

CALCULATING LOGS, ANTI-LOGS, AND ROOTS OF NUMBERS

GENERAL

This Application Note will be of assistance to those HP-80 owners who require the ability to calculate *common and natural logarithms, anti-logarithms (base 10 and base e), and the "nth" root of a number.*

COMMON (BASE 10) AND NATURAL (BASE e) LOGARITHMS

The following keystrokes will simultaneously calculate the common logarithm (log) and natural logarithm (ln) of a number (B).

Keystrokes:

- 900 **i** 1 **PV** B **FV** **n** \longrightarrow log B (Base 10)
- x \rightarrow y** \longrightarrow ln B (Base e)

Example:

Determine the common logarithm and natural logarithm of 256.

Procedure:

- 900 **i** 1 **PV** 256 **FV** **n** \longrightarrow 2.41
(log, base 10)
- x \rightarrow y** \longrightarrow 5.55
(ln, base e)

See Displayed:

LOGARITHMS FOR ANY BASE

The following keystrokes solve for the exponent c in the equation $A^c = B$ when A and B are known. This procedure may be labeled "finding the logarithm of B to the base A ".

The natural logarithm of B will again be available in the y register.

Keystrokes:

- A **SAVE** \uparrow 1 **-** 100 **x** **i** 1 **PV** B **FV** **n** \longrightarrow c
- x \rightarrow y** \longrightarrow ln B (base e)

Example:

Find the exponent c in the equation: $16^c = 4096$

Procedure:

- 16 **SAVE** \uparrow 1 **-** 100 **x** **i** 1 **PV** 4096 **FV** **n** \longrightarrow 3.00
(log 4096, base 16)
- x \rightarrow y** \longrightarrow 8.32
(ln 4096, base e)

See Displayed:

Note:

When calculating logarithmic values, features that are required for other purposes are being used. Specifically, when solving for **n** in the compound interest equation,

$$FV = PV (1 + i/100)^n$$

the HP-80 uses natural logarithms and the expression becomes;

$$n = \frac{\ln (FV/PV)}{\ln (1 + i/100)}$$

Therefore, the keystroke sequence, 900 **i** 1 **PV** B **FV** **n**, results in the following solution:

$$n = \frac{\ln (B/1)}{\ln 1 + \frac{900}{100}} = \frac{\ln(B)}{\ln (10)} = \log B \text{ (base 10).}$$

Similarly the keystroke sequence,

A **SAVE** 1 **-** 100 **x** **i** 1 **PV** B **FV** **n**, gives:

$$\frac{\ln B}{\ln A} = \log B \text{ (base A)}$$

As an intermediate step the HP-80 places the $\ln (FV/PV)$ in the y register, and for the values discussed this becomes $\ln (B/1)$ or simply $\ln B$ (base e).

ANTI-LOGARITHMS (BASE e)

The following keystrokes solve for B in the equation $e^c = B$, where e is the base of natural logarithms, and the exponent c is the natural logarithm of B. Step 1 generates the value of e correct to 9 decimal places.

Keystrokes:

- 1. 1.000001 **SAVE** 1000000 **y^x** → 2.718281828
- 2. c **y^x** → B

Example:

Determine the number whose natural logarithm equals 2.36.

Procedure:

See Displayed:

- 1. 1.000001 **SAVE** 1000000 **y^x** → 2.72
- 2. 2.36 **y^x** → 10.59

Note:

Since a portion of the value of e repeats itself some will find it easier to remember 2.718281828 than the keystrokes that generate this number. In this case step 1 may be replaced by simply entering e and pressing **SAVE**.

ANTI-LOGARITHMS (BASE 10)

The following keystrokes solve for B in the equation $10^c = B$ where the exponent c is the common logarithm of B.

Keystrokes:

- 10 **SAVE** c **y^x** → B

10 **SAVE** 2.41 **y^x** → 257.04

“nth” ROOT OF A NUMBER

The key sequence, A **Gold Key** **y^x**, where A is a positive number, will calculate the 2nd root (i.e., square root) of A. This operation is commonly written as \sqrt{A} or $\sqrt[2]{A}$. However, the square root of A may also be written in mathematical notation as

$$A^{1/2}$$

and in this form it may be said that A is being raised to the $\frac{1}{2}$ power. A more general representation for finding the “nth” root of a number would therefore be:

$$A^{1/n}$$

where $n = 2$ for square or 2nd root, $n = 3$ for cube or 3rd root, and so on. Since the **y^x** key will raise a positive number to any power, the HP-80 may be used to calculate the “nth” root of positive numbers as shown below.

Keystrokes:

A **SAVE** 1 **SAVE** n **÷** **y^x** → “nth” root of A

Example:

Find the cube (3rd) root of 6859.

Procedure:

6859 **SAVE** 1 **SAVE** 3 **÷** **y^x** → *See Displayed:* 19.00