	RCL8	36 08	
028	-	-45		084	ENT↑	-21	
029	RCL1	36 01		085	X	-35	
030	÷	-24		086	+	-55	
031	+	-55		087	0	00	
032	RCL7	36 07		088	X≠Y?	16-35	Test for existance of weak shock Blinking display for no solution possible
033	X	-35		089	1/X	52	
034	RCL1	36 01		090	RCL2	36 02	
035	2	02		091	TAN	43	
036	X	-35		092	ST02	35 02	
037	1	01		093	RAD	16-22	
038	+	-55		094	RCL8	36 08	
039	RCL1	36 01		095	RCL6	36 06	
040	ENT↑	-21		096	CHS	-22	
041	X	-35		097	JX	54	
042	÷	-24		098	÷	-24	
043	+	-55		099	COS ⁻¹	16 42	
044	3	03		100	Pi	16-24	
045	÷	-24		101	4	04	
046	ST05	35 05	C/3 R5	102	X	-35	
047	RCL2	36 02		103	+	-55	
048	COS	42		104	3	03	
049	RCL1	36 01		105	÷	-24	
050	ENT↑	-21		106	COS	42	
051	X	-35		107	RCL7	36 07	
052	÷	-24		108	CHS	-22	
053	CHS	-22		109	JX	54	
054	ST06	35 06	d R6	110	X	-35	
055	RCL5	36 05		111	2	02	
056	RCL4	36 04		112	X	-35	

REGISTERS

0	1 M ₁ ²	2 δ and ton δ	3 k	4 Used	5 Used	6 Used	7 Used	8 σ in RAD	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

97 Program Listing II

27

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
113	RCL4	36 04	σ in RAD from direct solution of the equation. Iteration improves accuracy. A R/S in step 30 would eliminate iteration	169	SIN	41	
114	-	-45		170	-	-45	
115	JX	54		171	\div	-24	
116	SIN ⁻¹	16 41		172	CHS	-22	
117	ST08	35 08		173	RCL1	36 01	
118	.	-62		174	-	-45	
119	0	00		175	RTN	24	
120	1	01					
121	ST06	35 06					
122	RCL8	36 08					
123	+	-55		180			
124	GSB0	23 00					
125	ST07	35 07					
126	RCL8	36 08					
127	GSB0	23 00					
128	RCL7	36 07					
129	X \leftrightarrow Y	-41					
130	-	-45					
131	RCL6	36 06					
132	\div	-24					
133	ST07	35 07		190			
134	*LBL1	21 01					
135	RCL8	36 08					
136	GSB0	23 00					
137	RCL7	36 07					
138	\div	-24					
139	ST-8	35-45 08					
140	RCL8	36 08					
141	\div	-24					
142	ABS	16 31					
143	EEX	-23	σ in deg after convergence	200			
144	CHS	-22					
145	6	06					
146	X \leftrightarrow Y?	16-35					
147	GT01	22 01					
148	RCL8	36 08					
149	R \leftrightarrow D	16 46					
150	RTN	24					
151	*LBL0	21 00					
152	ST05	35 05					
153	TAN	43		210			
154	1/X	52					
155	RCL2	36 02					
156	+	-55					
157	2	02					
158	x	-35					
159	RCL5	36 05					
160	2	02					
161	x	-35					
162	ST05	35 05					
163	COS	42		220			
164	RCL3	36 03					
165	+	-55					
166	RCL2	36 02					
167	x	-35					
168	RCL5	36 05					

LABELS					FLAGS	SET STATUS		
A	B	C	D	E	0	FLAGS	TRIG	DISP
σ						ON OFF		
a	b	c	d	e	1	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
0	1	2	3	4	2	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5	6	7	8	9	3	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>4</u>

Program Description I

Program Title Mach Number and True Airspeed
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables, etc.

This program converts calibrated airspeed (CAS) to mach number and true airspeed (TAS). Pressure altitude (PALT) must be known to calculate mach number (M). Aircraft recovery coefficient (C_T) and indicated air temperature (IT) must also be known to calculate true airspeed. The recovery coefficient varies from 0.6 to 1.0 but is around 0.8 for most aircraft.

$$\text{Pressure ratio} \left(\frac{P}{P_0} \right) = \left[\frac{518.67 - 3.566 \times 10^{-3} \text{ PALT}}{518.67} \right]^{5.2563}$$

$$M^2 = 5 \left[\left(\frac{P_0}{P} \right) \left\{ \left[1 + 0.2 \left(\frac{\text{CAS}}{661.5} \right)^2 \right]^{3.5} - 1 \right\} + 1 \right]^{0.286}$$

$$\text{TAS} = 39M \sqrt{(IT + 273) \left[C_T \left(\frac{1}{(1 + 0.2 M^2)} - 1 \right) + 1 \right]}$$

Operating Limits and Warnings

Accuracy degenerates for mach numbers in excess of one.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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[illegible]

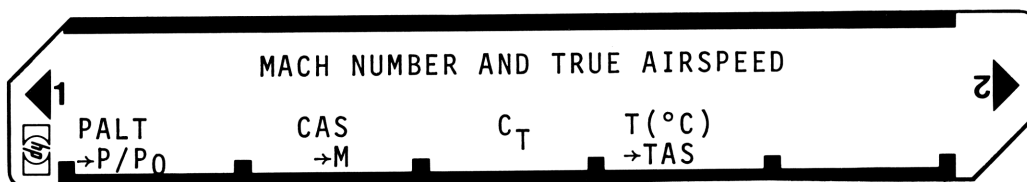
Sample Problem(s)

For a pressure altitude of 25,500 feet, a calibrated airspeed of 350 knots, a recovery factor of 0.8, and an indicated air temperature of 5 degrees Celsius, what is the flight mach number and the true airspeed?

Solution(s)	
M = 0.84	
TAS = 515.76 knots	
Keystrokes	See Displayed
25500 A 350 B	0.84
.8 C 5 D	515.76

Reference(s) _____
This program is a translation of the HP-65 Users' Library program
#00531B submitted by Hewlett-Packard.

User Instructions



STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Enter program *		<input type="text"/> <input type="text"/>	
2	Input pressure altitude	PALT	<input type="text"/> A <input type="text"/>	P/P ₀
3	Input calibrated airspeed in		<input type="text"/> <input type="text"/>	
	knots and calculate mach		<input type="text"/> <input type="text"/>	
	number	CAS	<input type="text"/> B <input type="text"/>	M
4	Input recovery coefficient		<input type="text"/> <input type="text"/>	
	(.8 for most aircraft)	C _T	<input type="text"/> C <input type="text"/>	C _T
5	Input indicated air temperature		<input type="text"/> <input type="text"/>	
	and calculate true airspeed		<input type="text"/> <input type="text"/>	
	in knots	IT (°C)	<input type="text"/> D <input type="text"/>	TAS
6	For same aircraft at same		<input type="text"/> <input type="text"/>	
	PALT go to step 3 and skip		<input type="text"/> <input type="text"/>	
	step 4. For different PALT go		<input type="text"/> <input type="text"/>	
	to step 2 and skip step 4. For		<input type="text"/> <input type="text"/>	
	totally new case go to step 2.		<input type="text"/> <input type="text"/>	

*For pressure altitudes above 36089 feet, calculate P/P₀ using *Standard Atmosphere*,

97 Program Listing I

31

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11	Convert pressure altitude to pressure ratio	057	ST04	35 04	Input recovery coefficient
002	3	03		058	RTH	24	
003	5	05		059	*LBLC	21 13	
004	6	06		060	ST03	35 03	
005	6	06		061	RTN	24	
006	EEX	-23		062	*LBLD	21 14	
007	CHS	-22		063	2	02	
008	6	06		064	7	07	Calculate TAS
009	x	-35		065	3	03	
010	CHS	-22		066	+	-55	
011	5	05		067	ST05	35 05	
012	1	01		068	RCL4	36 04	
013	8	08		069	GSBE	23 15	
014	.	-62		070	=	-24	
015	6	06		071	RCL5	36 05	
016	7	07		072	-	-45	
017	+	-55		073	RCL3	36 03	
018	LSTX	16-63		074	x	-35	
019	=	-24		075	RCL5	36 05	
020	5	05		076	+	-55	
021	.	-62		077	JX	54	
022	2	02		078	3	03	
023	5	05		079	3	09	
024	6	06		080	x	-35	
025	3	03		081	RCL4	36 04	
026	Y*	31		082	x	-35	
027	ST06	35 06	Convert CAS to mach number	083	RTN	24	
028	RTN	24		084	*LBLE	21 15	
029	*LBLB	21 12		085	ENT↑	-21	
030	6	06		086	x	-35	
031	6	06		087	.	-62	
032	1	01		088	2	02	
033	.	-62		089	x	-35	
034	5	05		090	1	01	
035	=	-24		091	+	-55	
036	GSBE	23 15		092	RTN	24	
037	3	03					
038	.	-62					
039	5	05					
040	Y*	31					
041	1	01					
042	-	-45					
043	RCL6	36 06					
044	=	-24		100			
045	1	01					
046	+	-55					
047	.	-62					
048	2	02					
049	8	08					
050	6	06					
051	Y*	31					
052	1	01					
053	-	-45					
054	5	05		110			
055	x	-35					
056	JX	54					

REGISTERS									
0	1	2	3 C _T	4 M	5 T	6 P/P ₀	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

SET STATUS					
FLAGS		TRIG		DISP	
ON	OFF				
0	<input type="checkbox"/>	<input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>	
1	<input type="checkbox"/>	<input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>	
2	<input type="checkbox"/>	<input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>	
3	<input type="checkbox"/>	<input checked="" type="checkbox"/>		n <u>2</u>	

Program Description I

Program Title	TAKE-OFF RUN VS. DENSITY ALTITUDE		
Contributor's Name	Hewlett-Packard, Corvallis Division		
Address	1000 N. E. Circle Blvd.		
City	Corvallis	State	OR
		Zip Code	97330

Program Description, Equations, Variables

$$A_D = 145366 \left[1 - \left(\frac{\rho}{\rho_0} \right)^{0.235} \right] \quad \text{Density altitude}$$

$$\rho/\rho_0 = (288/T_{0K}) (1 - 6.87 \times 10^{-6} A_p)^{5.256}$$

where A_p = Pressure altitude (Ft)

$$F = 1 + 2.18 \times 10^{-5} A_D + 2.032 \times 10^{-8} A_D^2$$

$$D_A = (D_{STD}/W_G) \cdot W_A \cdot F$$

where

D_A = Actual take-off run (Ft)

D_{STD} = Sea level take-off run at 15°C and full gross weight

W_G = Gross weight

W_A = Actual take-off weight

Operating Limits and Warnings Computed value of D_A is an approximation to be tempered by caution and good sense. It depends on runway surface condition, aircraft condition, pilot skill; assumes zero wind. No provision for obstructions.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample Problem(s) Land performance of a popular twin engine amphibian is a ground run of 965 feet (sea level) at 15°C at full gross weight of 6,000 lbs.

How much runway will it require at Laramie, Wyoming (elev, 7300 ft.) on a summer day when outside air temperature is 35°C (95°F) and plane is loaded to 5750 lbs?

Solution(s) $965/6000 = .1608$ - Aircraft parameter to be inserted in program at LBL 1.

A_D (density altitude) = 11094 ft

D_A (actual take-off distance) = 3461 ft

Outpoints:

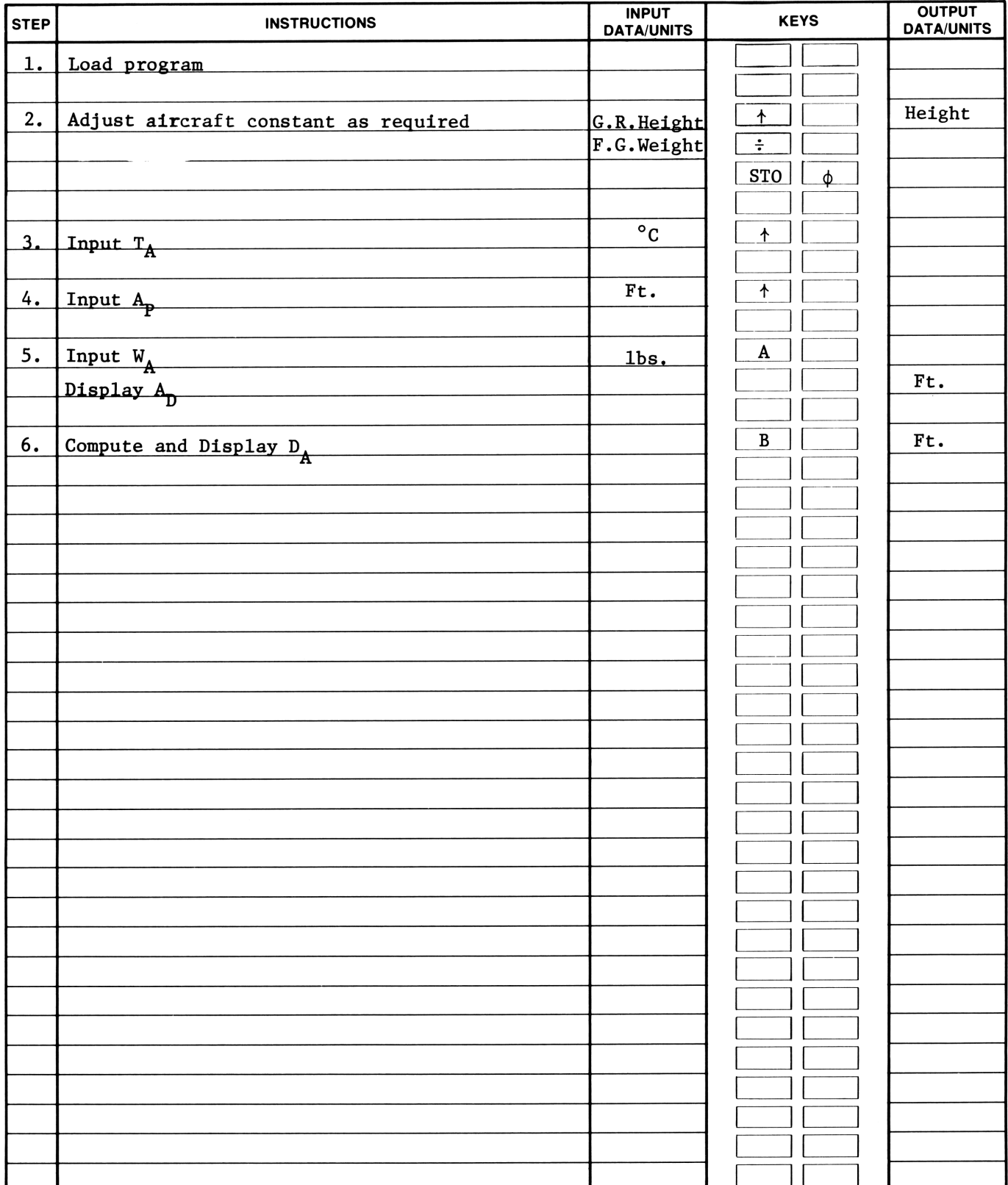
Keystrokes: 965[ENT ↑] 6000[+][STD][O] 35[ENT ↑] 7300[ENT ↑] 5750[A] → 11094

[B] → 3461

Reference(s) 1) HP-65 Users' Library Program #532A

2) "AOPA Handbook for Pilots - 1974", page 15 (F VS A_D)

3) "Aerodynamics of the airplane", Millikan, John Wiley & Sons, 1941, page 132.



97 Program Listing I

35

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS		
001	*LBLA	21 11	W _A (Take off Wt.) A _P (Pressure Alt.) Temp. °k	057	ENT↑	-21	A _D ² D _A (Actual Take-Off Distance, Ft.)		
002	DSP0	-63 00		058	2	02			
003	ST01	35 01		059	.	-62			
004	R↓	-31		060	1	01			
005	ST02	35 02		061	8	08			
006	R↓	-31		062	EEX	-23			
007	2	02		063	CHS	-22			
008	7	07		064	5	05			
009	3	03		065	X	-35			
010	ST03	35 03		066	1	01			
011	+	-55		067	+	-55			
012	ST04	35 04		068	XZY	-41			
013	6	06		069	ENT↑	-21			
014	.	-62		070	X	-35			
015	8	08		071	2	02			
016	7	07		072	.	-62			
017	6	06		073	0	00			
018	EEX	-23		074	3	03			
019	CHS	-22		075	2	02			
020	6	06		076	EEX	-23			
021	RCL2	36 02		077	CHS	-22			
022	X	-35	078	8	08				
023	CHS	-22	079	X	-35				
024	1	01	080	+	-55				
025	+	-55	081	RCL0	36 00				
026	5	05	082	X	-35				
027	.	-62	083	RCL1	36 01				
028	2	02	084	X	-35				
029	5	05	085	RTN	24				
030	6	06	086	R/S	51				
031	Y*	31							
032	RCL3	36 03							
033	1	01							
034	5	05	090						
035	+	-55							
036	X	-35							
037	RCL4	36 04							
038	÷	-24							
039	.	-62							
040	2	02							
041	3	03							
042	5	05							
043	Y*	31							
044	CHS	-22	100						
045	1	01							
046	+	-55							
047	1	01							
048	4	04							
049	5	05							
050	3	03							
051	6	06							
052	6	06							
053	X	-35							
054	RTN	24	110						
055	*LBLB	21 12							
056	ENT↑	-21							
REGISTERS									
0	1 W _A	2 A _P	3 273	4 T°k	5	6	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

Program Description I

Program Title TRUE AIR TEMPERATURE AND DENSITY ALTITUDE

Contributor's Name Hewlett-Packard, Corvallis Division

Address 1000 N. E. Circle Blvd.

City Corvallis **State** OR **Zip Code** 97330

Program Description, Equations, Variables This program accounts for the compressibility effects of high speed flight. Given the mach number (M) and the aircraft recovery coefficient ($C_T = 0.8$ for most aircraft), indicated air temperature (IT) is converted to true air temperature (T). True air temperature and pressure altitude are then converted to density altitude. For low flight mach numbers, compressibility effects are small. In such cases only temperature and pressure altitude (PALT) are needed to calculate density altitude (DALT).

$$T(K) = C_T \left(\frac{IT(K)}{0.205 M^2 + 1} - IT \right) + IT(K)$$

$$DALT = 145366 \left[1 - \left(\frac{\rho}{\rho_0} \right)^{0.235} \right]$$

where

$$\frac{\rho}{\rho_0} = \frac{288.15}{T(K)} \left[1 - 6.879 \times 10^{-6} PALT \right]^{5.256}$$

Operating Limits and Warnings

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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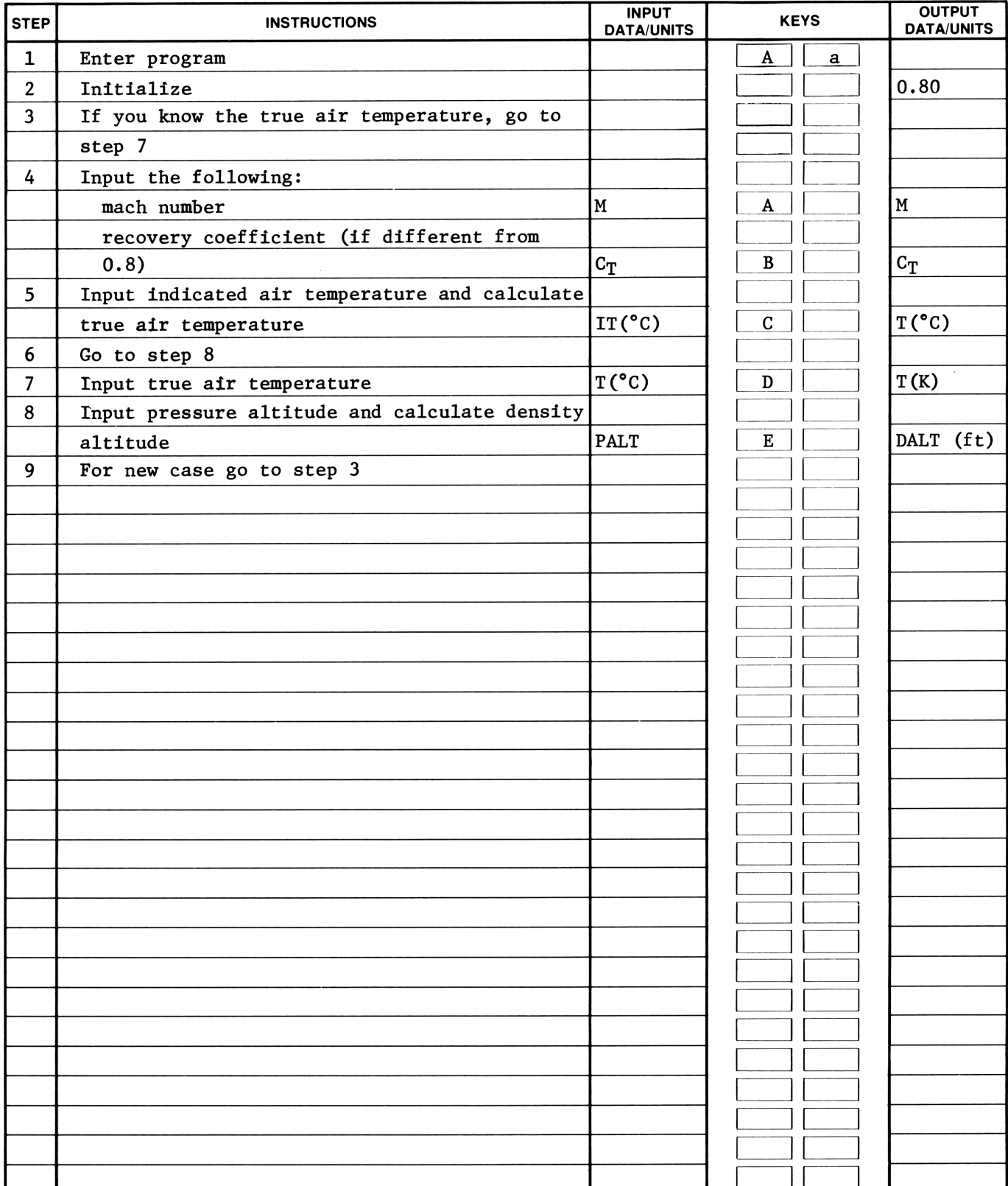
[illegible]

Sample Problem(s)

1. $M = 0.87$
 $C_T = 0.80$
 $IT = 8^\circ\text{C}$
 $PALT = 10,000 \text{ ft}$
2. For a low speed aircraft
 $T = 12^\circ\text{C}$
 $PALT = 9,000 \text{ ft}$

Solution(s)	1. T = -22.21°C	
	DALT = 7852.96 ft	
	2. DALT = 10,703.11 ft	
	Keystrokes [f][a]	See Displayed
	1. .87[A]8[C]	-22.21
	10000[E]	7852.96
	2. 12[D]9000[E]	10703.11

Reference(s) This program is a translation of the HP-65 Users' Library Program
#00532A Submitted by User's Library.



39

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 16 11		057	1	01	
002	.	-62		058	+	-55	
003	8	08	Initialize	059	5	05	
004	ST03	35 03		060	.	-62	
005	RTN	24		061	2	02	
006	*LBLA	21 11		062	5	05	
007	ST04	35 04	Input mach number	063	6	06	
008	RTN	24		064	Y*	31	
009	*LBLB	21 12		065	RCL6	36 06	
010	ST03	35 03		066	1	01	
011	RTN	24	Input recovery	067	5	05	
012	*LBLC	21 13	factor	068	+	-55	
013	GSBD	23 14		069	X	-35	
014	RCL4	36 04		070	RCL5	36 05	
015	ENT†	-21		071	=	-24	
016	X	-35		072	.	-62	
017	.	-62	Calculate true	073	2	02	
018	2	02	temperature	074	3	03	Calculate density
019	0	00		075	5	05	altitude
020	5	05		076	Y*	31	
021	X	-35		077	CHS	-22	
022	1	01		078	1	01	
023	+	-55		079	+	-55	
024	=	-24		080	1	01	
025	RCL5	36 05		081	4	04	
026	-	-45		082	5	05	
027	RCL3	36 03		083	3	03	
028	X	-35		084	6	06	
029	RCL5	36 05		085	6	06	
030	+	-55		086	X	-35	
031	ST05	35 05		087	RTN	24	
032	RCL6	36 06					
033	-	-45					
034	RTN	24		090			
035	*LBLD	21 14					
036	2	02					
037	7	07	Convert T(°C) to				
038	3	03	T(K) and store it.				
039	.	-62					
040	1	01					
041	5	05					
042	ST06	35 06					
043	+	-55					
044	ST05	35 05		100			
045	RTN	24					
046	*LBLE	21 15					
047	6	06					
048	.	-62					
049	8	08					
050	7	07					
051	9	09					
052	EEX	-23					
053	CHS	-22					
054	6	06	Calculate density	110			
055	X	-35	ratio				
056	CHS	-22					

SET STATUS

FLAGS	TRIG	DISP
<div style="display: flex; justify-content: space-between;"> ON OFF </div> <div style="display: flex; justify-content: space-between;"> <div>0 <input type="checkbox"/> <input checked="" type="checkbox"/></div> <div>1 <input type="checkbox"/> <input checked="" type="checkbox"/></div> <div>2 <input type="checkbox"/> <input checked="" type="checkbox"/></div> <div>3 <input type="checkbox"/> <input checked="" type="checkbox"/></div> </div>	<div style="display: flex; justify-content: space-between;"> <div>DEG <input checked="" type="checkbox"/></div> <div>GRAD <input type="checkbox"/></div> <div>RAD <input type="checkbox"/></div> </div>	<div style="display: flex; justify-content: space-between;"> <div>FIX <input checked="" type="checkbox"/></div> <div>SCI <input type="checkbox"/></div> <div>ENG <input type="checkbox"/></div> <div>n <input type="text" value="2"/></div> </div>

REGISTERS

0	1	2	3 C _T	4 M	5 T(K)	6 273.15	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9

A

B

C

D

E

I

Program Description I

Program Title Aircraft Climb

Contributor's Name Carroll F. Lam

Address 4411 Random Ct.

City Annadale

State VA

Zip Code 22003

Program Description, Equations, Variables

Given current and new higher altitudes, A_1 and A_2 , and associated headwinds at these altitudes, W_1 and W_2 , this program will compute the following:

$$1. D_{\min} = [(V_{cr} - V_{cl}) + (\frac{W_1 - W_2}{2})] (\frac{V_{cr} - W_1}{W_1 - W_2}) T_c$$

where: V_{cr} = cruise air speed
 V_{cc} = climb air speed
 T_c = time to climb, A_1 to A_2

$$2. T_{\text{climb}} = \frac{A_m}{ROC_{\max}} \ln \left(\frac{A_m - A_1}{A_m - A_2} \right)$$

where: A_m = aircraft ceiling
 ROC_{\max} = sea level rate-of-climb

$$3. T_{\text{act}} = \frac{D_{\text{act}} - [V_{cl} - (\frac{W_1 + W_2}{2})] T_c}{V_{cr} - W_2} + T_c$$

$$4. T_{\text{save}} = \frac{D_{\text{act}}}{V_{cr} - W_1} - T_{\text{act}}$$

Operating Limits and Warnings

$$W_1, W_2 \geq 0$$

$$A_2 > A_1$$

$$D_{\text{act}} > D_{\min} \text{ if steps 9,10,11 are to be used.}$$

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description I

Program Title Aircraft Climb

Contributor's Name Carroll F. Lam

Address 4411 Random Ct.

City Annandale State VA Zip Code 22003

Program Description, Equations, Variables (con't)

The equation for D_{\min} is derived by setting up an equation for the two time possibilities for traveling between points A and B_1 and solving for the D that assures that the travel time based on climbing to a higher altitude with a smaller headwind component is less than the travel time that would result from remaining at altitude A_1 .

Although the program doesn't incorporate it, there would in general be an additional benefit in climbing to a higher altitude, namely a higher true airspeed will generally result.

Operating Limits and Warnings

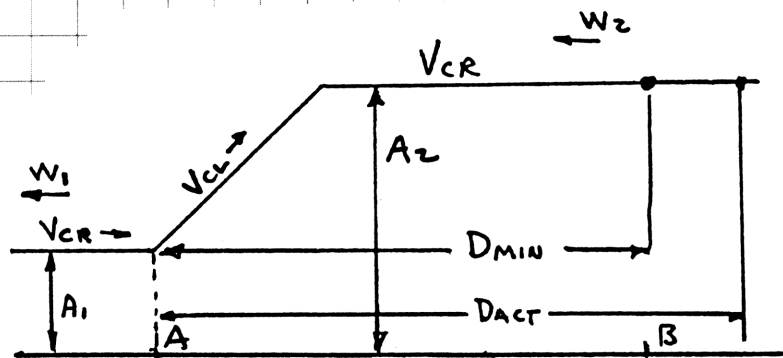
See previous page.

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Program Description II

Sketch(es)



Sample Problem(s)

Assumed aircraft parameters: $V_{cr} = 150$ mph
 $V_{cl} = 85$ mph
 $ROC_{max} = 850$ ft/min
 $A_{max} = 18.5$ kft

Given: Current Altitude (A_1) = 3.5 kft
 Current Headwind Component (W_1) = 38 mph
 Potential Altitude (A_2) = 11.5 kft
 Headwind Component at A_2 (W_2) = 10 mph
 Distance Remaining (D_{act}) = 185 miles

Find: 1. Distance required for climb to breakeven
 2. Time to fly distance remaining if climb is made
 3. Time saved by climbing to higher altitude
 4. Time to climb to new altitude

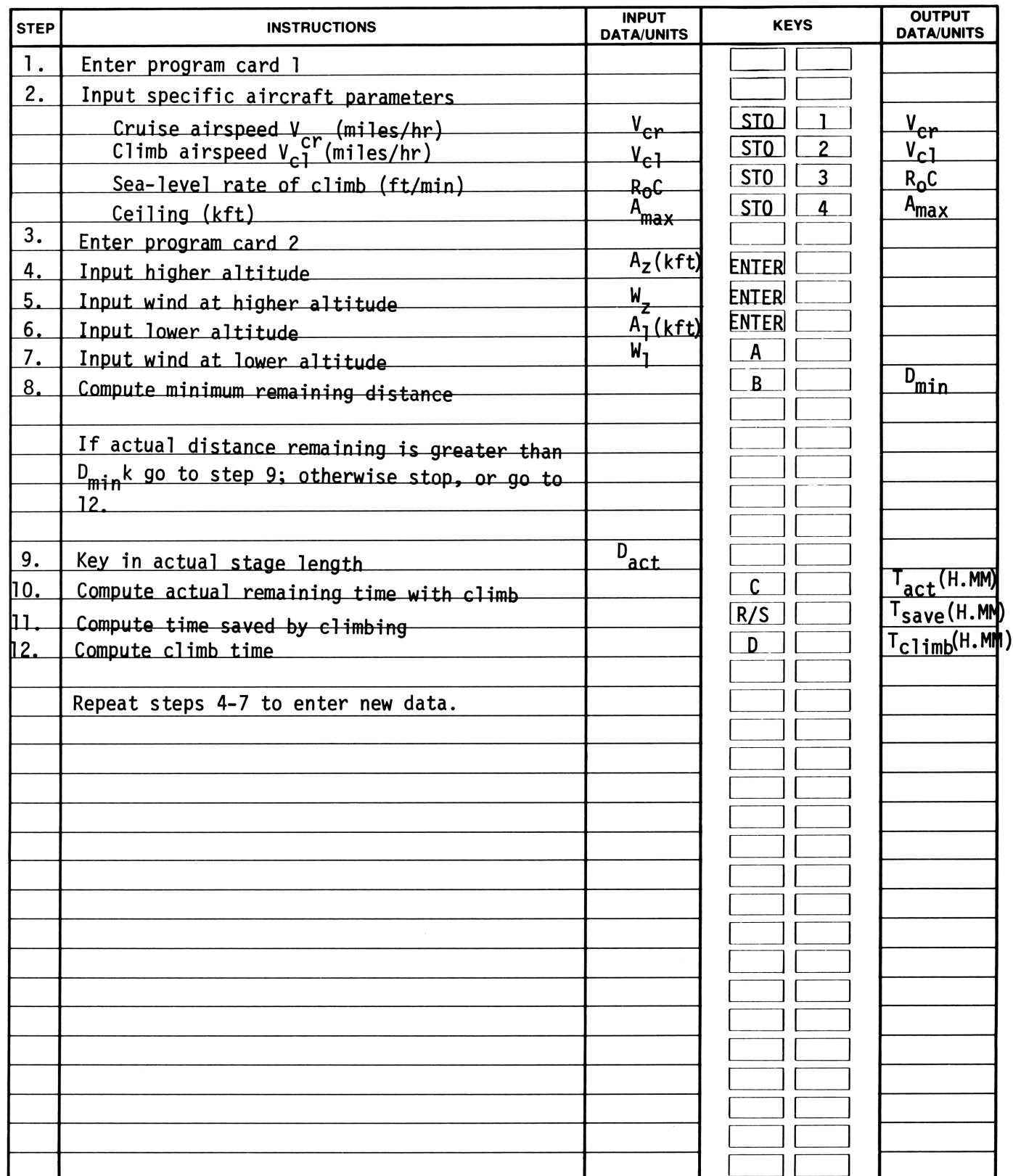
Solution(s) 150[STO] [1] 85[STO] [2] [850] [STO] [3] 18.5 [STO] [4]
 11.5 [ENTER] ----- Store A_2 11.50
 10 [ENTER] ----- Store W_2 10.50
 3.5 [ENTER] ----- Store A_1 3.50
 38 [A] ----- Store W_1 11.50
 1. [B] ----- Compute D_{min} 87.54
 2. 185 [C] ----- Compute T_{act} for 185 miles 1.28 (1 hr, 28 mins)
 3. [R/S] ----- Compute T_{saved} 0.10 (10 mins)
 4. [D] ----- Compute T_{climb} 0.16 (16 mins)

Reference(s) Equations (1),(2), and (4) are submitter's own derivations based on the geometry of the problem.

Equation (3) is based on an assumption that ROC varies lineary with altitude
 $[ROC(A) = A_{max} (1 - \frac{A}{A_{max}})]$ and straight forward integration. See any good aeronautical engineering text.

This program is a translation of the HP-65 Users Library program # 01815A submitted by Carroll F. Lam.

43



NOTES

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