# HP 39gll graphing calculator 

## user's guide

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## Printing History

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## Preface

## Manual conventions

The following conventions are used in this manual to represent the keys that you press and the menu options that you choose to perform the described operations.

- Key presses are represented as follows:

- Shift keys, that is the key functions that you access by pressing the shatial key first, are represented as follows:

- Numbers and letters are represented normally, as follows:

5, 7, A, B, etc.

- Menu options, that is, the functions that you select using the menu keys at the top of the keypad are represented as follows:


## STO $¥$ CANCL, DOK.

- Input form fields and choose list items are represented as follows:

Function, Polar, Parametric

- Your entries as they appear on the command line or within input forms are represented as follows:
$2 * x^{2}-3 x+5$


## Notice

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The programs that control your HP 39gll are copyrighted and all rights are reserved. Reproduction, adaptation, or translation of those programs without prior written permission from Hewlett-Packard Company is also prohibited.

For Hardware warranty information, please refer to the HP 39gll Quick Start Guide.
For Product Regulatory and Environment Information, please refer to the HP 39gll Quick Start Guide.

## Getting started

## On/off, cancel operations

## To turn on

To cancel

To turn off

The Home view

Protective cover

Press $[\mathrm{ON} / \mathrm{C}$ to turn on the calculator.
When the calculator is on, the $\mathrm{OF}_{\mathrm{OF} / \mathrm{C}}$ key cancels the current operation.

Press off to turn the calculator off.
To save power, the calculator turns itself off after several minutes of inactivity. All stored and displayed information is saved.

If you see the 四, annunciator, then the calculator needs fresh batteries.

Home is the calculator's home view and is common to all apps. If you want to perform calculations, or you want to quit the current activity (such as an app, a program, or an editor), press $\substack{\text { tome } \\ \text { Hodeses }}$. All mathematical functions are available in the Home view. The name of the current app is displayed in the title of the home view.

The calculator is provided with a slide cover to protect the display and keyboard. Remove the cover by grasping both sides of it and pulling down.
You can reverse the slide cover and slide it onto the back of the calculator. This will help you keep track of the cover while you are using the calculator.
To prolong the life of the calculator, always place the cover over the display and keyboard when you are not using the calculator.

## The display

To adjust the contrast

To adjust the contrast, press and hold ${ }^{\circ N / C / C}$, then press the $\left.\Sigma^{+}\right]$or $\tau^{-}$w keys to increase or decrease the contrast. The contrast will change with each press of the $\left.\Sigma^{+}\right]$or $c^{-}$w keys.

To clear the display - Press CANCEL to clear the edit line.

- Press CLEAR once to clear an active edit line and again to clear the display history.


## Parts of the display



Menu key labels. The top row of keys on the HP 39gll keyboard (F1-F6) are the menu keys. These keys give you access to the menu items shown at the bottom of the display. STO- is the label for the first menu key in the figure above. "Press STO-" means press the F1 menu key.

Edit line. The line of current entry.
History. The Home display ( of history: the most recent input and output. Older lines scroll off the top of the display but are retained in memory.

Title. The name of the current app is displayed at the top of the Home view. RAD or DEG specifies whether Radians or Degrees is the current angle measurement mode. The $\boldsymbol{\nabla}$ and $\mathbf{\Delta}$ symbols indicate there is more history in the display. Press $\odot$ and $\odot$ to scroll in the history display.

Annunciators. Annunciators are symbols that appear above the title bar and give you important status information.

| Annunciator | Description |
| :---: | :---: |
| 6 | To activate, press Shtir . Shift in effect for next keystroke. To cancel, press shill again. |
| A.. Z | To activate, press $\square$ . Alpha in effect for next keystroke. To lock, press $\square$ again. To cancel, press $\square$ a third time. |
| a..z | To activate, press $\square$ . Lower-case alpha in effect for next keystroke. To lock, press again. To cancel, press a third time. To switch to uppercase, press $\square$ |
| 四 | Low battery power. |
| Z | Busy. |
| 口-0 | Data is being transferred via cable. |

## The keyboard

| Number | Feature | HP 39gll |
| :---: | :---: | :---: |
| 1 | $256 \times 128$ pixel display |  |
| 2 | Context-sensitive menu | HP 39gll <br> Grophing Colculator |
| 3 | F1-F6 menu keys | $\square^{\text {m }}$ Az ${ }^{2 z}$ |
| 4 | HP Apps keys | 1 |
| 5 | Modes |  |
| 6 | Common math and science functions | (0amiracep |
| 7 | Shift keys | [回 |
| 8 | On (cancel) | $(-15$ |
| 9 | Last Answer (ANS) |  |
| 10 | Enter key | $6 \xrightarrow{\rightarrow} \rightarrow \infty$ |
| 11 | Alphabetic entry | $\square \square^{2}+12$ |
| 12 | Catalogs and editors | $\therefore 0$ |
| 13 | Backspace (Clear) |  |
| 14 | Help key |  |
| 15 | Cursor keys | $-9$ |
| 16 | USB Connectivity |  |

Menu keys

- On the calculator keyboard, the keys in the top row of keys (labeled F1-F 16) are called menu keys. Their meanings depend on the context; that is, the view you are in.
- The bottom line of the display shows the labels for the menu keys' current meanings.

App control keys
The app control keys are:

| Key | Meaning |
| :--- | :--- |
| S. <br> Smbu <br> semp | Displays the Symbolic view <br> for the current app. |


| Key | Meaning (Continued) |
| :---: | :---: |
| (Plot <br> Selup | Displays the Plot view for the current app. |
| Num | Displays the Numeric view for the current app. |
| ( $\begin{aligned} & \text { Home } \\ & \text { Modes }\end{aligned}$ | Displays the Home view, for performing calculations. |
| $\underbrace{\text { ate }}_{\substack{\text { Apps } \\ \text { lito }}}$ | Displays the App Library menu. |
| (Views | Displays the VIEWS menu. |

## Entry/Edit keys

The entry and edit keys are:

| Key | Meaning |
| :---: | :---: |
| ON/C (CANCEL) | Cancels the current operation if the calculator is on by pressing ON/C. Pressing shlire, then OFF turns the calculator off. <br> Accesses the function printed at the bottom left of a key. |
| AIPFA | Accesses the alphabetical characters printed at the bottom right of a key. Press allent twice to lock this shift so you can enter a string of characters. |
| ENTER | Enters an input or executes an operation. In calculations, $\underset{\text { ANS }}{\text { ENTER }}$ acts like " $=$ ". When OK or START is present as a menu key, ENTER acts the same as pressing OK or START. |
| ${ }_{\text {ABS }}(\underline{(H)}$; | Enters a negative number. To enter -25 , press $\widehat{A B S}_{(-)}^{(-)}$25. Note: this is not the same operation that the subtraction key performs ( $\Sigma^{-} \mathrm{w}$ ). |


| Key | Meaning (Continued) |
| :---: | :---: |
| (exten | Enters the independent variable by inserting $X, T, \theta$, or $N$ into the edit line, depending on the current active app. <br> Backspace. Deletes the character to the left of the cursor. |
|  | Clears all data on the screen. On a settings screen, for example Plot Setup, SHHIT CLEAR returns all settings to their default values. <br> Moves the cursor around the display. Press shlir first to move to the beginning, end, top or bottom. <br> Displays a menu of all available characters. To type one, use the arrow keys to highlight it, and press <br> OK. To select multiple characters, select each and press ECHO, then press OK. |

## Shifted keystrokes

There are two shift keys that you use to access the operations and characters printed on the bottom of the keys: and alata

| Key | Description |
| :---: | :---: |
| Stlic | Press to access the operations printed on the bottom (or bottom left) of a key. For instance, to access the Modes input form, press and then press Hences because Modes is printed on the bottom of the Home key. |


| Key | Description (Continued) |
| :---: | :---: |
| AIPHA | Press the $\square$ key to access the alphabetic character printed on the bottom right of a key. For instance, to type $Z$, press $\square$ and then press $\pi^{3} Z$ because $Z$ is printed on the bottom right of the $\pi^{3}$ key. For a lower case letter, press antam then shlim To type more than one letter, press $\square$ a second time to lock the Alpha shift. |

Help

 system. The Help system always opens in your current context or view, giving you information about the current view and its menu items. Once in the Help system, you can navigate to other topics and find help on any view or command.

## Example:

Press $\xlongequal[\substack{\text { Apps } \\ m i m}]{ }$ and select Function. Press to get help on the purpose of the Function App.

## Math keys

Home (
Keyboard keys. The most common operations are available from the keyboard, such as the arithmetic (like $\left.\mathrm{E}^{+}\right]$) and trigonometric (like $\frac{\sin }{\text { sin } e}$ ) functions. Press (ENTER to complete the operation: SHITM 256 displays 16.

Math menu. Press ${ }_{c}^{\text {Matat }}$ to open the Math menu. The Math menu is a comprehensive list of math functions that do not appear
 on the keyboard. It also includes categories for all other functions and constants. The functions are grouped by category, ranging in alphabetical order from Calculus to Trigonometry.

- Use the up- and down-arrow keys to scroll through the list. Use the right- and left-arrow keys to move between the category and item columns.
- Press OK to insert the selected command into the edit line at the curent cursor position.
- Press CANCL to dismiss the Math menu without selecting a command.
- Press LINTS to attach units to a number in the edit line.
- Press FHYS to display a menu of physical constants from the fields of chemistry, physics, and quantum mechanics. You can use these constants in calculations.
- Press MATH to return to the Math menu.

See the chapter Using Mathematical Functions for details.

Program
commands

Inactive keys

When using the Math menu, or any menu on the HP 39gll, the categories and items are numbered for your convenience. For example, ITERATE is the first item under Loop, which is the eighth category. With the Math menu open, press ${ }^{8}{ }_{8}$ Prgm $\times$ to insert the ITERATE function in the edit line at the cursor position. If there are more than 9 items in a category, the letters $A, B, C$, etc. are used. For example, the Matrix category uses the number 8. In this category, the RREF command uses the letter H . With the Math menu open, press $\mathrm{Ca}_{\mathrm{R}} \mathrm{e}^{\mathrm{LN}}{ }_{\mathrm{H}}$ to insert the RREF command into the edit line. You do not need to press alpha to access the letter you want.

Pressing CMDS displays the list of Program Commands. See the chapter Programming for more details.

If you press a key that does not operate in the current context, a warning symbol like this appears. There is no beep.

## Menus

To search a menu
$\uparrow$ or $\uparrow$, you'll go all the way to the end or the beginning of the list. Highlight the item you


- If there are two columns, the left column shows general categories and the right column shows specific contents within a category. Highlight a general category in the left column, then highlight an item in the right column. The list in the right column changes when a different category is highlighted.
- If there are three columns, the left column shows a general category while the second column shows a useful sub-category. Highlight a general category, then highlight a sub-category of interest. Finally, select an item from the third column.
- To speed-search a list, type the number or letter of the category, followed by the number or letter of the item.

press $4{ }^{7}{ }^{7}$.
Press ${ }_{0}^{0 N / C /}$ (for CANCEL) or CANCL. This cancels the current operation.


## Input forms

An input form shows several fields of information for you to examine and specify. After highlighting the field to edit, you can enter or edit a number (or expression). You can also select options from a list (CHOOS). Some input forms include items to check (CHK ). See below for example input forms.



Reset input form values

To reset a field to its default value in an input form, move the cursor to that field and press clear . To reset all field values in the input form to their default values, press $\qquad$ CLEAR.

## Mode settings

You use the Modes input form to set the modes for Home.
HIN T Although the numeric setting in Modes affects only Home, the angle setting controls Home and the current app. The angle setting selected in Modes is the angle setting used in both Home and the current app. To further configure an app, you use the SETUP keys ( SHin and ssilia

Press shire form. Press PAGE $\mathbb{P}$ (F4) to enter the second page of the form and press PAGE (F3) to return to the first page

| Setting | Options |
| :--- | :--- |
| Angle | Angle values are: <br> Degrees. 360 degrees in a circle. <br> Radians. $2 \pi$ radians in a circle. <br> The angle mode you set is the angle <br> setting used in both Home and the <br> current app. This is done to ensure that <br> trigonometric calculations done in the <br> current app and Home give the same <br> result. |


| Setting | Options (Continued) |
| :---: | :---: |
| Number Format | The number format mode you set is the number format used in all Home view calculations. <br> Standard. Full-precision display. Fixed. Displays results rounded to a number of decimal places. Example: 123.456789 becomes 123.46 in Fixed 2 format. <br> Scientific. Displays results with an exponent, one digit to the left of the decimal point, and the specified number of decimal places. Example: 123.456789 becomes $1.23 E 2$ in Scientific 2 format. <br> Engineering. Displays result with an exponent that is a multiple of 3 , and the specified number of significant digits beyond the first one. Example: 123.456 E 7 becomes 1.23 E 9 in Engineering 2 format. |
| Complex | If checked, allows operations involving complex numbers; if unchecked, only real-number operations are allowed. |
| Language | Choose language preference for menus and input forms. |
| Font Size | Choose a smaller or larger font for most display purposes. |
| Calculator Name | Calculator NameEnter a descriptive name to identify your calculator to the HP 39gll Connectivity Kit. |
| Textbook Display | Disable or enable Textbook Format Display for expressions entered in the Home and Symbolic views. |

## Setting a mode

This example demonstrates how to change the angle measure from the default mode, radians, to degrees for
the current app. The procedure is the same for changing number format, language, and complex number modes.

1. Press SHITI MODES to open the Home Modes input form.
The cursor (highlight) is in the first field, Angle Measure.

| Home Modes |  |  |
| :---: | :---: | :---: |
| Angle Measure: Radians |  |  |
| Number Format: Standard |  |  |
| Language: English |  |  |
| Complex: - |  |  |
| Choose Angle Measure |  |  |
| CHOOS | PAGE 7 |  |

2. Press choos to display a list of choices.

3. Use the up- and downarrow keys to select Degrees and press OK. The angle measure changes to
 degrees.
4. Press $\xlongequal{\substack{\text { Home } \\ \text { Modes }}}$ to return to Home.

HINT Whenever an input form has a list of choices for a field, you can press $\Sigma^{+}$_ to cycle through them instead of using choos.

## Mathematical calculations

The most commonly used math operations are available from the keyboard. Access to the rest of the math functions is via the Math menu ( ${ }_{c}^{\mathrm{C}_{\mathrm{mas}} \mathrm{B}} \mathrm{B}$ ).
To access programming commands, press SHIIT CMDS. See the chapter Programming for more information.

Where to start
The home base for the calculator is the Home view ( $\left.\begin{array}{l}\text { Home } \\ \text { Modss }\end{array}\right)$ ). You can do all calculations here, and you can


## Entering expressions

## Example

- Enter an expression into the HP 39 gll in the same left-to-right order that you would write the expression. This is called algebraic entry.
- To enter functions, select the key or Math menu item for that function. You can also enter a function by using the Alpha keys to spell out its name.
- Press 舟TER $^{\text {N }}$ to evaluate the expression you have in the edit line (where the blinking cursor is). An expression can contain numbers, functions, and variables.
Calculate $\frac{23^{2}-14 \sqrt{8}}{-3} \ln (45)$ :


Long results

## Negative numbers

If the result is too long to fit on the display line, or if you want to see an expression in textbook format, press to highlight it and then press SHOW

Type $\int_{\text {ass }}^{(-)}$; to start a negative number or to insert a negative sign.

To raise a negative number to a power, enclose it in parentheses. For example, $(-5)^{2}=25$, whereas $-5^{2}=$ -25 .

A number like $5 \times 10^{4}$ or $3.21 \times 10^{-7}$ is written in scientific notation, that is, in terms of powers of ten. This is simpler to work with than 50000 or 0.000000321 . To enter numbers like these, use EEx. This is easier than using $4 x^{x} 100^{x}$.
Calculate $\frac{\left(4 \times 10^{-13}\right)\left(6 \times 10^{23}\right)}{3 \times 10^{-5}}$


## Explicit and implicit multiplication

## ENTER ANS

Implied multiplication takes place when two operands appear with no operator in between. If you enter $A B$, for example, the result is $A * B$.

However, for clarity, it is better to include the multiplication sign where you expect multiplication in an expression. It is clearest to enter AB as $\mathrm{A} * \mathrm{~B}$.

You need to use parentheses to enclose arguments for functions, such as $\operatorname{SIN}(45)$. You can omit the final parenthesis at the end of an edit line. The calculator inserts it automatically.

Parentheses are also important in specifying the order of operation. Without parentheses, the HP 39gll calculates according to the order of algebraic precedence (the next topic). Following are some examples using parentheses.

| Entering... | Calculates... |
| :---: | :---: |
|  | $\begin{aligned} & \sin (45+\pi) \\ & \sin (45)+\pi \\ & \sqrt{85} \times 9 \\ & \sqrt{85 \times 9} \end{aligned}$ |

> Algebraic precedence order of evaluation

Functions within an expression are evaluated in the following order of precedence. Functions with the same precedence are evaluated in order from left to right.

1. Expressions within parentheses. Nested parentheses are evaluated from inner to outer.
2. Prefix functions, such as SIN and LOG.
3. Posffix functions, such as !
4. Power function, ^, NTHROOT.
5. Negation, multiplication, and division.
6. Addition and subtraction.
7. AND and NOT.
8. OR and XOR.
9. Left argument of | (where).
10. Equals, $=$.

The HP 39 gll represents $1 \times 10^{-499}$ (as well as all numbers smaller than this) as zero. The largest number displayed is $9.99999999999 \times 10^{499}$. A greater result is displayed as this number.

- dear deletes the character to the left of the cursor; that is, it is a backspace key.
- CANCEL $(\underset{O N}{O N} / \mathrm{C})$ clears the edit line.
- SLIF CLEAR clears all input and output in the display, including the display history.


## Using previous results

The Home display ( $\left.\begin{array}{c}\text { Home } \\ \text { Modes }\end{array}\right)$ ) shows you $4-6$ lines of input/ output history. An unlimited (except by memory) number of previous lines can be displayed by scrolling. You can retrieve and reuse any of these values or expressions.


When you highlight a previous input or result (by pressing ()), the CoPY and SHOW menu labels appear.


To copy a previous
line line

To reuse the last result

To repeat a previous line

Example

Highlight the line (press ${ }^{*}$ ) and press COPY. The number (or expression) is copied into the edit line.

Your last few entries are always copied to the clipboard, so in most cases, you can just paste a recent result. Press
$\odot$ and $\Theta$ to highlight the result you want, and press

## OK

Press ANS (last answer) to put the last result from the Home display into an expression. AnS is a variable that is updated each time you press ENTSR
 previous line is an expression containing ans, the calculation is repeated iteratively.

See how Ans retrieves and reuses the last result (50), and (ENSTER updates ANS (from 50 to 75 to 100).


You can use the last result as the first expression in the edit line without pressing ${ }^{\mathrm{x}}{ }^{\mathrm{s}}, x_{x^{+}} \mathrm{N}$, (or other operators that require a preceding argument) automatically enters ans before the operator.

You can reuse any other expression or value in the Home display by highlighting the expression (using the arrow keys), then pressing [COPY.

The variable ans is different from the numbers in Home's display history. A value in ANS is stored internally with the full precision of the calculated result, whereas the displayed numbers match the display mode.

HIN T When you retrieve a number from ANs, you obtain the result to its full precision. When you retrieve a number from the Home's display history, you obtain exactly what was displayed.

Pressing 䍐TER evaluates (or re-evaluates) the last input, whereas pressing ${ }^{\text {sthir }}$ ANS copies the last result (as ANS) into the edit line.

Copy and paste In addition to the COPY menu key that lets you copy expressions from the Home view, there is a more universal copy and paste clipboard that you can use. You can highlight the value or expression you want in most fields or the Home view history (e.g. F1 (x) in the Function App) and then paste it into the edit line or into another compatible field. To copy a value or expression to the clipboard, press cove 1. To open the clipboard to select and paste a value or expression, press Byllim bat $m$.

You can save an answer in a variable and use the

## Storing a value

 in a variablevariable in later calculations. There are 27 variables available for storing real values. These are $A$ to $Z$ and $\theta$. See the chapter Variables and memory management for more details on variables. For example:

1. Perform a calculation.

2. Store the result in the $A$ variable.


| [日G] | Function |  |
| :---: | :---: | :---: |
| $45+8 \wedge 3$ |  |  |
| AnsmA |  |  |
|  |  | 557 |
| STO |  |  |

3. Perform another calculation using the $A$ variable.


## Accessing the display history

Pressing $\odot$ enables the highlight bar in the display history. While the highlight bar is active, the following menu and keyboard keys are very useful:

| Key | Function |
| :--- | :--- |
| COPY | Scrolls through the display history. <br> Copies the highlighted expression to <br> the position of the cursor in the edit line. |
| SHOW | Displays the current expression using <br> Textbook Format Display. <br> Deletes the highlighted expression from <br> the display history, unless there is a <br> Cursor in the edit line. <br> Clears all lines of display history and <br> the edit line. |

Clearing the display history

It's a good habit to clear the display history ( SHITI CLEAR) whenever you have finished working in Home. It saves calculator memory to clear the display history. Remember
that all your previous inputs and results are saved until you clear them.

## Numerical representations

## Converting decimals to fractions

Any decimal result can be displayed as a decimal, a fraction, or a mixed number. Enter your expression in the
 Home view and then
 and decimal representations of the numerical result. For example, enter $18 / 7$ to see the decimal result:
2.5714.... Press ance to see $\frac{18}{7}$ and again to see $2+\frac{4}{7}$. The 39 gll will approximate fraction and mixed number representations in cases where it cannot find exact ones. Enter $\sqrt{5}$ to see the decimal
approximation: $2.236 \ldots$... Press ance to see
$\frac{930249}{416020}$ and again to see $2+\frac{98209}{416020}$.
Pressing $\sqrt{a-b-b / c)}$ a third time will cycle back to the original decimal representation.

Converting decimals to degrees, minutes, and seconds

Any decimal result can de displayed in hexagesimal; that is, in units subdivided into groups of 60. This includes degrees, minutes, and seconds as well as hours, minutes, and seconds. For example, enter $\frac{11}{8}$ to see the decimal result: 1.375. Press antict and to see $1^{\circ} 22^{\prime} 30^{\prime \prime}$. Press shilia representation. The 39 gll will produce the best approximation in cases where an exact result is not possible. Again, enter $\sqrt{5}$ to see the decimal
 $2^{\circ} 14^{\prime} 9.844719^{\prime \prime}$.

## Complex numbers

Complex results

To enter complex numbers

Storing complex numbers

If the Complex mode setting is checked, then the HP 39gll can return a complex number as a result for some math functions. A complex number appears as $x+y \times i$. For example, entering $\sqrt{-1}$ returns $i$ and entering $(4,5)$ returns $4+5 \times i$.

Enter the number in either of these forms, where $x$ is the real part, $y$ is the imaginary part, and $i$ is the imaginary constant, $\sqrt{-1}$ :

- $(x, y)$ or
- $x+i y$

To enter $i$ :

- press SHITI Alpha ${ }^{10^{200}}$ or

(1) to move to the right column of the menu, $\sigma$ to select $i$, and OK

There are ten variables available for storing complex numbers: Z0 to Z9. To store a complex number in a variable:

- Enter the complex number, press [STO • - enter the variable to store the number in, and press $\frac{\text { ENTER }}{\text { NOR }}$

```
STO.
ALPHA
```

Z 0
ENTER



STO.

ALPHA
ans


## Catalogs and editors

The HP 39gll has several catalogs and editors. You use them to create and manipulate objects. They access objects with stored data (lists of numbers or notes with text) that are independent of apps, as well as notes and programs aftached to the current HP App.

- A catalog lists items, which you can delete or transmit, for example an app.
- An editor lets you create or modify items and numbers, for example a note or a matrix.

| Catalog/Editor | Keystrokes | To create and edit |
| :---: | :---: | :---: |
| App library | (taps | HP Apps |
| Info |  | Notes attached to the current HP App |
| List | $\begin{aligned} & \text { SHIIT }{ }^{7{ }^{7}{ }_{p}} \\ & \text { (List) } \end{aligned}$ | Lists |
| Matrix |  | Matrices and vectors |
| Program | $\begin{aligned} & \text { SHIITI }{ }^{\text {Prgm } \mathrm{x}} \\ & \text { (Prgm) } \end{aligned}$ | Programs |
| Notes | $\text { SHIFT } \begin{array}{cc} \mathbf{0} & \\ \text { Notes } & \text { II } \end{array}$ <br> (Notes) | Notes |

## Apps and their views

## HP Apps

HP Apps are applications designed for the study and exploration of a branch of mathematics or to solve problems of one or more types. The following table lists the name of each HP App and gives a general description of its purpose.
\(\left.$$
\begin{array}{|l|l|}\hline \text { App name } & \text { Use this app to explore: } \\
\hline \text { Function } & \begin{array}{l}\text { Real-valued, rectangular functions } y \\
\text { in terms of } x \text {. Example: } \\
y=2 x^{2}+3 x+5 .\end{array} \\
\text { Solve } & \begin{array}{l}\text { Equations in one or more real-valued } \\
\text { variables. Example: } \\
x+1=x^{2}-x-2 . \\
\text { Statistics } \\
\text { One-variable statistical data }(x)\end{array} \\
\begin{array}{l}\text { Statistics } \\
\text { 2Var } \\
\text { Inference }\end{array} & \begin{array}{l}\text { Two-variable statistical data ( } x \text { and } y \text { ) }\end{array}
$$ <br>
Confidence intervals and Hypothesis <br>
tests based on the Normal and <br>

Students-t distributions.\end{array}\right\}\)| Parametric relations $x$ and $y$ in terms |
| :--- |
| of $t$. Example: $x=\cos (t)$ and $y=$ |
| sin $(t)$. |$\quad$| Polar functions $r$ in terms of an angle |
| :--- |
| $\theta$. |
| Example: $r=2 \cos (4 \theta)$. |


| App name | Use this app to explore: (Continued) |
| :--- | :--- |
| Sequence | Sequence functions U in terms of $n$, or <br> in terms of previous terms in the same <br> or another sequence, such as $U_{n-1}$ <br> and $U_{n-2}$. Example: $U_{1}=0$, <br> $U_{2}=1$ and $U_{n}=U_{n-2}+U_{n-1}$. <br> Fime Value of Money (TVM) problems <br> and amortization tables. <br> Solutions to sets of two or three linear <br> equations. |
| Linear Solver |  |
| Triangle | Unknown values for the lengths and <br> angles of triangles. |
| Data | Real-world data collected from <br> Streamer |
| scientific sensors. |  |

In addition to these apps, which can be used in a variety of applications, the HP 39gll is supplied with three apps for exploring function families: The Linear, Quadratic, and Trig Explorers. These apps will retain their data so you can return to them and find them as you left them, but they are not designed to be customized and saved like the other HP Apps.

As you use an app to explore a lesson or solve a problem, you add data and definitions in the app's views. All of this information is automatically saved in the app. You can come back to the app at any time and the information is all still there. Or you can save the app with a name you give it and then use the original app for another problem or purpose. See the chapter Extending Your Aplet Library for more information regarding customizing and saving HP Apps.

## App library

To open an app
Apps are stored in the App library.
Press ${ }_{\text {Apps }}^{\text {Apto }}$ lo display the App library menu. Select the app and press START or $\overline{\text { ENNSTRR }}$.

From within an app, you can return to Home any time by pressing $\xlongequal[\substack{\text { Home } \\ \text { Nodes } \\ \hline}]{\substack{\text { mon } \\ \hline}}$

## App views

## Symbolic view


You use this view to define the function(s) or equation(s) that you want to explore.

Symbolic setup

Press SHITT SETUP-SYMB to display the app's Symbolic setup. The purpose of this view is to allow you to overwrite one or more of the
 Modes settings for an app. This view is not used by the Solvers and Explorers, as the few mode settings needed for each app can already be changed by using menu keys within the app.

Plot-Detail view 
Select Plot-Detailok
Splits the screen into the
 current plot and a userdefined zoom.

Plot-Table view Press $\underset{\substack{\text { Vems } \\ \text { hed }}}{\substack{\text { nen }}}$
Select Plot-Table OK
Splits the display, showing both the plot and tabular views.


## Preset zooms The Views menu also contains the same preset zooms

 from the Zoom menu:- Auto Scale
- Decimal
- Integer
- Trig
These are described in more detail in the Zoom options section later in this chapter.


## Standard app views

This section examines the options and functionality of the three main views (Symbolic, Plot, and Numeric), as well as their setups, for the Function, Polar, Parametric, and Sequence apps.

## About the Symbolic view

The Symbolic view is the defining view for the Function, Parametric, Polar, and Sequence apps. The other views are derived from the symbolic expression.

You can create up to 10 different definitions for each Function, Parametric, Polar, and Sequence app. You can graph any of the relations (in the same app) simultaneously by selecting them.

## Defining an expression (Symbolic view)

Choose the app from the App Library.

Apps

Press $\uparrow$ or to select an app.


## START

The Function, Parametric, Polar, and Sequence apps start in the Symbolic view.
If the highlight is on an existing expression, scroll to an empty line-unless you don't mind writing over the expression-or, clear one line (clort ) or all lines ( SHIT CLEAR).

Expressions are selected (check marked) on entry. To deselect an expression, press CHK All selected expressions are plotted.

- For a Function definition, enter an expression to define $F(X)$. The only independent variable in the expression is $X$.
- For a

Parametric definition, enter a pair of expressions to define $X(T)$ and
 $Y(T)$. The only independent variable in the expressions is $T$.

- For a Polar definition, enter an expression to define $R(\theta)$. The only independent variable in the
 expression is $\theta$.
- For a Sequence definition, either enter the first term, or the first and second terms for $U$. Then define the $n$th
 term of the sequence in terms of $N$ or the prior terms, $U(N-1)$ and/or $U(N-2)$. The expressions should produce real-valued sequences with integer domains. Or define the Nth term as a non-recursive expression in terms of N only.
- Note: you will have to enter the second term if the HP 39gll is unable to calculate it automatically. Typically if $U_{x}(N)$ depends on $U_{x}(N-2)$ then you must enter Ux(2).


## Evaluating expressions

In apps
In the Symbolic view, a variable is a symbol only, and does not represent one specific value. To evaluate a function in Symbolic view, press EVAL. If a function calls another function, then EVAL resolves all references to other functions in terms of their independent variable.

1. Choose the Function app.


Select Function

## START

2. Enter the expressions in the Function app's Symbolic view.

3. Highlight F3 (X).


## 4. Press EVAL

Note how the values for F1 (X) and F2 (X) are substituted into F3 (X).

| DEG Function Symbolic View |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\sim F 1(X)=A^{*} X^{2}$ |  |  |  |  |
| $\sim F 2(X)=B$ |  |  |  |  |
| $\checkmark F 3(X)=A^{*} X^{2}+B$ |  |  |  |  |
| $F 4(X)=$ |  |  |  |  |
| $F 5(X)=$ |  |  |  |  |
| Enter function |  |  |  |  |
| EDIT | CHK | X | SHOW | EVAL |

## In Home

You can also evaluate any function expression in Home by entering it into the edit line and pressing $\begin{aligned} & \text { NNTER } \\ & \text { NNS }\end{aligned}$

For example, define F4 as below. In Home, type F4 (9) and press $\underset{\text { ENTHR }}{\text { ENTR }}$. This evaluates the expression, substituting 9 in place of x in F 4 .

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| RRDD Function Symbolic View |  |  |  |  |
| $\sim F 2(X)=B$ |  |  |  |  |
| $\checkmark F 3(X)=A^{*} X^{2}+B$ |  |  |  |  |
| $V F 4(X)=3 * X^{2}+2 * X+1$ |  |  |  |  |
| F5 ( |  |  |  |  |
| Enter function |  |  |  |  |
| EDIT | CHK | X | SHOW | EVAL |


| DEG | Function |  |
| :--- | :--- | :--- | :--- | F4(9)

Symb view keys The following table describes the keys that you use to work with the Symbolic view.

| Key | Meaning |
| :---: | :---: |
| EEDT | Copies the highlighted expression to the edit line for editing. Press when done. |
| CHK | Checks/unchecks the current expression (or set of expressions). Only checked expression(s) are evaluated in the Plot and Numeric views. |
| - | Enters the independent variable in the Function app. Or, you can use <br>  |
| T | Enters the independent variable in the Parametric app. Or, you can use the [xiten |


| Key | Meaning (Continued) |
| :---: | :---: |
| 日 | Enters the independent variable in the <br>  key on the keyboard. |
| N | Enters the independent variable in the Sequence app. Or, you can use <br>  |
| SHOW | Displays the current expression in Textbook Format. |
| EVAL | Resolves all references to other definitions in terms of variables. |
| ${ }_{\text {Chars }} \mathrm{V}$ | Displays a menu for entering variable names or contents of variables. |
| ${ }_{\text {cmath }}^{\text {M }}$ | Displays the menu for entering math operations. |
| SHIIT CHARS | Displays special characters. To enter one, place the cursor on it and press <br> OK . To remain in the Chars menu and enter another special character, press ECHO. |
| $\stackrel{\square}{\text { clear }}$ | Deletes the highlighted expression or the current character in the edit line. |
| SHIIT CLEAR | Deletes all expressions in the list or clears the edit line. |

## About the Plot view

After entering and selecting (check marking) the expression in the Symbolic view, press ${ }_{\text {Plot }}^{\text {Potw }}$. To adjust the appearance of the graph or the interval that is displayed, you can change the Plot view settings.

You can plot up to ten expressions at the same time. Select the expressions you want to be plotted together.

## Plot setup

Press Shlir setup-Plot to define any of the settings shown in the next two tables.

1. Highlight the field to edit.

- If there is a number to enter, type it in and press $\underset{\text { ENS }}{\text { ENTER }}$ or OK .
- If there is an option to choose, press CHOOS highlight your choice, and press $\begin{aligned} & \text { ENTER } \\ & \text { ANs } \\ & \text { OR }\end{aligned}$ As a shortcut to CHOOS , just highlight the field to change and press $\varepsilon^{+}$to cycle through the options.
- If there is an option to select or deselect, press CHK to check or uncheck it.

2. Press PAGE 7 to view more settings.
3. When done, press $\xlongequal[\substack{\text { potet } \\ \text { selp }}]{ }$ to view the new plot.

## Plot setup settings

The fields in the Plot setup are:

| Field | Meaning |
| :---: | :---: |
| XRNG, YRNG | Specifies the minimum and maximum horizontal $(X)$ and vertical $(Y)$ values for the plotting window. |
| TRNG | Parametric app: Specifies the $\dagger$ values ( $T$ ) for the graph. |
| ӨRNG | Polar app: Specifies the angle ( $\theta$ ) value range for the graph. |
| NRNG | Sequence app: Specifies the index $(N)$ values for the graph. |
| TSTEP | For Parametric plots: the increment for the independent variable. |
| OSTEP | For Polar plots: the increment value for the independent variable. |
| SEQPLOT | For Sequence app: Stairstep or Cobweb types. |
| XTICK | Horizontal spacing for tickmarks. |
| YTICK | Vertical spacing for tickmarks. |

Those items with space for a checkmark are settings you can turn on or off. Press PAGE 7 to display the second page.
$\left.\begin{array}{|l|l|}\hline \text { Field } & \text { Meaning } \\ \hline \text { AXES } & \begin{array}{l}\text { Draws the axes. } \\ \text { Labels the axes with XRNG and } \\ \text { YRNG values. }\end{array} \\ \text { GRID DOTS } & \begin{array}{l}\text { Draws grid points using XTICK } \\ \text { and YTICK spacing. }\end{array} \\ \text { Cursor } & \begin{array}{l}\text { Draws grid lines using XTICK and } \\ \text { YTICK spacing. }\end{array} \\ \text { Method } & \begin{array}{l}\text { Choose between the Standard } \\ \text { cursor and Inverting or } \\ \text { Blinking cursors. } \\ \text { Choose between the default } \\ \text { Adaptive method for drawing } \\ \text { accurate graphs and just plotting }\end{array} \\ \text { Fixed-Step Segments or } \\ \text { Fixed-Step Dots. }\end{array}\right\}$

Reset Plot setup To reset the default values for all plot settings, press SHIT CLEAR in the Plot Setup. To reset the default value for a field, highlight the field, and press clear .

## Exploring the graph

The Plot view gives you a selection of keys and menu keys to explore a graph further. The options vary from app to app.

## Plot view keys

The following tables describe the keys that you use to work with the Plot view.

| Key | Meaning |
| :--- | :--- |
| SHITI CLEAR | Erases the plot and axes. |
| Offers additional pre-defined views |  |
| for spliting the screen and for scaling |  |
| ("zooming") the axes. |  |
| Shews |  |
| Hele | Stops refining the graph |


| Key | Meaning (Continued) |
| :--- | :--- |
| MENU | Turns menu-key labels on and off. <br> When the labels are off, pressing <br> MENU turns them back on. |
| TRACE |  |
| GOTO | Displays the Zoom menu list. <br> Turns trace mode on/off. <br> Opens an input form for you to enter <br> an $X$ (or $T$ or $N$ or $\theta$ ) value. Enter the <br> value and press ok . The cursor <br> iumps to the point on the graph that <br> you entered. <br> Function app only: displays a list of <br> commands for analyzing functions <br> (see the chapter Function app for more <br> details). <br> Displays the current, defining <br> expression. Press MENU to restore the <br> menu. |
| DEFN |  |

The following tables detail the use of the arrow keys.

| Key | Meaning (with trace mode off) |
| :--- | :--- |
| (4) | Moves cursor one pixel left and right, <br> respectively. <br> Moves cursor one pixel up and down, <br> respectively. <br> Moves cursor to far left or right edge <br> of the display, respectively. |



Trace a graph

To move between relations

To jump directly to a value

Press the (4) and keys to move the trace cursor along the current graph (left or right respectively). The display also shows the current coordinate position $(x, y)$ of the cursor. Trace mode and the coordinate display are automatically set when a plot is drawn.

If there is more than one relation displayed, press $\otimes$ or $\checkmark$ to move between relations.

To jump straight to a value rather than using the Trace function, use the GOTO menu key. Press GOTO, then enter a value. Press $O K$ to jump to the value.

To turn trace on/off If the menu labels are not displayed, press [MENU first.

- Turn off trace mode by pressing TRACE• .
- Turn on trace mode by pressing TRACE.


## Zoom within a graph

One of the menu key options is ZOOM . Zooming redraws the plot on a larger or smaller scale. It is a shortcut for changing the Plot Setup.

The set Factors. . . option enables you to set the factors by which you zoom in or zoom out, and whether the zoom is centered about the cursor.

## Zoom options

Press [ZOOM, select an option, and press OK. (If
ZOOM is not displayed, press MENU.) Not all options are available in all apps.

| Option | Meaning |
| :--- | :--- |
| Center on <br> Cursor | Re-centers the plot around the <br> current position of the cursor without <br> changing the scale. |
| In . . | Lets you draw a box to zoom in on. <br> Divides horizontal and vertical <br> scales by the X-factor and Y-factor. <br> For instance, if zoom factors are 4, <br> then zooming in results in 1/4 as <br> many units depicted per pixel. (see <br> Set Factors...) |
| Out | Multiplies horizontal and vertical <br> scales by the X-factor and Y-factor <br> (see Set Factors. ..). |
| X In | Divides horizontal scale only, using <br> X-factor. <br> Multiplies horizontal scale only, <br> using X-factor. |
| Y In | Divides vertical scale only, using <br> Y-factor. <br> Multiplies vertical scale only, using <br> Y-factor. <br> Changes the vertical scale to match <br> the horizontal scale. (Use this after <br> doing a Box Zoom, X-Zoom, or <br> Y-Zoom.) |
| Square | Sets the X-Zoom and Y-Zoom factors <br> for zooming in or zooming out. <br> Includes option to recenter the plot <br> before zooming. |
| Factors |  |


| Option | Meaning (Continued) |
| :--- | :--- |
| Auto Scale | Rescales the vertical axis so that the <br> display shows a representative <br> piece of the plot, for the supplied $x$ <br> axis settings. (For Sequence and <br> Statistics apps, autoscaling rescales <br> both axes.) <br> The autoscale process uses the first <br> selected function only to determine <br> the best scale to use. <br> Decimal <br> Rescales both axes so each pixel $=$ <br> 0.1 units. Resets default values for <br> XRNG (-12.7 to 12.7) and YRNG (- <br> $5.5,5.5)$. <br> Integer <br> Rescales horizontal axis only, <br> making each pixel =1 unit. |
| Rescales horizontal axis so |  |
| 1 pixel = $\pi / 24$ radians or 7.58 |  |
| degrees; rescales vertical axis so |  |
| 1 pixel = 0.1 unit. |  |

## Zoom examples

The following screens show the effects of zooming options on a plot of $3 \sin x$.
Plot of $3 \sin x$


## Zoom In:



As a shortcut, press $\Sigma^{+} \sqsupset$ while in the Plot
 view to zoom in.

## Un-zoom:

ZOOM Un-zoom OK
Note: press $\uparrow$ to move to the bottom of the Zoom list.


## X-Zoom Out:

## 700M X Out <br> OK

Now un-zoom.


Y-Zoom In:
ZOOM Y In OK


## Y-Zoom Out:

## ZOOM Y Out OK



## Zoom Square:

```
ZOOM Square OK
```



To box zoom
The Box Zoom option lets you draw a box around the area you want to zoom in on by selecting the endpoints of one diagonal of the zoom rectangle.

1. If necessary, press MENU to turn on the menu-key labels.
2. Press zoom and select Box. . .
3. Position the cursor on one corner of the rectangle. Press OK
4. Use the cursor keys
( $\odot$, etc.) to drag to the opposite corner.

5. Press OK to zoom in on the boxed area.


To set zoom factors

1. In the Plot view, press MENU.
2. Press ZOOM.
3. Select Set Factors... and press OK.
4. Enter the zoom factors. There is one zoom factor for the horizontal scale (хzоom) and one for the vertical scale (yzoom).
Zooming out multiplies the scale by the factor, so that a greater scale distance appears on the screen.
Zooming in divides the scale by the factor, so that a shorter scale distance appears on the screen.

## Views menu options

| Option | Meaning |
| :--- | :--- |
| Plot- <br> Detail <br> Plot-Table | Splits the screen into the current plot <br> and a zoom. <br> Splits the screen into the plot and a <br> numeric table. |
| Reale | Rescales the vertical axis so that the <br> display shows a representative <br> portion of the plot, based on the <br> current XRNG. For Sequence and <br> Statistics apps, auto scale rescales <br> both axes. |
| Decimal | The auto scale process uses the first <br> selected function only to determine <br> the best scale to use. |
| Rescales both axes so each pixel = |  |
| Integer | XRNG(-1 12.7 to 12.7) and YRNG <br> (-5.5 to 5.5 ). <br> Rescales horizontal axis only, <br> making each pixel=1 unit. |
| Trig | Trig Rescales horizontal axis so 1 <br> pixel = $\pi / 48$ radians or 3.75 <br> degrees. |

Plot-Detail
The Plot-Detail view can give you two simultaneous views of the plot.

The graph is plotted twice. You can now zoom in on the right side.
2. Press MENU ZOOM, select the zoom method and press OK
or ENTER . This zooms

the right side. Here is an example of split screen with Zoom In.

- The Plot menu keys are available as for the full plot (for tracing, coordinate display, equation display, and so on).
- The $\mathbb{E - a}$ menu key copies the right plot to the left plot.

3. To un-split the screen, press over the whole screen.

## Plot-Table

The Plot-Table view gives you a plot view and a table view simultaneously.
1.
Press $\xlongequal[\substack{\text { Veievs } \\ \text { Help }}]{\substack{\text { Select } \\ \text { Plot-Table and }}}$ press OK. The screen displays the plot
 on the left side and a table of numbers on the right side.
2. To move up and down in the table, use
the and cursor keys. These keys move the trace point left or right along the plot, and in the table, the corresponding values are highlighted.
3. To move between functions, use the $\Theta$ and cursor keys to move the cursor from one graph to another.
4. To return to a full Numeric (or Plot) view,

press \begin{tabular}{l}

| Num |
| :---: |
| Setup | <br>

(or $\left.\begin{array}{c}\text { Plot } \\
\text { Setup }\end{array}\right) . ~$
\end{tabular}

| Decimal scaling | Decimal scaling is the default scaling. If you have <br> changed the scaling to Trig or Integer, you can <br> change it back with Decimal. |
| :--- | :--- |
| Integer scaling | Integer scaling compresses the axes so that each pixel is <br> $1 \times 1$ and the origin is near the screen center. |
| Trigonometric | Use trigonometric scaling whenever you are plotting an <br> scalingexpression that includes trigonometric functions. <br> Trigonometric plots are more likely to intersect the axis at <br> points factored by $\pi$ |

## About the Numeric view

After entering and selecting (check marking) the expression or expressions that you want to explore in the Symbolic view,
 press $\underset{\substack{\text { Num } \\ \text { sewp }}}{ }$ to view a table of data values for the independent and dependent variables.

## Setting up the table (Numeric view setup)

Press ${ }^{\text {sHIIFI}}$ NUM to define any of the table settings. Use the Numeric Setup input form to configure the table.

```
| RRD 
```

1. Highlight the field to edit. Use the arrow keys to move from field to field.

- If there is a number to enter, type it in and press ${ }^{\text {ENSTRR }}$ or or . To modify an existing number, press EDIT.
- Shortcut: press the FLOT $\rightarrow$ key to copy values from the Plot Setup into NUMSTART and NUMSTEP. Effectively, the FLOT $\rightarrow$ menu key allows you to make the table values match the tracer values in the graph view.

2. When done, press $\xlongequal[\substack{\text { Nom } \\ \text { seme }}]{ }$ to view the table of numbers.

Numeric view settings

The following table details the fields on the Numeric Setup input form.

| Field | Meaning |
| :--- | :--- |
| NUMSTART | The independent variable's <br> starting value. |
| NUMSTEP | The size of the increment from <br> one independent variable value <br> to the next. |
| NUMTYPE | Type of numeric table: <br> Automatic or Bui idYourOwn. <br> To build your own table, you must <br> type each independent value into <br> the table yourself. |
| NUMZOOM | Sets the zoom factor for zooming <br> in or out on a row of the table. |

Reset numeric settings

To reset the default values for all table settings, press shllia CLEAR.

## Exploring the table of numbers

Num view menu The following table details the menu keys that you use to keys work with the numerical table.

| Key | Meaning |
| :--- | :--- |
| ZOOM | Displays the Zoom menu list. <br> Toggles between two character <br> sizes. |
| DEFN | Displays the defining function <br> expression for the highlighted <br> column. To cancel this display, press <br> [DEFN* |
| WDTH3 | Toggles between showing 1, 2, 3, or <br> 4 columns of dependent variable <br> values. |

## Zoom within a table

Zoom options
Zooming recalculates the table of numbers with greater or lesser common differences among $X$-values.

The following table lists the zoom options:
\(\left.$$
\begin{array}{|l|l|}\hline \text { Option } & \text { Meaning } \\
\hline \text { In } & \begin{array}{l}\text { Decreases the step value for the } \\
\text { independent variable so a narrower } \\
\text { range is shown. Uses the NUMZOoM } \\
\text { factor in Numeric Setup. }\end{array} \\
\text { Out } & \begin{array}{l}\text { Increases the step value for the } \\
\text { independent variable so that a } \\
\text { wider range is shown. Uses the } \\
\text { NUMZOOM factor in Numeric Setup. } \\
\text { Changes intervals for the } \\
\text { independent variable to 0.1 units. } \\
\text { Starts at zero (shortcut to changing } \\
\text { NUMSTART and NUMSTEP). } \\
\text { Changes intervals for the } \\
\text { independent variable to 1 unit. } \\
\text { Starts at zero (shortcut to changing } \\
\text { NUMSTART and NUMSTEP). }\end{array}
$$ <br>
Integer <br>
Changes intervals for independent <br>
variable to \pi / 24 radians or 7.5 <br>

degrees. Starts at zero.\end{array}\right\}\)| Returns the display to the previous |
| :--- |
| zoom. |

The display on the right is a Zoom In of the display on the left. The zoom factor is 4 .

| X | F1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 |  |  |  |
| 0.1 | 9.9833342E-3 |  |  |  |
| 0.2 | 1.996668E-2 |  |  |  |
| 0.3 | $2.995002 \mathrm{E}-2$ |  |  |  |
| 0.4 | 3,993337E-2 |  |  |  |
| 0.5 | $4.991671 \mathrm{E}^{-2}$ |  |  |  |
| 0,00998334166468 |  |  |  |  |
| 200m |  | B/G | DEFN | WIDTH3 |


| X | F1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.75 | 7,4875016E-2 |  |  |  |
| 0.85 | 8,485840E-2 |  |  |  |
| 0.95 | $9.484175 \mathrm{E}-2$ |  |  |  |
| 1.05 | $1.048251 \mathrm{E}-1$ |  |  |  |
| 1.15 | 1.148084E-1 |  |  |  |
| 1.25 | 1,247918E-1 |  |  |  |
| 0.0848584041498 |  |  |  |  |
| 200M |  | EIG | DEFN | WIDTH3 |

HIN T To jump to an independent variable value in the table, use the arrow keys to place the cursor in the independent variable column, then enter the value to jump to.

## Automatic recalculation

You can enter any new value in the $X$ column. When you press $\begin{gathered}\text { ENSER } \\ \text { ANS }\end{gathered}$, the values for the dependent variable(s) are
recalculated, and the entire table is regenerated with the same interval between $X$-values.

## Building your own table of numbers

The default NUMTYPE is Automatic, which fills the table with data for regular intervals of the independent ( $X, T, \theta$, or $N$ ) variable. With the NUMTYPE option set to Build YourOwn, you fill the table yourself by typing in the independent-variable values you want. The dependent values are then calculated and displayed.

## Build a table

2. In the Numeric Setup (sthir $N U M$ ), choose NUMTYPE: BuildYourOwn.
3. Open the Numeric view ( $\left.\begin{array}{l}\text { Num } \\ \text { Sevep }\end{array}\right)$.
4. Clear existing data in the table (SHIT CLEAR).
5. Enter the independent values in the left-hand column.

Type in a number and press $\underset{\substack{\text { ENNS } \\ \text { ANSR }}}{\text {. You do not have }}$ to enter them in order, because the SORT function can rearrange them. To insert a number between two others, use $\mathbb{N} \mathbb{N}$


Press SHITI CLEAR, OK to erase the data from a table.

## BuildYourOwn table keys

Besides the EEG and DEEN menu keys, you can use the following keys to explore the table when BuildYour Own is active.


Example: plotting a circle

Plot the circle, $x^{2}+y^{2}=25$. First rearrange it to read $y= \pm \sqrt{25-x^{2}}$.

To plot both the positive and negative $y$-values, use two equations as follows:
$y=\sqrt{25-x^{2}}$ and $y=-\sqrt{25-x^{2}}$

1. In the Function app, specify the functions.


2. Reset the graph setup to the default settings.

3. Plot the two functions.

4. Reset the numeric setup
 to the default settings.

5. Display the functions in numeric form.

## Function app

## About the Function app

The Function app enables you to explore up to 10 realvalued, rectangular functions y in terms of x . For example, $y=1-x$ and $y=(x-1)^{2}-3$.
Once you have defined a function you can:

- create graphs to find roots, intercepts, slope, signed area, and extrema
- create tables to evaluate functions at particular values

This chapter demonstrates the basic tools of the Function app by stepping you through an example.

## Getting started with the Function app

Throughout this chapter, we will use an example involving two functions: a linear, $y=1-x$, and a quadratic, $y=(x-1)^{2}-3$.

## Open the Function app

1. Open the Function app.
```
\begin{subarray}{c}{\mathrm{ Apps }}\\{\mathrm{ Info}}\end{subarray}
Select
```

Function


RESET OK START
The Function app starts in the Symbolic view.
The Symbolic view is the defining view for the Function app. The other views are derived from any symbolic expressions defined here.

Define the expressions

There are 10 function definition fields on the Function app's Symbolic view. They are labelled F1 (X) through $\mathrm{F9}$ (X) and FO (X). Highlight the function definition field you want to use, and enter an expression. You can press
EDIT to edit an existing expression or just start typing to enter a new expression. Press cher to delete an existing expression, or Clear to clear all expressions.
2. Enter the linear function in $\mathrm{F} 1(\mathrm{X})$.

3. Enter the quadratic function in $\mathrm{F} 2(\mathrm{X})$.


```
DEG Function Symbolic View


3 剘
NOTE You can use the \(X\) menu key to assist in the entry of


Set up the plot You can change the scales of the \(x\) - and \(y\)-axes and the spacing of the axis tick marks.
4. Display plot settings.


SETUP-PLOT
\begin{tabular}{|l|l|l|l|l|}
\hline DEG & & Function Plot Setup & & \\
\hline
\end{tabular}

Note: for our example, you can leave the plot settings at their default values. If your settings do not match this example, press CLEAR to restore the default values.

\section*{Plot the functions}
5. Plot the functions.

\section*{Trace a graph}
6. Trace the linear function.


Note: by default, the tracer is active.
7. Jump from tracing the linear function to the quadratic function.


\section*{Change the scale}

You can change the scale to see more or less of your graph. This can be done in four ways:
- Press \(\Sigma^{+}\)to zoom in or \(\Sigma^{-}\)w to zoom out on the current cursor coordinates. This method uses the zoom factors set in the Zoom menu. The default for both x and y is 2 .
- Use the Plot Setup to define XRNG and YRNG exactly as you want.
- Use the Zoom menu to zoom in or out, horizontally or vertically, or both, etc.
- Use the Views menu to select a pre-defined window.

You can also use Autoscale, in either the Zoom or Views menus, to choose a vertical range for the current horizontal range, based on your function definitions.

Display the
Numeric view
1. Display the Numeric view.

Num
Sum Setup
\begin{tabular}{|l|l|l|l|}
\hline \multicolumn{1}{|c|}{\(X\)} & \(F 1\) & \multicolumn{1}{c|}{\(F 2\)} & \\
\hline 6 & -5 & 22 & \\
\hline 6.1 & -5.1 & 23.01 & \\
6.2 & -5.2 & 24.04 & \\
6.3 & -5.3 & 25.09 & \\
\hline 6 & \multicolumn{4}{|c|}{} \\
\hline 700 M & & & EIG• \\
\hline \multicolumn{5}{|c|}{} & DEFN & WIDTH3 \\
\hline
\end{tabular}
2. Display the Numeric setup.


You can set the starting value and step value for the \(x\) column, as well as the zoom factor for zooming in or out on a row of the table. You can also choose the table type. Press SHITI CLEAR to reset all values to their defaults.
3. Match the table settings to the pixel columns in the graph view.


Explore the table
4. Display the table of values.
\begin{tabular}{|c|c|c|c|}
\hline\(X\) & \(F 1\) & \(F 2\) & \\
\hline-12.7 & 13.7 & 184.69 & \\
-12.6 & 13.6 & 181.96 & \\
-12.5 & 13.5 & 179.25 & \\
-12.4 & 13.4 & 176.56 & \\
\hline-12.7 & \multicolumn{4}{|c|}{} \\
\hline ZOOM & & & EIGU \\
\hline
\end{tabular}

To navigate around a table
5. Move to \(x=-12.1\).
\(\bigcirc 6\) times.
\begin{tabular}{|c|c|c|c|}
\hline\(X\) & \(F 1\) & \(F 2\) & \\
\hline-12.4 & 13.4 & 176.56 & \\
-12.3 & 13.3 & 173.89 & \\
-12.2 & 13.2 & 171.24 & \\
-12.1 & 13.1 & 168.61 & \\
\hline-12.1 & \multicolumn{4}{|c|}{} \\
\hline ZOOM & & & EIG• \\
\hline
\end{tabular}

To go directly to a
value
6. Move directly to \(X=10\).

10 OK
\begin{tabular}{|l|l|l|l|}
\hline \multicolumn{1}{|c|}{\(X\)} & \(F 1\) & \multicolumn{1}{c|}{\(F 2\)} & \\
\hline 10 & -9 & 78 & \\
10.1 & -9.1 & 79.81 & \\
10.2 & -9.2 & 81.64 & \\
10.3 & -9.3 & 83.49 & \\
\hline 10 & \multicolumn{4}{|c|}{} \\
\hline \(200 M\) & & & EIG• \\
\hline
\end{tabular}

NOTE to navigate directly to a value, ensure the cursor is in the independent variable column, in this case, \(x\), before typing the desired value.

To access the zoom options

\author{
To change font size
}

To display the
symbolic definition of a column
7. Zoom in on \(\mathrm{X}=10\) by a factor of 4. Note:
numzoom has a setting of 4 .

\section*{zoom In}

\section*{OK}
8. Display table numbers in smaller font.

\section*{BlG*}
9. Display the symbolic definition for the F1 column.

DEFN
\begin{tabular}{|c|c|c|c|c|}
\hline X & F1 & F2 & & \\
\hline & -9 & & & \\
\hline 10.025 & -9.025 & 78,450625 & & \\
\hline 10.05 & -9.05 & 78.9025 & & \\
\hline 10.075 & -9.075 & 79,355625 & & \\
\hline 10.1 & -9.1 & 79.81 & & \\
\hline 10.125 & -9.125 & 80.265625 & & \\
\hline \multicolumn{5}{|l|}{1-X} \\
\hline Z00M & & E/G & DEFN* & WIDTH3 \\
\hline
\end{tabular}

The symbolic definition of Fl is displayed at the bottom of the screen.
10. Press WITHA 3 times to toggle from showing 3 function columns to showing 4 , then 1 , then 2.
\begin{tabular}{|c|c|c|c|c|}
\hline X & F1 & F2 & & \\
\hline 10 & -9 & 78 & & \\
\hline 10.025 & -9.025 & 78.450625 & & \\
\hline 10.05 & -9.05 & 78.9025 & & \\
\hline 11.075 & -9.075 & 79.355625 & & \\
\hline \[
\left\lvert\, \begin{aligned}
& 10.1 \\
& 10.125
\end{aligned}\right.
\] & \[
\begin{aligned}
& -.1 \\
& -9.125
\end{aligned}
\] & \[
\left.\right|_{89.265625}
\] & & \\
\hline \multicolumn{5}{|l|}{\multirow[t]{2}{*}{10}} \\
\hline & & & & \\
\hline 200M & & E/G & DEFN & WDIH3 \\
\hline
\end{tabular}

\begin{tabular}{|l|l|l|l|l|}
\hline \(200 M\) & & EIG & DEFN & WIDTH3 \\
\hline
\end{tabular}

To change column width

\section*{Function app interactive analysis}

From the Plot view ( \({ }_{\text {Plot }}^{\text {Pole }}\) ), you can use the functions on the FCN menu to find roots, intersections, slopes, signed areas and extrema for a function defined in the Function app (and any Function-based apps). The FCN functions act on the currently selected graph.

\section*{Display the Plot menu}

\section*{To find a root of the} quadratic function

To find the intersection of the two functions
1. Display the Plot view menu.

Plot
Setup
MENUL

2. Move the cursor so that it is near \(x=3\).
(2) or \(\odot\) to select the quadratic
(1) or (1) to move the cursor near \(x=3\)

\section*{FCN Select Root}

OK


The root value is displayed at the bottom of the screen.

Note: if there is more than one root (as in our example), the coordinates of the root
 closest to the current cursor position are displayed.
3. Find the intersection of the two functions.



To find the slope of the quadratic function

To find the signed area between the two functions
4. Choose the function whose intersection with the quadratic function you wish to find.

OK to select F1 (X)
The coordinates of the intersection point are displayed at the bottom of the screen.

Note: if there is more than one intersection (as in our example), the coordinates of the intersection point closest
 to the current cursor position are displayed.
5. Find the slope of the quadratic function at the intersection point.


Select Slope

OK
The slope value is displayed at the bottom of the screen. You can use the left-and right-cursor keys to trace along the curve and see the slope at other points. You can also use the up- and down-cursor keys to jump to another function and see the slope at points on that graph. Press CANCI to quit and return to the Plot view.
6. To find the area between the two functions in the range \(-1.3 \leq x \leq 2.3\), first move the cursor to F 1 ( X ) and select the signed area option.
\(\Theta\) or \(\odot\) to select the linear

\section*{MENU}

\section*{FCN}

Select Signed area
7. Move the cursor to \(x=-1.3\) by pressing
(1) or (4) to move to \(x=-1.3\)

OK

8. Press OK to accept
using F 2 (X) as the other boundary for the integral.

9. Choose the end value for
\(x\).
GOTO
2.3


OK

The cursor jumps to
\(x=2.3\) on the linear
function and the area is

shaded. The shading shows " + " (plus) if the area is positive, and "-" (minus) if negative.
10. Display the numerical value of the integral.

CK to display the value
OK to return to the plot menu


\author{
To find the extremum of the quadratic
}
11. Move the cursor to the quadratic equation and find the extremum of the quadratic.

\(\odot\) (to move the tracer to the quadratic)

Select Extremum

The coordinates of the extremum are displayed at the bottom of the screen.

HINT The ROOT and EXTREMUM functions return one value only even if the function has more than one root or extremum. The function finds the value closest to the position of the cursor. You need to re-locate the cursor to find other roots or extrema that may exist.

\section*{The FCN \\ Variables}

The results of the FCN functions are saved in the following variables:
- Root
- Isect
- Slope
- SignedArea
- Extremum

The FCN functions are:
\begin{tabular}{|l|l|}
\hline Function & \begin{tabular}{l} 
Description
\end{tabular} \\
\hline Root & \begin{tabular}{l} 
Select Root to find the root of the \\
current function nearest the cursor. If \\
no root is found, but only an \\
extremum, then the result is labeled \\
Extremum: instead of Root:. The \\
cursor is moved to the root value on \\
the x-axis and the resulting x-value is \\
saved in a variable named Root.
\end{tabular} \\
Extremum & \begin{tabular}{l} 
Select Extremum to find the \\
maximum or minimum of the current \\
function nearest the cursor. The cursor \\
moves to the extremum and the \\
coordinate values are displayed.The \\
resulting value is saved in a variable \\
named Extremum.
\end{tabular} \\
Select Slope to find the numeric \\
derivative of the current function at \\
the current position of the cursor. The \\
result is saved in a variable named \\
Slope. \\
Signed \\
area
\end{tabular}

To access FCN variables

The FCN variables are contained on the Vars menu.
To access FCN variables in the Home view:

\begin{tabular}{|c|c|}
\hline Vars \\
Chars A
\end{tabular}


APP.

Select Function Results
(1) © or \(\odot\) to choose a variable

OK
You can access and use the FCN variables to define functions in the Symbolic view the same way as you do in the Home view.

\section*{Solve app}

\section*{About the Solve app}

The Solve app solves an equation or an expression for one of its unknown variables. You define an equation or expression in the Symbolic view, then supply values for all the variables except one in the Numeric view. Solve works only with real numbers.

Note the differences between an equation and an expression:
- An equation contains an equals sign. Its solution is a value for the unknown variable that makes both sides of the equation have the same value.
- An expression does not contain an equals sign. Its solution is a root, a value for the unknown variable that makes the expression have a value of zero.

You can use the Solve app to solve an equation for any one of its variables. In addition, if the equation or expression is a polynomial in a single variable and there is more than one solution for the variable, then ALT appears in the menu. Pressing this menu key will display a list of all real solutions for the variable.

You can solve the equation as many times as you want, using new values for the knowns and highlighting a different unknown for which to solve.

NOTE You can only have one equation checked at a time. Other apps can have multiple equations checked, but not the Solve app. Once solved, the app carries the values of solved variables into new equations, and you can solve for new variables using the recently calculated values. It is not possible to solve for more than one variable at once. Simultaneous linear equations, for example, should be solved using the Linear Solver app, matrices or graphs in the Function app.

\section*{Getting started with the Solve app}

Suppose you want to find the acceleration needed to increase the speed of a car from \(16.67 \mathrm{~m} / \mathrm{sec}(60 \mathrm{kph})\) to \(27.78 \mathrm{~m} / \mathrm{sec}(100 \mathrm{kph})\) in a distance of 100 m .

The equation to solve is:
\(V^{2}=U^{2}+2 A D\)

\section*{Open the Solve} app
1. Open the Solve app.

Apps
Info Select Solve
START


The Solve app starts in the Symbolic view, where you specify the expression or equation to solve. You can define up to ten equations (or expressions), named E0 to E9. Each equation can contain up to 27 real variables, named \(A\) to \(Z\) and \(\theta\).

\section*{Define the} equation

Enter known variables
2. Define the equation.


Note: you can use the \(\quad=\quad\) menu key to assist in the entry of equations.
3. Display the Solve numeric view screen.


In the Numeric view, you specify the values of the known variables,

highlight the variable that you want to solve for, and press SOLVE
4. Enter the values for the known variables.
\begin{tabular}{|l|l|l|l|}
\hline \multicolumn{4}{|c|}{ SOLVE NUMERIC VIEW } \\
\hline V: 27.78 & \\
U: 16.67 \\
A: 0 \\
D: 100 & & \\
Enter value or press SOLVE & \\
\hline EDIT & & & \\
\hline
\end{tabular}
\(27{ }^{-}\): 78 ENTER \(16=\) 67 (ENTER


Solve the unknown variable

\section*{Plot the equation}
5. Solve for the unknown variable (A).

\begin{tabular}{||l|l|l|l|}
\hline \multicolumn{4}{|c|}{ SOLVE NUMERIC VIEW } \\
\\
V: 27.78 \\
U: 16.67 \\
A: 2.4691975 & \\
D: 100 & & \\
Enter value or press SOLVE & & \\
\hline EDIT & INFO & & \\
\hline
\end{tabular}

Therefore, the acceleration needed to increase the speed of a car from \(16.67 \mathrm{~m} / \mathrm{sec}(60 \mathrm{kph})\) to 27.78 \(\mathrm{m} / \mathrm{sec}(100 \mathrm{kph})\) in a distance of 100 m is approximately \(2.47 \mathrm{~m} / \mathrm{s}^{2}\).
Because the variable \(A\) in the equation is linear we know that we need not look for any other solutions.

The Plot view shows one graph for each side of the selected equation. You can choose any of the variables to be the independent variable.
The current equation is \(V^{2}=U^{2}+2 A D\).
Select \(A\) as the variable. The plot view will now plot two equations. One of these is \(Y=V^{2}\), with \(V=27.78\), that is, \(Y=771.7284\). This graph will be a horizontal line. The other graph will be
\(Y=U^{2}+2 A D\), with \(U=16.67\) and \(D=100\), that is, \(Y=200 A+277.8889\). This graph is also a line. The desired solution is the value of \(A\) where these two lines intersect.
6. Plot the equation for variable A.

Select Auto Scale

\section*{OK}

7. Trace along the graph representing the left side of the equation until the cursor nears the intersection. Note the value of A
 displayed near the bottom left corner of the screen. The Plot view provides a convenient way to find an approximation to a solution instead of using the Numeric view Solve option.

\section*{Solve app's Numeric view keys}

The Solve app's Numeric view keys are:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline EEDIT & \begin{tabular}{l} 
Copies the highlighted value to the \\
edit line for editing. Press OK \\
when done.
\end{tabular} \\
PAGE 7 & \begin{tabular}{l} 
Displays information about the nature \\
of the solution found. \\
Displays other pages of variables, if \\
any. \\
If available, displays a list of multiple \\
solutions for the selected variable. \\
Aisplays the symbolic definition of the \\
current expression. Press OK \\
when done. \\
DEFN
\end{tabular} \\
SOLVE & \begin{tabular}{l} 
Finds a solution for the highlighted \\
variable, based on the values of the \\
other variables.
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|l|}
\hline Key & Meaning (Continued) \\
\hline clear & \begin{tabular}{l} 
Clears highlighted variable to zero or \\
deletes current character in the edit \\
line, if the edit line is active.
\end{tabular} \\
CHIT & \begin{tabular}{l} 
Resets all variable values to zero or \\
clears the edit line, if cursor is in the \\
edit line.
\end{tabular} \\
\hline
\end{tabular}

\section*{Interpreting results}

After Solve has returned a solution, press \(\mathbb{N F}\) in the Numeric view for more information. You will see one of the following three messages. Press \(O K\) to clear the message.
\(\left.\begin{array}{|l|l|}\hline \text { Message } & \text { Condition } \\
\hline \text { Zero } & \begin{array}{l}\text { The Solve app found a point where } \\
\text { both sides of the equation were } \\
\text { equal, or where the expression was } \\
\text { zero (a root), within the calculator's } \\
\text { Reversal } \\
12 \text {-digit accuracy. } \\
\text { Solve found two points where the } \\
\text { difference between the two sides of } \\
\text { the equation has opposite signs, but } \\
\text { it cannot find a point in between } \\
\text { where the value is zero. Similarly, } \\
\text { for an expression, where the value } \\
\text { of the expression has different signs } \\
\text { but is not precisely zero. This might } \\
\text { be because either the two points are } \\
\text { neighbours (they differ by one in the } \\
\text { twelfth digit), or the equation is not } \\
\text { real-valued between the two points. } \\
\text { Solve returns the point where the } \\
\text { value or difference is closer to zero. } \\
\text { If the equation or expression is } \\
\text { continuously real, this point is } \\
\text { Solve's best approximation of an } \\
\text { actual solution. }\end{array} \\
\text { Extremum } \\
\text { Solve found a point where the value } \\
\text { of the expression approximates a } \\
\text { local minimum (for positive values) } \\
\text { or maximum (for negative values). } \\
\text { This point may or may not be a } \\
\text { solution. } \\
\text { Or: Solve stopped searching at } \\
\text { 9.99999999999E499, the largest } \\
\text { number the calculator can } \\
\text { represent. }\end{array}\right\}\)\begin{tabular}{l} 
Note that the value returned is \\
probably not valid.
\end{tabular}

If Solve could not find a solution, you will see one of the following two messages.
\begin{tabular}{|l|l|}
\hline Message & Condition \\
\hline \begin{tabular}{l} 
Bad \\
Guess (es)
\end{tabular} & \begin{tabular}{l} 
The initial guess lies outside the \\
domain of the equation. \\
Therefore, the solution was not a \\
real number or it caused an error.
\end{tabular} \\
Constant? & \begin{tabular}{l} 
The value of the equation is the \\
same at every point sampled.
\end{tabular} \\
\hline
\end{tabular}

HIN T It is important to check the information relating to the solve process. For example, the solution that the Solve app finds is not a solution, but the closest that the function gets to zero. Only by checking the information will you know that this is the case.

\section*{Multiple solutions}

Consider the polynomial equation:
\(x^{2}-x-1=0\)
Since this equation is quadratic for \(x\), there can be (and in this case are) two solutions. In the case of polynomials, the HP 39 gll offers a quick way to find multiple solutions.
1. Select the Solve app and enter the equation.


Select Solve START



2. Solve for \(x\).

ALT appears in the menu to alert you that there are multiple solutions.


Press ALT to see the list of solutions and to select the one you want.

\section*{Using variables in equations}

You can use any of the real variable names, \(A\) to \(Z\) and \(\theta\). Do not use variable names defined for other types, such as M1 (a matrix variable).

Home variables
All home variables (other than those for app settings, like Xmin and Ytick) are global, which means they are shared throughout the different apps of the calculator. A value that is assigned to a home variable anywhere remains with that variable wherever its name is used.

Therefore, if you have defined a value for \(T\) (as in the above example) in another app or even another Solve equation, that value shows up in the Numeric view for this Solve equation. When you then redefine the value for \(T\) in this Solve equation, that value is applied to \(T\) in all other contexts (until it is changed again).

This sharing allows you to work on the same problem in different places (such as Home and the Solve app) without having to update the value whenever it is recalculated.

HINT As the Solve app uses existing variable values, be sure to check for existing variable values that may affect the solve process. (You can use SLEAR to reset all values to zero in the Solve app's Numeric view if you wish.)

App variables
Functions defined in other apps can also be referenced in the Solve app. For example, if you define \(F 1(X)=X^{2}+10\) in the Function app, you can enter \(\mathrm{Fl}(\mathrm{X})=50\) in the Solve app to solve the equation \(X^{2}+10=50\).

\section*{Statistics 1Var app}

\section*{About the Statistics 1Var app}

The Statistics 1Var app can store up to ten data sets at one time. It can perform one-variable statistical analysis of one or more sets of data.

The Statistics 1Var app starts with the Numeric view which is used to enter data. The Symbolic view is used to specify which columns contain data and which column contains frequencies.

You can also compute statistics values in Home and recall the values of specific statistics variables.

The values computed in the Statistics 1Var app are saved in variables, and many of these variables are listed by the STATS function accessible from the Statistics 1Var app's Numeric view.

\section*{Getting started with the Statistics 1Var app}

The following example is about the heights of students in a classroom. We will use the example to introduce the structure and function of the Statistics 1Var app. You are measuring the heights of students in a classroom to find the mean height. The first five students have the following measurements: \(160 \mathrm{~cm}, 165 \mathrm{~cm}, 170 \mathrm{~cm}, 175 \mathrm{~cm}\), 180 cm .
1. Open the Statistics 1Var app.

2. Enter the measurement data.


170
\begin{tabular}{l} 
ENTER \\
\hline ANS
\end{tabular}

175 \(\qquad\)

180 ENTER
3. Find the mean of the sample.

Press STATS to see the statistics calculated from the sample data in
 D1.
Note that the title of the column of statistics is H 1 . There are 5 data set definitions available for onevariable statistics: \(\mathrm{H} 1-\mathrm{H} 5\). If data is entered in D1, H1 is automatically set to use D1 for data, and the frequency of each data point is set to 1 . You can select other columns of data from the Symbolic view of the app.
4. Press OK to close the statistics window.
 data set definitions.


The first column indicates the associated column of data for each data set definition, and the second column indicates the constant frequency, or the column that holds the frequencies.

\section*{Statistics 1Var app's Symb View keys}

The keys you can use from this window are:
\begin{tabular}{|c|c|}
\hline Key & Meaning \\
\hline EEDT & Copies the column variable (or variable expression) to the edit line for editing. Press oK when done. \\
\hline CHK & Checks/unchecks the current data set. Only the checkmarked data set(s) are computed and plotted. \\
\hline D & Typing aid for the column names. \\
\hline SHOW & Displays the current expression is Textbook Format. Press OK when done. \\
\hline EVAL & Evaluates the highlighted expression, resolving any references to function expressions. \\
\hline  & Displays the menu for entering variable names or contents of variables. \\
\hline \({ }_{\text {cosem }}^{\text {Matas }}\) & Displays the menu for entering math operations. \\
\hline ccores & Deletes the highlighted variable or the character to the left of the cursor in the edit line. \\
\hline \({ }_{\text {shlir }}\) & Resets default specifications for the data sets or clears the edit line (if it was active). \\
\hline
\end{tabular}

To continue our example, suppose that the heights of the rest of the students in the class are measured, but each one is rounded to the nearest of the five values first recorded. Instead of entering all the new data in D1, we
shall simply add another column, D2, that holds the frequencies of our five data points in D1.
\begin{tabular}{|c|c|}
\hline Height (cm) & Frequency \\
\hline 160 & 5 \\
165 & 3 \\
170 & 8 \\
175 & 2 \\
180 & 1 \\
\hline
\end{tabular}
5. Move the highlight bar into the right column of the H 1 definition and enter the column variable name D 2 .


\section*{D 2}
6. Return to the numeric view.
7. Enter the frequency data shown in the above table.


8
```

ENTER
ANS

```
\(2{ }^{\text {ENTER }}\)

1 有NER
8. Display the computed statistics.

\section*{STATS}

The mean height is

\begin{tabular}{|l|l|l|l|l|l|}
\hline EDIT & INS & SORT & BIG & MAKE & STATS \\
\hline
\end{tabular}

approximately
167.63 cm .
9. Setup a histogram plot for the data.

OK
 SETUPPLOT

Enter set up information appropriate to your data.
10. Plot a histogram of the data.


\section*{Entering and editing statistical data}

The Numeric view ( \(\begin{aligned} & \text { Nom } \\ & \text { Sevep }\end{aligned}\) ) is used to enter data into the Statistics 1Var app. Each column represents a variable named D0 to D9. After entering the data, you must define the data set in the Symbolic view ( \(\left.\begin{array}{l}\text { Symb } \\ \text { Sevep }\end{array}\right)\).

HIN T A data column must have at least two data points for onevariable statistics.

You can also store statistical data values by copying lists from Home into statistics data columns. For example, in Home, L1 STO - D1 stores a copy of the list L1 into the data-column variable D1.

\section*{Statistics 1Var app's Num View keys}

The Statistics 1Var app's Numeric view keys are:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline EDIT & \begin{tabular}{l} 
Copies the highlighted item into \\
the edit line.
\end{tabular} \\
\hline \(\mathbb{N} E\) & \begin{tabular}{l} 
Inserts a zero value above the \\
highlighted cell.
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Key & Meaning (Continued) \\
\hline SORT & Sorts the specified independent data column in ascending or descending order, and rearranges a specified dependent (or frequency) data column accordingly. \\
\hline ElG & Switches between larger and smaller font sizes. \\
\hline MAKE & Opens a dialog box for creating a sequence based on an expression and storing it in a data column. \\
\hline STATS & Computes descriptive statistics for each data set specified in the Symbolic view. \\
\hline Clear & Deletes the currently highlighted value. \\
\hline SHIT CLEAR & \begin{tabular}{l}
Clears the current column or all columns of data. \\
Press CLEAR to display a menu list, then select the current column or all columns option, and press OK.
\end{tabular} \\
\hline SHIT CURSOR KEY & Moves to the first or last row, or first or last column. \\
\hline
\end{tabular}

The data that you enter is automatically saved. When you are finished entering data values, you can press a key for
 another app or Home.

Edit a data set

Delete data

Insert data

Sort data values

In the Numeric view of the Statistics 1Var app, highlight the data value to change. Type a new value and press \(\underset{\text { ENs }}{ }\) NTR , or press EDIT to copy the value to the edit
 on the edit line.
- To delete a single data item, highlight it and press
cher . The values below the deleted cell will scroll up one row.
- To delete a column of data, highlight an entry in that column and press CLEAR. Select the column name and press OK
- To delete all columns of data, press
 Select All columns and press \(\mathrm{OK}^{2}\)

Highlight the entry following the point of insertion. Press
\(\mathbb{N S}\), then enter a number. It will write over the zero that was inserted.
1. In Numeric view, highlight the column you want to sort, and press SORT
2. Specify the Sort Order. You can choose either Ascending or Descending.
3. Specify the INDEPENDENT and DEPENDENT data columns. Sorting is by the independent column. For instance, if Age is D1 and Income is D2 and you want to sort by Income, then you make D2 the independent column for the sorting and D1 the dependent column.
- To sort just one column, choose None for the dependent column.
- For one-variable statistics with two data columns, specify the frequency column in the Frequency field.
4. Press \(O K\)

\section*{Computed statistics}

Pressing STATS displays the results in the following table.
\begin{tabular}{|l|l|}
\hline Statistic & Definition \\
\hline n & \begin{tabular}{l} 
Number of data points. \\
Qin \\
Qinimum data value in data set.
\end{tabular} \\
Med & \begin{tabular}{l} 
First quartile: median of values to \\
left of median. \\
Q3
\end{tabular} \\
Max & \begin{tabular}{l} 
Median value of data set. \\
Third quartile: median of values to \\
right of median.
\end{tabular} \\
\(\Sigma X^{2}\) & \begin{tabular}{l} 
Maximum data value in data set. \\
Sum of data values (with their \\
frequencies). \\
Sum of the squares of the data \\
values.
\end{tabular} \\
sX Mean of the data values. \\
\(\sigma X\) & \begin{tabular}{l} 
Sample standard deviation of the \\
data set. \\
Population standard deviation of \\
the data set. \\
Standard error of the data set.
\end{tabular} \\
\hline
\end{tabular}

When the data set contains an odd number of values, the data set's median value is not used when calculating Q1 and Q3 in the table above. For example, for the following data set:
\(\{3,5,7,8,15,16,17\}\)
only the first three items, 3,5 , and 7 are used to calculate Q1, and only the last three terms, 15,16 , and 17 are used to calculate Q3.

\author{
Plotting \\ \section*{To plot statistical data}
}

You can plot:
- Histograms
- Box-and-Whisker plots
- Normal Probability plots
- Line plots
- Bar graphs
- Pareto charts

Once you have entered your data and defined your data set, you can plot your data. You can plot up to five box-and-whisker plots at a time; however, with the other types, you can only plot one of them at a time.
1. In the Symbolic view (( \(\substack{\text { smmp } \\ \text { smap }})\), select (CHK) the data sets you want to plot.
2. Select the plot type. Highlight the Plot field for your data set, press the choos menu key, and scroll to the plot type you want. Press the OK menu key when you have made your choice.
3. For any plot, but especially for a histogram, adjust the plotting scale and range in the Plot Setup view. If you find histogram bars too fat or too thin, you can adjust them by changing the HWIDTH setting.
4. Press Slemp . If you have not adjusted the Plot Setup yourself, you can try \(\xlongequal[\substack{\text { news } \\ \text { mad }}]{\substack{\text { nel }}}\) select Auto Scale

\section*{OK}

AutoScale can be relied upon to give a good starting scale which can then be adjusted in the Plot Setup view.

\section*{Plot types}

\author{
Histogram \\ Box-and-Whisker plot
}
```

normal probability plot

```

Line plot

The numbers below the plot mean that the current bar (where the cursor is) starts at 0 and ends at 2 (not including 2), and the
 frequency for this column, (that is, the number of data elements that fall between 0 and 2) is 1 . You can see information about the next bar by pressing ( .

The left whisker marks the minimum data value. The box marks the first quartile, the median (where the cursor is), and the third quartile.
 The right whisker marks the maximum data value. The numbers below the plot mean that this column has a minimum of 1.2.

The normal probability plot is used to determine whether or not sample data is more or less normally distributed. The more linear the data
 appear, the more likely that the data is normally distributed.

The line plot connects points of the form \((x, y)\), where \(x\) is the row number of the data point and \(y\) is the value of the data point.


The bar graph shows the value of a data point as a vertical bar placed along the \(x\)-axis at the row number of the data point.

\begin{tabular}{ll} 
Pareto chart & \begin{tabular}{l} 
A pareto chart places the \\
data in descending order \\
and displays each with its \\
percentage of the whole.
\end{tabular}
\end{tabular}

\section*{Setting up the plot (Plot Setup view)}

The Plot Setup (SHIIT SETUP-PLOT) sets most of the same plotting parameters as it does for the other built-in HP Apps. Settings unique to the Statistics 1Var app are as follows:

Histogram width

Histogram range

HWIDTH enables you to specify the width of a histogram bar. This determines how many bars will fit in the display, as well as how the data is distributed (how many values each bar represents).

HRNG enables you to specify the range of values for a set of histogram bars. The range runs from the left edge of the leftmost bar to the right edge of the rightmost bar. You can limit the range to exclude any values you suspect are outliers.

\section*{Exploring the graph}

The Plot view has menu keys for zooming, tracing, and coordinate display. There are also scaling options under Views
Help

\section*{Statistics 1Var app's Plot View keys}

The Plot view keys are:
\begin{tabular}{|c|c|}
\hline Key & Meaning \\
\hline SHIIT CLEAR & Erases the plot. \\
\hline  & Offers additional pre-defined views for splitting the screen and autoscaling the axes. \\
\hline  & Moves cursor to far left or far right. \\
\hline ZOOM & Displays the Zoom menu. \\
\hline TRACE & Turns trace mode on/off. The white box appears next to the option when Trace mode is active. \\
\hline DEFN & Displays the definition of the current statistical plot. \\
\hline MENU & Toggles the menu off and on. \\
\hline
\end{tabular}

\section*{Statistics 2Var app}

\section*{About the Statistics 2Var app}

The Statistics 2Var app can store up to ten data sets at one time. It can perform two-variable statistical analysis of one or more sets of data.

The Statistics 2Var app starts with the Numeric view which is used to enter data. The Symbolic view is used to specify which columns contain data and which column contains frequencies.

You can also compute statistics values in Home and recall the values of specific statistics variables.

The values computed in the Statistics \(2 V\) ar app are saved in variables, and many of these variables are listed by the STATS function accessible from the Statistics 2 Var app's Numeric view.

\section*{Getting started with the Statistics 2Var app}

The following example is based on the advertising and sales data in the table below. In the example, you will enter the data, compute summary statistics, fit a curve to the data, and predict the effect of more advertising on sales.
\begin{tabular}{|c|c|}
\hline \begin{tabular}{l} 
Advertising minutes \\
(independent, \(\mathbf{x}\) )
\end{tabular} & \begin{tabular}{l} 
Resulting Sales (\$) \\
(dependent, \(\mathbf{y}\) )
\end{tabular} \\
\hline 2 & 1400 \\
1 & 920 \\
3 & 1100 \\
5 & 2265 \\
5 & 2890 \\
4 & 2200 \\
\hline
\end{tabular}

Open the
Statistics 2Var
app
1. Clear existing data and open the Statistics 2 Var app.

\section*{Apps}

Select Statistics
2Var
RESET OK
START


The Statistics 2Var app starts in the Numeric view.
2. Enter the data into the columns.

\(3 \underset{\text { ENS }}{\text { ENTER }} 5 \stackrel{\text { ENTER }}{\text { ENS }}\)
\begin{tabular}{|l||l|l|l|l||}
\hline & C1 & \multicolumn{1}{c|}{ C2 } & C3 & C4 \\
\hline 1 & 2 & & 1400 & \\
2 & 1 & & 920 & \\
3 & 3 & & 1100 & \\
4 & 5 & & 2265 & \\
5 & 5 & & 2890 & \\
6 & 4 & & 2200 & \\
\hline
\end{tabular}
\(5 \stackrel{\text { ENTER }}{\text { ENS }} 4\) ENTER
( ) to move to the next column
\(1400 \xlongequal{\text { ENNTER }}\) 920 ENTER
 \(2890 \stackrel{\text { ENTER }}{\text { ANS }}\) \(2200 \stackrel{\text { ANTER }}{\text { ANS }}\)

Choose data columns and fit
3. Specify the columns that hold the data you want to analyze.


You could have entered your data into columns other than C1 and C2.
4. Select a fit.


Select Linear


You can create up to five explorations of two-variable data, named S1 to \(\mathrm{S5}\). In this example, we will create just one: sl .
5. Find the correlation, \(r\), between advertising time and sales.
```

Num
Setup
STATS

```

The correlation is \(r=0.8995\)...

6. Find the mean advertising time ( \(\bar{x}\) ) and the mean sales ( \(\bar{y}\) ).
\begin{tabular}{|c|c|c|c|c|c|}
\hline & & & & & \\
\hline \(\overline{\mathrm{X}}\) & 3,333 & 333 & & & \\
\hline \({ }_{\text {区 }} \mathrm{X}^{2}\) & & & & & \\
\hline \(\frac{2}{2} \mathrm{X}^{2}\) & & & & & \\
\hline \[
\left\lvert\, \begin{aligned}
& \stackrel{3}{\alpha x} \\
& \hline x
\end{aligned}\right.
\] & \[
\begin{aligned}
& 1.632 \\
& 1.490
\end{aligned}
\] & 162 & & & \\
\hline \[
\|_{\operatorname{sex}}^{\sigma X}
\] & 6.666 & E-1 & & & \\
\hline \multicolumn{6}{|l|}{3.33333333333} \\
\hline STATS & X & Y & E|G & WIDTH3 & OK \\
\hline
\end{tabular}

X
The mean advertising time, \(\bar{x}\), is approximately 3.3 minutes.

Y
The mean sales, \(\bar{y}\), is approximately \(\$ 1,796\).

OK
\begin{tabular}{|c|c|c|c|c|c|}
\hline & & & & & \\
\hline \% & 11.79 & 33] & & & \\
\hline EV\% & & & & & \\
\hline \[
{ }_{s}^{5} V_{V}^{2}
\] & 2233 & 25 & & & \\
\hline \({ }_{\sigma} Y\) & 7.05 & 46E2 & & & \\
\hline seY & & 46E2 & & & \\
\hline \multicolumn{6}{|l|}{1795.83333333} \\
\hline STATS & X & V* & EIG & WIDTH3 & OK \\
\hline
\end{tabular}

\section*{Setup plot}
7. Change the plotting range to ensure all the data points are plotted (and select a different point mark, if you wish).


\section*{Plot the graph}

\section*{Draw the regression curve}
8. Plot the graph.
9. Draw the regression curve (a curve to fit the data points).


This draws the regression line for the best linear fit.

Display the equation
10. Return to the Symbolic view.

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multicolumn{2}{|l|}{DEG Statistics 2-Var Symb View} & & & & \\
\hline \multicolumn{6}{|l|}{- S1:C1} \\
\hline \multicolumn{6}{|l|}{\(\checkmark\) Type1:Linear} \\
\hline \multicolumn{6}{|l|}{-Fit 1:425.875*X+376.25} \\
\hline \multicolumn{6}{|l|}{S2:} \\
\hline \multicolumn{6}{|l|}{Type2:Linear} \\
\hline \multicolumn{6}{|l|}{Enter Independent Column} \\
\hline EDIT & \(\checkmark \mathrm{CHK}\) & C & FIT* & SHOW & EVAL \\
\hline
\end{tabular}

The slope \((m)\) is 425.875 . The \(y\)-intercept ( \(b\) ) is 376.25 .

\section*{Predict values}

Predict the sales figure if advertising were to go up to 6 minutes.
11. Return to the Plot view.

12. Trace to \(x=6\) on the linear fit.
* to move the tracer to the fit
(1) 40 times to find \(\mathrm{x}=6\)


The model predicts that sales would rise to \(\$ 2,931.50\) if advertising were increased to 6 minutes.

\section*{Entering and editing statistical data}

The Numeric view ( Statistics 2 Var app. Each column represents a variable named c 0 to C 9 . After entering the data, you must define the data set in the Symbolic view ( \(\left.\begin{array}{c}\text { ssmm } \\ \text { semp }\end{array}\right)\).
H IN T A data column must have at least four data points to provide valid two-variable statistics.

You can also store statistical data values by copying lists from Home into Statistics data columns. For example, in Home, L1 STO C1 stores a copy of the list L1 into the data-column variable C 1 .

\section*{Statistics 2Var app's NUM view keys}

The Statistics 2Var app's Numeric view keys are:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline EEDT & \begin{tabular}{l} 
Copies the highlighted item into the \\
edit line. \\
Inserts a zero value above the \\
highlighted cell.
\end{tabular} \\
\hline INS & \begin{tabular}{l} 
I
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Key & Meaning (Continued) \\
\hline SORT & Sorts the specified independent data column in ascending or descending order, and rearranges a specified dependent (or frequency) data column accordingly. \\
\hline EIG* & Switches between larger and smaller font sizes. \\
\hline MAKE & Opens a dialog box to create a column of data based on an expression. \\
\hline STATS & Computes descriptive statistics for each data set specified in the Symbolic view. \\
\hline \(\square\) & Deletes the currently highlighted value. \\
\hline  & Clears the current column or all columns of data. Press \(\square\) CLEAR to display a menu list, then select the current column or all columns option, and press \(\square\) ok. \\
\hline \begin{tabular}{l}
SHITI \\
CURSOR KEY
\end{tabular} & Moves to the first or last row, or first or last column. \\
\hline
\end{tabular}

Save data
The data that you enter is automatically saved. When you are finished entering data values, you can press a key for another Statistics view (like Sespe semb ), or you can switch to another app or Home.

Edit a data set
In the Numeric view of the Statistics 2Var app, highlight the data value to change. Type a new value and press \(\underset{\text { ENS }}{\text { ENTR }}\), or press EDIT to copy the value to the edit line for modification. Press \(\underset{\text { ©NTER }}{\text { ENTER }}\) after modifying the value on the edit line.

\section*{Delete data}

Insert data

Sort data values
- To delete a single data item, highlight it and press
clear . The values below the deleted cell will scroll up one row.
- To delete a column of data, highlight an entry in that column and press CLIFIT Select the column name.
- To delete all columns of data, press SHIT CLEAR. Select All columns.

Highlight the entry following the point of insertion. Press INS , then enter a number. It will write over the zero that was inserted.
1. In Numeric view, highlight the column you want to sort, and press SORT.
2. Specify the Sort Order. You can choose either Ascending or Descending.
3. Specify the INDEPENDENT, DEPENDENT, and (if applicable) the FREQUENCY data columns. Sorting is by the independent column. For instance, if Age is C1 and Income is C2 and you want to sort by Income, then you make C 2 the independent column for the sorting and C1 the dependent column.
- To sort just one column, choose None for the dependent column.
- For one-variable statistics with two data columns, specify the frequency column as the dependent column.
4. Press OK

\section*{Defining a regression model}

The Symbolic view includes an expression (Fit1 through Fit5) that defines the regression model, or "fit", to use for the regression analysis of each two-variable data set.
There are three ways to select a regression model:
- Accept the default option to fit the data to a straight line.
- Select one of the available fit options in the Symbolic view.
- Enter your own mathematical expression in the Symbolic view. This expression will be plotted, but it will not be fitted to the data points.

\section*{Angle Setting}

\section*{Choose the fit}

Fit models

You can ignore the angle measurement mode unless your Fit definition (in the Symbolic view) involves a trigonometric function. In this case, you should specify in the Symbolic setup whether the trigonometric units are to be interpreted as degrees or radians.
 Type number (Type1 through Type5) you want to define.
2. Press and select from the list. Press ok when done. The regression formula for the fit is displayed in the Symbolic view.

Eleven fit models are available:
\begin{tabular}{|l|l|}
\hline Fit model & Meaning \\
\hline Linear & \begin{tabular}{l} 
(Default.) Fits the data to a \\
straight line, \(y=m x+b\). Uses a \\
least-squares fit.
\end{tabular} \\
Exponarithmic & \begin{tabular}{l} 
Fits to a logarithmic curve, \\
\(y=m \ln x+b\). \\
Fits to an exponential curve, \\
\(y=b e^{m x}\). \\
Power \\
Exponent
\end{tabular} \\
\begin{tabular}{l} 
Fits to a power curve, \(y=b x^{m}\). \\
Fits to an exponent curve, \\
\(y=a b^{x}\). \\
Inverse
\end{tabular} & \begin{tabular}{l} 
Fits to an inverse variation, \\
\(y=\frac{m}{x+b}\)
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Fit model & Meaning (Continued) \\
\hline Logistic & \begin{tabular}{l}
Fits to a logistic curve,
\[
y=\frac{L}{1+a e^{(-b x)}}
\] \\
where \(L\) is the saturation value for growth. You can store a positive real value in \(L\), or-if \(L=0\)-let \(L\) be computed automatically.
\end{tabular} \\
\hline Quadratic & Fits to a quadratic curve, \(y=a x^{2}+b x+c\). Needs at least three points. \\
\hline Cubic & Fits to a cubic polynomial,
\[
y=a x^{3}+b^{2} x+c x+d
\] \\
\hline Quartic & Fits to a quartic polynomial, \(y=a x^{4}+b x^{3}+c x^{2}+d x+e\) \\
\hline Trigonometric & Fits to a trigonometric curve, \(y=a \cdot \sin (b x+c)+d\). Needs at least three points. \\
\hline User Defined & Define your own expression (in the Symbolic view.) \\
\hline
\end{tabular}

To define your own fit
1. Display the Symbolic view.
2. Highlight the Fit expression (Fit1, etc.) for the desired data set.
3. Type in an expression and press \(\stackrel{\text { ENNER }}{\text { ENS }}\). The independent variable must be \(X\), and the expression must not contain any unknown variables.
Example: \(1.5 \times \cos x+0.3 \times \sin x\).

\section*{Computed statistics}

When you press STATS, there are three sets of statistics available. By default, the statistics involving both the independent and dependent columns are shown. Press
\(x\) to see the statistics involving just the independent column or Y to display the statistics derived from the
dependent column. Press [SAATS to return to the default view. The tables below describe the statistics displayed in each view.

Here are the statistics computed when you press STAIS.
\begin{tabular}{|l|l|}
\hline Statistic & Definition \\
\hline n & \begin{tabular}{l} 
The number of data points. \\
r \\
Correlation coefficient of the \\
independent and dependent data \\
columns, based only on the linear \\
fit (regardless o the fit type chosen). \\
Returns a value from - - to 1, where \\
1 and -1 indicate best fits.
\end{tabular} \\
\(\mathrm{R}^{2}\) & \begin{tabular}{l} 
The coefficient of determination, \\
which is the square of the \\
correlation coefficient. The value of \\
this statistics is dependent on the Fit \\
type chosen. \\
Sample covariance of independent \\
and dependent data columns.
\end{tabular} \\
\(\operatorname{sCOV}\) & \begin{tabular}{l} 
Population covariance of \\
independent and dependent data \\
columns. \\
Sum of \(x y\) products.
\end{tabular} \\
\hline
\end{tabular}

Here are the statistics displayed when you press \(x\)
\begin{tabular}{|l|l|}
\hline Statistic & Definition \\
\hline \(\bar{x}\) & \begin{tabular}{l} 
Mean of \(x\)-(independent) values. \\
\(\Sigma \mathrm{X}\) \\
XX \\
SX
\end{tabular} \\
Sum of \(x\)-values. \\
SerrX & \begin{tabular}{l} 
Sum of \(x^{2}\)-values. \\
The sample standard deviation of \\
the independent column.
\end{tabular} \\
\begin{tabular}{l} 
The population standard deviation \\
of the independent column. \\
the standard error of the \\
independent column
\end{tabular} \\
\hline
\end{tabular}

Here are the statistics displayed when you press
\begin{tabular}{|l|l|}
\hline Statistic & Definition \\
\hline \(\bar{y}\) & Mean of \(y\)-(dependent) values. \\
\(\Sigma Y\) & Sum of \(y\)-values. \\
\(\Sigma \mathrm{Y}^{2}\) & \begin{tabular}{l} 
Sum of \(y^{2}\)-values. \\
SY \\
\(\sigma Y\) \\
Serry \\
the sample standard deviation of \\
the dendent column. \\
The population standard deviation \\
of the dependent column. \\
The standard error of the \\
dependent column.
\end{tabular} \\
\hline
\end{tabular}

\section*{Plotting}

\section*{To plot statistical data}

Once you have entered your data ( data set and your fit model ( \((\substack{\text { smmb } \\ \text { smop } \\ \text { som }}\) ), you can plot your data. You can plot up to five scatter plots at a time.
 you want to plot.
2. Adjust the plotting scale and range in the Plot Setup view.
3. Press \(\xlongequal[\substack{\text { Poot } \\ \text { solup }}]{\text {. If you have not adjusted the Plot Setup }}\) yourself, you can try \({ }_{\substack{\text { Vems } \\ \text { Hep }}}^{\text {velect Auto Scale ok }}\)

Auto Scale can be relied upon to give a good starting scale which can then be adjusted in the Plot Setup.

Tracing a Scatter Plot

The numbers below the plot indicate that the cursor is at the first data point for S1, at \((1,6)\). Press © to move to the next data point and display information about it.


Fitting a curve
Press MENI Hire. The graph of the fit will be displayed with the scatter plot. Press \(\rightarrow\) to move the tracer to the graph of the fit. Press (1) and (4) to trace along the fit and IIEN to see the equation of the fit.

Press \(\underset{\substack{\text { Scmb } \\ \text { semp }}}{ }\) to see the equation of the fit in the Fitl field. To see the full equation, highlight the fit equation and press

\section*{SHOW'}

The expression in Fit2 shows the slope ( \(\mathrm{m}=1.98082191781\) ) and the \(y\)-intercept \((b=2.26575)\).


Correlation Coefficient, \(r\)

The correlation coefficient is stored in the variable \(r\). It is a measure of fit to a linear curve only. Regardless of the fit model you have chosen, \(r\) relates to the linear model. The value of \(r\) can range from -1 to 1 , where -1 and 1 indicate best fits.

\section*{Coefficient of}

\section*{Plot setup}

Plotting mark

HINT In order to access the \(r\) and \(R^{2}\) variables after you plot a data set, you must press \({ }_{S \text { som }}^{\text {Nom }}\) to access the numeric view and then STAIS to display the correlation values. The values are stored in the variables when you access the Numeric view Stats page.
The Coefficient of Determination is a measure of the goodness of fit of your model, regardless of whether that model is linear or not. A measure of 1 indicates a perfect fit.

The Plot Setup (stiri SETUP-PLOT) sets most of the same plotting parameters as it does for the other built-in apps; in addition, it has one unique setting:

S1MARK through S5MARK enables you to specify one of five symbols to use to plot each data set. Press CHOOS to change the highlighted setting.

\section*{Trouble-shooting a plot}

If you have problems plotting, check that you have the following:
- The correct fit (regression model).
- Only the data sets to compute or plot are checkmarked (Symbolic view).
- The correct plotting range. Try using \(\underset{\substack{\text { Vems } \\ \text { Hep }}}{\substack{\text { ento }}}\) Auto Scale (instead of (in Plot Setup) for the ranges of the axes.
- Ensure that both paired columns contain data, and that they are the same length.
- Ensure that a paired column of frequency values is the same length as the data column to which it refers.

Exploring the graph The Plot view has menu keys for zooming, tracing, and coordinate display. There are also scaling options under \begin{tabular}{|c} 
Views \\
Help
\end{tabular}

\section*{Statistics 2Var app's Plot view keys}
\begin{tabular}{|c|c|}
\hline Key & Meaning \\
\hline \({ }^{\text {strin }}\) CLEAR & Erases the plot. \\
\hline  & Offers additional pre-defined views for splitting the screen and autoscaling the axes. \\
\hline  & Moves cursor to far left or far right. \\
\hline ZOOM & Displays the Zoom menu. \\
\hline TRACE* & Turns trace mode on/off. The white dot appears next to the option when Trace mode is active. \\
\hline FIT* & Turns fit mode on or off. Turning Fire on draws a curve to fit the data points according to the current regression model. \\
\hline GOTO & Enables you to specify a value on the line of best fit to jump to or a data point number to jump to. \\
\hline DEFN & Displays the equation of the regression curve or the definition of the current statistical plot. \\
\hline MENU & Hides and displays the menu key labels. \\
\hline
\end{tabular}

\section*{Calculating predicted values}

The functions PREDX and PREDY estimate (predict) values for X or Y given a hypothetical value for the other. The estimation is made based on the equation that has been calculated to fit the data according to the specified fit.

\section*{Find predicted values}
1. In the Plot view, draw the regression curve for the data set.
2. Press \(\odot\) to move to the regression curve.
3. Press and anter the value of X . The cursor jumps to the specified point on the curve and the coordinate display shows X and the predicted value of \(Y\).

In the Home view:
 for the independent variable given a hypothetical dependent value.
- Enter PREDY( \(x\)-value) to find the predicted value of the dependent variable given a hypothetical independent variable.

You can type PREDX and PREDY into the edit line, or you can copy these function names from the Commands menu under the Apps, Statistics 2 Var category.
HINT In cases where more than one fit curve is displayed, the PREDX and PREDY functions use the first active fit defined in the Symbolic view.

\section*{Inference app}

\section*{About the Inference app}

The Inference app's capabilities include calculation of confidence intervals and hypothesis tests based on the Normal Z-distribution or Student's t-distribution.

Based on statistics from one or two samples, you can test hypotheses and find confidence intervals for the following quantities:
- mean
- proportion
- difference between two means
- difference between two proportions

\section*{Example data}

When you first access an input form for an Inference test, by default, the input form contains example data. This example data is designed to return meaningful results that relate to the test. It is useful for gaining an understanding of what the test does, and for demonstrating the test. The calculator's on-line help provides a description of what the example data represents.

\section*{Getting started with the Inference app}

This example describes the Inference app's options and functionality by stepping you through an example using the example data for the Z-Test on 1 mean.

\section*{Open the Inference app}
1. Open the Inference app.


Select Inference
RESET OK START
The Inference app opens in the Symbolic view.

\section*{Inference app's Symbolic view options}

The table below summarizes the options available in Symbolic view.
\begin{tabular}{|c|c|}
\hline Hypothesis Tests & Confidence Intervals \\
\hline \begin{tabular}{l}
Z-Test: \(1 \mu\), the Z- \\
Test on 1 mean
\end{tabular} & Z-Int: \(1 \mu\), the confidence interval for 1 mean, based on the Normal distribution \\
\hline Z-Test: \(\mu_{1}-\mu_{2}\), the Z-Test on the difference of two means & Z-Int: \(\mu_{1}-\mu_{2}\), the confidence interval for the difference of two means, based on the Normal distribution \\
\hline Z-Test: 1 p, the \(Z\) Test on 1 proportion & Z-Int: 1 p, the confidence interval for 1 proportion, based on the Normal distribution \\
\hline Z-Test: \(p_{1}-p_{2}\), the Z-Test on the difference of two proportions & Z-Int: \(p_{1}-p_{2}\), the confidence interval for the difference of two proportions, based on the Normal distribution \\
\hline T-Test: \(1 \mu\), the T Test on 1 mean & T-Int: \(1 \mu\), the confidence interval for 1 mean, based on the Student's \(t\)-distribution \\
\hline T-Test: \(\mu_{1}-\mu_{2}\), the T-Test on the difference of two means & T-Int: \(\mu_{1}-\mu_{2}\), the confidence interval for the difference of two means, based on the Student's \(\ddagger\)-distribution \\
\hline
\end{tabular}

If you choose one of the hypothesis tests, you can choose the alternative hypothesis to test against the null hypothesis. For each test, there are three possible choices for an alternative hypothesis based on a quantitative comparison of two quantities. The null hypothesis is always that the two quantities are equal. Thus, the alternative hypotheses cover the various cases for the two quantities being unequal: \(<,>\), and \(\neq\).

\section*{Select the inferential method}

In this section, we will use the example data for the Z-Test on 1 mean to illustrate how the app works and what features the various views present.
2. Select the Hypothesis Test inferential method.

\section*{CHOOS}

Select Hypothesis
Test

OK

3. Define the type of test.


CHOOS
Z-Test: \(1 \mu\)


\section*{OK}
4. Select an alternative hypothesis.


\section*{CHOOS}
\(\mu<\mu_{0}\)


OK
5. Go to the Numeric view to see the default data.
\begin{tabular}{|c|c|c|c|}
\hline \multicolumn{4}{|c|}{Inf Stats Numeric View} \\
\hline \multicolumn{4}{|c|}{或 0.461368 n: 50} \\
\hline \multicolumn{4}{|c|}{\multirow[t]{2}{*}{\(\begin{array}{cc}\mu_{0}: 0.5 & 0: 0.2887 \\ \alpha: 0.05\end{array}\)}} \\
\hline & & & \\
\hline \multicolumn{4}{|l|}{Sample mean} \\
\hline EDIT & & IMPRT & CALC \\
\hline
\end{tabular}

The table below lists the fields in this view for our current \(z\)-Test: \(1 \mu\) example.
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\overline{\mathrm{x}}\) & Sample mean \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition (Continued) \\
\hline n & Sample size \\
\(\mu_{0}\) & Assumed population mean \\
\(\sigma\) & Population standard deviation \\
\(\alpha\) & Alpha level for the test \\
\hline
\end{tabular}

\section*{Display test results}
6. Display the test results in numeric format.

\section*{CALC EIG}

The test distribution value and its associated probability are
 displayed, along with the critical value(s) of the test and the associated critical value(s) of the statistic.
7. Display a graphical view of the test results.


The graph of the distribution is displayed,
 with the test \(Z\)-value marked. The corresponding \(X\) value is also shown, as well as the critical \(Z\)-value. Press the \(\alpha\) menu key to see the critical Z-value as well. With the menu key active, you can use the left- and right-cursor keys to decrease and increase the \(\alpha\)-level.

\section*{Importing sample statistics}

The Inference app supports the calculation of confidence intervals and the testing of hypotheses based on data in the Statistics 1Var and Statistics 2Var apps. Computed statistics for a sample of data in a column in any Statisticsbased app can be imported for use in the Inference app. The following example illustrates the process.
A calculator produces the following 6 random numbers:
\(0.529,0.295,0.952,0.259,0.925\), and 0.592

\section*{Open the Statistics IVar app}
1. Open the Statistics IVar app and reset the current settings.


The Statistics app opens in the Numeric view.
2. In the D1 column, enter the random numbers produced by the calculator.


295


\begin{tabular}{|l|l|l|l|l|}
\hline EDIT & INS & SORT & BIG & MAKE \\
\hline
\end{tabular}

259

\section*{ENTER}



HIN T If the Decimal Mark setting in the Modes input form O modes) is set to Comma, use men o instead of

\section*{Calculate statistics}
3. Calculate statistics.

\section*{STATS}

The mean of 0.592 seems a little large compared to the
 expected value of 0.5 . To see if the difference is statistically significant, we will use the statistics computed here to construct a confidence interval for the true mean of the population of random numbers and see whether or not this interval contains 0.5 .
4. Press \(\triangle\) OK to close the computed statistics window.

Open the
Inference app

Select inference method and type
5. Open the Inference app and clear current settings.


Inference


START
6. Select an inference method.

CHOOS
Select CONF INTERVAL

\section*{OK}

7. Select a distribution statistic type.

\section*{CHOOS}

Select T-Int: \(1 \mu\)
OK

8. Set up the interval calculation. Note: The default values are derived from sample data from the on-line help example.
9. Import the data from the Statistics app. Note: The data from D1 is displayed by default.

\section*{IMFRT}

Use the App field to select the Statistics-based app from which you want to import data.


Use the Column field to choose the column in that app where the data is stored. You can view the data before you import it. Press ok to import the statistics into the inference app. confidence interval in the C field.
\(\odot \odot\) to move to the \(C\) field
0.9
ENTER
ENTER
Sample mean
11.Display the confidence interval in the Numeric view.
```

CALC EIG

```


\section*{Display results graphically}
12. Display the confidence interval in the Plot view.
```

OK

```

You can see that the
 mean is contained within the \(90 \%\) confidence interval (CI) of 0.3469814 to 0.8370186 .

\section*{Hypothesis tests}

You use hypothesis tests to test the validity of hypotheses that relate to the statistical parameters of one or two populations. The tests are based on statistics of samples of the populations.

The HP 39gll hypothesis tests use the Normal Z-distribution or Student's \(t\)-distribution to calculate probabilities.

\section*{One-Sample Z-Test}

Menu name
Z-Test: \(1 \mu\)
On the basis of statistics from a single sample, the One-Sample Z-Test measures the strength of the evidence for a selected hypothesis against the null hypothesis. The null hypothesis is that the population mean equals a specified value, \(\mathrm{H}_{0}: \mu=\mu_{0}\).
You select one of the following alternative hypotheses against which to test the null hypothesis:
\[
\begin{aligned}
& \mathrm{H}_{1}: \mu<\mu_{0} \\
& \mathrm{H}_{1}: \mu>\mu_{0} \\
& \mathrm{H}_{1}: \mu \neq \mu_{0}
\end{aligned}
\]

Inputs
The inputs are:
\begin{tabular}{|l|l|}
\hline Field name & Definition \\
\hline\(\overline{\mathrm{x}}\) & Sample mean. \\
n & Sample size. \\
\(\mu_{0}\) & Hypothetical population mean. \\
\(\sigma\) & Population standard deviation. \\
\(\alpha\) & Significance level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\(\left.\begin{array}{|l|l|}\hline \text { Result } & \text { Description } \\ \hline \text { Test Z } & \begin{array}{l}\text { Z-test statistic. } \\ \text { Value of } \overline{\mathrm{x}} \text { associated with the } \\ \text { test Z-value. } \\ \text { P }\end{array} \\ \text { Probability associated with the } \\ \text { Z-Test statistic. } \\ \text { Boundary 1 1 value(s) of Z } \\ \text { associated with the } \alpha \text { level that } \\ \text { you supplied. }\end{array}\right\}\)
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Critical \(\overline{\mathrm{x}}\) & \begin{tabular}{l} 
Boundary value(s) of \(\overline{\mathrm{x}}\) \\
required by the \(\alpha\) value that you \\
supplied.
\end{tabular} \\
\hline
\end{tabular}

\section*{Two-Sample Z-Test}

Menu name
Z-Test: \(\mu_{1}-\mu_{2}\)
On the basis of two samples, each from a separate population, this test measures the strength of the evidence for a selected hypothesis against the null hypothesis. The null hypothesis is that the mean of the two populations are equal, \(\mathrm{H}_{0}: \mu_{1}=\mu_{2}\).

You select one of the following alternative hypotheses to test against the null hypothesis:
\[
\begin{aligned}
& \mathrm{H}_{1}: \mu_{1}<\mu_{2} \\
& \mathrm{H}_{1}: \mu_{1}>\mu_{2} \\
& \mathrm{H}_{1}: \mu_{1} \neq \mu_{2}
\end{aligned}
\]

\section*{Inputs}

The inputs are:
\begin{tabular}{|l|l|}
\hline Field name & Definition \\
\hline\(\overline{\mathrm{x}}_{1}\) & Sample 1 mean. \\
\(\overline{\mathrm{x}}_{2}\) & Sample 2 mean. \\
\(\mathrm{n}_{1}\) & Sample 1 size. \\
\(\mathrm{n}_{2}\) & \begin{tabular}{l} 
Sample 2 size. \\
\(\sigma_{1}\)
\end{tabular} \\
\(\sigma_{2}\) & \begin{tabular}{l} 
Population 1 standard \\
deviation. \\
Population 2 standard \\
deviation. \\
Significance level.
\end{tabular} \\
\(\alpha\) & \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Test Z & Z-Test statistic. \\
\hline
\end{tabular}
\(\left.\begin{array}{|l|l|}\hline \text { Result } & \text { Description } \\
\hline \text { Test } \Delta \overline{\mathrm{x}} & \begin{array}{l}\text { Difference in the means associ- } \\
\text { ated with the test Z-value. }\end{array} \\
\text { Critical Z } & \begin{array}{l}\text { Probability associated with the } \\
\text { Z-Test statistic. }\end{array} \\
\text { Critical } \Delta \overline{\mathrm{x}} & \begin{array}{l}\text { Boundary value(s) of Z associ- } \\
\text { ated with the } \alpha \text { level that you } \\
\text { supplied. }\end{array} \\
\text { Difference in the means associ- } \\
\text { ated with the } \alpha \text { level you sup- } \\
\text { plied. }\end{array}\right]\)\begin{tabular}{l} 
\\
\hline
\end{tabular}

\section*{One-Proportion Z-Test}

Z-Test: \(1 \pi\)
On the basis of statistics from a single sample, this test measures the strength of the evidence for a selected hypothesis against the null hypothesis. The null hypothesis is that the proportion of successes is an assumed value, \(\mathrm{H}_{0}: \pi=\pi_{0}\).

You select one of the following alternative hypotheses against which to test the null hypothesis:
\[
\begin{aligned}
& \mathrm{H}_{1}: \pi<\pi_{0} \\
& \mathrm{H}_{1}: \pi>\pi_{0} \\
& \mathrm{H}_{1}: \pi \neq \pi_{0}
\end{aligned}
\]

\section*{Inputs}

The inputs are:
\begin{tabular}{|l|l|}
\hline Field name & Definition \\
\hline x & Number of successes in the sample. \\
n & Sample size. \\
\(\pi_{0}\) & Population proportion of successes. \\
\(\alpha\) & Significance level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Test Z & Z-Test statistic. \\
Test \(\hat{p}\) & Proportion of successes in the sample. \\
P & \begin{tabular}{l} 
Probability associated with the Z-Test \\
statistic.
\end{tabular} \\
Critical Z & \begin{tabular}{l} 
Boundary value(s) of Z associated \\
with the \(\alpha\) level that you supplied.
\end{tabular} \\
Critical \(\hat{p}\) & \begin{tabular}{l} 
Proportion of successes associated \\
with the level you supplied.
\end{tabular} \\
\hline
\end{tabular}

\section*{Two-Proportion Z-Test}

Menu name
Z-Test: \(\pi_{1}-\pi_{2}\)
On the basis of statistics from two samples, each from a different population, the Two-Proportion Z-Test measures the strength of the evidence for a selected hypothesis against the null hypothesis. The null hypothesis is that the proportions of successes in the two populations are equal, \(\mathrm{H}_{0}: \pi_{1}=\pi_{2}\).

You select one of the following alternative hypotheses against which to test the null hypothesis:
\[
\begin{aligned}
& \mathrm{H}_{1}: \pi_{1}<\pi_{2} \\
& \mathrm{H}_{1}: \pi_{1}>\pi_{2} \\
& \mathrm{H}_{1}: \pi_{1} \neq \pi_{2}
\end{aligned}
\]

The inputs are:
\begin{tabular}{|l|l|}
\hline Field name & Definition \\
\hline \(\mathrm{x}_{1}\) & Sample 1 success count. \\
\(\mathrm{x}_{2}\) & Sample 2 success count. \\
\(\mathrm{n}_{1}\) & Sample 1 size. \\
\(\mathrm{n}_{2}\) & Sample 2 size. \\
\(\alpha\) & Significance level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Test Z & \begin{tabular}{l} 
Z-Test statistic. \\
Difference between the \(\Delta \hat{p}\) \\
proportions of successes in the \\
two samples that is associated \\
with the test Z-value.
\end{tabular} \\
P Critical Z & \begin{tabular}{l} 
Probability associated with the \\
Z-Test statistic. \\
Boundary value(s) of Z \\
associated with the \(\alpha\) level that \\
you supplied.
\end{tabular} \\
Critical \(\Delta \hat{p}\) & \begin{tabular}{l} 
Difference in the proportion of \\
successes in the two samples \\
associated with the level you \\
supplied.
\end{tabular} \\
\hline
\end{tabular}

\section*{One-Sample T-Test}

\section*{Menu name}

T-Test: \(1 \mu\)
The One-Sample T-Test is used when the population standard deviation is not known. On the basis of statistics from a single sample, this test measures the strength of the evidence for a selected hypothesis against the null hypothesis. The null hypothesis is that the sample mean has some assumed value, \(\mathrm{H}_{0}: \mu=\mu_{0}\).

You select one of the following alternative hypotheses against which to test the null hypothesis:
\[
\begin{aligned}
& \mathrm{H}_{1}: \mu<\mu_{0} \\
& \mathrm{H}_{1}: \mu>\mu_{0} \\
& \mathrm{H}_{1}: \mu \neq \mu_{0}
\end{aligned}
\]

\section*{Inputs}

The inputs are:
\begin{tabular}{|l|l|}
\hline Field name & Definition \\
\hline\(\overline{\mathrm{x}}\) & Sample mean. \\
s & Sample standard deviation. \\
n & Sample size. \\
\(\mu_{0}\) & Hypothetical population mean. \\
\(\alpha\) & Significance level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Test T & \begin{tabular}{l} 
T-Test statistic. \\
Value of \(\bar{x}\) associated with the \(\overline{\mathrm{x}}\) \\
test t-value.
\end{tabular} \\
P & \begin{tabular}{l} 
Probability associated with the \\
T-Test statistic.
\end{tabular} \\
DF & Degrees of freedom. \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Critical T & \begin{tabular}{l} 
Boundary value(s) of T \\
associated with the \(\alpha\) level that \\
you supplied.
\end{tabular} \\
Critical \(\overline{\mathrm{x}}\) & \begin{tabular}{l} 
Boundary value(s) of \(\overline{\mathrm{x}}\) \\
required by the \(\alpha\) value that you \\
supplied.
\end{tabular} \\
\hline
\end{tabular}

\section*{Two-Sample T-Test}

Menu name
T-Test: \(\mu_{1}-\mu_{2}\)
The Two-sample T-Test is used when the population standard deviation is not known. On the basis of statistics from two samples, each sample from a different population, this test measures the strength of the evidence for a selected hypothesis against the null hypothesis. The null hypothesis is that the two populations means are equal, \(\mathrm{H}_{0}: \mu_{1}=\mu_{2}\).
You select one of the following alternative hypotheses against which to test the null hypothesis
\[
\begin{aligned}
& \mathrm{H}_{1}: \mu_{1}<\mu_{2} \\
& \mathrm{H}_{1}: \mu_{1}>\mu_{2} \\
& \mathrm{H}_{1}: \mu_{1} \neq \mu_{2}
\end{aligned}
\]

\section*{Inputs}

The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\overline{\mathrm{x}}_{1}\) & Sample 1 mean. \\
\(\overline{\mathrm{x}}_{2}\) & Sample 2 mean. \\
\(\mathrm{s}_{1}\) & Sample 1 standard deviation. \\
\(\mathrm{s}_{2}\) & Sample 2 standard deviation. \\
\(\mathrm{n}_{1}\) & Sample 1 size. \\
\(\mathrm{n}_{2}\) & Sample 2 size. \\
\(\alpha\) & Significance level. \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline Pooled & \begin{tabular}{l} 
Check this option to pool samples \\
based on their standard deviations.
\end{tabular} \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Test T & \begin{tabular}{l} 
T-Test statistic. \\
Test \(\Delta \overline{\mathrm{x}}\)
\end{tabular} \\
\begin{tabular}{l} 
Difference in the means associated \\
with the test t-value. \\
Probability associated with the T-Test \\
statistic.
\end{tabular} \\
Critical T & \begin{tabular}{l} 
Degrees of freedom. \\
Boundary values of T associated with \\
the \(\alpha\) level that you supplied.
\end{tabular} \\
Critical & \begin{tabular}{l} 
Difference in the means associated \\
with the \(\alpha\) level you supplied.
\end{tabular} \\
\(\Delta \overline{\mathrm{x}}\)
\end{tabular}

\section*{Confidence intervals}

The confidence interval calculations that the HP 39gll can perform are based on the Normal Z-distribution or Student's t-distribution.

\section*{One-Sample Z-Interval}

Menu name
Z-int: \(1 \mu\)
This option uses the Normal Z-distribution to calculate a confidence interval for \(\mu\), the true mean of a population, when the true population standard deviation, \(\sigma\), is known.

The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline \(\bar{x}\) & Sample mean. \\
n & Sample size. \\
\(\sigma\) & Population standard deviation. \\
C & Confidence level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline C & Confidence level. \\
Critical Z & Critical values for Z. \\
Lower & Lower bound for \(\mu\). \\
Upper & Upper bound for \(\mu\). \\
\hline
\end{tabular}

\section*{Two-Sample Z-Interval}

Menu name

Inputs

Z-int: \(\mu_{1}-\mu_{2}\)
This option uses the Normal Z-distribution to calculate a confidence interval for the difference between the means of two populations, \(\mu_{1}-\mu_{2}\), when the population standard deviations, \(\sigma_{1}\) and \(\sigma_{2}\), are known.

The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\overline{\mathrm{x}}_{1}\) & Sample 1 mean. \\
\(\overline{\mathrm{x}}_{2}\) & Sample 2 mean. \\
\(\mathrm{n}_{1}\) & Sample 1 size. \\
\(\mathrm{n}_{2}\) & Sample 2 size. \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\sigma_{1}\) & Population 1 standard deviation. \\
\(\sigma_{2}\) & Population 2 standard deviation. \\
C & Confidence level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline C & Confidence level. \\
Critical Z & Critical values for Z. \\
Lower & Lower bound for \(\Delta \mu\). \\
Upper & Upper bound for \(\Delta \mu\). \\
\hline
\end{tabular}

\section*{One-Proportion Z-Interval}

Menu name

Inputs
The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline x & Sample success count. \\
n & Sample size. \\
C & Confidence level. \\
\hline
\end{tabular}

\section*{Results}

Z-int: \(1 \pi\)
This option uses the Normal Z-distribution to calculate a confidence interval for the proportion of successes in a population for the case in which a sample of size, \(n\), has a number of successes, \(x\).

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline C & Confidence level. \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline Critical Z & Critical values for \(Z\). \\
Lower & Lower bound for \(\pi\). \\
Upper & Upper bound for \(\pi\). \\
\hline
\end{tabular}

\section*{Two-Proportion Z-Interval}

Menu name
Z-Int: \(\pi_{1}-\pi_{2}\)
This option uses the Normal Z-distribution to calculate a confidence interval for the difference between the proportions of successes in two populations.

Inputs
The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\overline{\mathrm{x}}_{1}\) & Sample 1 success count. \\
\(\overline{\mathrm{x}}_{2}\) & Sample 2 success count. \\
\(\mathrm{n}_{1}\) & Sample 1 size. \\
\(\mathrm{n}_{2}\) & Sample 2 size. \\
C & Confidence level. \\
\hline
\end{tabular}

Results
The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline C & Confidence level. \\
Critical Z & Critical values for \(Z\). \\
Lower & Lower bound for \(\Delta \pi\). \\
Upper & Upper bound for \(\Delta \pi\). \\
\hline
\end{tabular}

\section*{One-Sample T-Interval}
Menu \(n\)

Inputs

T-int: \(1 \mu\)
This option uses the Student's \(t\)-distribution to calculate a confidence interval for \(\mu\), the true mean of a population, for the case in which the true population standard deviation, \(\sigma\), is unknown.

The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\overline{\mathrm{x}}\) & Sample mean. \\
s & Sample standard deviation. \\
n & Sample size. \\
C & Confidence level. \\
\hline
\end{tabular}

\section*{Results}

The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline C & Confidence level. \\
DF & Degrees of freedom. \\
Critical T & Critical values for T. \\
Lower & Lower bound for \(\mu\). \\
Upper & Upper bound for \(\mu\). \\
\hline
\end{tabular}

\section*{Two-Sample T-Interval}

\section*{Menu name}

T-int: \(\mu_{1}-\mu_{2}\)
This option uses the Student's \(t\)-distribution to calculate a confidence interval for the difference between the means of two populations, \(\mu_{1}-\mu_{2}\), when the population standard deviations, \(\sigma_{1}\) and \(\sigma_{2}\), are unknown.

The inputs are:
\begin{tabular}{|l|l|}
\hline \begin{tabular}{l} 
Field \\
name
\end{tabular} & Definition \\
\hline\(\overline{\mathrm{x}}_{1}\) & Sample 1 mean. \\
\(\overline{\mathrm{x}}_{2}\) & Sample 2 mean. \\
\(\mathrm{s}_{1}\) & \begin{tabular}{l} 
Sample 1 standard deviation. \\
\(\mathrm{s}_{2}\) \\
\(\mathrm{n}_{1}\)
\end{tabular} \\
\(\mathrm{n}_{2}\) & \begin{tabular}{l} 
Sample 2 standard deviation. \\
C
\end{tabular} \\
Sample 1 size.
\end{tabular}

Results
The results are:
\begin{tabular}{|l|l|}
\hline Result & Description \\
\hline C & Confidence level. \\
DF & Degrees of freedom. \\
Critical T & Critical values for T. \\
Lower & Lower bound for \(\Delta \mu\). \\
Upper & Upper bound for \(\Delta \mu\). \\
\hline
\end{tabular}

\section*{Parametric app}

\section*{About the Parametric app}

The Parametric app allows you to explore parametric equations. These are equations in which both \(x\) and \(y\) are defined as functions of \(t\). They take the forms \(x=f(t)\) and \(y=g(t)\).

\section*{Getting started with the Parametric app}

The following example uses the parametric equations
\[
\begin{aligned}
& x(t)=5 \sin t \\
& y(t)=5 \cos t
\end{aligned}
\]

Note: this example will produce a circle. For this example to work, the angle measure must be set to degrees.

\author{
Open the Parametric app
}
1. Open the Parametric app.


Like the function app, the Parametric app opens in the Symbolic view.

Define the expressions

Set angle measure
2. Define the expressions.


3. Set the angle measure to degrees.


CHOOS
Select Degrees


OK
4. Set up the plot by displaying the graphing options.


The Plot Setup input form has two fields not included in the Function app, TRNG and TSTEP. TRNG specifies the range of \(t\) values. TSTEP specifies the step value between \(t\) values.
5. Set the TRNG and TSTEP so that \(t\) steps from \(0^{\circ}\) to \(360^{\circ}\) in \(5^{\circ}\) steps.


5 OK

6. Plot the expression.


\section*{Explore the graph}
your own table, and the split screen functionality available in the Function app.

\section*{Polar app}

\section*{About the Polar app}

The Polar app allows you to explore polar equations. Polar equations are equations in which \(r\) is defined in terms of \(\theta\). They take the form \(r=f(\theta)\).

\section*{Getting started with the Polar app}

\author{
Open the Polar app
}

\author{
Define the expression
}
1. Open the Polar app.


\section*{RESET OK START}

Like the Function app, the Polar app opens in
 the Symbolic view.
2. Define the polar equation \(r=4 \pi \cos (\theta / 2) \cos (\theta)^{2}\).


Set angle measure
3. Set the angle measure to radians.

\section*{SHIIT} MODES

CHOOS
Select Radians


\section*{OK}

Set up the plot

\section*{Plot the} expression

\author{
Explore the graph
}
4. Set up the plot. In this example, we will use the default settings, except for the \(\theta\) Rng fields.
5. Plot the expression.

6. Display the Plot view menu key labels.

\section*{MENU}

The Plot view options available are the same as those found in the Function app, except
 there is no FCN menu.
7. Display the table of values for \(\theta\) and \(\mathrm{R1}\) in the Numeric view.
\begin{tabular}{|l|c|l|l|}
\hline \multicolumn{1}{|c|}{\(\theta\)} & R1 & & \\
\hline 0 & 6.283185307 & & \\
\hline 0.1 & 6.212788531 & & \\
0.2 & 6.005040289 & & \\
0.3 & 5.670069143 & & \\
0.4 & 5.224108991 & & \\
0.5 & 4.688569542 & & \\
\hline 0 & \multicolumn{5}{|c|}{} \\
\hline ZOOM & & & BIG \\
\hline
\end{tabular}
8. With a \(\theta\)-value selected, type in a replacement value and press OK and see the table jump to that value. You can also zoom in or zoom out on any \(\theta\) value in the table.

\section*{Sequence app}

\section*{About the Sequence app}

The Sequence app allows you to explore sequences.
You can define a sequence named, for example, U1:
- in terms of \(n\)
- in terms of \(\mathrm{Ul}(n-1)\)
- in terms of \(\mathrm{Ul}(n-2)\)
- in terms of another sequence, for example, U2(n)
- in any combination of the above.

The Sequence app allows you to create two types of graphs:
- A Stairsteps graph plots \(n\) on the horizontal axis and \(U_{n}\) on the vertical axis.
- A Cobweb graph plots \(U_{n-1}\) on the horizontal axis and \(U_{n}\) on the vertical axis.

\section*{Getting started with the Sequence app}

The following example defines and then plots an expression in the Sequence app. The sequence illustrated is the well-known Fibonacci sequence where each term, from the third term on, is the sum of the preceding two terms. In this example, we specify three sequence fields: the first term, the second term and a rule for generating all subsequent terms.

However, you can also define a sequence by specifying just the first term and the rule for generating all subsequent terms. You will, though, have to enter the second term if the HP 39 gll is unable to calculate it automatically. Typically if the \(n\)th term in the sequence depends on \(n-2\), then you must enter the second term.

\section*{Open the Sequence app}

Define the expression
2. Define the Fibonacci sequence, in which each term (after the first two) is the sum of the preceding two terms:
\(U_{1}=1, U_{2}=1, U_{n}=U_{n-1}+U_{n-2}\) for \(n>2\).
In the Symbolic view of the Sequence app, highlight the Ul (1) field and begin defining your sequence.
```

1 ENNTER 1 ENTER
U1
(N-1) \Sigma+

| EFID SEQUENCE SYMBOLIC VIEW |  |  |  |
| :---: | :---: | :---: | :---: |
| U1(1)=1 |  |  |  |
| $\checkmark$ U1(2)=1 |  |  |  |
| $\sim \cup 1(\mathrm{~N})=\mathrm{U} 1(\mathrm{~N}-1)+\mathrm{U} 1(\mathrm{~N}-2)$ |  |  |  |
| U2(1) $=$ |  |  |  |
|  |  |  |  |
| EDIT | CHK | SHOW | EVAL |

```

\section*{( \(\mathrm{N}-2\) ) \({ }_{\text {ENS }}^{\text {ENS }}\)}
```

Note: You can use the
U1, $N,(\mathbb{N}-1)$, and $(\mathbb{N}-2)$ menu keys to assist in the entry of expressions.

```

Set up the plot
3. In Plot Setup, set the SEQPLOT option to Stairstep and reset the default plot settings by clearing the Plot Setup view.
\begin{tabular}{|l|l|l|l|}
\hline RRD & Sequence Plot Setup & & \\
\hline SEQPLOT: Stairstep & & & \\
NRNG: 1 & 8 & & \\
XRNG: & -2 & 8 & \\
YRNG: & -2 & 10.6 & \\
XTICK: & I & YTICK: 1 & \\
\hline Enter horizontal tick spacing & & \\
\hline EDIT & & PAGE & \\
\hline
\end{tabular}ENTER
- 8
ENTER

\section*{Plot the expression}
4. Plot the Fibonacci sequence.

Plot Setup

5. In Plot Setup, set the SEQPLOT option to Cobweb.


Display the numeric view
6. Display the Numeric view for this example.

7. With any n-value selected, type in a replacement value, and see the table jump to that value.


\section*{Finance app}

\section*{About the Finance app}

The Finance app, or Finance Solver, provides you with the ability to solve time-value-of-money (TVM) and amortization problems. These problems can be used for calculations involving compound interest applications as well as amortization tables.

Compound interest is the process by which earned interest on a given principal amount is added to the principal at specified compounding periods, and then the combined amount earns interest at a certain rate. Financial calculations involving compound interest include savings accounts, mortgages, pension funds, leases, and annuities.

\section*{Getting Started with the Finance app}

Suppose you finance the purchase of a car with a 5 -year loan at \(5.5 \%\) annual interest, compounded monthly. The purchase price of the car is \(\$ 19,500\), and the down payment is \(\$ 3,000\). What are the required monthly payments? What is the largest loan you can afford if your maximum monthly payment is \(\$ 300\) ? Assume that the payments start at the end of the first period.
1. Start the Finance app.

select Finance

\section*{RESET OK START.}
\begin{tabular}{|l|r|r|}
\hline \multicolumn{3}{|c|}{ Application Library } \\
\hline Finance & [250KB \\
\hline Function & .24 KB & \\
Inference & .28 KB \\
Linear Explorer & .26 KB \\
Linear Solver & .082 KB \\
\hline SAVE & RESET & SORT \\
\hline
\end{tabular}

The Finance app opens in the Numeric view.
2. Select N , type \(5 \times 12\) and
\begin{tabular}{|c|c|c|c|c|}
\hline \multicolumn{5}{|c|}{Time Value of Money} \\
\hline \multicolumn{2}{|r|}{\multirow[t]{2}{*}{}} & \multicolumn{3}{|c|}{1\%YR: 0} \\
\hline & & & P/VR & \\
\hline \multicolumn{2}{|r|}{PMT: 0.00} & \multicolumn{3}{|c|}{C/YR: 12} \\
\hline \multicolumn{2}{|r|}{\multirow[t]{2}{*}{FV: 0.00}} & & & \\
\hline & & \multicolumn{3}{|l|}{Group Size: 12} \\
\hline \multicolumn{5}{|l|}{Enter Number Of Payments Or Solve} \\
\hline EDIT & & AMORT & & SOLVE \\
\hline
\end{tabular}

N O TE After you type in a value and press \(\left[\begin{array}{c}\text { ENSTER } \\ \text { NS } \\ \text { OK }\end{array}\right.\) another variable is automatically highlighted. To manually navigate to a desired field, press the arrow keys. Be sure that values are entered for six of the seven TVM variables: \(\mathrm{N}, \mathrm{I} \% \mathrm{YR}, \mathrm{PV}, \mathrm{P} / \mathrm{YR}, \mathrm{PMT}, \mathrm{C} / \mathrm{YR}\), and FV .
3. With \(I \% /\) YR highlighted, type 5.5 and press \(\begin{gathered}\text { ©NTER } \\ \text { ©N }\end{gathered}\)
4. With pv highlighted, type \(19,500-3,000\) and press
\(\qquad\)
5. Leave \(P / Y R\) and \(C / Y R\) both at 12 (their default values). Leave End as the payment option. Also, leave Future Value,
 \(\mathrm{FV}=0.00\).
6. With PMT highlighted, press SOLVE to obtain a payment of -315.17 (i.e., PMT \(=-\$ 315.17\) ) as


NOTE The payment is negative to indicate it is money owed.
7. To determine the maximum loan possible if the monthly payments are only \(\$ 300\), type the value -300 in the PMT
\begin{tabular}{|c|c|c|c|c|}
\hline \multicolumn{5}{|c|}{Time Value of Money} \\
\hline \multicolumn{2}{|r|}{N: 60} & \multicolumn{3}{|c|}{1\%YR: 5.5} \\
\hline \multicolumn{2}{|r|}{PV: 15,705.85} & & P/YR: 12 & \\
\hline \multicolumn{2}{|r|}{PMT: \(\mathbf{- 3 0 0 . 0 0}\)} & & C/VR: 12 & \\
\hline \multicolumn{2}{|r|}{FV: 0.00} & & End: \(\downarrow\) & \\
\hline \multicolumn{5}{|c|}{Group Size: 12} \\
\hline \multicolumn{5}{|l|}{Enter Present Value Or Solve} \\
\hline EDIT & & AMORT & & SOLVE \\
\hline
\end{tabular}
field, highlight the PV field using © , and press
Solve. The resulting value is \(\mathrm{PV}=\$ 15,705.85\).

\section*{Cash flow diagrams}

TVM transactions can be represented by using cash flow diagrams. A cash flow diagram is a time line divided into equal segments representing the compounding periods. Arrows represent the cash flows, which could be positive (upward arrows) or negative (downward arrows), depending on the point of view of the lender or borrower. The following cash flow diagram shows a loan from a borrower's point of view:


The following cash flow diagram shows a loan from the lender's point of view:


Cash flow diagrams also specify when payments occur relative to the compounding periods. The diagram to the right shows lease payments at the begin-
 ning of the period.

This diagram shows deposits (PMT) into an account at the end of each period.


\section*{Time value of money (TVM)}

Time Value of Money (TVM) calculations, as the name implies, make use of the notion that a dollar today will be worth more than a dollar sometime in the future. A dollar today can be invested at a certain interest rate and generate a return that the same dollar in the future cannot. This TVM principal underlies the notion of interest rates, compound interest and rates of return. There are seven TVM variables:
\(\left.\left.\left.\begin{array}{|l|l|}\hline \text { Variable } & \begin{array}{l}\text { Description } \\ \text { N } \\ \text { The total number of compounding periods } \\ \text { or payments. }\end{array} \\ \text { PV } & \begin{array}{l}\text { The nominal annual interest rate (or } \\ \text { investment rate). This rate is divided by } \\ \text { the number of payments per year (P/YR) } \\ \text { to compute the nominal interest rate per } \\ \text { compounding period - which is the } \\ \text { interest rate actually used in TVM } \\ \text { calculations. }\end{array} \\ \text { The present value of the initial cash flow. }\end{array}\right\} \begin{array}{l}\text { To a lender or borrower, PV is the amount } \\ \text { of the loan; to an investor, PV is the initial } \\ \text { investment. PV always occurs at the } \\ \text { beginning of the first period. }\end{array}\right\} \begin{array}{l}\text { The number of payments made in a year. } \\ \text { The periodic payment amount. The } \\ \text { payments are the same amount each } \\ \text { period and the TVM calculation assumes } \\ \text { that no payments are skipped. Payments } \\ \text { can occur at the beginning or the end of } \\ \text { each compounding period - an option } \\ \text { you control by un-checking or checking } \\ \text { the End option. }\end{array}\right\}\)
\begin{tabular}{|l|l|}
\hline FV & \begin{tabular}{l} 
The future value of the transaction: the \\
amount of the final cash flow or the \\
compounded value of the series of \\
previous cash flows. For a loan, this is the \\
size of the final balloon payment (beyond \\
any regular payment due). For an \\
investment this is the cash value of an \\
investment at the end of the investment \\
period.
\end{tabular} \\
\hline
\end{tabular}

\section*{Performing TVM calculations}
1. Launch the Finance App as indicated at the beginning of this section. It is recommended you reset the Finance app as shown before beginning a TVM problem.
2. With a variable highlighted, type in the known values starting with \(N\), and press \(\underset{\substack{\text { ENTER }}}{\operatorname{ANS}}\) or or to store the desired value. To manually navigate to a desired field, press the arrow keys.
3. Type in a different value for \(P / Y R\) as required. The default value is 12, i.e., monthly payments.
4. With the End field highlighted, press the Check menu key CHK to uncheck this option for payments made at the beginning of each period or leave it checked for payments made at the end of each period.
5. Use the arrow keys to highlight the unknown variable and press SOLVE .

\section*{Example-mortgage with balloon payment}

Suppose you have taken out a 30-year, \$150,000 house mortgage at \(6.5 \%\) annual interest. You expect to sell the house in 10 years, repaying the loan in a balloon payment. Find the size of the balloon payment, the value of the mortgage after 10 years of payment.

\section*{Solution}

The following cash flow diagram illustrates the case of the mortgage with balloon payment:

1. Start the Finance App. Use the arrow keys to highlight \(\mathrm{P} / \mathrm{YR}\). Verify that \(\mathrm{P} / \mathrm{YR}=12\) and End is set for payments occurring at the end of the compounding period.
2. Enter the known TVM variables from the example as shown in the figure.

3. Highlight PMT and press SOLVE to obtain a payment of -\$948.10.
4. To determine the balloon payment or future value (FV) for the mortgage after 10 years, enter 120 for N , highlight FV, and press SOLVE . This calculates the future value of the loan as \(-\$ 127,164.19\).
NOTE The negative values indicate payments from the homeowner.

\section*{Calculating Amortizations}

Amortization calculations, which also use the TVM variables, determine the amounts applied towards principal and interest in a payment, or a series of payments.

To calculate amortizations:
1. Start the Finance Solver as indicated at the beginning of this section.
2. Set the following TVM variables:
- Number of payments per year (P/YR)
- Payment at beginning or end of periods

\section*{Example- \\ Amortization for home mortgage}
3. Type and store values for the TVM variables, \(I \% Y R\), \(\mathrm{PV}, \mathrm{PMT}\), and FV , which define the payment schedule.
4. Enter the number of payments per amortization period in the GSize field. By default, the group size is 12 to reflect annual amortization.
5. Press AMORT. The calculator displays an amortization table. The table contains amounts applied to interest and principal, as well as the remaining balance of the loan, for each amortization period.

Using the data from the previous example of a home mortgage with balloon payment, calculate how much has been applied to the principal, how much has been applied to the interest, and the remaining balance of the loan after the first 10 years ( \(12 \times 10=120\) payments).
1. Verify and compare your data from the previous example with the figure to the right.

2. Press AMORT

3. Scroll down the table to Group 10 to see the same results as shown previously. After 10 years, \(\$ 22,835.81\) has
 been paid on the principal, with an additional \(\$ 90,936.43\) paid in interest, leaving a balloon payment due of \(\$ 127,164\).19.

Press the Plot key to see the amortization schedule presented graphically. The tracer shows the principal and interest paid in each payment group. Use the right- and left-cursor keys to trace among the payment groups.

\section*{Linear Solver app}

\section*{About the Linear Solver app}

The Linear Solver app allows you to solve a set of linear equations. The set can contain two or three linear equations.
In a two-equation set, each equation must be in the form \(a x+b y=k\). In a three-equation set, each equation must be in the form \(a x+b y+c z=k\).

You provide values for \(a, b\), and \(k\) (and \(c\) in threeequation sets) for each equation, and the Linear Solver app will attempt to solve for \(x\) and \(y\) (and \(z\) in threeequation sets).
The HP 39gll will alert you if no solution can be found, or if there is an infinite number of solutions.

\section*{Getting started with the Linear Solver app}

The following example defines a set of three equations and then solves for the unknown variables. In this example, we are going to solve the following equation set:
\[
\begin{aligned}
& 6 x+9 y+6 z=5 \\
& 7 x+10 y+8 z=10 \\
& 6 x+4 y=6
\end{aligned}
\]

Hence we need the three-equation input form.

\section*{Open the Linear Solver app}
1. Open the Linear Solver app.


The Linear Equation Solver opens in the Numeric view.

NOTE If the last time you used the Linear Solver app you solved for two equations, the two-equation input form is displayed. To solve a three-equation set, press \(3 \times 3\); now the input form displays three equations.

\section*{Define and solve the equations}
2. You define the equations you want to solve by entering the coefficients of each variable in each equation and the constant term. Notice that the cursor is immediately positioned at the coefficient of \(x\) in the first equation. Enter that coefficient and press \(O K\) or \(\underset{\text { ENTER }}{\text { ENT }}\).
3. The cursor moves to the next co-efficient. Enter that coefficient, press OK or ancer , and continue doing likewise until you have defined all the equations.
Once you have entered enough values for the solver to be able to generate solutions, those solutions appear on
 the display. In the example at the right, the solver was able to find solutions for \(x, y\), and \(z\) as soon as the first co-efficient of the last equation was entered.
As you enter each of the remaining known values, the solution changes. The example at the right shows the final solution once all
 the coefficients and constants are entered for the set of equations we set out to solve.

\title{
Solve a two-bytwo system
}

If the three-equation input form is displayed and you want to solve a twoequation set, press
\begin{tabular}{|c|c|c|c|c|}
\hline \multicolumn{5}{|l|}{} \\
\hline \multicolumn{5}{|l|}{Linear Equation Solver} \\
\hline & \(0 \times+\) & & \(\mathrm{Y}=\) & 0 \\
\hline \multicolumn{5}{|l|}{Infinite number of solutions 0} \\
\hline EDIT & 2X2* & \(3 \times 3\) & & \\
\hline
\end{tabular}

NOTE You can enter any expression that resolves to a numerical result, including variables; you can enter the name of a stored variable. For more information on storing variables, see the chapter titled Using mathematical functions.

\section*{Triangle Solver app}

\section*{About the Triangle Solver app}

The Triangle Solver app allows you to determine the length of a side of a triangle, or the measure of an angle of a triangle, from information you supply about the other lengths and/or angles.
You need to specify at least three of the six possible values - the lengths of the three sides and the measures of the three angles-before the solver can calculate the other values. Moreover, at least one value you specify must be a length. For example, you could specify the lengths of two sides and one of the angles; or you could specify two angles and one length; or all three lengths. In each case, the solver will calculate the remaining lengths or angle measures.
The HP 39gll will alert you if no solution can be found, or if you have provided insufficient data.
If you are determining the properties of a right-angled triangle, a simpler input form is available by pressing the RECT menu key.

\section*{Getting started with the Triangle Solver app}

The following example solves for the unknown length of the side of a triangle whose two known sides-of lengths 4 and 6 -meet at an angle of 30 degrees.

\author{
Open the Triangle Solver app
}
1. Open the Triangle Solver app.


RESET OK START
The Triangle Solver app opens in the Numeric view. This is the only view for this app.

Set angle measure

Make sure that your angle measure mode is appropriate. By default, the app starts in degree mode. If the angle information you have is in radians and your current angle measure mode is degrees, change the mode to degrees before running the solver. The Degree menu key is a toggle. Press it once to see it change to Radians for angles expressed in radians; press it again to return to degrees.

The lengths of the sides are labeled \(A, B\), and \(C\), and the angles are labeled \(\alpha, \beta\), and \(\delta\). It is important that you enter the known values in the appropriate fields. In our example, we know the length of two sides and the angle at which those sides meet. Hence if we specify the lengths of sides \(A\) and \(B\), we must enter the angle as \(\delta\) (since \(\delta\) is the angle where \(A\) and \(B\) meet). If instead we entered the lengths as B and C, we would need to specify the angle as \(\alpha\). The illustration on the display will help you determine where to enter the known values.

\section*{Specify the known values}
2. Using the arrow keys, move to a field whose value you know, enter the value and press OK or \(\begin{aligned} & \text { ENSTRR } \\ & \text { ENS }\end{aligned}\) Repeat for each known value.


30 NANTER
3. Press Solve . The
solver calculates and displays the values of the unknown variables. As the illustration at the right


Solve shows, the length of the unknown side in our example is 3.22967 . The other two angles have also been calculated.
Note: to clear all values and solve another problem, CLEAR.

\section*{Choose the triangle type}
4. The Triangle Solver app offers you two input forms: a general input form and a more specialized form for right triangles. If the
 general input form is displayed, and you are investigating a right-angled triangle, press RECT to display the simpler input form. To return to the general input form, press
RECT* . If the triangle you are investigating is not a right-angled triangle, or you are not sure what type it is, you should use the general input form.

\section*{Special cases}

The indeterminate case

If two sides and an adjacent acute angle are entered and there are two solutions, only one will be displayed initially.


In this case, an ALT menu key is displayed (as in this example). You press
ALT to display the second solution and
ALT again to return to the first solution.

\author{
No solution with given data
}

If you are using the general input form and you enter more than 3 values, the values might not be consistent, that is, no triangle could possibly
 have all the values you specified. In these cases, No sol with given data appears on the screen.

The situation is similar if you are using the simpler input form (for a right-angled triangle) and you enter more than two values.

Not enough data
If you are using the general input form, you need to specify at least three values for the Triangle Solver to be able
 to calculate the remaining EDIT \(\quad\) Degrees RECT attributes of the triangle. If you specify less than three, Not enough data appears on the screen.

If you are using the simplified input form (for a rightangled triangle), you must specify at least two values.

In addition, you cannot specify only angles and no lengths.

\section*{The Explorer Apps}

\section*{Linear Explorer App}

The Linear Explorer app is used to investigate the behavior of the graphs of \(y=a x\) and \(y=a x+b\) as the values of \(a\) and \(b\) change, both by manipulating the graph and seeing the change in the equation, and by manipulating the equation and seeing the change in the graph.

\section*{Open the app}

\section*{Graph mode}

Equation mode

Press Explorer, and press START. The app opens in Graph mode (note the dot in the GRAPH menu label).


In Graph mode, \(\odot\) and \(\odot\) translate the graph vertically, effectively changing the \(y\) intercept of the line. For
 vertical translations, press
INC 1 (F3) to change the magnitude of the increment for the translation. The (4) and (©) keys (as well as \(\varepsilon^{-} w\) and \(\Sigma^{+} \sqsupset\) ) increase and decrease the slope. Press \(\operatorname{Aass}^{(-)}\); to change the sign of the slope.

The form of the linear function is shown at the top right of the display, with the current equation that matches the graph just below it. As you manipulate the graph of the line, the equation updates in real time to reflect the changes. Press LEV2 (F4) to switch between direct variation and slope-intercept forms of linear functions.

Press EQ (F1) to toggle to Equation mode. You will see the dot in the EQ menu key indicating the switch from Graph mode. You will also
see one of the parameters in the equation highlighted. In Equation mode, you change the values of one or more of the parameters in the equation and those changes are reflected in the graph. Press \(\odot\) and to increase or decrease the value of the selected parameter, respectively. Press ( ) and (4) to select another parameter. Press \(\frac{\left.\operatorname{Lass}^{(-)}\right)}{}\)) to change the sign of \(a\).

\section*{Test mode}

Press TEST (F5) to enter Test mode. In Test mode, the app displays the graph of a randomly chosen linear function of the form dictated
 by your choice of level.
Press LEV 2 (F3) to choose between direct variation (LEV 1) and slope-intercept (LEV 2) forms of linear functions. Test mode then works like Equation mode. Use the arrow keys to select each parameter and set its value. When you are ready, press CHECK (F4) to see whether or not you have correctly matched your equation to the given graph. Press ANSW (F5) to see the correct answer. Press
END (F6) to exit Test mode and return to Graph mode.

\section*{Quadratic Explorer app}

The Quadratic Explorer app is used to investigate the behaviour of \(y=a(x+h)^{2}+v\) as the values of \(a\), \(h\) and \(v\) change, both by manipulating the equation and seeing the change in the graph, and by manipulating the graph and seeing the change in the equation.

Quadratic Explorer, and then press START. The Quadratic Explorer app opens in GRAFH* mode, in
 which the arrow keys, the \(\Sigma^{+} \square\) and \(\Sigma^{-}\)weys, and the aes \(_{(-)}^{(-)}\); key are used to change the shape of the graph. This changing shape is reflected in the equation displayed at the top right corner of the screen, while the original graph is retained for comparison. In this mode the graph controls the equation.

It is also possible to have the equation control the graph. Press EQ to enter Equation mode. Press \({ }^{(1)}\) and \((1)\) to move
 between parameters and press \(\Theta\) and \(\Theta\) to change the value of a parameter. The graph of the equation will update in real time as you change the values of the parameters. Press LEv 2 to cycle through the various forms of quadratic functions available.

A TEST menu key is provided to evaluate the student's knowledge. Press
TEST to display a target quadratic graph. The student
 must manipulate the equation's parameters to make the equation match the target graph. When a student feels that they have correctly chosen the parameters a CHECK menu key evaluates the answer and provide feedback. An ANSW menu key is provided for those who give up!

\section*{Trig Explorer app}

The Trig Explorer app is used to investigate the behaviour of the graph of \(y=a \sin (b x+c)+d\) as the values of \(a\), \(b, c\) and \(d\) change, both by manipulating the equation and seeing the change in the graph, or by manipulating the graph and seeing the change in the equation.

Press, select Trig Explorer, and then press START to display the screen shown right.

The app opens in Graph mode. Note that the first menu key (F1) is labeled GRAPH. In this mode, you can manipulate the graph
 and the changes are reflected in the equation. Press \(\odot, \odot,(\uparrow\) and \((\square)\) to transform the graph, with the transformations reflected in the equation.
\begin{tabular}{|c|c|}
\hline The button labelled ORIG is toggle between ORIG and &  \\
\hline ExTR. When ORIG is & -1 \({ }_{-2}{ }^{-1}\) \\
\hline arol vertical and &  \\
\hline
\end{tabular}
horizontal translations. For horizontal translations, the F6 menu key controls the magnitude of the increment. By default, the increment is set at \(\pi / 9\). When EXTR is chosen \(\ominus, \odot,(1\) and \(\oplus\) control vertical and horizontal dilations with respect to their respective axes. Thus, the arrow keys effectively change the amplitude and frequency of the graph. This is most easily seen by experimenting.

Press the F1 menu key to toggle from GRAPH to EQ. In this mode, the graph is controlled by the equation. In the equation displayed at the
 top of the screen, one of the parameters is highlighted. Press \(\odot\) or \(\odot\) to increase or decrease the value of the highlighted parameter. Press (1) and to move from parameter to parameter.

The default angle setting for this app is radians. The angle setting can be changed to degrees by pressing RAD

Like the Quadratic Explorer app, the Trig Explorer app also has a TEST view.

\section*{Extending your App Library}

Apps are the application environments where you explore different classes of mathematical operations.

You can extend the capability of the HP 39gll by adding additional apps to the Apps Library. Adding new apps to the library can be done in a number of ways:
- Create new apps, based on existing apps, with specific configurations such as angle measure, graphical or tabular settings, and annotations.
- Transmit apps between HP 39gll calculators via micro-USB cable.
- Program new apps. See the chapter titled Programming for more details.

\section*{Creating new apps based on existing apps}

You can create a new app based on an existing app. To create a new app, save an existing app under a new name, then modify the app to add the configurations and the functionality that you want.

Information that defines an app is saved automatically as it is entered into the calculator.

To keep as much memory available for storage as possible, delete any apps you no longer need.

\section*{Example}

This example demonstrates how to create a new app by saving a copy of the built-in Solve app. The new app is saved under the name TRIANGLES and contains familiar formulas for solving problems involving triangles.
1. Open the Solve app and save it under the new name.

\begin{tabular}{|c|c|c|}
\hline \multicolumn{3}{|c|}{Select New App Name} \\
\hline \multicolumn{3}{|l|}{Name: Solve} \\
\hline \multicolumn{3}{|l|}{TRIANGLES} \\
\hline & CANCL & OK \\
\hline
\end{tabular}

TRIANGLES

\section*{ENTER \\ ANS \\ START}
2. Enter the formulas:

3. Decide whether you want the app to operate in Degrees or Radians.

4. View the App Library. The triangles app is listed in the App Library.

The Solve app can now be reset and used for other
\begin{tabular}{|l|r|r||}
\hline \multicolumn{2}{|c|}{ Application Library } & 251KB \\
\hline TRIANGLES & .39 KB \\
\hline Solve & .27 KB \\
Polar & .29 KB \\
Function & .30 KB \\
Statistics 1-Var & .71 KB \\
\hline SAVE & DELETE & SORT \\
\hline
\end{tabular} problems. The advantage of storing an app is to allow you to keep a copy of a working environment for later use.

\section*{Resetting an app}

Resetting an app clears all data and resets all default settings.

To reset an app, open the Library, select the app and press RESEI.
You can only reset an app that is based on a built-in app if the programmer who created it has provided a Reset option.

\section*{Annotating an app with notes}
 app. See the chapter Notes and Info for more details.

\section*{Sending and receiving apps}

A convenient way to distribute or share problems in class and to turn in homework is to transmit (copy) apps directly from one HP 39gll to another. Transfer of apps between calculators is done with the micro-USB cable that comes with each HP 39gll.

You can also send apps to, and receive apps from, a PC via the PC Connectivity Kit. A USB cable with a microUSB connector is provided with the HP 39gll for connecting with a PC. It plugs into the micro-USB port on the calculator. The PC Connectivity Kit can be installed from the product CD included with the HP 39gll.

To transmit an 1. Connect the two HP 39gll calculators with the microapp USB cable that came with each calculator.
2. On the sending calculator, open the Apps Library and select the app you wish to send.
3. Press the SEND menu key.
4. You may see the data transfer annunciator briefly.
5. On the receiving unit, open the Apps Library to see the new app.
To transmit an app from your PC to an HP 39gll, use the HP 39gll Connectivity Kit. This soffware application controls the transfer of all data from your PC to your HP 39gll.

\section*{Managing apps}

The app library is where you go to manage your apps.
 the app you want to act on.

To sort the app list

In the app library, press SORTI. Select the sorting scheme and press \({ }_{\text {ENSTRR }}^{\text {Niter }}\).
- Chronologically produces a chronological order based on the date an app was last used. (The lastused app appears first, and so on.)
- Alphabetically produces an alphabetical order by app name.

To delete a customized app, open the app library, highlight the app to be deleted, and press scor . To delete all custom apps, press CLEARIT
You cannot delete a built-in app. You can only clear its data and reset its default settings.

\section*{Using mathematical functions}

\section*{Math functions}

The HP 39gll contains many mathematical functions. To use a math function, you enter the function onto the command line, and include the function's argument(s) in parentheses after the function name. The most common math functions have their own key (or Shift of a key) on the keyboard. All the rest of the mathematical functions are found in the Math menu.

\section*{Keyboard functions}

The most frequently used functions are available directly from the keyboard. Many of the keyboard functions also accept complex numbers as arguments.


Natural logarithm. Also accepts complex numbers.
LN(value)
Example:
LN (1) returns 0
\(e^{X}\)
Natural exponential. Also accepts complex numbers.
\[
e^{\wedge} \text { value }
\]

Example:

Common logarithm. Also accepts complex numbers.
LOG(value)
Example:

LOG (100) returns 2


Common exponential (antilogarithm). Also accepts complex numbers.
\(10^{\wedge}\) value

\section*{Example:}
\(10^{\wedge} 3\) returns 1000

Sine, cosine, tangent. Inputs and outputs depend on the current angle format (Degrees, Radians, or Grads).

SIN(value) cos(value) TAN(value)

\section*{Example:}

TAN (45) returns 1 (Degrees mode).
Arc sine: \(\sin ^{-1} x\). Output range is from \(-90^{\circ}\) to \(90^{\circ}\) or \(-\pi /\) 2 to \(\pi / 2\). Inputs and outputs depend on the current angle format. Also accepts complex numbers.
ASIN(value)

\section*{Example:}

ASIN (1) returns 90 (Degrees mode).
Arc cosine: \(\cos ^{-1} x\). Output range is from \(0^{\circ}\) to \(180^{\circ}\) or 0 to \(\pi\). Inputs and outputs depend on the current angle format. Also accepts complex numbers. Output will be complex for values outside the normal cosine domain of \(-1 \leq x \leq 1\).
Acos(value)

\section*{Example:}

ACOS (1) returns 0 (Degrees mode).

Arc tangent: \(\tan ^{-1} x\). Output range is from \(-90^{\circ}\) to \(90^{\circ}\) or \(-\pi / 2\) to \(\pi / 2\). Inputs and outputs depend on the current angle format. Also accepts complex numbers.

Atan(value)
Example:
ATAN (1) returns 45 (Degrees mode).

Square. Also accepts complex numbers. value \({ }^{2}\)

Example:
\(18^{2}\) returns 324

Square root. Also accepts complex numbers.
\(\sqrt{ }\) value or \(\sqrt{ }\) (expression)
Example:
\(\sqrt{324}\) returns 18

Power ( \(x\) raised to \(y\) ). Also accepts complex numbers. value^power

Example:
\(2^{\wedge} 8\) returns 256

Nth root \((\sqrt[n]{x})\). Takes the \(n\)th root of \(x\). root NTHROOT value

Example:
3 NTHROOT 8 returns 2

Negation. Also accepts complex numbers.

> -value

Example:
- (1+2*i) returns -1-2*i

Absolute value. For a complex number, this is \(\sqrt{x^{2}+y^{2}}\).
ABS(value)
\[
\operatorname{ABS}\left(\left(x+y^{*} i\right)\right)
\]

Example:
ABS ( -1 ) returns 1
ABS ( \((1,2))\) returns 2.2360679775

\section*{The Math menu}

The Math menu provides access to math functions, units, and physical constants.
 menu. Each of the three menus (Math Functions, Units, and SI Constants) has its own menu key. The Math menu is organized by category. For each category of functions on the left, there is a list of function names on the right. The highlighted category is the current category.


When you press Somb \(_{\text {Math }}^{8}\), you see the menu list of Math categories in the left column and the corresponding functions of the highlighted category in the right column. The menu key MAT• indicates that the Math Functions menu list is active.

appear in alphabetical order. Press \(\vartheta\) or \(\odot\) to scroll through the categories. To skip directly to a category, type the number (1-9) or letter (A-E) of the category.
2. The list of functions (on the right) applies to the currently highlighted category (on the left). Use (1)
and (4) to switch between the category list and the function list.
3. Highlight the name of the function you want and press \(O K\). This copies the function name (and an initial parenthesis, if appropriate) to the edit line.
\begin{tabular}{|c|c|c|}
\hline Function categories & \begin{tabular}{l}
- Calculus \\
- Complex numbers \\
- Constant \\
- Distribution \\
- Hyperbolic trigonometry \\
- Integer \\
- List
\end{tabular} & \begin{tabular}{l}
Loop \\
Matrix \\
Polynomial \\
Probability \\
Real numbers \\
(Real) \\
Tests \\
Trigonometry
\end{tabular} \\
\hline
\end{tabular}

\section*{Math functions by category}

\author{
Syntax
}

Each function's definition includes its syntax, that is, the exact order and spelling of a function's name, its delimiters (punctuation), and its arguments. Note that the syntax for a function does not require spaces.

\section*{Calculus functions}

This category contains the numerical derivative and integral functions, as well as the Where function (|).

Differentiates expression with respect to variable then substitutes value for variable and evaluates the result.

д (expression, variable=value)
Example:
\(\partial\left(x^{2}-x, x=3\right)\) returns 5
Integrates expression from lower to upper limits with respect to the variable of integration. To find the definite integral, both limits must have numeric values (that is, be numbers or real variables).
\(\int\) (expression, variable, lower, upper)
Example:
\[
\int\left(x^{2}-x, x, 0,3\right) \text { returns } 4.5
\]

Evaluates expression where each given variable is set to the given value. Defines numeric evaluation of a symbolic expression.
expression |(variable 1 =value 1, variable2=value \(2, \ldots\) )
Example:
3* ( \(\mathrm{X}+1\) ) | (X=3) returns 12

\section*{Complex number functions}

These functions are for complex numbers only. You can also use complex numbers with all trigonometric and hyperbolic functions, and with some real-number and keyboard functions. Enter complex numbers in the form
\((x+y * i)\), where \(x\) is the real part and \(y\) is the imaginary part.

ARG

Complex conjugate. Conjugation is the negation (sign reversal) of the imaginary part of a complex number.
\(\operatorname{ConJ}\left(\left(x+y^{*}\right)\right)\)
Example:
CONJ (3+4*i) returns (3-4*i)
Imaginary part, \(y\), of a complex number, \(\left(x+y^{*} i\right)\). IM (( \(\left.x+y^{*} i\right)\) )

Example:
IM (3+4*i) returns 4
RE
Real part \(x\), of a complex number, ( \(x+y^{*}\) ).
\(\operatorname{RE}\left(\left(x+y^{*} i\right)\right)\)
Example:
\(\operatorname{RE}(3+4 * i)\) returns 3

\section*{Constants}
e
The constants available from the Math Functions menu are mathematical constants. These are described in this section. The HP 39 gll has two other menus of constants: program constants and physical constants. The physical constants are described further on in this chapter, while the program constants are described in the programming chapter.

Natural logarithm base. Internally represented as 2.71828182846 .

MAXREAL

MINREAL
\(\pi\)

\section*{Distribution}
normald
normald_cdf

Imaginary value for \(\sqrt{-1}\), the complex number \((0,1)\). i

Maximum real number. Internally represented as \(9.99999999999 \times 10^{499}\).

MAXREAL
Minimum real number. Internally represented as \(1 \times 10^{-499}\).

MINREAL
Internally represented as 3.14159265359 .
\(\pi\)

This category contains probability density functions, and both cumulative probability functions and their inverses, for the common probability distributions. These distributions include the Normal, Binomial, Chi-square, Fisher, Poisson, and Student's \(\dagger\) distributions.

Normal probability density function. Computes the probability density at the value x , given the mean, \(\mu\) and standard deviation, \(\sigma\) of a normal distribution. If only a single value ( x ) is supplied, assumes \(\mu=0\) and \(\sigma=1\).
```

normald([\mu, \sigma,] x)

```

Example:
normald(0.5) and normald(0, \(1,0.5\) ) both return 0.352065326765 .

Cumulative normal distribution function. Returns the lower-tail probability of the normal probability density function for the value x , given the mean, \(\mu\) and standard deviation, \(\sigma\) of a normal distribution. If only a single value (x) is supplied, assumes \(\mu=0\) and \(\sigma=1\).
```

normald_cdf([\mu,\sigma,] x)

```

Example:
normald_cdf(0, 1, 2) returns 0.97724986805.
\begin{tabular}{|c|c|}
\hline normald_icdf & \begin{tabular}{l}
Inverse cumulative normal distribution function. Returns the cumulative normal distribution value associated with the lower-tail probability, \(p\), given the mean, \(\mu\) and standard deviation, \(\sigma\) of a normal distribution. If only a single value \((x)\) is supplied, assumes \(\mu=0\) and \(\sigma=1\). \\
normald_cdf( \([\mu, \sigma] p\),
\end{tabular} \\
\hline & \begin{tabular}{l}
Example: \\
normald_icdf(0, 1, 0.841344746069) returns 1.
\end{tabular} \\
\hline \multirow[t]{3}{*}{binomial} & \begin{tabular}{l}
Binomial probability density function. Computes the probability of \(k\) successes out of \(n\) trials, each with a probability of success, \(p\). Returns \(\operatorname{Comb}(n, k)\) if there is no third argument. Note that \(n\) and \(k\) are integers with \(k \leq n\) \\
binomial( \(n, k, p\) )
\end{tabular} \\
\hline & Example: \\
\hline & binomial (4, 2, 0.5) returns 0.375. \\
\hline \multirow[t]{4}{*}{binomial_cdf} & Cumulative binomial distribution function. Returns the probability of \(k\) or fewer successes out of \(n\) trials, with a probability of success, \(p\) for each trial. Note that \(n\) and \(k\) are integers with \(k \leq n\). \\
\hline & binomial_cdf( \(n, p, k\) ) \\
\hline & Example: \\
\hline & binomial_cdf( \(4,0.5,2)\) returns 0.6875. \\
\hline \multirow[t]{4}{*}{binomial_icdf} & Inverse cumulative binomial distribution function. Returns the number of successes, \(k\) out of \(n\) trials, each with a probability of \(p\), such that the probability of \(k\) or fewer successes is \(q\). \\
\hline & binomial_icdf( \(n, p, q)\) \\
\hline & Example: \\
\hline & binomial_icdf( \(4,0.5,0.6875)\) returns 2. \\
\hline
\end{tabular}
chisquare_cdf
chisquare_icdf
\(\chi^{2}\) probability density function. Computes the probability density of the \(\chi^{2}\) distribution at x , given n degrees of freedom.
\[
\text { chisquare }(n, x)
\]

Example:
```

chisquare(2, 3.2) returns 0.100948258997.

```

Cumulative \(\chi^{2}\) distribution function. Returns the lower-tail probability of the \(\chi^{2}\) probability density function for the value \(x\), given \(n\) degrees of freedom.
```

chisquare_cdf(n, k)

```

Example:
```

chisquare_cdf(2, 6.1) returns 0.952641075609.

```

Inverse cumulative \(\chi^{2}\) distribution function. Returns the value x such that the \(\chi^{2}\) lower-tail probability of x , with \(n\) degrees of freedom, is \(p\).
```

chisquare_icdf(n, p)

```

Example:
```

chisquare_icdf(2, 0.952641075609) returns

```
6.1.

Fisher (or Fisher-Snedecor) probability density function. Computes the probability density at the value x , given numerator \(n\) and denominator \(d\) degrees of freedom.
\[
\text { fisher }(n, d, x)
\]

\section*{Example:}
fisher(5, 5, 2) returns 0.158080231095.
fisher_cdf

Cumulative Fisher distribution function. Returns the lowertail probability of the Fisher probability density function for the value x , given numerator \(n\) and denominator \(d\) degrees of freedom.
```

fisher_cd£(n, d, x)

```

Example:
```

fisher_cdf(5,5, 2) returns 0.76748868087.

```
fisher_icdf
poisson
poisson_cdf
poisson_icdf

Inverse cumulative Fisher distribution function. Returns the value \(x\) such that the Fisher lower-tail probability of \(x\), with numerator \(n\) and denominator \(d\) degrees of freedom, is \(p\).
```

fisher_icdf(n,d, p)

```

Example:
fisher_icdf(5, 5, 0. .76748868087) returns 2.
Poisson probability mass function. Computes the probability of \(k\) occurrences of an event in a time interval, given \(\mu\) expected (or mean) occurrences of the event in that interval. For this function, \(k\) is a non-negative integer and \(\mu\) is a real number.
```

poisson(\mu,k)

```

Example:
poisson(4, 2) returns 0.14652511111 .
Cumulative poisson distribution function. Returns the probability \(x\) or fewer occurrences of an event in a given time interval, given \(\mu\) expected occurrences.
```

poisson_cdf( }\mu,x

```

Example:
poisson_cdf(4, 2) returns 0.238103305554.
Inverse cumulative poisson distribution function. Returns the value \(x\) such that the probability of \(x\) or fewer occurrences of an event, with \(\mu\) expected (or mean) occurrences of the event in the interval, is \(p\).
```

poisson_icdf( }\mu,p

```

Example:
poisson_icdf(4, 0.238103305554) returns 2.
Student's \(\dagger\) probability density function. Computes the probability density of the Student's-t distribution at x , given \(n\) degrees of freedom.
```

student(n, x)

```

Example:
student \((3,5.2)\) returns 0.00366574413491.
```

student_cdf
student_icdf
Cumulative student's $\dagger$ distribution function. Returns the lower-tail probability of the student's $\dagger$ probability density function at $x$, given $n$ degrees of freedom.

```
```

student_cdf(n, x)

```
student_cdf(n, x)
Example:
student_cdf \((3,-3.2)\) returns
0.0246659214813.
student_icdf
Inverse cumulative student's \(\dagger\) distribution function. Returns the value x such that the student's-t lower-tail probability of \(x\), with \(n\) degrees of freedom, is \(p\).
```

```
student_icdf(n, p)
```

student_icdf(n, p)
Example:
student_icdf(3, 0.0246659214813) returns 3.2.

```

\section*{Hyperbolic trigonometry}

The hyperbolic trigonometry functions can also take complex numbers as arguments.

ACOSH
Inverse hyperbolic cosine : \(\cosh ^{-1} x\).
Acosh(value)
ASINH

ATANH

COSH
Inverse hyperbolic sine : \(\sinh ^{-1} x\).
ASINH(value)
Inverse hyperbolic tangent: \(\tanh ^{-1} x\).
Atanh(value)
Hyperbolic cosine
cosh(value)
SINH

TANH
Hyperbolic tangent.
tanh(value)
ALOG
Antilogarithm (exponential). This is more accurate than \(10^{\wedge} x\) due to limitations of the power function.

ALOG(value)

EXP \(\quad\) Natural exponential. This is more accurate than \(e^{x}\) due to limitations of the power function.
```

EXP(value)

```

EXPM1
Exponent minus \(1: e^{x}-1\). This is more accurate than EXP when \(x\) is close to zero.

EXPM1 (value)

\section*{LNP 1}

Natural log plus \(1: \ln (x+1)\). This is more accurate than the natural logarithm function when \(x\) is close to zero.

LNP1(value)

\section*{Integer}
ichinrem

\section*{idivis}
iegcd

Integer Chinese Remainder Theorem for two equations. Takes two lists \([a, p]\) and \([b, q]\) and returns a list of two integers, \([r, n]\), such that \(x=r\) modn. In this case, \(x\) is such that \(x \equiv a \bmod p\) and \(x \equiv b\) modq; also, \(n=p \cdot q\)
ichinrem \(([a, p],[b, q])\)
Example:
ichinrem( \([2,7],[3,5])\) returns \([-12,35]\).
Integer divisors. Returns a list of all the factors of the integer \(a\).
idivis(a)
Example:
idivis(12) returns \([1,2,3,4,6,12]\).
Integer extended greatest common divisor. For integers a and \(b\), returns \([u, v, i g c d]\) such that \(u \cdot a+v \cdot b=\operatorname{igcd}(a, b)\).
iegcd \((a, b)\)
Example:
iegcd(14, 21) returns \([-1,1,7]\).
\begin{tabular}{|c|c|}
\hline ifactor & \begin{tabular}{l}
Prime factorization. Returns the prime factorization of the integer a as a product. \\
ifactor(a)
\end{tabular} \\
\hline & Example: \\
\hline & ifactor(150) returns \(2 \cdot 3 \cdot 5^{2}\). \\
\hline \multirow[t]{3}{*}{ifactors} & \begin{tabular}{l}
Prime factors. Similar to ifactor, but returns a list of the factors of the integer a with their multiplicities. \\
ifactor(a)
\end{tabular} \\
\hline & Example: \\
\hline & ifactor(150) returns [2, 1, 3, 1, 5, 2]. \\
\hline \multirow[t]{3}{*}{igcd} & Greatest common divisor. Returns the integer that is the greatest common divisor of the integers \(a\) and \(b\).
\[
\operatorname{igcd}(a, b)
\] \\
\hline & Example: \\
\hline & igcd \((24,36)\) returns 12. \\
\hline \multirow[t]{4}{*}{iquo} & Euclidean quotient. Returns the integer quotient when the integer \(a\) is divided by the integer \(b\). \\
\hline & iquo( \(a, b\) ) \\
\hline & Example: \\
\hline & iquo(46, 21) returns 2. \\
\hline \multirow[t]{4}{*}{iquorem} & Euclidean quotient and remainder. Returns the integer quotient and remainder when the integer \(a\) is divided by the integer \(b\). \\
\hline & iquorem( \(a, b\) ) \\
\hline & Example: \\
\hline & iquorem(46, 21) returns [2, 4]. \\
\hline \multirow[t]{4}{*}{irem} & Euclidean remainder. Returns the integer remainder when the integer \(a\) is divided by the integer \(b\). \\
\hline & irem( \(a, b\) ) \\
\hline & Example: \\
\hline & irem(46, 21) returns 4. \\
\hline
\end{tabular}
```

isprime
ithprime
nextprime

Power and modulo. For the integers $a, n$, and $p$, returns $a^{n} \bmod$.
$\operatorname{powmod}(a, n, p)$
Example:
powmod $(5,2,13)$ returns 12.
Previous prime. Returns the previous prime number before the integer $a$.

```
prevprime(a)
```

```
```

prevprime(a)

```
```

Example:
prevprime(11) returns 7.
euler

Euler's phi (or totient) function. Takes a positive integer $x$ and returns the number of positive integers less than or equal to $x$ that are coprime to $x$.
euler(x)

Example:
euler(6) returns 2.

## List functions

These functions work on list data. See the chapter Lists for details.

## Loop functions

The loop functions display a result after evaluating an expression a given number of times.

ITERATE
Repeatedly for \#times evaluates an expression in terms of variable. The value for variable is updated each time, starting with initialvalue.

ITERATE ( expression, variable, initialvalue, \#times)

Example:
ITERATE ( $\mathrm{X}^{2}, \mathrm{X}, 2,3$ ) returns 256
$\Sigma$
Summation. Finds the sum of expression with respect to variable from initialvalue to finalvalue.
$\Sigma$ (expression, variable, initialvalue, finalvalue)
Example:

$$
\Sigma\left(x^{2}, x, 1,5\right) \text { returns } 55
$$

## Matrix functions

These functions are for matrix data stored in matrix variables. See the chapter Matrices for details.

## Polynomial functions

Polynomials are products of constants (coefficients) and variables raised to powers (terms).

## POLYCOEF

Polynomial coefficients. Returns the coefficients of the polynomial with the specified roots.

POLYCOEF ([roots])
Example:
To find the polynomial with roots $2,-3,4,-5$ :
poLYCOEF ( $[2,-3,4,-5]$ ) returns $[1,2,-25$, $-26,120]$, representing $x^{4}+2 x^{3}-25 x^{2}-26 x+120$.

Polynomial evaluation. Evaluates a polynomial with the specified coefficients for the value of $x$.

POLYEVAL ([coefficients], value)
Example:
For $x^{4}+2 x^{3}-25 x^{2}-26 x+120$ :
POLYEVAL ( $[1,2,-25,-26,120], 8$ ) returns 3432.

## POLYROOT

Polynomial roots. Returns the roots for the nth-order polynomial with the specified $n+1$ coefficients.

POLYROOT([coefficients])
Example:

$$
\begin{aligned}
& \text { For } x^{4}+2 x^{3}-25 x^{2}-26 x+120 \text { : } \\
& \text { POLYROOT }([1,2,-25,-26,120]) \text { returns } \\
& {[4,-5,-3,2] \text {. }}
\end{aligned}
$$

HINT The results of POLYROOT will often not be easily seen in Home due to the number of decimal places, especially if they are complex numbers. It is better to store the results of POLYROOT to a matrix.

For example, POLYROOT ( $[1,0,0,-8]$ STO M1 will store the three complex cube roots of 8 to matrix M1 as a complex vector. Then you can see them by going to the Matrix Catalog. You can also access them individually in calculations by referring to $\mathrm{MI}(1), \mathrm{MI}(2)$ etc.

## Probability functions

## COMB

Number of combinations (without regard to order) of $n$ things taken $r$ at a time: $n!/(r!(n-r))$.

$$
\operatorname{COMB}(n, r)
$$

Example:
$\operatorname{COMB}(5,2)$ returns 10 . That is, there are ten different ways that five things can be combined two at a time.

Factorial of a positive integer. For non-integers, $!=\Gamma(x+$ 1). This calculates the gamma function.
value!
Example:
5 ! Returns 120

PERM
Number of permutations (with regard to order) of $n$ things taken $r$ at a time: $n!/(r!(n-r)!$

$$
\operatorname{PERM}(n, r)
$$

## Example:

$\operatorname{PERM}(5,2)$ returns 20 . That is, there are 20 different permutations of five things taken two at a time.

Random number. With no argument, this function returns a random number between zero and one. With one integer argument $a$, it returns a random integer between 0 and $a$. With three integer arguments, $n, a$, and $b$, returns $n$ random integers between $a$ and $b$.

RANDOM
RANDOM (a)
$\operatorname{RANDOM}(\mathrm{n}, \mathrm{a}, \mathrm{b})$
Upper-Tail Chi-Squared Probability given degrees of freedom, evaluated at value. Returns the probability that a $\chi^{2}$ random variable is greater than value.

UTPC(degrees, value)
UTPF
Upper-Tail Snedecor's F Probability given numerator degrees of freedom and denominator degrees of freedom (of the F distribution), evaluated at value. Returns the probability that a Snedecor's F random variable is greater than value.

UTPF(numerator, denominator, value)
Upper-Tail Normal Probability given mean and variance, evaluated at value. Returns the probability that a normal random variable is greater than value for a normal distribution. Note: the variance is the square of the standard deviation.

UTPN(mean, variance, value)
Upper-Tail Student's t-Probability given degrees of freedom, evaluated at value. Returns the probability that the Student's $t$ - random variable is greater than value.

UTPT(degrees, value)

## Real-number functions

Some real-number functions can also take complex arguments.

## CEILING

Smallest integer greater than or equal to value.
CEILING(value)
Examples:

CEILING (-3.2) returns -3

| DEG $\rightarrow$ RAD | Degrees to radians. Converts value from Degrees angle format to Radians angle format. $D E G \rightarrow R A D(\text { value })$ |
| :---: | :---: |
|  | Example: |
|  | DEG $\rightarrow$ RAD (180) returns 3.14159265359 , the value of $\pi$. |
| FLOOR | Greatest integer less than or equal to value. FLOOR(value) |
|  | Example: |
|  | FLOOR (-3.2) returns -4 |
| FNROOT | Function root-finder (like the Solve app). Finds the value for the given variable at which expression most nearly evaluates to zero. Uses guess as initial estimate. <br> FNROOT(expression, variable, guess) |
|  | Example: |
|  | FNROOT (M*9.8/600-1, M, 1) returns 61.224489796. |
| FRAC | Fractional part. FRAC(value) |
|  | Example: |
|  | FRAC (23.2) returns . 2 |
| HMS $\rightarrow$ | Hours-minutes-seconds to decimal. Converts a number or expression in H.MMSSs format (time or angle that can include fractions of a second) to $x . x$ format (number of hours or degrees with a decimal fraction). $\text { HMS } \rightarrow(H . M M S S s)$ |
|  | Example: <br> HMS $\rightarrow$ (8.30) returns 8.5 |
| $\rightarrow$ HMS | Decimal to hours-minutes-seconds. Converts a number or expression in $x . x$ format (number of hours or degrees with a decimal fraction) to H.MMSSs format (time or angle up to fractions of a second). $\rightarrow \operatorname{HMS}(x \cdot x)$ |
|  | Example: |
|  | $\rightarrow$ HMS (8.5) returns 8.3 |


| INT | Integer part. INT(value) |
| :---: | :---: |
|  | Example: |
|  | INT (23.2) returns 23 |
| MANT | Mantissa (significant digits) of value. MANT(value) |
|  | Example: |
|  | MANT (21.2E34) returns 2.12 |
| MAX | Maximum. The greater of two values. MAX(value 1, value2) |
|  | Example: |
|  | MAX $(210,25)$ returns 210 |
| MIN | Minimum. The lesser of two values. MIN(value 1, value2) |
|  | Example: |
|  | MIN ( 210,25 ) returns 25 |
| MOD | Modulo. The remainder of value $1 /$ value 2 . value 1 MOD value 2 |
|  | Example: |
|  | 9 MOD 4 returns 1 |
| \% | $x$ percent of $y$; that is, $x / 100 * y$. |
|  | \% ( $x, y$ ) |
|  | Example: |
|  | \% ( 20,50 ) returns 10 |
| \%CHANGE | Percent change from $x$ to $y$, that is, $100(y-x) / x$. \%CHANGE $(x, y)$ |
|  | Example: |
|  | \%CHANGE $(20,50)$ returns 150 |

\%TOTAL

RAD $\rightarrow$ DEG

ROUND

SIGN

## TRUNCATE

Percent total : (100) $y / x$. What percentage of $x$, is $y$. \%TOTAL $(x, y)$

Example:
\%TOTAL $(20,50)$ returns 250
Radians to degrees. Converts value from radians to degrees.

RAD $\rightarrow$ DEG (value)
Example:
RAD $\rightarrow$ DEG ( $\pi$ ) returns 180
Rounds value to decimal places. Accepts complex numbers.

ROUND(value, places)
Round can also round to a number of significant digits as showed in the second example below.

Examples:
ROUND (7.8676,2) returns 7.87
ROUND ( $0.0036757,-3$ ) returns 0.00368
Sign of value. If positive, the result is 1 . If negative, -1 . If zero, result is zero. For a complex number, this is the unit vector in the direction of the number.

SIGN(value)
$\operatorname{SIGN}((x, y))$
Example:
SIGN (-2) returns -1
SIGN( $(3,4)$ ) returns (.6,.8)
Truncates value to decimal places. Accepts complex numbers.

TRUNCATE(value, places)
Example:
TRUNCATE (2.3678,2) returns 2.36

Exponent of value.
xpon(value)
Example:
XPON(123.4) returns 2

## Test functions

The test functions are logical operators that always return either 1 (true) or 0 (false).

Less than. Returns 1 if true, 0 if false.
value 1 <value 2

Greater than. Returns 1 if true, 0 if false. value 1> value 2

Greater than or equal to. Returns 1 if true, 0 if false. value $1 \geq$ value 2

Compares value 1 and value 2 . Returns 1 if they are both non-zero, otherwise returns 0 .
value 1 AND value2
If expression is true, do the trueclause; if not, do the falseclause.

IFTE (expression, trueclause, falseclause)
Example:
$\operatorname{IFTE}\left(X>0, X^{2}, X^{3}\right)$ with $\mathrm{X}=-2$ returns -8
Returns 1 if value is zero, otherwise returns 0 .
NOT value returns 0 .
valuel OR value2
Exclusive OR. Returns 1 if either value 1 or value2-but not both of them-is non-zero, otherwise returns 0 .
valuel XOR value2

## Trigonometry functions

The trigonometry functions can also take complex numbers as arguments. For SIN, COS, TAN, ASIN, ACOS, and ATAN, see the Keyboard category.

ACOT
Arc cotangent.
АСОт(value)

ACSC
Arc cosecant. ACSC(value)

ASEC
Arc secant.
ASEC(value)

COT
Cotangent: $\cos x / \sin x$. Сот(value)

CSC
Cosecant: 1/sinx
CSC(value)

SEC
Secant: 1/cosx.
SEC(value)

## Units and physical constants

When you press $C_{C_{m s}{ }^{\text {Math }} \text { B }}^{\text {and }}$, three menus become available:

- the Math Functions menu (which appears by default)
- the Units menu
- the Physical Constants menu

The math functions menu is described extensively earlier in this chapter.

## Units

You can aftach physical units to any numerical calculation or result. A numerical value with units attached is referred to as a measurement. You can operate on measurements just as you do on numbers without units attached, except that the units are carried along with the operations. The function usimplify (unit simplify) will simplify the results back to the simplest unit structure. The units are found in the Units menu. Like the Math menu, the Units menu is divided into a set of categories on the left and units in each category on the right. The categories are:

## Unit categories

| - Length | - Acceleration | Electricity |
| :--- | :--- | :--- |
| - Area | - Force | - Light |
| - Volume | • Energy | - Angle |
| - Time | • Power | - Viscosity |
| - Speed | • Pressure | - Radiation |
| - Mass | - Temperature |  |

Suppose you wish to add 20 centimeters and 5 inches.

1. If you want the result in cm , start by entering the 20 cm .


(1) $)$ (to select _cm)
2. Now add 5 inches.

(8 times for _inch)
OK

ENTER
The result is shown as 32.7 cm . If you had wanted the result in inches, then you would have entered the 5 inches first.
3. To continue the example, we divide this result by 4 seconds and convert the result to kilometers per hour.


$\odot \ominus$ (to select Time)
(
(to select $\qquad$

OK ENTER
The result is shown as $8.175 \mathrm{~cm} / \mathrm{s}$.
4. Now convert the result to kilometers per hour.

|  select Functions) |
| :---: |
|  |  |



- (to select
convert) OK
copy 1
© (to select 8.175 _( $\mathrm{cm} / \mathrm{s}$ ) )

COPY


- (6 times to select Speed)
(4 times to select _km/h)
The result is shown as 0.2943 kilometers per hour.


## Physical constants

There are 29 physical constants you can use in calculations. These constants are grouped into the categories chemistry, physics and quantum mechanics. A list of all these constants can be found in Physical Constants in the Reference Information chapter.

To access the menu of physical constants:

2. Press PHYS

3. Use the arrow keys to navigate through the options.
4. While in the Physical Constants menu, pressing Values toggles between showing the entire value of the constant and a description of the constant in the help line. To attach units to the constant when you paste it into the command line, keep VALIE: active when you press OK ; to paste just the value without units, deactivate VAlUE: before pressing OK .

5. To use the selected constant in a calculation, press
ok. The constant appears at the position of the cursor on the edit line.

Example:
Suppose you want to know the potential energy of a mass of 5 units according to the equation $E=m c^{2}$.

1. Enter the mass and multiplication.

2. Go to the Physical Constants menu.
```
Math
Cmds B
PHYS
```


3. Select the speed of light.
$\odot$ (to select Physics)
( $)$ (to select c)

4. Enter the speed of light into the current expression.

OK

5. Square the speed of light and evaluate the expression.

| RAD | Function |  |
| :---: | :---: | :---: |
| 5*299792458 ${ }^{2}$ |  |  |
|  | 4.49377589368E17 |  |
| STO - |  |  |

## Lists

## Introduction

You can do list operations in Home and in programs. A list consists of comma-separated real or complex numbers, expressions, or matrices, all enclosed in braces. A list may, for example, contain a sequence of real numbers such as $\{1,2,3\}$. Lists represent a convenient way to group related objects.

There are ten list variables available, named L0 to L9. You can use them in calculations or expressions in Home or in a program. Retrieve the list names from the Vars menu, or just type their names from the keyboard.

You can create, edit, delete, send, and receive named lists in the List catalog ( SHIT LIST ). You can also create and store lists-named or unnnamed-in Home.

List variables are identical in behavior to the columns C1CO in the Statistics 2Var app and the columns D1-DO in the Statistics 1Var app. You can store a statistics column to a list (or vice versa) and use any of the list functions on the statistics columns, or the statistics functions on the list variables.

## Create a list in the List Catalog

1. Open the List catalog.

| Lists |  |  |  |
| :---: | :---: | :---: | :---: |
| L1 0 |  |  | OKB ${ }^{-1}$ |
| L2 0 |  |  | OKB |
| L3 0 |  |  | OKB |
| L4 0 |  |  | OKB |
| L5 0 |  |  | OKB |
| EDIT | DELETE | SEND |  |

2. Highlight the list name you want to assign to the new list ( LI, etc.) and press EDIT to display the List editor.
3. Enter the values you want in the list, pressing ${ }^{\text {ENTER }}$ after each one.
Values can be real or complex numbers (or an expression). If you enter a expression, it is evaluated and the
 result is inserted in the list.
4. When done, press $\qquad$ LIST to see the List catalog, or


List Catalog keys The list catalog keys are:

| Key | Meaning |
| :---: | :---: |
| EDIT | Opens the highlighted list for editing. |
| DEEIEE or cher | Deletes the contents of the selected list. |
| SEND | Transmits the highlighted list to another HP 39gll. |
| SHHTH CLEAR | Clears all lists. |
|  | Moves to the end or the beginning of the catalog. |

## The List Editor

Press EDIT to create or edit a list. Once you press this menu key, you enter the List Editor. The List Editor is a special environment for entering data into lists.

## List edit keys

When you press EDIT to create or change a list, the following keys are available to you:

| Key | Meaning |
| :---: | :---: |
| INS | Inserts a new value before the highlighted item. |
| EDIT | Copies the highlighted list item into the edit line. |
| EIG | Toggles between large and small fonts. |
| WDTHI | Toggles between showing 1, 2, 3 , or 4 lists at a time. |
| DELETE or Clear | Deletes the highlighted item from the list. |
| SHIIT CLEAR | Clears all elements from the list. |
| SHIIT $\uparrow$ or $\odot$ | Moves to the end or the beginning of the list. |

To edit a list

1. Open the List catalog.

LIST.

| Lists |  |  |  |
| :---: | :---: | :---: | :---: |
| L1 4 |  |  | . 031 KB |
| L2 0 |  |  | 0 KB |
| L3 0 |  |  | OKB |
| L4 0 |  |  | OKB |
| L5 0 |  |  | OKB |
| EDIT | DELETE | SEND |  |

2. Press $\circlearrowleft$ or to highlight the name of the list you want to edit (L1, etc.) and press EDIT to display the list contents.

|  |  | L1 |  |
| :--- | :--- | :--- | :--- |
| 1 | 88 |  |  |
| 2 | 90 |  |  |
| 3 | 89 |  |  |
| 4 | 65 |  |  |
| 88 |  |  |  |
| EDIT | INS | DELETE |  |



## Deleting lists

To delete a list

To delete all lists

In the List catalog, highlight the list name and press clas.
You are prompted to confirm that you want to delete the contents of the highlighted list variable. Press ${ }^{[\text {CNTER }}$ to delete the contents, or ${ }^{8 N / C / C}$ to cancel the deletion.

In the List catalog, press CLEAR.

## Lists in the Home view

You can enter and operate on lists directly in the Home view. The lists you work on in the Home view can be named or not.

1. Enter the list on the edit line. Start and end the list with braces (the shifted ${ }^{8}$ and ${ }^{9}$ keys) and separate each element with a comma.
 Immediately after typing in the list, you can store it in
 variable names are L0 through L9.
This example stores the list $\{25,147,8\}$ in L1.


## To display a list

To display one element

## To store one element

To display a list in the Home view, type its name and press $\stackrel{\text { ENTER }}{ }$.

To display one element of a list in the Home view, enter listname (element\#). For example, if L 2 is $\{3,4,5,6\}$, then L2 (2) (ENTER) returns 4.

To store a value in one element of a list in the Home view, enter value STOM listname (element\# ). For example, to store 148 as the second element in L2, type


You can send lists to another calculator or a PC just as you can apps, programs, matrices, and notes. To send lists between two HP 39gll calculators:

1. Connect the two HP 39gll calculators with the microUSB cable provided with the calculators and turn both calculators on.
2. Open the List catalog on the sending calculator.
3. Highlight the list to send.

## 4. Press SEND.

5. The transfer will occur immediately.
6. Open the List Catalog on the receiving calculator to see the new list.

## List functions

List functions are found in the Math menu. You can use them in Home, as well as in programs.

You can type in the name of the function, or you can copy the name of the function from the List category of the MATH
 menu. Press Kchat 7 to highlight the List category in the left column of the Math menu (List is the seventh category in the Math menu). Press $\Theta$ and $\Theta$ to select the list function you want, select a function, and press OK

List functions have the following syntax:
Functions have arguments that are enclosed in parentheses and separated by commas. Example: CONCAT (L1, L2). An argument can be either a list variable name (such as $L T$ ) or the actual list. For example, $\operatorname{REVERSE}(\{1,2,3\})$.
Common operators like,,$+- x$, and / can take lists as arguments. If there are two arguments and both are lists, then the lists must have the same length, since the calculation pairs the elements. If there are two arguments and one is a real number, then the calculation pairs the number with each element of the list.

Example:

$$
5 *\{1,2,3\} \text { returns }\{5,10,15\} .
$$

Besides the common operators that can take numbers, matrices, or lists as arguments, there are commands that can only operate on lists.

Example:
$\operatorname{CONCAT}(\{1,2,3\},\{4\})$ returns $\{1,2,3,4\}$.
Creates a new list composed of the first differences of a list, that is, the differences between the sequential elements in the list. The new list has one less element than the original list. The first differences for $\left\{x_{1}, x_{2}, x_{3}, \ldots x_{n-1}\right.$, $\left.x_{n}\right\}$ are $\left\{x_{2}-x_{1}, x_{3}-x_{2}, \ldots x_{n}-x_{n-1}\right\}$.

## $\Delta$ LIST (listl)

Example:
In Home, store $\{3,5,8,12,17,23\}$ in $L 5$ and find the first differences for the list.


Calculates a sequence of elements for a new list. Evaluates expression with respect to variable, as variable takes on values from begin to end values, taken at increment steps.

> MAKELIST (expression, variable, begin, end, increment)

The MAKELIST function generates a sequence by automatically producing a list from the repeated evaluation of an expression.

## Example:

In Home, generate a series of squares from 23 to 27.


Returns the position of an element within a list. The element can be a value, a variable, or an expression. If there is more than one instance of the element, the position of the first occurrence is returned. A value of 0 is returned if there is no occurrence of the specified element.
pOS (list, element)
Example:
$\operatorname{POS}(\{3,7,12,19\}, 12)$ returns 3
REVERSE
Creates a list by reversing the order of the elements in a list.

REVERSE (list)

## Example:

```
REVERSE({1,2,3}) returns {3,2,1}
```

Calculates the number of elements in a list.
SIZE (list)
Also works with matrices.
Example:
$\operatorname{SIZE}(\{1,2,3\})$ returns 3

Calculates the sum of all elements in a list.
ELIST (list)
Example:
$\operatorname{ELIST}(\{2,3,4\})$ returns 9.
SORT
Sorts the elements in a list in ascending order.
SORT (list)
Example:
$\operatorname{SORT}(\{2,5,3\})$ returns $\{2,3,5\}$

## Finding statistical values for lists

To find values such as the mean, median, maximum, and minimum of a list, use the Statistics IVar app.

## Example

In this example, use the Statistics IVar app to find the mean, median, maximum, and minimum values of the elements in the list LI .

1. Create L1 with values $88,90,89,65,70$, and 89 .

2. In Home, store L1 into D1. You will then be able to see the list data in the Numeric view of the Statistics 1 Var app.

3. Start the Statistics 1 Var app.


Note: your list values are now in column 1 (D1).
4. Select the column upon which to base the statistical calculations. This is done in the Symbolic view.


By default, H 1 is defined to use D1, so
 nothing further remains to be done in the Symbolic view; however, if the data were in D2 or any column other than D1, you would have to enter the desired data column here.
5. Calculate summary statistics.


See the chapter titled, Statistics IVar for the meaning of each computed statistic.

## Matrices

## Introduction

You can perform matrix calculations in Home and in programs. The matrix and each row of a matrix appear in brackets, and the elements and rows are separated by commas. For example, the following matrix:

$$
\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6
\end{array}\right]
$$

is displayed in the history as: [[1,2,3],[4,5,6]]

You can enter matrices directly in the command line, or create them in the matrix editor.

| Vectors | Vectors are one-dimensional arrays. They are composed <br> of just one row. A vector is represented with single <br> brackets; for example, $[1,2,3]$. A vector can be a real <br> number vector or a complex number vector, for example <br> $[(1,2),(7,3)]$. |
| :--- | :--- |
| Matrices | Matrices are two-dimensional arrays. They are composed <br> of more than one row and at least one column. <br> Two-dimensional matrices are represented with nested <br> brackets; for example, $[[1,2,3],[4,5,6]]$. You can create <br> complex matrices, for example, $[[(1,2),(3,4)],[(4,5)$, <br> $(6,7)]]$. |

Matrix Variables
There are ten matrix variables available, named мо to m9. You can use them in calculations in Home or in a program. You can retrieve matrix names from the Vars menu, or just type their names from the keyboard.

## Creating and storing matrices

The Matrix Catalog contains the matrix variables $\mathrm{M0} 0$ - 9 . Once you select a matrix variable to use, you can create,

| Matrix |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| M1 1* |  |  |  | OKB |
| M22* |  |  |  | .039KB |
| M3 ${ }^{*}$ |  |  |  | 0 KB |
| M4 1* |  |  |  | OKB |
| M5 1* |  |  |  | OKB |
| EDIT | DELETE | VECT | SEND |  | edit, and delete matrices in the Matrix Editor. You may then return to the Matrix Catalog to send your matrix to another HP 39gll.

To open the Matrix catalog, press MATRIX.
In the Matrix Catalog, a matrix is listed with two dimensions, even if it has only one row. A vector is listed with the number of its elements

You can also create and store matrices-named or unnamed-in Home. For example, the command:

POLYROOT ([1, 0,-1, 0]) M1
stores the roots of the complex vector of length 3 into the M1 variable. M1 now contains the three roots of

$$
x^{3}-x=0
$$

$\begin{array}{ll}\text { Matrix Catalog } & \begin{array}{l}\text { The table below lists the operations of keys in the Matrix } \\ \text { Catalog. }\end{array}\end{array}$

| Key | Meaning |
| :--- | :--- |
| EEDII | Opens the highlighted matrix for <br> editing. |
| or clear | Clears the selected matrix of all <br> data <br> Changes the selected matrix into <br> a one-dimensional vector <br> Transmits the highlighted matrix <br> to another HP 39gll via USB. <br> Clears all matrices. <br> Moves to the end or the <br> beginning of the catalog. |

## Working with matrices

To start the Matrix Editor

Matrix Editor keys
The following table lists the matrix edit key operations.

| Key | Meaning |
| :---: | :---: |
| E00] | Copies the highlighted element to the edit line. |
| Wis | Inserts a row of zeros above, or a column of zeros to the left, of the highlighted cell. You are prompted to choose row or column. |
| WIDTHn | Toggles between showing 1, 2, 3, or 4 columns at a time in the Matrix Editor. |
| Eig | Switches between larger and smaller font sizes. |
| 60 | A three-way toggle for cursor advancement in the Matrix editor. GO $\rightarrow$ advances to the right, Gol? advances downward, and Go does not advance at all. |
| coict | Deletes the highlighted cell, replacing it with a zero. |
| CLHEAR | Deletes the highlighted row, column, or the entire matrix (you are prompted to make a choice). |
|  | Moves to the first row, last row, first column, or last column respectively. |

To create a matrix in the Matrix Editor

1. Press matrix to open the Matrix Catalog. The Matrix catalog lists the 10 matrix variables, mo to m9.
2. Highlight the matrix variable name you want to use and press EDIT or ENTER . Press VECT first if you want to create a vector.
3. For each element in the matrix, type a number or an expression, and press [NNSTR.

For complex numbers, enter each number in complex form, that is, $(a, b)$, where $a$ is the real part and $b$ is the imaginary part. You can also enter them in the form, $a+b i$.
4. Upon entry, the highlight moves to the next column in the same row by default. Use the cursor keys to move to a different row or column. You can change the direction of the highlight bar by pressing 60 . The 60 menu key toggles between the following options:

- Gol specifies that the cursor moves to the cell

- $60 \rightarrow$ specifies that the cursor moves to the cell to the right of the current cell when you press [NTSRR
- 60 specifies that the cursor stays in the current cell when you press ( $\operatorname{NiNTR}$.

5. When done, press matrix to see the Matrix catalog, or press $\xlongequal[\substack{\text { tome } \\ \text { moceses }}]{ }$ to return to Home. The matrix entries are automatically saved.

You can enter and operate on matrices directly in the

Home view. The matrices you work on in the Home view can be named or not.

1. Enter the vector or matrix on the edit line. Start and end the vector or matrix with square brackets (the shifted 5 and 6 keys). Start each row of a matrix with square brackets as well.
2. Separate each element and each row with a comma.

Matrices in the Home view
3. Press ${ }_{\text {ENNS }}^{\text {NNER }}$ to evaluate and display the vector or matrix. Immediately after entering the matrix, you can store it in a variable by pressing sor matrixname. The matrix variables are M0 through M9.
The left screen below shows the matrix [ [2.5, 729], [16, 2] ] being stored into M5. The screen on the right shows the vector $[66,33,11]$ being stored into M6. Note that you can enter an expression (like $5 / 2$ ) for an element of the matrix, and it will be evaluated.


To display a matrix

## To display one element

To store one element

In Home, enter the name of the matrix variable and


In Home, enter matrixname (row, column). For example, if M 2 is $[[3,4],[5,6]]$, then $\mathrm{M} 2(1,2)$ ) ${ }^{\text {ENSTRR }}$ returns 4 .

In Home, enter value STOM matrixname (row, column). For example, to change the element in the first row and second column of M5 to 728, then display the resulting matrix:


An attempt to store an element to a row or column beyond the size of the matrix results in re-sizing the matrix to allow the storage. Any intermediate cells will be filled with zeroes.

To transmit a matrix

You can send matrices between calculators just as you can send apps, programs, lists, and notes.

1. Connect the two HP 39gll calculators with the microUSB cable provided with the calculators and turn both calculators on.
2. Open the Matrix catalog on the sending calculator.
3. Highlight the matrix or vector to send.
4. Press $\operatorname{SEND}$
5. The transfer will occur immediately.
6. Open the List Catalog on the receiving calculator to see the new list.

## Matrix arithmetic

You can use the arithmetic functions (,,$+- \times, /$ and powers) with matrix arguments. Division left-multiplies by the inverse of the divisor. You can enter the matrices themselves or enter the names of stored matrix variables. The matrices can be real or complex.
For the next examples, store $[[1,2],[3,4]]$ into $M 1$ and [[5,6],[7,8]] into M2.

## Example

1. Create the first matrix.

2. Create the second matrix.


3. Add the matrices that you created.



To multiply two
matrices

For division by a scalar, enter the matrix first, then the operator, then the scalar. For multiplication, the order of the operands does not matter.
The matrix and the scalar can be real or complex. For example, to divide the result of the previous example by 2 , press the following keys:

$$
x_{x^{1} \div{ }_{N}} 2 \underset{\text { ENSTER }}{\text { ENTE }}
$$



To multiply the two matrices M1 and M2 that you created for the previous example, press the following keys:
 first, then the vector. The number of elements in the vector must equal the number of columns in the matrix.

To raise a matrix to a power

You can raise a matrix to any power as long as the power is an integer. The following example shows the result of raising matrix $\mathrm{M1}$, created earlier, to the power of 5 .


Note: you can also raise a matrix to a power without first storing it as a variable.

Matrices can be raised to negative powers. In this case, the result is equivalent to $1 /\left[\right.$ matrix] ${ }^{\wedge} A B S$ (power). In the following example, $\mathrm{M1}$ is raised to the power of -2 .


To divide by a square matrix

## To invert a matrix

To negate each element

For division of a matrix or a vector by a square matrix, the number of rows of the dividend (or the number of elements, if it is a vector) must equal the number of rows in the divisor.

This operation is not a mathematical division: it is a leftmultiplication by the inverse of the divisor. $\mathrm{M} 1 / \mathrm{M} 2$ is equivalent to $\mathrm{M}^{-1}$ * M 1 .
To divide the two matrices M1 and M2 that you created for the previous example, press the following keys:


You can invert a square matrix in Home by typing the matrix (or its variable name) and pressing shiri $x^{-1}{ }_{\text {ENTSR }}^{\text {Niter }}$. Or you can use the matrix INVERSE command ( -1 ) from the Matrix category of the Math menu.

You can change the sign of each element in a matrix by pressing Aass ${ }^{(-)}$; before the matrix name.

## Solving systems of linear equations

Solve the following linear system:

$$
\begin{array}{r}
2 x+3 y+4 z=5 \\
x+y-z=7 \\
4 x-y+2 z=1
\end{array}
$$

1. Open the Matrix catalog and create a vector.


## OK VECT EDIT

2. Create the vector of the constants in the linear system.
$5 \underbrace{\text { ENTER }}_{\text {ANS }} 7 \underset{\text { ANS }}{\text { ENTER }}$


1 ENTER ANS
3. Return to the Matrix Catalog.

| Matrix |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| M13 |  |  |  | .016KB |
| M2 ${ }^{*} 1$ |  |  |  | OKB |
| M31*1 |  |  |  | OKB |
| M4 1*1 |  |  |  | OKB |
| M5 2*2 |  |  |  | . 023 KB . |
| EDIT | DELETE | VECT* | SEND |  |

In this example, the vector you created is listed as M1.
4. Create a new matrix.

5. Enter the equation coefficients.

$4 \underset{\substack{\text { ENNS } \\ \text { ENS }}}{\text { ET (4) (4) }}$
1 ENNTER 1 ENSTER

${ }_{A B S}^{(-)} ; 1$ ENTER
$4 \stackrel{\text { EnNTE }}{\text { ANS }}$


In this example, the matrix you created is listed as M2.
6. Return to Home and enter the calculation to left-multiply the constants vector by the inverse of the coefficients matrix.


The result is a vector of the solutions $x=2, y=3$ and $z=$ -2 .

An alternative method, is to use the RREF function.

## Matrix functions and commands

## About functions

## About commands

- Functions can be used in any app or in Home. They are listed in the Math menu under the Matrix category. They can be used in mathematical expressions - primarily in Home-as well as in programs.
- Functions always produce and display a result. They do not change any stored variables, such as a matrix variable.
- Functions have arguments that are enclosed in parentheses and separated by commas; for example, CROSS(vectorl, vector2 ). The matrix input can be either a matrix variable name (such as M1) or the actual matrix data inside brackets. For example, CROSS (M1, [1,2]).

Matrix commands are listed in the CMDS menu CMDS ), in the matrix category.

See the chapter titled Programming for more information on matrix commands.

Functions differ from commands in that a function can be used in an expression. Commands cannot be used in an expression.

## Argument conventions

- For row\# or column\#, supply the number of the row (counting from the top, starting with 1) or the number of the column (counting from the left, starting with 1 ).
- The argument matrix can refer to either a vector or a matrix.


## Matrix functions

COLNORM
Column Norm. Finds the maximum value (over all columns) of the sums of the absolute values of all elements in a column.

COLNORM(matrix)
COND
Condition Number. Finds the 1-norm (column norm) of a square matrix.

COND (matrix)
Cross Product of vector 1 with vector2.
CROSS(vectorl, vector2)
Determinant of a square matrix.
DET(matrix)
Dot Product of two arrays, matrix 1 and matrix2.
DOT(matrix 1, matrix2)
EIGENVAL

EIGENVV
Eigenvectors and Eigenvalues for a square matrix. Displays a list of two arrays. The first contains the eigenvectors and the second contains the eigenvalues.

> EIGENVV(matrix)

IDENMAT
Identity matrix. Creates a square matrix of dimension size $\times$ size whose diagonal elements are 1 and offdiagonal elements are zero.

IDENMAT(size)

| INVERSE | Inverts a square matrix (real or complex). |
| :---: | :---: |
|  | INVERSE (matrix) |
| LQ | LQ Factorization. Factors an $m \times n$ matrix into three matrices: <br> \{[[ $m \times n$ lowertrapezoidal]],[[ $n \times n$ orthogonal]], [[ $m \times m$ permutation]]\}. |
|  | LQ (matrix) |
| LSQ | Least Squares. Displays the minimum norm least squares matrix (or vector). |
|  | LSQ(matrix 1, matrix2) |
| LU | LU Decomposition. Factors a square matrix into three matrices: <br> \{[[lowertriangular]],[[uppertriangular]],[[permutation]]\} The uppertriangular has ones on its diagonal. |
|  | LU(matrix) |
| MAKEMAT | Make Matrix. Creates a matrix of dimension rows $\times$ columns, using expression to calculate each element. If expression contains the variables I and J, then the calculation for each element substitutes the current row number for I and the current column number for J. <br> MAKEMAT (expression, rows, columns) |
|  | Example |
|  | MAKEMAT $(0,3,3)$ returns a $3 \times 3$ zero matrix, $[[0,0,0],[0,0,0],[0,0,0]]$. |
| QR | QR Factorization. Factors an $m \times n$ matrix into three matrices: $\{[[m \times m$ orthogonal $]],[[m \times n$ uppertrapezoidal]],[[ $n \times n$ permutation]]\}\}. |
|  | QR(matrix) |
| RANK | Rank of a rectangular matrix. |
|  | RANK(matrix) |
| ROWNORM | Row Norm. Finds the maximum value (over all rows) for the sums of the absolute values of all elements in a row. <br> ROWNORM (matrix) |

```
ROWNORM (matrix)
```

RREF

SCHUR

SIZE

SPECNORM

SPECRAD

SVD

SVL

TRACE

Reduced-Row Echelon Form. Changes a rectangular matrix to its reduced row-echelon form.

```
RREF(matrix)
```

Schur Decomposition. Factors a square matrix into two matrices. If matrix is real, then the result is \{[[orthogonal]],[[upper-quasi triangular]]\}. If matrix is complex, then the result is \{[[unitary]],[[upper-triangular]]\}.

SCHUR(matrix)
Dimensions of matrix. Returned as a list: \{rows,columns\}.
SIZE(matrix)
Spectral Norm of matrix.
SPECNORM(matrix)
Spectral Radius of a square matrix.
SPECRAD(matrix)
Singular Value Decomposition. Factors an $m \times n$ matrix into two matrices and a vector:
$\{[[m \times m$ square orthogonal $]],[[n \times n$ square orthogonal $]]$, [real]\}.

```
SVD(matrix)
```

Singular Values. Returns a vector containing the singular values of matrix.

## SVL(matrix)

Finds the trace of a square matrix. The trace is equal to the sum of the diagonal elements. (It is also equal to the sum of the eigenvalues.)

## TRACE (matrix)

TRN

Transposes matrix. For a complex matrix, TRN finds the conjugate transpose.
TRN(matrix)

## Examples

Identity Matrix

Transposing a Matrix

You can create an identity matrix with the IDENMAT function. For example, IDENMAT(2) creates the $2 \times 2$ identity matrix $[[1,0],[0,1]]$.

You can also create an identity matrix using the MAKEMAT (make matrix) function. For example, entering MАКЕМАТ $(l \neq J, 4,4)$ creates a $4 \times 4$ matrix showing the numeral 1 for all elements except zeros on the diagonal. The logical operator $(\neq)$ returns 0 when I (the row number) and $J$ (the column number) are equal, and returns 1 when they are not equal.

The TRN function swaps the row-column and column-row elements of a matrix. For instance, element 1,2 (row 1, column 2 ) is swapped with element 2,1 ; element 2,3 is swapped with element 3,2 ; and so on.

For example, $\operatorname{TRN}([[1,2],[3,4]$ ) creates the matrix [ $[1,3],[2,4]]$.

Reduced-Row Echelon Form

The following set of equations $x-2 y+3 z=14$

$$
2 x+y-z=-3
$$

$$
4 x-2 y+2 z=14
$$

can be written as the augmented matrix

$$
\left[\begin{array}{ccc|c}
1 & -2 & 3 & 14 \\
2 & 1 & -1 & -3 \\
4 & -2 & 2 & 14
\end{array}\right]
$$

which can then be stored as a $3 \times 4$ real matrix in any matrix variable. Ml is used in this example.


You can use the RREF function to change this to reduced row echelon form, storing it in any matrix variable. $M 2$ is used in this
 example.

The reduced row echelon matrix gives the solution to the linear equation in the fourth column.


An advantage of using the RREF function is that it will also work with inconsistent matrices resulting from systems of equations which have no solution or infinite solutions.

For example, the following set of equations has an infinite number of solutions:
$x+y-z=5$
$2 x-y=7$
$x-2 y+z=2$
The final row of zeros in the reduced-row echelon form of the augmented matrix indicates an inconsistent system with infinite
 solutions.

## Notes and Info

The HP 39gll has text editors for entering notes. There are two text editors:

- The Notes Editor runs from within the Notes Catalog, a collection of notes independent of apps. These notes can be sent to another calculator from the Note Catalog.
- The Info Editor runs from the Info view of an app. A note created in the Info view is associated with the app. When you save the app or send it to another calculator, this note is saved or sent as well.


## The Notes Catalog

Subject to available memory, you can store as many notes as you want in the Note Catalog. These notes are independent of any app. The Note Catalog lists the existing entries by name. The list does not include notes that were created in any apps' Info view, but these can be copied and pasted using the clipboard. From the Note Catalog, you create or edit individual notes in the Note Editor.

To create a note in the Note Editor

1. Open the Note Catalog.

Shlic
NOTES

2. Create a new note.

| New Note |  |  |  |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
| Name: |  |  |  |
|  |  |  |  |
| Enter name for new note |  |  |  |
| EDIT |  |  |  |

3. Enter a name for your note.


4. Write your note, using the note editing keys and formatting options shown in the following sections.


While you are in the Note Catalog, you can use the following keys.

## Notes Catalog keys

| Key | Meaning |
| :--- | :--- |
| EEDIT | Opens the selected note for <br> editing. <br> Begins a new note, and asks <br> for a name. <br> Transmits the selected note to <br> another HP 39gll or PC. |
| CELETE or Clear | Deletes the selected note. |
| SHHITI CLEAR | Deletes all notes in the <br> catalog. |

To create a note in the Info view

1. In an app, press Info for the Info view and EDII to start your note.
2. Use the note editing keys and formatting options. These are identical to those found in the Note Editor (see previous section). Your work is automatically saved. To exit Info view, press any view key or | $\begin{array}{l}\text { Home } \\ \text { Modes }\end{array}$ |
| :---: |

While you are in the Note or Info Editors, you can use the following keys:

| Key | Meaning |
| :---: | :---: |
| ERMAT | Opens the text formatting menu. See Formatting options later in this chapter. |
| SPACE | Space key for text entry. |
| PAGE | Moves from page to page in a multi-page note. |
| EEGIN | Starts text selection. Use the arrow keys to select existing text for formatting. |
| comer | Backspaces cursor and deletes character. |
| \%NTER | Starts a new line. |
| SHIT CLEAR | Erases the entire note. |
|  | Menu for entering variable names, and contents of variables. |
| ( ${ }_{\text {cost }}^{\text {matb }}$ | Menu for entering math operations, and constants. |
| SHIIT CMDS | Menu for entering program commands. |


| Key | Meaning (Continued) |
| :--- | :--- |
| sHIIT CHARS | Displays special characters. <br> To type one, highlight it and <br> press OK . To copy a <br> character without closing the <br> Chars menu, press ECHO. |

## Entering alphanumeric characters

While in the Note or Info editors, you will want to enter upper-case and lower-case alphabetical characters. The table below describes the various options available for entering these characters.

| Purpose | Keystroke |
| :--- | :--- |
| Upper-case <br> alpha shift (one <br> character) | ALIPHA |
| Upper-case <br> alpha lock | ALIPHA AIPHA |
| Lower-case <br> alpha shift |  |
| Lower-case <br> alpha lock |  |

To release upper-case or lower-case alpha lock, just press arman one more time. While in an alpha lock, you can switch cases for one keystroke by pressing ; to switch cases and lock, press stliri glata .

Text formatting

You can format text in any Note or Info. To format existing text, follow these steps:

1. Open the Note or Info view.
2. Move the cursor to the beginning of the text you wish to format.
3. Press EEGN .
4. Move the cursor to the end of the text you wish to format.
5. Press fremat to open the Format menu.

The Format menu is a two-column menu. The left column contains a list of categories and the right column lists the formatting options within each category. Select a category on the left and then a formatting option on the right.
6. Use $\odot$ and $\odot$ to select the formatting category. Use (1) to switch to the right column and then use $($ and
$\odot$ again to select the formatting option you wish to apply to the selected text.
7. Press OK to apply or canclal to cancel.

## Formatting Options

The formatting options are listed in the table below.

| Category | Options |
| :---: | :---: |
| Align | - Left |
| Text alignment | - Center |
|  | - Right |
| Font | - Small |
| Font size | - Large |
| FG Color | - Black |
| Foreground color | - Dark Gray |
|  | - Light Gray |
|  | - White |
| BG Color Background color | - Black |
|  | - Dark Gray |
|  | - Light Gray |
|  | - White |


| Category | Options |
| :---: | :---: |
| Bullets | - Level 1 <br> - Level 2 <br> - Level 3 |
| Style <br> Font style | - Underline <br> - Strikethrough <br> - Superscript <br> - Subscript <br> - Normal |

To import a note
You can import a note from the Note Catalog into an app's Info view and vice versa.
Suppose you want to copy a note named Assignments from the Note Catalog into the Function Info view:

1. Open the note Assignment.
$\square$ NOTES
2. Move the cursor to the beginning of the text you wish to copy and begin text selection.

## EEGIN

3. Move the cursor to the end of the text you wish to format.
4. Copy the selected text to the clipboard.
5. Open the app's Info view
$\underset{\substack{\text { Apps } \\ \text { anic }}}{\text { And }}$ Select Function
6. Move the cursor to the location where you want the copied text to be pasted and open the clipboard.
PASTE
```

\section*{To import a graphics variable}

\section*{To transmit a note}

You can copy the contents of a graphics variable into a note or the Info view of an app.
1. Open the note or the Info view of the app. Place the insert cursor where you want the graphic to appear. The graphic will be copied here.
2. Press Vars
Chars A
3. Highlight Graphic, then press \((\bullet\) and highlight the name of the variable ( GI , etc.).
4. Press VAILE to recall the contents of the graphic variable and then press OK

You can send notes between calculators just as you can send apps, programs, matrices, and lists.
1. Connect the two HP 39gll calculators with the microUSB cable provided with the calculators and turn both calculators on.
2. Open the Notes Catalog on the sending calculator.
3. Highlight the name of the note to send.
4. Press SEND
5. The transfer will occur immediately.
6. Open the Notes Catalog on the receiving calculator to see the new list.

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\section*{Variables and memory management}

\section*{Introduction}

The HP 39 gll has approximately 250 Kb of user memory, as well as 80 Mb of flash memory. You use the calculator's memory to store the following objects:
- copies of apps with specific configurations
- new apps that you download
- home variables
- app variables
- user-defined variables
- variables created through a catalog or editor, for example a matrix or a text note
- programs that you create.

A variable is an object that you create in memory to hold data. The HP39gll has three types of variables: Home variables, App variables, and User variables.
- Home variables are available in all apps. For example, you can store real numbers in variables \(A\) to \(Z\) and complex numbers in variables zo to \(\mathrm{Z9}\). These can be numbers you have entered, or the results of calculations. These variables are available within all apps and within any programs.
- App variables apply only to a single app. Apps have specific variables allocated to them which vary from app to app.
- User variables are added to the Vars menu via programs. These variables can be either local to the program or global. See Programming for more details.

You can use the Memory Manager ( SHIIT MEMORY) to view the amount of memory available. The catalog views, which are accessible via the Memory Manager, can be used to transfer variables such as lists or matrices between calculators.

\section*{Storing and recalling variables}

You can store numbers or expressions from a previous input or result into variables.

Numeric Precision

To store a value

To store the results of a calculation
1. In the Home view, enter
a value, expression or
object, followed by the
1. In the Home view, enter
a value, expression or
object, followed by the
1. In the Home view, enter
a value, expression or
object, followed by the Store command.


5 sTo
2. Enter a name for the
variable suitable for the
2. Enter a name for the
variable suitable for the object.


A number stored in a variable is always stored as a 12 digit mantissa with a 3 -digit exponent. Numeric precision in the display, however, depends on the display mode (Standard, Fixed, Scientific, or Engineering). A displayed number has only the precision that is displayed. If you copy it from the Home view display history, you obtain only the precision displayed, not the full internal precision. On the other hand, the variable Ans always contains the most recent result to full precision.

If the value you want to store is the last result just calculated, then just press STO \(\boldsymbol{1}\), followed by the variable name and press \(\mathbb{\text { CNNTER}}\). If the value you want to store is further up in the Home view display history, then use to highlight the value, CCOPV to copy it to the command line, and then proceed to store it.

The following example illustrates the procedure.
1. Perform the calculation for the result you want to store.

\begin{tabular}{|c|c|c|}
\hline ERID & Function & \\
\hline \multicolumn{2}{|l|}{\multirow[t]{2}{*}{\(3^{*}\left(8^{*} 6\right)^{\wedge} 3\)}} & \\
\hline & & 331776 \\
\hline STO - & & \\
\hline
\end{tabular}
2. Highlight the result you wish to store
3. Copy the result to the edit line
```

COPY

```
4. Store the result


The results of a calculation can also be stored directly to a variable. For example:


To recall a value
To recall a variable's value, type the name of the variable and press \(\frac{\text { ENTER }}{}\).
\begin{tabular}{|l|l|l|}
\hline EARD & & Function \\
\\
& & \\
\hline A & & \\
\hline & & \\
\hline STO & & \\
\hline
\end{tabular}

To use variables in calculations

You can use variables in calculations. The calculator substitutes the variable's value in the calculation: \(65 \Sigma^{+} \quad\) ALPHA \(A\) ENTER
\begin{tabular}{|l|l|l|}
\hline RFRD & Function & \\
\hline \(65+\mathrm{A}\) & & \\
\hline
\end{tabular}

\section*{The Vars menu}

You use the Vars menu to access all variables in the calculator. There are menu keys for Home, App, and User variables. When you press chas \(\begin{gathered}\text { vars }\end{gathered}\), the Vars menu opens with the Home variables menu open by default. The Vars menu is organised by category. For each variable category in the left column, there is a list of variables in the right column. You select a category and then select a variable in the category.
1. Open the Vars menu and press Howe

2. Use the cursor keys or press the number of the category (1-5) to select a variable category. In the figure to the right,
 the Matrix category has been selected.
3. Move the highlight to the variables column.

4. Use the cursor keys to select the variable that you want. For example, to select \(M 2\), press \(\vartheta\).

5. Choose whether to place the variable name or the variable contents on the command line.
- Press VAIUEI to indicate that you want the variable's contents to appear on the command line.
- Press ok to indicate that you want the variable's name to appear on the command line.
6. Press \(O K\) to place the contents or name on the command line. The selected object appears on the command line.


Note: the Vars menu can also be used to enter the names or values of variables into programs.

\section*{Example}

This example demonstrates how to use the Vars menu to add the contents of two list variables, and to store the result in another list variable.
1. Display the List Catalog.

2. Enter the data for L1.
88 OK 90 OK

89 OK 65 OK
70 OK


Note: you can press [EG•• for the smaller font. Press
to scroll up and view the data you entered.
3. Return to the List Catalog to create L2.

SHIFT
LIST
\(\odot\) to select L2
EDIT

4. Enter data for L2.

\begin{tabular}{|l|l|l|l|}
\hline & & L2 & \\
\hline 1 & 55 & & \\
2 & 48 & & \\
3 & 86 & & \\
4 & 90 & & \\
\hline 55 & & & \\
\hline EDIT & INS & DELETE & \\
\hline
\end{tabular}
5. Press \(\begin{aligned} & \text { Home } \\ & \text { Modes } \\ & \text { to access Home. }\end{aligned}\)
6. Open the variable menu and select L1.

7. Copy it to the command line.

\section*{OK}

8. Insert the + operator and select the L2 variable from the List variables.


9. Store the answer in the List catalog L3 variable.


\section*{Home variables}

The following table lists the categories of Home variables and the available variable names in each category.

It is not possible to store data of one type in a variable of another type. For example, you use the Matrix catalog to create matrices. You can create up to ten matrices, and you can store these in variables mo to m9. You cannot store matrices in variables other than M0 to M9.
\begin{tabular}{|c|c|}
\hline Category & Available names \\
\hline \multirow[t]{3}{*}{Complex numbers} & Z0 to Z9 \\
\hline & To store a complex number, enter it in the form \(a+b^{*} i\). \\
\hline & For example, \(2+3 * 1\) siov Z . \\
\hline \multirow[t]{2}{*}{Lists} & LO to L9 \\
\hline & For example, \(\{1,2,3\}\) sro \(=\) L1. \\
\hline \multirow[t]{3}{*}{Matrices} & M0 to M9 \\
\hline & Store matrices and vectors in these variables. See the chapter Matrices for more information on matrices and vectors. \\
\hline & For example, [[1,2],[3,4]] STO*M1. \\
\hline Mode settings & Modes variables store the modes settings in \(\square\) MODES. \\
\hline Programs & Program variables store programs. \\
\hline \multirow[t]{2}{*}{Real numbers} & \(A\) to \(Z\) and \(\theta\) \\
\hline & For example, 7.45 srovA. \\
\hline
\end{tabular}

\section*{App variables}

To access an app variable

Most app variables store values that are unique to a particular app. These include symbolic expressions and equations, settings for the Plot and Numeric views, and the results of some calculations such as roots and intersections.
See Reference Information for a complete listing of app variables and Programming for more information about using app variables in programs.
1. Open the app that contains the variable you want.

2. Go to where you want to paste the variable.

\section*{Home}

Modes
3. Open the Vars menu and switch to the App Vars menu.
```

Views
Help

```

AfP (to select App Vars)
4. Use the cursor keys to select the view and then the variable you want.

5. To copy the variable name to the edit line, press OK ; to copy the variable contents,

press VALIEE and OK

You can qualify the name of any app variable so that it can be accessed from anywhere on the HP 39gll. For example, both the Function app and the Parametric app have an app variable named \(X_{\text {min }}\). If you are in the Parametric app and enter Xmin in the Home view, you
will see the value of \(X_{\text {min }}\) from the Parametric app. To access the value of Xmin in the Function app, you must either start the Function app (as above) or qualify the name by entering Function::Xmin. For more information on qualifying variable names, see the chapter Programming.

User variables
The HP 39gll supports both user-defined functions and user-defined variables. Both of these object types can be local (within an app or a program) or global (visible and accessible anywhere on the calculator). For more information about creating and using user-defined variables and functions (as well as declaring them local or global), see the chapter Programming.

\section*{Memory Manager}

Use the Memory Manager to view the amount of available memory and organize it. If the available memory is low, use the Memory Manager to determine which variables you might delete to free up memory. You can also use the Memory manager to send sets of variables to another HP 39gll or to clone your entire memory to another HP 39gll.

Start the Memory Manager by pressing MEMORY. When the Memory Manager is open the keys listed in the table on the following page are available to you:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline CIONE & \begin{tabular}{l} 
Replace the memory of a \\
connected HP 39gll with the \\
current memory of the \\
cloning 39gll.
\end{tabular} \\
SEND & \begin{tabular}{l} 
Sends all variables of the \\
selected type (lists, matrices, \\
etc.) to another HP 39gll.
\end{tabular} \\
Opens the catalog or library \\
of the selected variable type.
\end{tabular}
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline Clear & \begin{tabular}{l} 
Deletes the contents of all \\
variables of the selected \\
type. \\
Deletes all memory.
\end{tabular} \\
\hline
\end{tabular}

\section*{Example}
1. Start the Memory Manager. A list of variable categories is displayed.
\begin{tabular}{|l|r|r||}
\hline & Memory Manager & 251KD \\
\hline Apps & & 4.3 KB \\
\hline Programs & & 0 KB \\
Notes & & 0 KB \\
Matrices & & 0 KB \\
Lists & & .12 KB \\
\hline & & \\
\hline & & \\
\hline
\end{tabular}

SHIFT
MEMORY

Free memory is displayed in the top right corner and the body of the screen lists each category of variable and the total memory used by the variables of that type.
2. Select a category and press VEW. Memory Manager opens the selected catalog or library so you can edit, delete, or clear variables of a selected type. To delete variables in a category:
- Press clear to delete the selected variable.
- Press SHIIT CLEAR to delete all variables in the selected category.

\section*{To send all variables of a single type}

You can send all the variables of a single type (all lists, matrices, programs, notes, etc.) from your HP 39 gll to another HP 39 gll or a PC. To send variables of a single type between two HP 39gll calculators:
1. Connect the two HP 39gll calculators with the microUSB cable provided with the calculators and turn both calculators on.
2. Open the Memory Manager on the sending calculator.
3. Use \(\odot\) and \(\Theta\) to highlight the variable type to send.
4. Press SEND
5. The transfer will occur immediately.
6. Open the Memory Manager on the receiving calculator to see the new variables.

You can clone the entire memory of your HP 39gll to another HP 39gll calculator, effectively copying your HP 39 gll to another HP 39 gll . This is helpful if you want to backup your calculator's memory, or in settings where calculators in a classroom or in a group require similar configuration. To clone your HP 39gll:
1. Connect the two HP 39gll calculators with the microUSB cable provided with the calculators and turn both calculators on.
2. Open the Memory Manager on the sending calculator.
3. Press CIONE
4. You will see the transfer annunciator flash briefly.
5. The cloned HP 39gll is now ready for use.

\section*{Programming}

\section*{Introduction}

This chapter describes how to program the HP 39gll. In this chapter you'll learn about:
- programming commands
- writing functions in programs
- using variables in programs
- executing programs
- debugging programs
- creating programs for building custom apps
- sending a program to another HP39gll

\section*{HP 39gll \\ Programs}

Command Structure

An HP 39gll program contains a sequence of commands that execute automatically to perform a task.

Commands are separated by a semicolon ( ; ).
Commands that take multiple arguments have those arguments enclosed in parentheses and separated by a comma(, ). For example,

PIXON (xposition, yposition);
Sometimes, arguments to a command are optional. If an argument is omitted, a default value is used in its place. In the case of the PIXON command, a third argument could be used that specifies the color of the pixel:

PIXON (xposition, yposition [ , color]);
The last argument indicates which of four colors to use when lighting up the pixel. Here, the default value is 0 (black). In this manual, optional arguments to commands appear inside square brackets, as shown above. In the PIXON example, a graphic variable (G) could be
specified as the first argument. The default is G0, which always contains the currently displayed screen. Thus, the full syntax for the PIXON command is:

PIXON([G,] xposition, yposition [ ,color]);
Some built-in commands employ an alternate syntax, whereby function arguments do not appears in parentheses. Examples include RETURN and RANDOM.

\section*{Program Structure}

Programs can contain any number of subroutines (each of which is a function or procedure). Subroutines start with a heading consisting of the name, followed by parentheses that contain a list of parameters or arguments, separated by commas. The body of a subroutine is a sequence of statements enclosed within a BEGIN END; pair. For example, the body of a simple program, called MYPROGRAM, could look like this:

EXPORT MYPROGAM ()

BEGIN
PIXON(1,1);
END;

\section*{Comments}

When a line of a program begins with two slashes, //, the rest of the line will be ignored. This allows the programmer to insert comments in the program:

EXPORT MYPROGAM()
BEGIN
PIXON (1,1);
//This line is just a comment.
END;

\section*{The Program Catalog}

The Program catalog is where you name, delete, send, or run programs. This is also where you start the Program Editor, where you create and edit programs. Programs can also be run from the Home view or other programs.

\author{
Open the \\ Program \\ Catalog
}

Press \(\begin{aligned} & \text { shrir } \\ & \text { the Program Catalog. } \\ & \text { The Program Catalog } \\ & \text { displays a list of program } \\ & \text { names. The first item in the }\end{aligned}\).
\begin{tabular}{|c|c|c|c|}
\hline \multicolumn{4}{|c|}{Program Catalog} \\
\hline \multicolumn{2}{|l|}{Function} & & .014KB \\
\hline EDIT & NEW & SEND & \\
\hline
\end{tabular}

Program Catalog is a built-in entry that has the same name as the active app. This entry is the app program for the active app, if such a program exists. See the section on App Programming.
Before starting to work with programs, you should take a few minutes to become familiar with the Program Catalog menu keys. You can use any of the following keys (both menu and keyboard) to perform tasks in the Program Catalog.

\section*{Program catalog keys}

The program catalog keys are:
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline EEDIT & \begin{tabular}{l} 
Opens the highlighted \\
program for editing. \\
Prompts for a new \\
program name, then \\
opens an empty \\
program. Not displayed \\
if the app program is \\
selected
\end{tabular} \\
SENDD & \begin{tabular}{l} 
Transmits the highlighted \\
program to another HP \\
\(39 g l l\) \\
RU to a PC.
\end{tabular} \\
Runs the highlighted \\
program.
\end{tabular}
\begin{tabular}{|l|l|}
\hline Key & Meaning \\
\hline or & \begin{tabular}{l} 
Moves to the beginning \\
or end of the Program \\
catalog.
\end{tabular} \\
Deletes the highlighted \\
program. \\
Deletes all programs.
\end{tabular}

\section*{Creating a New Home Program}
1. Open the Program catalog and start a new program.


NEW'
2. The HP 39gll prompts you for a name.


\section*{OK OK}

A template for your program is automatically created. The template consists of a heading for a
function with the same name as the program, EXPORT MYPROGRAM (), and a BEGIN. . .END pair that blocks off the statements for the function.

HIN T A program name can contain only alphanumeric characters (letters and numbers) and the underscore character. The first character must be a letter. For example, GOOD_NAME and Spin2 are valid program names, while нот STUFF (no space allowed) and 2 Cool ! (starts with number and no !) are not valid.

\section*{The Program Editor}

Until you become familiar with the HP 39gll commands, the easiest way to enter commands is to select them from menus.

\author{
Entering a program
}
1. Position the cursor where you want the command to go using the navigation keys.

2. Press IMPLT to open the Program Templates menu.

TMPLT


The Program Templates menu contains structures that control execution flow, such as IF THEN statements and FOR loops. Use the cursor keys to highlight a command and press OK to paste the command into the program at the cursor position.
3. Insert a FOR loop.

(1) Select FOR OK

Again, a template is inserted. Use the keyboard to fill in the missing parts of the command, then


position the cursor on
the blank line after the FOR command. In this case, complete the statement "FOR N FROM 1 TO 3 DO".
\begin{tabular}{|c|c|}
\hline & \\
\hline EXPORT MYPR & \\
\hline BEGIN & \\
\hline FOR N FROM & \\
\hline END; & \\
\hline STO - CHECK & BEGIN \\
\hline
\end{tabular}

highlight a command category, then press to access the commands in the category. Select the command that you want and press OK to paste the command into the program. You can also use keyboard shortcuts indicated in the menu title bar in the Program Commands menu to quickly select a command.
4. Insert the MSGBOX
(Message Box) command.


(or enter 5)
Select I/O
(1) (switch columns)
\begin{tabular}{|c|c|c|}
\hline \multicolumn{3}{|l|}{\begin{tabular}{l}
MYPROGRAM \\
EXPORT MYPROGRAM() BEGIN \\
FOR N FROM 1 TO 3 DO MSGBOXI END;
\end{tabular}} \\
\hline STO - CHECK & TMPLT & BEGIN \\
\hline
\end{tabular}
(or enter 6)
Select MSGBX
5. Fill in the arguments to the MSGBOX command, and type a semicolon at the end of the command.


HIN T Use the Characters menu to enter the quote, ("). Press CHARS, highlight the quote character, and press ENTER ANS

HIN T For lower-case alpha lock, press:

When you are done, press PRGM to return to the Program Catalog or \(\xlongequal[\substack{\text { Home } \\ \text { Nomes }}]{ }\) to go to the Home view. You can also press any of the app-control keys to enter the current app's views. You are ready now to execute the program.

\section*{Run a Program}

From Home, type the name of the program, with open and closing parentheses after it. If the program takes any arguments, insert these in the parentheses, separated by commas. Press

From the Program Catalog, highlight the program you want to run and press RIN . When a program is executed from the catalog, the system looks for a function named \(\operatorname{START}()\) (no parameters). If it finds one, that function is executed. Otherwise, it looks for a function with the same name as the program. If it finds that, it executes. Otherwise, nothing happens when RLIN is pressed.
1. Run MYPROGRAM.


USER


Select MYPROGRAM
( (switch columns) Select MYPROGRAM
\(\square\) )
Paste
\(M\) ENTER

The program executes, displaying a message box.
2. Press ok three times to see the FOR loop finish.

3. After the program terminates, you can resume any other activity with the HP39gll.
Regardless of where you start the program, all programs run in Home. What you see will differ slightly depending on where you started the program. If you start the program from Home, the HP 39gll displays the contents of Ans (Home variable containing the last result), when the program has finished. If you start the program from the Program catalog using the RUN key, the HP 39gll returns you to the Program catalog when the program ends.

\section*{Debug a \\ Program}

You cannot run a program that contains syntax errors. You must first correct all the syntax errors before executing the program.

If there is an error detected at run-time, such as division by zero, the program will stop and you will see an error message. If the program does not do what you expect it to do, or if there is a run-time error detected by the system, you can execute the program step by step, and look at the values of local variables. To do that, type debug(MYPROGRAM()) on the edit line.
1. Start the debug tool for the program you just wrote.
\begin{tabular}{|l|l|l|}
\hline RARD & Function & \\
\hline \\
MYPROGRAM([]) & \\
\hline Mebug(MYPROGRAM()X & \\
\hline STO - & & \\
\hline
\end{tabular}
shira debug conf 1 EHili CMDS USER

\author{
Select MYPROGRAM
}

While debugging a program, the \(>\) indicator at the left of the screen points to the current command. The current value of each local variable is visible at the bottom of the screen. Since there are no local variables in our program, nothing is shown. While in the debugger, the menu keys perform the following actions:
- F2-Execute the next command
- F3-Step in
- F4-Continue
- F5-Stop program execution
- F6-Display Help
2. Execute the first command.
\(\square\)

The FOR loop starts and the pointer moves to Line 2.
3. Execute Line 2.


The message box appears. Note that when each message box is displayed, you still have to dismiss the message box by pressing \({ }^{\text {ENTRR}}\). Press \({ }^{2}\) and \({ }^{\text {©NN }}\) NTRR repeatedly to execute the program step-by-step.

When the next instruction to be executed is a user function or subroutine, pressing \({ }^{52}\) will execute that function or subroutine all at once, while pressing
\({ }^{53}\) will enter in the subroutine and execute it step by step (Step In).

Edit an existing program

To edit an existing program, use the Program Catalog.
1. Open the Program catalog.

SHIIT
PRGM
2. Use the arrow keys to highlight the program you want to edit, and press EEDIT. The HP 39 gll opens the Program Editor. The name of your program appears in the title bar of the display. You can use the following keys to edit your program.

\section*{Editing Keys}
\begin{tabular}{|c|c|}
\hline Keys & Meaning \\
\hline STO- & Inserts the STORE character ( \(\boldsymbol{\triangleright}\) ) at the cursor location. \\
\hline CHECK & Checks the current program for errors. \\
\hline PAGE & Displays previous page of the program. \\
\hline PAGE \({ }^{\text {I }}\) & Displays next page of the program. \\
\hline TMPLT & Displays the catalog of program commands. Select a command and press \(\underset{\text { ENSTR }}{\text { Enter }}\) to insert the command into your program. \\
\hline \(\bigcirc\) & Moves up or down one line. \\
\hline
\end{tabular}
\begin{tabular}{|c|c|}
\hline Keys & Meaning \\
\hline  & Moves up or down one page \\
\hline (1) direction keys & Moves left or right one character. \\
\hline SHITI (4) or SHIT ( & Moves to beginning or end of line \\
\hline ENTER & Starts a new line. \\
\hline clear & Deletes the character to the left of the cursor (Backspace) \\
\hline SHITP CLEAR & Erases the entire program. \\
\hline \({ }_{\text {chers }}^{\text {chars }}\) A & Displays menus for selecting variable names, contents of variables, functions names, and constants. \\
\hline \({ }_{\text {cmathem }}\) & Displays menus for selecting mathematical functions, units, and constants. \\
\hline \({ }^{\text {SHIIT }}\) CMDS & Displays menus for selecting program conmmands. \\
\hline SHIT CHARS & Displays all characters. To type one, highlight it and press OK. To enter several characters in a row, ECHO while in the Chars menu. \\
\hline
\end{tabular}

\section*{Copy a program or part of a program}

You can use the global Copy and Paste commands to copy part or all of a program. The following steps illustrate the process:
1. Press PRGM to open the Program catalog.
2. Highlight the program containing the commands you wish to copy and press EDIT.
3. Move the cursor to the beginning of the commands you wish to copy.
4. Press EEGIN.
5. Move the cursor to the end of the commands you wish to copy. The selected commands will be highlighted as you move the cursor.
6. When all the commands you want are highlighted, press COPY to copy the selected commands to the clipboard.
7. Return to the Program Catalog and open the target program.
8. Move the cursor to the line where you wish to insert the copied commands.
9. Press \(\square\) PASTE and the clipboard will open. Your commands will be first in the list and highlighted already, so just press OK. The commands will be pasted into the program, beginning at the cursor location.

Delete a To delete a program: program
1. Press shlim \(P R G M\) to open the Program catalog.
2. Highlight a program to delete, then com or DELETE .
3. Press OK

Delete all You can delete all programs at once.
programs
1. In the Program catalog, press CLHEAR
2. Press OK

\section*{Delete the contents of a program}

To transmit a program

You can clear the contents of a program without deleting the program name.
1. Press \(P R G M\) to open the Program catalog.
2. Highlight a program, then press EDIT
3. Press SHIIT CLEAR, then press OK
4. The contents of the program are deleted, but the program name remains.

You can send programs between calculators just as you can send apps, notes, matrices, and lists.
1. Connect the two HP 39gll calculators with the microUSB cable provided with the calculators and turn both calculators on.
2. Open the Program Catalog on the sending calculator.
3. Highlight the name of the program to send.
4. Press SEND
5. The transfer will occur immediately.
6. Open the Program Catalog on the receiving calculator to see the new list.

\section*{The HP 39gll Programming Language}

Variables and visibility

Variables in an HP 39gll program can be used to store numbers, lists, matrices, graphics objects, and strings. The name of a variable must be a sequence of alphanumeric characters (letters and numbers), starting with a letter. Names are case-sensitive, so the variables named MaxTemp and maxTemp would be different.

The HP39gll has built-in variables of various types, visible globally. The following table illustrates many of these,
with an example showing how to store a value into the variable:
\begin{tabular}{|c|c|c|}
\hline Type & Names & Store Example \\
\hline Real number & A-Z and \(\theta\) & 2.7 - R \\
\hline Complex numbers & Z0-Z9 & \((2,3) \bullet \mathrm{Zl}\) \\
\hline Lists & LO-L9 & \(\{1,2,3,4\}\) L1 \\
\hline & CO-C9 & \\
\hline & D0-D9 & \\
\hline Matrices & MO-M9 & \[
\begin{aligned}
& {[[1,2],[3,4],[5,6]]} \\
& \bullet M 1
\end{aligned}
\] \\
\hline Graphics & G0-G9 & See graphics section \\
\hline Functions & FO-F9 & \(\cos (\mathrm{X})\) - Fl \\
\hline
\end{tabular}

These names are reserved by the system. These (and all other) system variables are visible everywhere, and users may not use the names for other data. That is, you may not name a program L1, for example, nor store a real number into a variable named G1. A full list of system variables appears in the chapter titled, Reference Information. Besides these reserved variables, each HP app has its own reserved variables. For more information on these variables, see the section in this chapter Variables and programs.
Within a program, you can declare variables for use only within a particular function. This is done using a LOCAL declaration. The use of LOCAL variables allows the programmer to declare and use variables that will not affect the rest of the calculator. LOCAL variables declared by the programmer are not bound to a particular type. That is, you can store floating-point numbers, integers, lists, matrices, and symbolic expressions into a variable with any local name. Although the system will allow you to store different types
into the same local variable, this is poor programming practice and should be avoided.

The HP39gll system has many system variables with names that are apparently the same. For example, the Function app has a variable named Xmin, but so, too, do the Polar, Parametric, Sequence, and Solve apps. In a program, or in the Home view, you can reference different versions of these by fully "qualifying" the name of the variable. This is done by inserting the name of the app (or program) that the variable belongs to, followed by two colons, and then the actual variable name. For example, the qualified variables Function: : Xmin and Parametric: : Xmin refer to the value of Xmin within each app, and could contain different values. Similarly, if you declare a local variable inside a program, you could reference that variable using the name of the program, followed by the two colons and the variable name.

Variables declared in a program should have descriptive names. For example, a variable used to store the radius of a circle can be named RADIUS. If such a variable is needed after the program executes, it can be exported from the program using the EXPORT command. To do this, the first command in the program (located before the program heading) would be EXPORT RADIUS. Then, if a value is assigned to RADIUS, the name would appear on the Vars menu and be visible globally. This feature allows for extensive and powerful interactivity among different environments in the HP39gll. Note that if more than one program exports a variable with the same name, the most recently exported version will be active, unless the name is fully qualified.

This program prompts the user for the value of RADIUS, and exports the variable for use outside the program.
```

EXPORT RADIUS;
EXPORT GETRADIUS()
BEGIN
INPUT(RADIUS);
END;

```

The EXPORT command for the variable RADIUS must appear before the heading of the function where RADIUS is assigned. After
 you execute this program, a new variable named RADIUS appears on the USER GETRADIUS section of the Vars menu.

\section*{Functions, their arguments, and parameters}

\section*{Program ROLLDIE}

The programming environment for the HP39gll is highly structured. You can define your own functions in a program, and data can be passed to a function using parameters. Functions can return a value (using the RETURN statement) or not. When a program is executed from Home, the program will return the value returned by the last statement that was executed.

Furthermore, functions can be defined in a program and exported for use by other programs in the same way that this is done for variables. This feature makes the HP39gll an incredibly powerful programming plafform.
In this section, we will create a small set of programs, each illustrating some aspect of programming on the HP 39 gll . Each of these programs will be used as a building block for a custom app described in the next section, App Programs.
Here is a program that defines a function called ROLLDIE that simulates the rolling of a single die, returning a random integer between 1 and whatever number is passed into the function:
First, create a new program named Rolldie. Then enter the program.

EXPORT ROLLDIE(N)
BEGIN
RETURN 1 + FLOOR (N*RANDOM);
END;
The first line is the heading of the function. Execution of the RETURN statement causes a random integer from 1 to N to be calculated and returned as the result of the function. Note that execution of a RETURN command causes execution of the function to terminate.

Any statements between the end of the RETURN statement and END are ignored.

On the Home screen (or in fact, anywhere in the calculator where a number can be used), you can enter ROLLDIE ( 6 ) and a random integer between 1 and 6 , inclusive will be returned.

Another program could use the ROLLDIE function, and generate \(n\) rolls of a die with any number of sides. In the following program, the ROLLDIE function is used to generate \(n\) rolls of 2 dice, each with the number of sides given by the local variable sides. The results are stored into the list \(L 2\), so that \(L 2(1)\) shows the number of times the dies came up with a \(1, L 2(2)\) shows the frequency of 2 ' \(s\), etc. L2(1) should be 0 as a result.

\section*{Program ROLLMANY}
```

EXPORT ROLLMANY(n,sides)
BEGIN
LOCAL k,roll;
// initialize list of frequencies
MAKELIST(0,X,1,2*sides,1) L L2;
FOR k FROM 1 TO n DO
ROLLDIE(sides) + ROLLDIE(sides) roll;
L2(roll)+1- L2(roll);
END;
END;

```

This program uses a FOR loop, explained in the section on loops.

A function's visibility can be restricted to within the program where it is defined by omitting the EXPORT command when the function is declared. For example, you could define the Rolldie function inside the ROLLMANY program like this:

EXPORT ROLLMANY(n,sides)
BEGIN
LOCAL k,roll;
// initialize list of frequencies

MAKELIST (0, X, 1, 2*sides,1) L2;
FOR k FROM 1 TO n DO
ROLLDIE (sides) +ROLLDIE (sides) roll; L2 (roll) +1 L2 (roll);

END;
END;
ROLLDIE ( n )
BEGIN
RETURN 1 + FLOOR (n*RANDOM) ;
END;
In this scenario, assume there is no ROLLDIE function exported from another program. Instead, ROLLDIE is visible only in the context of ROLLMANY.

Finally, the list of results could be returned as the result of calling ROLLMANY instead of being stored directly into the global list variable, L2. This way, if the user wanted to store the results elsewhere, it could be done easily.

EXPORT ROLLMANY(n,sides)
BEGIN
LOCAL k,roll,results;
MAKELIST (0, X, 1, 2*sides, 1) results;
FOR k FROM 1 TO n DO
ROLLDIE (sides) +ROLLDIE (sides) roll;
results (roll) +1 results (roll);
END;
RETURN results;
END;
On the Home screen, you would enter \(\operatorname{ROLLMANY}(100,6)\) L5 and the results of the simulation of 100 rolls of two six-sided dice would be stored into list L5.

\section*{App programs}

Apps are a unified collection of views, programs, notes, and associated data. Creating an app program allows you to redefine the app's views and how a user will interact with those views. This is done through two mechanisms: dedicated program functions with special names and redefining the views in the Views menu.

Using dedicated program functions

There is a set of special program names which run the named programs if they exist. These programs are run on the keyboard events shown in the table below. These program functions are designed to be used in the context of an app.
\begin{tabular}{|c|c|c|}
\hline Program & Name & Keystrokes \\
\hline Symb & Symbolic view &  \\
\hline SymbSetup & \begin{tabular}{l}
Symbolic \\
Setup
\end{tabular} &  \\
\hline Plot & Plot view & Stome \\
\hline PlotSetup & Plot Setup & Estric \\
\hline Num & Numeric view & , \\
\hline NumSetup & Numeric Setup & Stire \\
\hline Info & Info view & SHIF \\
\hline START & Starts an app & START \\
\hline RESET & Resets or initializes an app & REEET \\
\hline
\end{tabular}

\section*{Redefining the Views menu}

\section*{Customizing an app}

The Views menu allows any app to define views in addition to the standard seven views shown in the table above. By default, each HP app has its own set of additional views contained in this menu. The vIEWS command allows you to redefine these views to run programs you have created for an app. The syntax for the VIEWS command is:
```

vIEWS "text"

```

By adding vIEWS "text", before the declaration of a function, you will override the list of views for the app. For example, if your app program defines 3 views "SetSides", "RollDice" and "PlotResults", when the user presses the Views key, he will see SetSides, RollDice, and PlotResults instead of the app's default view list.

When an app is active, its associated program appears as the first item in the Program Catalog. It is within this program that you put functions to create a custom app. A useful procedure for customizing an app is illustrated below:
1. Decide on the HP app that you want to customize. For example, you could customize the Function app or the Statistics 1Var app. The customized app inherits all the properties of the HP app. Go to the apps Catalog and save the customized app with a unique name.
2. Customize the new app if you need to by configuring the settings, for example by setting axes or angle measures.
3. Develop the functions to work with your customized app. When you develop the app's functions, use the app naming conventions described above.
4. Put the VIEWS command into your program to modify the app's Views menu.
5. Decide if your app will create new global variables. If such variables are appropriate, you should EXPORT them from a separate user program that is called from the Start () function in the app program, so they will not have their values lost.
6. Test the customized app and debug the associated programs.
It is possible to link more than one app via programs. For example, a program associated with the Function app
could execute a command to start the Statistics 1Var app, and a program associated with the Statistics 1Var app could return to the Function app (or launch any other app).

\section*{Example:}

The following example illustrates the process of creating a custom app. This app creates an environment to simulate the rolling of a pair of dice, each with a number of sides specified by the user. The results are tabulated, and can be viewed either in a table or graphically. The app is based on the Statistics 1Var app.
1. Save the Statistics 1 Var app with a unique name.
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline Apps
Info & select Statistics 1 Var & & & pplicatio & Librar & 251KB] \\
\hline \multirow[t]{6}{*}{SAWE} & & \multicolumn{4}{|l|}{\multirow[t]{3}{*}{\begin{tabular}{l}
Function Solve \\
Statistics 1Var
\end{tabular}}} & . 30 KB \\
\hline & & & & & & . 26 KB \\
\hline & & & & & & . 71 KB \\
\hline & & \multicolumn{4}{|l|}{Statistic's 2Var} & .88KB \\
\hline & & \multicolumn{4}{|l|}{Inference} & . 22 KB - \\
\hline & & SAVE & RESET & SORT & SEND & START \\
\hline
\end{tabular}
2. Name the app DiceSimulation and press the OK menu key.

3. Start the new app.

\section*{START}
4. Open the Program Catalog.

Each app has one program attached to it. Initially, this program is empty. You customize the app by entering functions into that program.
5. Edit the program

DiceSimulation.

Select DiceSimulation
\begin{tabular}{|c|c|c|c|c|c|}
\hline \multicolumn{6}{|c|}{Program Catalog} \\
\hline \multicolumn{3}{|l|}{DiceSimulation} & & & . 021 KB \\
\hline DRAR & & & & & .066KB \\
\hline DRBL & & & & & .070KB \\
\hline DRBC & & & & & .066KB \\
\hline GETR & LLS & & & & .072KB \\
\hline EDIT & NEW & SAVE & SEND & DELETE & \\
\hline
\end{tabular}

\section*{EDilT}

It is here that you enter functions to customize the app. At this point, you decide how you expect the user to interact with the
 app. In this case, we will create views to do the following:
- START: start the app
- SETSIDES: specify the number of sides (faces) on each die
- SETNUMROLLS: specify number of times to roll the dice
- RESET: start over

The START option will initialize the app and display a note embedded in the app containing instructions for the user. The user will also interact with the app through the Numeric view and the Plot view. These views will be activated by pressing some and some , but the functions Num and plot in our app program will actually launch those views after doing some configuration.

Recall the program to get the number of sides for a die, presented earlier in this chapter. It is expanded here, so that the possible sums of two such dice are stored in the list D1. Enter the following sub-routines into the app program for the DiceSimulation app.
```

The program
DiceSimulation
START()
BEGIN
DICESIMVARS();
// Empty data columns D1 and D2
{ } D1;
{}DD2;
SETSAMPLE(H1,D1);
SETFREQ (H1 , D2 ) ;
0 H1TYpe;
END;
VIEWS "Roll Dice",ROLLMANY()
BEGIN
LOCAL k,roll;
MAKELIST(X+1,X,1,2*SIDES-1,1)\D1;
MAKELIST(0,X,1,2*SIDES-1,1)\D2;
FOR k FROM 1 TO ROLLS DO
Roll:=ROLLDIE (SIDES) +ROLLDIES (SIDES) ;
D2 (roll-1) +1-D2(roll-1);
END;
-1\Xmin;
MAX (D1) + 1 Xmax;
O\Ymin;
MAX (D2) +1\Ymax;
STARTVIEW(1,1);
END;
VIEWS "Set Sides", SETSIDES()
BEGIN
REPEAT
INPUT(SIDES,"Die Sides", "N = ", "Enter num
sides",2);
FLOOR (SIDES)\SIDES;

```
```

IF SIDES<2 THEN
MSGBOX("Must be >= 2");
END;
UNTIL SIDES>=2;
END;
// specify num times to roll the dice.
VIEWS "Set Rolls",SETROLLS()
BEGIN
REPEAT
INPUT(ROLLS,"Num of Rolls","N = ","Enter
num rolls",10);
FLOOR (ROLLS)\ROLLS;
IF ROLLS<1 THEN
MSGBOX("You must enter a number >= 1");
END;
UNTIL ROLLS>=1;
END;
Plot()
BEGIN
-1\Xmin;
MAX (D1) +1 Xmax;
O\Mmin;
MAX(D2) +1 Ymax;
STARTVIEW (1,1);
END;
The ROLLMANY () routine is another adaptation from a program presented previously in this chapter. Since you cannot pass parameters into a program called through a selection from a custom Views menu, the exported variables SIDES and ROLLS are used in place of the parameters that were used in the previous versions.

```

The program above calls two other user programs: ROLLDIE() and DICESIMVARS(). ROLLDIE() appears earlier in this chapter. Here's dicesimvars. Store it into a new user program.

The program DICESIMVARS
```

EXPORT ROLLS,SIDES;
EXPORT DICESIMVARS()
BEGIN
10 - ROLLS;
6 SIDES;
END;

```

Press \(\sqrt[\substack{\text { Vown } \\ \text { Hope }}]{ }\) to see the custom app menu. Here you can set the number of sides of the dice, the number of rolls, and

execute a simulation.
After running a simulation, press Stor to see a histogram of your simulation results.


\section*{Program commands}

This section contains details on each of the individual commands grouped by category.

App commands

STARTAPP

STARTVIEW

These commands allow you to launch any HP app, bring up any view of the current app, and change the options in the Views menu.

Syntax: STARTAPP("name")
Starts the app with name. This will cause the app's program's START function to be run if present. The app's default view will be started. Note that the START function is always executed when the user presses START in the app library. Also works for user apps.

Example: STARTAPP("Function") launches the Function app.

Syntax: STARTVIEW(n [,draw?])
Starts the nth view of the current app. If draw? is true (non 0 ), it will force an immediate redrawing of the screen for that view.

The view numbers are as follows:
```

Symbolic:0
Plot:1
Numeric:2
Symbolic Setup:3
Plot Setup:4
Numeric Setup:5
App Info: 6
Views Menu:7
First special view(Split Screen Plot Detail):8
Second special view(Split Screen Plot Table):9
Third special view (Autoscale):10
Fourth special view (Decimal):11
Fifth special view (Integer):12
Sixth special view (Trig):13

```

The special views in parentheses refer to the Function app, and may differ for other apps. The numbers of special views for other apps correspond to their position in the Views menu for that app. The first special view is launched by STARTVIEW(6), the second with STARTVIEW(7), and so on.

Note that if \(n<0\), this allows starting global views:
```

HomeScreen:-1
Home Modes:-2
Memory Manager:-3
Apps Library:-4
Matrix Catalog:-5
List Catalog:-6
Program Catalog:-7
Notes Catalog:-8

```

VIEWS

DEBUG

Block commands

BEGIN...END

RETURN
Syntax: RETURN expression;
Returns the current value of expression.

\section*{Assignment Statements}
```

:=
Syntax: var := expression;
Syntax: expression \ var;
In each case, the expression is evaluated first, then the result stored into the variable var. 1 and := cannot be used with the graphics variables G0..G9. Instead, see the command BLIT.

```

When assigning a value to a cell in a list, vector, or matrix, use the command rather than :=. For example, the command \(73-L 1(5)\) will put the number 73 into the 5 th position of list L1. If you are entering a program using a calculator emulator running on a computer, then => can be used as a synonym for \(>\).

\section*{Branch Commands}
\begin{tabular}{|c|c|}
\hline \multirow[t]{3}{*}{IF...THEN...END} & Syntax: IF test THEN command(s) END; \\
\hline & Evaluate test. If test is true (non 0 ), execute command(s). Otherwise, nothing happens. \\
\hline & Example: \\
\hline \multirow[t]{2}{*}{IF...THEN...ELSE...END} & Syntax: IF test THEN command(s)1 ELSE command(s)2 END; \\
\hline & Evaluate test. If test is true (non 0 ), execute command(s) 1 , otherwise, execute command(s)2 \\
\hline \multirow[t]{2}{*}{IFTE} & Syntax: IFTE(test,true_xpr,false_xpr) \\
\hline & Evaluates test. If test is true (non 0 ), return true_xpr, otherwise return false_xpr \\
\hline \multirow[t]{2}{*}{IFERR...THEN...END} & IFERR commands 1 THEN commands2 [ELSE commands3] END; \\
\hline & Executes sequence of commands 1. If an error occurs during execution of commands 1 , execute sequence of commands2. Otherwise, execute sequence of commands3. \\
\hline
\end{tabular}

\section*{CASE...END}

Syntax:
CASE
```

IF test1 THEN commands1 END
IF test2 THEN commands2 END
[DEFAULT commands]

```
END;

Evaluates test1. If true, execute commands 1 and end the CASE. Otherwise, evaluate test2. If true, execute
commands2. Continue evaluating tests until a true is found. If no true test is found, execute commands \(D\), if provided.

Example:
CASE
IF \(x<0\) THEN RETURN "negative"; END
IF \(x<1\) THEN RETURN "small"; END
DEFAULT RETURN "large";
END;

\section*{Drawing Commands}

There are 10 graphic variables in the HP39gll, called GO to G9. G0 is always the current screen graphic.

G1 to G9 can be used to store temporary graphic objects (called GROBs for short) when programming applications that use graphics. Variables \(G 1\) to \(G 9\) are temporary and are cleared when the calculator turns OFF.

They are twenty-six functions that can be used to modify graphic variables. Thirteen of them work based on Cartesian coordinates using the Cartesian plane defined in the current app by the variables \(X \min , X \max , Y \min\), and \(Y\) max in the plot setup menu.

Thirteen of them work on pixel coordinates where the pixel 0,0 is the top left pixel of the GROB, and 255,126 is the bottom right. This second set of function has a _ \(P\) suffix on the function name.

PIXON and
PIXON_P
Syntax: PIXON([G], xposition, yposition [ ,color])
PIXON_P([G], xposition, yposition [, color])
Sets the color of the pixel of \(G\) with coordinates \(x, y\) to color. G can be any of the graphic variables and is optional. The default is G0, the current graphic. Color can be 0 to 3 ( \(0=\) black, \(1=\) dark gray, \(2=\) light gray, \(3=\) white) and is optional. The default is 0 .

PIXOFF and
PIXOFF_P

Syntax: PIXOFF([G], xposition, yposition)
PIXOFF_P([G], xposition, yposition)

Sets the color of the pixel of \(G\) with coordinates \(x, y\) to white. G can be any of the graphic variables and is optional. The default is GO, the current graphic

GETPIX and
GETPIX_P

Syntax: GETPIX([G], xposition, yposition)
GETPIX_P([G], xposition, yposition)

Returns the color of the pixel of \(G\) with coordinates \(x, y\). \(G\) can be any of the graphic variables and is optional. The default is GO, the current graphic.

\section*{RECT and}

RECT_P

Syntax: \(\operatorname{RECT}([G, x 1, y 1, x 2, y 2\), edgecolor, fillcolor]) RECT_P([G, x1, y1, x2, y2, edgecolor, fillcolor])
Draws a rectangle on G between points \(x 1, y 1\) and \(x 2, y 2\) using edgecolor for the perimeter and fillcolor for the inside.
\(G\) can be any of the graphic variables and is optional. The default is \(G 0\), the current graphic
\(x 7, y 7\) are optional. The default values represent the top left of the graphic.
\(x 2, y 2\) are optional. The default values represent the bottom right of the graphic.
edgecolor and fillcolor can be -1 to 3 ( \(-1=\) transparent, \(0=\) black, \(1=\) dark gray, \(2=\) light gray, \(3=\) white).
edgecolor is optional. The default is white.
fillcolor is optional. The default is edgecolor.
Note: To erase a GROB, execute RECT ( \(G\) ) . To clear the screen execute RECT ().

When optional arguments are provided in a command like RECT, with multiple optional parameters, provided arguments correspond to the leftmost parameters first. For example, in the program below, the arguments 40 and 90 in the RECT_P command correspond to \(x 1\) and \(y 1\). The argument 0 corresponds to edgecolor, since there is only the one additional argument. If there had been two additional arguments, they would have referred to \(x 2\) and \(y 2\) rather than edgecolor and fillcolor. The program produces the figure below to the right.

EXPORT BOX()
BEGIN

RECT () ;
RECT_P (40, 90, 0) ;


FREEZE;
END

The program below also uses the RECT_P command. In this case, the pair of arguments 0 and 3 correspond to \(\times 2\) and \(y 2\). The program produces the figure below to the right.

EXPORT BOX()
BEGIN
RECT() ; INVERT(GO);


RECT_P (40, 90, 0, 3);
FREEZE;

END

INVERT and
INVERT_P

Syntax: \(\operatorname{INVERT}([G, x 1, y 1, x 2, y 2])\)
INVERT_P([G, x1, y1, x2, y2])

Inverts a rectangle on \(G\) between points \(x 1, y 7\) and \(x 2, y 2\). This means that every black pixel becomes white and vice-versa. In the same way Light gray and dark gray are inverted. \(G\) can be any of the graphic variables and is optional. The default is \(G O\).
\(x 2, y 2\) are optional and if not specified will be the bottom right of the graphic.
\(x 1, y 1\) are optional and if not specified will be the top left of the graphic. If only one \(x, y\) pair is specified, it refers to the top left.

ARC and
ARC_P

Syntax; \(\operatorname{ARC}(G, x, y, r[, c, a 1, a 2])\)
ARC_P(G, x, y, r[,c, al, a2])

Draws an arc or circle on \(G\), centered on point \(x, y\), with radius \(r\) and color \(c\) starting at angle al and ending on angle \(a 2\).
\(G\) can be any of the graphic variables and is optional. The default is GO
\(r\) is given in pixels.
\(c\) is optional and if not specified black is used.
a 1 and a 2 follow the current angle mode and are optional. The default is a full circle.

LINE and
LINE_P

Syntax: \(\operatorname{LINE}(G, x 1, y 1, x 2, y 2, c)\)
LINE_P(G, x1, y1, x2, y2, c)

Draws a line of color \(c\) on \(G\) between points \(x 1, y 1\) and x2,y2.
\(G\) can be any of the graphic variables and is optional. The default is GO.
c can be 0 to 3 ( \(0=\) black, \(1=\) dark gray, \(2=\) light gray, \(3=\) white). \(c\) is optional. The default is black.

TEXTOUT and TEXTOUT_P

Syntax: TEXTOUT(text [ , G], x, y [,font, c1, width, c2]) TEXTOUT_P(fext [, G], x, y [, font, cl, width, c2])

Draws text using color clon graphic \(G\) at position \(x, y\) using font. Do not draw text more than width pixels wide and erase the background before drawing the text using color c2. G can be any of the graphic variables and is optional. The default is GO

Font can be:
0 : current font selected in mode screen, 1: small font 2 : large font. Font is optional and if not specified is the current font selected in mode screen.
cl can be 0 to 3 ( \(0=\) black, \(1=\) dark gray, \(2=\) light gray, \(3=\) white). c1 is optional. The default is black.
width is optional and if not specified, no clipping is performed.
c2 can be 0 to 3 ( \(0=\) black, \(1=\) dark gray, \(2=\) light gray, \(3=\) white). c2 is optional. If not specified the background is not erased.

Example:
This program displays the successive approximations for using the series for the arctangent(1).
```

EXPORT RUNPISERIES()
BEGIN
LOCAL sign;
2 K;4-A;
-1 sign;
RECT();
TEXTOUT_P("N=",0,0);
TEXTOUT_P("PI APPROX=",0,30);
REPEAT
A+sign*4/(2*K-1) A;
TEXTOUT_P(K
,35,0,2,0,100,3);
TEXTOUT_P(A
,90,30,2,0,100,3);
sign*-1 sign;
K+1-K;
UNTIL 0;
END;

```
N= 39252
```

N= 39252
PIAPPROX= 3.14156717583

```
```

PIAPPROX= 3.14156717583

```
```

BLIT and BLIT_P

Syntax: $\operatorname{BLIT}([\operatorname{trg} t G R B, d x 1, d y 1, d x 2, d y 2]$, srcGRB [ sx $x 1, s y 1, s x 2, s y 2, c])$
BLIT_P ([trgtGRB, dx $1, d y 1, d x 2, d y 2]$, srcGRB [ ,sx $1, s y 1, s x 2, s y 2, c])$

Copies the region of srcGRB between point $s \times 1$, sy 1 and $s \times 2$, sy2 into the region of trgtGRB between points $d x 1$, $d y 1$ and $d x 2$, dy2. Do not copy pixels from srcGRB that are color $c$.
trgtGRB can be any of the graphic variables. $\operatorname{trg}$ GRB can be any of the graphic variables and is optional. The default is GO .
srcGRB can be any of the graphic variables.
$d x 2$, dy2 are optional and if not specified will be calculated so that the destination area is the same size as the source area.
$s \times 2$, sy2 are optional and if not specified will be the bottom right of the srcGRB.
sxl, sylare optional and if not specified will be the top left of srcGRB.
$d x 1, d y 1$ are optional and if not specified will be the top left of trgtGRB.
c can be 0 to 3 ( $0=$ black, $1=$ dark gray, $2=$ light gray, $3=$ white). $c$ is optional. If not specified all pixels from G2 will be copied.

N OTE Using the same variable for trgtGRB and srcGRB can be unpredictable when the source and destination overlap.

## DIMGROB and DIMBROB_P

Syntax: $\operatorname{dimgrob}(G, w, h[, c])$ or $\operatorname{Dimgrob}\left(G\left[, l i n e \_1\right.\right.$, line_2,...,line_h])
$\operatorname{DImGRob}(G, w, h[, c])$ or DIMGROB( $G[$, line_l, line_2,...,line_h])

Sets the dimensions of $G R O B G$ to $w^{*}$ h. initializes the graphic $G$ with color $c$ or with the graphic data provided in the list. $G$ can be any graphic variable except G0. c can be 0 to 3 ( $0=$ black, $1=$ dark gray, $2=$ light gray, $3=$ white). $c$ is optional. The default is white.

If the graphic is initialized using graphic data, the list must have as many numbers as the height of the GROB. Each number, as seen in base 16 describes a line. Two bits are used for each pixel ( $00=$ black, $01=$ dark gray, $10=$ light gray, $11=$ white). Hence, each hex digit describes two pixels.

You can enter hexadecimal number using the 0xdigits syntax.
The first pixel of the line is defined by the 2 lest significant bit of the number. The 2 nd pixel by the 2 lest significant bit, etc.

## SUBGROB and SUBGROB_P

Syntax: SUBGRoB(srcGRB $[, x 1, y 1, x 2, y 2]$, trgtGRB)
SUBGROB_P(srcGRB [ ,x1, y1, x2, y2], trgtGRB)
Sets trgtGRB to be a copy of the area of srcGRB between points $x 1, y 1$ and $x 2, y 2$.
srcGRB can be any of the graphic variables and is optional. The default is GO.
trgtGRB can be any of the graphic variables except $G 0$.
$x 2, y 2$ are optional and if not specified will be the bottom right of $\operatorname{srcGRB}$.
$x 1, y 1$ are optional and if not specified will be the top left of srcGRB.

NOTE $\quad \operatorname{SUBGROB}(G 1, G 4)$ will copy G1 in G4.

## GROBH and GROBH_P

Syntax: GROBH(G)
GROBH_P(G)
Returns the height of $G$.
$G$ can be any of the graphic variables and is optional. The default is GO.

Syntax: GROBW(G)
GROBW_P(G)

Returns the width of $G$.
G can be any of the graphic variables and is optional. The default is GO.

Syntax: FREEze
Pauses program execution until a key is pressed. This prevents the screen from being redrawn after the end of the program execution, leaving the modified display on the screen for the user to see.

This section describes commands for inputting data into a program, and for outputting data from a program. These commands allow users to interact with programs.

These commands start the Matrix and List editors.

| EDITLIST | Syntax: EDITLISt(listvar) |
| :---: | :---: |
|  | Starts the list editor, loading listvar. |
|  | Example: EDITLIST(L1) edits list L1. |
| EDITMAT | Syntax: EDITMAT(matrixvar) |
|  | Starts the Marrix Editor and displays the specified matrix. If used in programming, returns to the program when user presses OK $\square$ |
|  | Example: EDITMAT(M1) edits matrix M1. |
| INPUT | Syntax: INPUT(var ["title", "label", "help", defaulf]); |
|  | Starts a dialog box with the title text, title, with one field named label, displaying help at the bottom and using the default value. Updates the variable var if the user presses OK and returns 1. If the user presses CANCL, it does not update the variable, and returns 0 . |
|  | ${ }^{\text {Die Sides }}$ |
|  | Example: |
|  | EXPORT SIDES; <br> EXPORT GETSIDES() |
|  | BEGIN |
|  | ```INPUT(SIDES,"Die Sides","N = ","Enter num sides",2);``` |
|  | End; |
| PRINT | Syntax: PRINT(expression or string); |
|  | Prints the result of expression or string to the terminal. |
|  | The terminal is a program text output viewing mechanism which is displayed only when PRINT commands are executed. When visible, you can use $\Theta$ and $\Theta$ to view the text, ccear to erase the text and any other key to hide the terminal. You can show the terminal at anytime using |

 press monem , then release both keys). Pressing on ${ }^{\mathbf{N} / \mathrm{C}}$ stops the interaction with the terminal.

There are also commands for outputting data in the Graphics section. In particular, the commands TEXTOUT and TEXTOUT_P can be used for test output.

This example prompts the user to enter a value for the radius of a circle, and prints the area of the circle on the terminal.

EXPORT AREACALC()
BEGIN
LOCAL radius;
INPUT(radius, "Radius of Circle",:"r = ", "Enter radius",1);

PRINT("The area is " $\pi+$ *radius^2);
END;



Notice the use of the LOCAL variable for the radius, and the naming convention that uses lower case letters for the local variable. Adhering to such a convention will improve the readability of your programs.

## GETKEY

Syntax: GETKEY
Returns the ID of the first key in the keyboard buffer, or - 1 if no key was pressed since the last call to GETKEY. Key IDs are integers from 0 to 50 , numbered from top leff (key 0 ) to boftom right (key 50) as shown on the following page.


ISKEYDOWN
Syntax: ISKEYDOWN(key_id);

Returns true (non-zero) if the key whose key_id is provided is currently pressed, and false (0) if it is not.

Syntax: MSGBOX(expression or string [ ,ok_cancel?]);
Displays a message box with the value of the given expression or string.

If ok_cancel? is true, displays OK and CANCL menu keys, otherwise only displays the OK key. Default value for ok_cancel is false.

Returns true (non-zero) if the user presses $\triangle$ OK , false (0) if the user presses CANCL.

Replace the PRINT command in the previous example with the MSGBOX command to:

```
EXPORT AREACALC()
BEGIN
LOCAL radius;
INPUT(radius, "Radius of Circle",:"r =
","Enter radius",1);
MSGBOX("The area is "\pi+ *radius^2);
END;
```

If the user enters 10 for the radius, the message box shows this:


## CHOOSE

Syntax:ChOOSE(var, "title", "item1", "item2",..." "itemn") Displays a choose box with the given title and containing the choose items. If the user selects an object, the variable whose name is provided will be updated to contain the number of the selected object (an integer, 1, 2, 3, ...) or 0 if the user presses CANCL.

Returns true (non zero) if the user selects an object, otherwise return false (0).

Example:
CHOOSE (N, "Pick
Hero", "Euler", "Gauss", "Newton") ;
IF N==1 PRINT("You picked Euler");END
ELSE IF N==2
PRINT("You picked
Gauss");END
ELSE IF $\mathrm{N}==3$
PRINT("You picked


Newton");END
END;
After execution of choose, the value of $n$ will be updated to contain $0,1,2$, or 3 . The IF THEN ELSE command
causes the name of the selected person will be printed to the terminal.

## Loop commands

FOR...FROM...TO...
DO...END
Syntax: FOR var FROM start TO finish [STEP increment] DO commands

END;
Sets variable var to start, and for as long as this variable's value is less than or equal to finish, executes the sequence of commands, and then adds 1 (increment) to var.

Example 1: This program determines which integer from 2 to N has the greatest number of factors.

```
EXPORT MAXFACTORS(N)
BEGIN
LOCAL cur, max,k,result;
1- max;1 result;
FOR k FROM 2 TO N DO
    SIZE(idivis(k)) D cur;
    IF cur > max THEN
            cur max;
            k result;
        END;
```

END;
MSGBOX("Max of "+ max +" factors for
"+result);

In Home, enter MAXFACTORS(100).


Example 2: This program draws an interesting pattern on the screen.

```
EXPORT DRAWPATTERN()
BEGIN
    LOCAL xinc,yinc,color;
    STARTAPP("Function");
    RECT();
xincr := (Xmax - Xmin)/254;
yincr := (Ymax - Ymin)/110;
FOR X FROM Xmin TO Xmax STEP xincr DO
FOR Y FROM Ymin TO Ymax STEP yincr DO
        color := FLOOR (X^2+Y^2) MOD 4;
        PIXON(X,Y,color);
        END;
        END;
FREEZE;
END;
```


## REPEAT...UNTIL... Syntax: REPEAT commands UNTIL test;

```
Repeats the sequence of commands until test is true (non \(0)\).
This code prompts for a positive value for SIDES, modifying an earlier program in this chapter.
Example:
EXPORT SIDES;
EXPORT GETSIDES()
BEGIN
REPEAT
INPUT (SIDES,"Die Sides","N = ","Enter num sides",2);
UNTIL SIDES>0;
END;
WHILE...DO...END Syntax: WHILE test DO commands END;
```

Evaluate test. If result is true (non 0 ), executes the commands, and repeat.

Example: A perfect number is one that is equal to the sum of all its proper divisors. For example, 6 is a perfect number because $6=1+2+3$. This function returns true when its argument is a perfect number.

## Example:

EXPORT ISPERFECT(n)
BEGIN
LOCAL d, sum;
$2-d ;$
1 - sum;
WHILE sum < = n AND $d<n$ DO
IF irem (n,d) ==0 THEN
sum+d sum;
END;
d+1 d;
END;
RETURN sum==n;
END;

This program displays all the perfect numbers up to 1000:

EXPORT PERFECTNUMS()
BEGIN
LOCAL k;
FOR k FROM 2 TO 1000 DO
IF ISPERFECT (k) THEN
MSGBOX(k+" is perfect, press OK");
END;
END;
END;

## Matrix Commands

Syntax: BREAK
Exits from a loop. Execution picks up with the first statement after the loop.

Syntax: CONTINUE
Transfer execution to the start of the next iteration of a loop.

Some matrix commands take as argument the matrix variable name on which the command is applied. Valid names are the global variables MO..M9 or a local variable that contains a matrix.

Syntax: ADDCOL
(name [ ,value 1, ..., valuen],column_number)
Add Column. Inserts values into a column before column_number in the specified matrix. You enter the values as a vector (these are not optional arguments!). The values must be separated by commas and the number of values must be the same as the number of rows in the matrix name.

Syntax: ADDROW
(name [ ,value 1, ..., valuen],row_number)
Add Row. Inserts values into a row before row_number in the specified matrix. You enter the values as a vector (these are not optional arguments!). The values must be separated by commas and the number of values must be the same as the number of columns in the matrix name.

Syntax: DELCOL(name ,column_number)
Delete Column. Deletes column column_number from matrix name.

Syntax: DELROW(name ,row_number)
Delete Row. Deletes row row_number from matrix name.
Syntax: EDITMAT(name)
Starts the Matrix Editor and displays the specified matrix. If used in programming, returns to the program when user presses OK . Even though this command returns the
matrix that was edited, EDITMAT cannot be used as an argument to other matrix commands.

RANDMAT

REDIM

REPLACE

SCALE

SCALEADD

SUB

SWAPROW

Syntax: RANDMAT (name, rows, columns)
Creates random matrix with a specified number of rows and columns and stores the result in name (name must be MO...M9). The entries will be integers ranging from -99 to 99.

Syntax: REDIM(name, size)
Redimensions the specified matrix (name) or vector to size. For a matrix, size is a list of two integers ( $n 1, n 2$ ). For a vector, size is a list containing one integer ( $n$ ). Existing values in the matrix are preserved. Fill values will be 0 .

Syntax: REPLACE(name, start, object)
Replaces portion of a matrix or vector stored in name with an object starting at position, start. Start for a matrix is a list containing two numbers; for a vector, it is a single number. REPLACE also works with lists and graphics.

Syntax: SCALE(name, value, rownumber)
Multiplies the specified row_number of the specified matrix by value.

Syntax: SCALEADD(name, value, row 1, row2)
Multiplies the specified row 1 of the matrix (name) by value, then adds this result to the second specified row2 of the matrix (name).

Syntax: SUB(name, object, start, end)
Extracts a sub-object, a portion of a list, matrix, or graphic from object, and stores it into name. Start and end are each specified using a list with two numbers for a matrix, a number for vector or lists, or an ordered pair, $(X, Y)$, for graphics.

Swaps columns. Exchanges column 1 and column2 of the specified matrix (name).

Syntax: SWAPROW(name, row 1, row2)
Swap Rows. Exchanges row 1 and row2 in the specified matrix (name).

A string is a sequence of characters enclosed in double quotes (""). To put a double quote in a string, use two consecutive double quotes. The $\backslash$ character starts an "escape" sequence, and the character(s) immediately following are interpreted specially. \n inserts a new line, two backslashes insert a single backslash.

Example: PRINT("Hello\nWorld!") displays
Hello
World!
on the terminal.

Syntax: char(vector or int)
Returns the string corresponding to the character codes in vector, or the single code int.

Examples: char(65) returns "A"; char([82,77,72]) returns "RMH"
$\operatorname{dim}$
expr
Syntax: dim(str)
Returns the number of characters in string str.
Example: $\operatorname{dim}(" 12345$ ") is $5, \operatorname{dim}(" n ")$ and $\operatorname{dim}(" \backslash n ")$ are both 1 (notice the use of the two double quotes and the escape sequence).

Syntax: expr(str)
Parses the string str into a number or expression.
Examples: $\operatorname{expr}($ ( $2+3$ ") returns 5 . If the variable $X$ has the value 90 , then expr(" $X+10$ ") returns 100. In a
program, if variables $a$ and $b$ are not declared and $X$ is 90 , then $\operatorname{expr}(" 2 X+a+b$ ") returns 180+a+b.
When used in tandem with other functionality built-in to the HP39gll, the expr command can be used in powerful ways. For example, you could build functions up out of strings and export these functions so they can be used throughout the calculator.

string

Syntax: string(object);
Returns a string representation of the object. The result varies depending on the type of object. For example, string(2/3); results in string(" $2 / 3$ ")
Examples:

| String | Result |
| :---: | :---: |
| $\begin{aligned} & \text { string(2/3) } \\ & \text { string(2.0/3) } \\ & \text { string(F1), when } \mathrm{Fl}(\mathrm{X}) \\ & =\operatorname{COS}(\mathrm{X}) \\ & \text { string(L1) when } \mathrm{LI}= \\ & \{1,2,3\} \\ & \text { string(M1) when } \mathrm{M} 1= \\ & {\left[\begin{array}{lll} 1 & 2 & 3 \\ 4 & 5 & 6 \end{array}\right]} \end{aligned}$ | $\begin{aligned} & \text { "2/3" } \\ & \text { "0.666666666667" } \\ & \text { "(X)>COS(X)" } \\ & " 1,2,3 \text { " } \\ & "[1,2,3],[4,5,6] \text { " } \end{aligned}$ |

inString
Syntax: inString(str 1,str2)
Returns the index of the first occurrence of str2 in str 1 . Returns 0 if str2 is not present in str1. Note that the first character in a string is a position 1 .

Examples:

> inString("vanilla", "van") returns 1.
> inString ("banana","na") returns 3
> inString("ab","abc") returns 0
left
rotate

Test Commands

Syntax: left(str,n)
Return the first $n$ characters of string str. If $n \geq \operatorname{dim}$ (str) or $n<0$, returns str. If $n==0$ returns the empty string.

Example: left("MOMOGUMBO",3) returns "MOM"
Syntax: right(str,n)
Returns the last n characters of string str. If $n<=0$, returns empty string. If $n>-\operatorname{dim}(s t r)$, returns str
Example: right("MOMOGUMBO",5) returns "GUMBO"

Syntax: mid(str,pos, [n])
Extracts $n$ characters from string str starting at index pos. $n$ is optional, if not specified, extracts all the remainder of the string.
Example: mid("MOMOGUMBO", 3,5 ) returns "MOGUM", mid("PUDGE",4) returns "GE"

Syntax: rotate(str,n)
Permutation of characters in string str. If $0<=n<\operatorname{dim}(s t r)$, shifts $n$ places to left. If $-\operatorname{dim}(s t r)<n<=-1$, shifts $n$ spaces to right. If $n>\operatorname{dim}(s t r)$ or $n<-\operatorname{dim}(s t r)$, returns str.

Examples:
rotate(" 12345 ", 2$)$ returns " 34512 "
rotate(" 12345 ",-1) returns " 51234 "
rotate(" 12345 ", 6) returns " 12345 "

The Test commands include both Boolean and relational operations. Boolean and relational expressions evaluate to true or false. A non-zero number is equivalent to true, and a number equal to 0 is equivalent to false. Note that in addition to real numbers, complex numbers, strings, lists, and matrices can be compared using the relational operators $==$, NOT (or ! $=$ ), and (or $<>$ or ! $=$ ). These commands are not in the CMDS menu. They appear in the Math menu but are listed here for convenience.

Relational expressions

## =

Equality.
Syntax: object1 == object2
Example: $3+1==4$ returns 1 .
$<$
$\leq$ (or $<=$ )
$>$
$\geq$ (or $>=$ )
$\neq$ (or <> or ! $=$ )
Not equal to.
Syntax: object1 $\neq$ object2
Example: $3+1 \neq 4$ returns 0 .

## Boolean expressions

AND (or \&\&) Logical And.
Syntax: expr1 AND expr2
Example: $3+1==4$ AND $4<5$ returns 1 .
OR (or ||) Logical Or.
Syntax: expr1 OR expr2
Example: $3+1==4$ OR $8<5$ returns 1 .

| XOR | Exclusive Or. |
| :--- | :--- |
|  | Syntax: expr 1 XOR expr2 |
|  | Example: $3+1==2$ OR $8<5$ returns 0. |

NOT (or !)
Variable
commands

Logical Negation.
Syntax: NOT(expr1)
Example: $\operatorname{NOT}(3+1==4)$ returns 0 .

## Variable commands

These commands allow you to control the visibility of a user-defined variable or function.

## Export

Export.
Syntax: EXPORT(FunctionName)
Exports the function FunctionName so that it is globally available and appears in the Program Commands menu SHIIT CMDS) when USER is pressed.

## Local

Local.
Syntax: LOCALvar 1,var2,...varn;
Makes the variables var 1, var2, etc. local to the program in which they are found.

## Variables and Programs

The HP 39gll has three types of variables: Home variables, App variables, and User variables. You use the Variable menu (chars A ) to retrieve Home, app, or User variables.

Home variables are used for real numbers, complex numbers, graphics, lists, and matrices among other things. Home variables keep the same value in Home and in apps.

App variables are those whose values depend on the current app. The app variables are used in programming to represent the definitions and settings you make when working with apps interactively.

User variables are variables exported from a user program. They provide one of several mechanisms to allow programs to communicate with the rest of the calculator, or with other programs. Once a variable has been exported from a program, it will appear among the User variables in the Vars menu, next to the program that exported it.
This chapter deals with App variables and User variables. For information on Home variables, see Variables and memory management.

## App variables

Not all app variables are used in every app. S1fit, for example, is only used in the Statistics 2 Var app. However, most of the variables are used in common by the Function, Parametric, Polar, Sequence, Solve, Statistics 1Var, and Statistics 2Var apps. If a variable is not available in all of these apps, or is available only in some other apps, then a list of the apps where the variable can be used appears under the variable name. The following sections list the app variables by the view in which they are used.

## Plot view variables

Axes
Cursor
Turns axes on or off. From Plot Setup, check (or uncheck) AXES.
Or, in a program, type:
1 Axes-to turn axes on (default).
0 Axes-to turn axes off.
Sets crosshairs type. (Inverted or blinking is useful if the background is solid).
From Plot Setup, choose Cursor.
Or, in a program, type:
2 CrossType-for blinking crosshairs.
1 CrossType-to invert the crosshairs.
0 CrossType-for solid crosshairs (default).

## GridDots

## GridLines

Hmin/Hmax
Statistics IVar

Hwidth<br>Statistics 7 Var

Turns the background dot grid in Plot view on or off. From Plot setup, check (or uncheck) GRID DOTS.

Or, in a program, type:
1 GridDots-to turn the grid dots on (default).
0 GridDots-to turn the grid dots off.
Turns the background line grid in Plot view on or off. From Plot setup, check (or uncheck) GRID LINES. Or, in a program, type:

1- GridLines-to turn the grid lines on (default).
0 GridLines-to turn the grid lines off.
Defines minimum and maximum values for histogram bars.
From Plot Setup for one-variable statistics, set values for HRNG.

Or, in a program, type:
$n_{1}$ - Hmin
$n_{2}$ - Hmax
where $n_{1}<n_{2}$

Sets the width of histogram bars.
From Plot Setup for one-variable statistics, set a value for Hwidth.
Or, in a program, type:
$n$ Hwidth
Defines the value of the independent variable used in tracing mode.
Or, in a program, type:

$$
n \vee \text { Indep }
$$

## Labels

Draws labels in Plot view showing $X$ and $Y$ ranges. From Plot Setup, check (or uncheck) Labels

Or, in a program, type:
1 Labels - to turn labels on.
0 Labels-to turn labels off (default).

Nmin/Nmax
Sequence

Recenter

S1mark-S5mark
Statistics 2Var

Defines the minimum and maximum independent variable values.
Appears as the NRNg fields in the Plot Setup input form. From Plot Setup, enter values for NRNG.
Or, in a program, type:
$n_{1} \triangleright$ Nmin
$n_{2}$ Nmax
where $n_{1}<n_{2}$
Recenters at the cursor location when zooming.
From Plot-Zoom-Set Factors, check (or uncheck)
Recenter.
Or, in a program, type:
1 Recenter - to turn recenter on (default).
0 Recenter - to turn recenter off.
Sets the mark to use for scatter plots.
From Plot Setup for two-variable statistics, highlight one of S1mark-S5mark and choose a mark.

Or, in a program, type:
$n$ Slmark
where $n$ is $1,2,3, \ldots 5$
Enables you to choose types of sequence plots: Stairstep or Cobweb.

From Plot Setup, select SeqPlot, then choose
Stairstep or Cobweb.
Or, in a program, type:
1 SeqPlot-for Stairstep.
2 SeqPlot-for Cobweb.

Sets the minimum and maximum independent values.

Appears as the Rng field in the Plot Setup input form. From Plot Setup, enter values for RNg.

Or, in a program, type:
$n_{1}-\theta \mathrm{min}$
$n_{2}-\theta \max$
where $n_{1}<n_{2}$
$\theta$ step
Polar

Imin/Tmax
Parametric

Sets the step size for the independent variable.
From Plot Setup, enter a value for STEP.
Or, in a program, type:
$n$ - $\theta$ step
where $n>0$
Sets the minimum and maximum independent variable values.

Appears as the trng field in the Plot Setup input form. From Plot Setup, enter values for TRNG.

Or, in a program, type:
$n_{1}$ Tmin
$n_{2}$-Tmax
where $n_{1}<n_{2}$

## Tracing

Turns tracing on or off in the Plot view.
From the Plot view, press MENU then TRACE to toggle tracing off or on.

Or, in a program, type:
1 - Tracing-to turn Tracing mode on (default).
0 - Tracing-to turn Tracing mode off.

Tstep
Parametric

Sets the step size for the independent variable.
From Plot Setup, enter a value for TSTEP.

Or, in a program, type
$n$ - Tstep
where $n>0$
Sets the horizontal coordinate of the crosshairs.
Only works with TRACE off (TRACE ). From the Plot view, use the cursor keys to move to the desired $x$-value.

Or, in a program, type:
$n$ - Xcross

Xcross

Ycross

Xtick

Ytick
$X_{\text {min }} / X_{\text {max }}$

Or, in a program, type:
$n>$ Ytick where $n>0$
Sets the minimum and maximum horizontal values of the plot screen.
Appears as the XRNG fields (horizontal range) in the Plot Setup input form. From Plot Setup, enter values for XRNG.

Or, in a program, type:
$n_{1} \triangleright$ Xmin
$n_{2}$ Xmax
where $n_{1}<n_{2}$

| Ymin/Ymax | Sets the minimum and maximum vertical values of the plot screen. |
| :---: | :---: |
|  | Appears as the YRNg fields (vertical range) in the Plot Setup input form. From Plot Setup, enter the values for YRNG. |
|  | Or, in a program, type: |
|  | $n_{1}$ Ymin |
|  | $n_{2} \triangleright$ Ymax |
|  | where $n_{1}<n_{2}$ |
| Xzoom | Sets the horizontal zoom factor. |
|  | From Plot setup ( $\left.\begin{array}{c}\text { Plot } \\ \text { Soup }\end{array}\right)$, press MENU then ZOOM. Scroll to set Factors, select it and press OK. Enter the value for XZOOM $\square$ OK |
|  | Or, in a program, type: |
|  | $n-$ XZOOM |
|  | where $n>0$ |
|  | The default value is 4 . |
| Yzoom | From Plot setup ( $\left.\begin{array}{l}\text { Plot } \\ \text { Sowp }\end{array}\right)$, press MENU then ZOOM. Scroll to set Factors, select it and press OK. Enter the value for YZOOM and press $\square$ OK |
|  | Or, in a program, type: |
|  | $n \downarrow \mathrm{YZOOM}$ |

The default value is 4 .

## Symbolic view <br> variables

| AltHyp | Determines the alternative hypothesis used for a |
| :--- | :--- |
| Inference | hypothesis testing. Choose an option from the Symbolic |
| view. |  |

Or, in a program, type:

$$
\begin{aligned}
& 0>\text { AltHyp-for } \mu<\mu_{0} \\
& 1 \text { AltHyp-for } \mu>\mu_{0} \\
& 2 \text { AltHyp-for } \mu \neq \mu_{0}
\end{aligned}
$$

EO...E9
Solve

FO...F9
Function

H1...H5

H1Type...H5Type

Can contain any equation or expression. Independent variable is selected by highlighting it in Numeric View.

Example:

```
X+Y*X-2=Y E1
```

Can contain any expression. Independent variable is x . Example:

```
SIN(X)\ F1
```

Contains the data values for a 1 -variable statistical analysis. For example, $\mathrm{Hl}(\mathrm{n})$ returns the nth value in the data set for the Hl analysis.

Sets the type of plot used to graphically represent the statistical analyses H1 through H5. From the Symbolic setup, specify the type of plot in the field for Type 1, Type 2 , etc.

Or in a program, store one of the following constant integers or names into the variables H1Type, H2Type, etc.

0 Histogram (default)
1 Box and Whisker
2 Normal Probability
3 Line
4 Bar
5 Pareto
Example:
2-H3Type

Method
Inference

Determines whether the Inference app is set to calculate hypothesis test results or confidence intervals.

```
Or, in a program, type:
    0 Method-for Hypothesis Test
    1-Method-for Confidence Interval
```

RO...R9

Polar

S1Type...S5Type
Statistics 2Var

Can contain any expression. Independent variable is $\theta$.
Example:

```
2*SIN(2* *)
```

Sets the type of fit to be used by the FIT operation in drawing the regression line. From Symbolic Setup view, specify the fit in the field for Type1, Type2, etc.

Or, in a program, store one of the following constant integers or names into a variable S1Type, S2Type, etc.

1 Linear
2 Logarithmic
3 Exponential
4 Power
5 Exponent
6 Inverse
7 Logistic
8 Quadratic
9 Cubic
10 Quartic
11 User Defined
Example:
Cubic ${ }^{\text {S }}$ Sit
or
9-S2fit

## Type

Inference

Determines the type of hypothesis test or confidence interval. Depends upon the value of the variable Method. Make a selection from the Symbolic view.

Or, in a program, store the constant number from the list below into the variable Type. With Method=0, the constant values and their meanings are as follows:

```
    0 Z-Test:1 }
    1 Z-Test: }\mp@subsup{\mu}{1}{}-\mp@subsup{\mu}{2}{
    2 Z-Test:1 \pi
    3 Z-Test: }\mp@subsup{\pi}{1}{}-\mp@subsup{\pi}{2}{
    4 T-Test:1 \mu
    5 T-Test: }\mp@subsup{\mu}{1}{}-\mp@subsup{\mu}{2}{
```

With Method=1, the constant values and their meanings are as follows:

```
O Z-Int:1 }
1 Z-Int: }\mp@subsup{\mu}{1}{}-\mp@subsup{\mu}{2}{
2 Z-Int:1 \pi
3 Z-Int: }\mp@subsup{\pi}{1}{}-\mp@subsup{\pi}{2}{
4 T-Int:1 }
5 T-Int: }\mp@subsup{\mu}{1}{}-\mp@subsup{\mu}{2}{
```

X0, Y0...X9,Y9
Parametric
Can contain any expression. Independent variable is T . Example:

SIN $(4 * T)$ Y1; $2 * \operatorname{SIN}(6 * T)$ X1

U0...U9
Sequence
Can contain any expression. Independent variable is N . Example:

```
RECURSE (U,U(N-1)*N,1,2) \ U1
```


## Numeric view <br> variables

C0...C9
Statistics 2Var
C0 through C9, for columns of data. Can contain lists.
Enter data in the Numeric view
Or, in a program, type:
LIST Cn
where $n=0,1,2,3 \ldots 9$ and LIST is either a list or the name of a list.

D0...D9
Statistics IVar
D0 through D9, for columns of data. Can contain lists.
Enter data in the Numeric view
Or, in a program, type:
LIST•Dn
where $n=0,1,2,3 \ldots 9$ and LIST is either a list or the name of a list.

## NumCol

Function
Parametric
Polar
Sequence
Sets the column to be highlighted in the Numeric view.
Or, in a program, type:
$n$ NumCol
where $n$ can be $0,1,2,3,4,5,6,7,8,9$.
NumFont
Enables you to choose the font size in the Numeric view. Does not appear in the Num Setup input form.
Corresponds to ${ }^{\text {EG}}$ - in the Numeric view.
Or, in a program, type:
0 NumFont-for small.
1 NumFont-for big (default).

## Numindep

Function
Parametric
Polar
Sequence
Specifies the list of independent values to be used by Build Your Own Table. Enter your values one-by-one in the Numeric view.

Or, in a program, type:
LIST NumIndep
List can be either a list itself or the name of a list.

NumRow
Function
Parametric
Polar
Sequence

NumStart
Function
Parametric
Polar
Sequence

NumStep
Function
Parametric
Polar
Sequence

NumType
Function
Parametric
Polar
Sequence

NumZoom
Function
Parametric
Polar
Sequence

Sets the row to be highlighted in the Numeric view. Use the cursor keys to select a row in the Numeric view.

Or, in a program, type:
$n$ - NumRow
where $n>0$

Sets the starting value for a table in Numeric view.
From Num Setup, enter a value for NUMSTART.
Or, in a program, type:
$n$ NumStart

Sets the step size (increment value) for an independent variable in Numeric view.
From Num Setup, enter a value for NUMSTEP.
Or, in a program, type:
$n$ NumStep
where $n>0$

Sets the table format.
From Num Setup, enter 0 or 1.
Or, in a program, type:
0 NumType-for BuildYourOwn.
1 NumType-for Automatic (default).
Sets the zoom factor in the Numeric view.
From Num Setup, type in a value for NUMZOOM.
Or, in a program, type:
$n$ - NumZoom
where $n>0$

## Inference app variables

The following variables are used by the Inference app. They correspond to fields in the Inference app Numeric view. The set of variables shown in this view depends on the hypothesis test or the confidence interval selected in the Symbolic view.

Alpha

Conf

Mean 1

Mean2
$\mu 0$

Sets the alpha level for the hypothesis test. From the Numeric view, set the value of Alpha.

Or, in a program, type:
$n$ - Alpha
where $0<n<1$
Sets the confidence level for the confidence interval. From the Numeric view, set the value of Conf.

Or, in a program, type:
$n>C o n f$
where $0<n<1$
Sets the value of the mean of a sample for a 1-mean hypothesis test or confidence interval. For a 2 -mean test or interval, sets the value of the mean of the first sample. From the Numeric view, set the value of mean1.

Or, in a program, type:
$n$ Mean1
For a 2 -mean test or interval, sets the value of the mean of the second sample. From the Numeric view, set the value of Mean2.

Or, in a program, type:
$n$ Mean2
The following variables are used to set up hypothesis test or confidence interval calculations in the Inference app.

Sets the assumed value of the population mean for a hypothesis test. From the Numeric view, set the value of $\mu 0$.

Or, in a program, type:
$n \triangleright \mu 0$
where $0<\mu 0<1$

For a test or interval involving the difference of two means or two proportions, sets the size of the second sample. From the Numeric view, set the value of n2.

Or, in a program, type:
$n>n 2$
Sets the assumed proportion of successes for the Oneproportion Z-test. From the Numeric view, set the value of $\pi 0$.

Or, in a program, type:
$n \gg 0$
where $0<\pi 0<1$

## Pooled

Determine whether or not the samples are pooled for tests or intervals using the Student's T-distribution involving two means. From the Numeric view, set the value of Pooled.

Or, in a program, type:
0 Pooled-for not pooled (default).
1 Pooled-for pooled.

Sets the sample standard deviation for a hypothesis test or confidence interval. For a test or interval involving the difference of two means or two proportions, sets the sample standard deviation of the first sample. From the Numeric view, set the value of $s 1$.

Or, in a program, type:
$n$-s1
s2

Or, in a program, type:
$n>s 2$ of $s 2$.

For a test or interval involving the difference of two means or two proportions, sets the sample standard deviation of the second sample. From the Numeric view, set the value

Sets the population standard deviation for a hypothesis test or confidence interval. For a test or interval involving the difference of two means or two proportions, sets the population standard deviation of the first sample. From the Numeric view, set the value of $\sigma 1$.

Or, in a program, type:
$n>\sigma 1$

For a test or interval involving the difference of two proportions, sets the number of successes of the second sample. From the Numeric view, set the value of x 2 .

Or, in a program, type:
$n>x 2$

| Finance app variables | The following variables are used by the Finance app. They correspond to the fields in the Finance app Numeric view. |
| :---: | :---: |
| CPYR | Compounding periods per year. Sets the number of compounding periods per year for a cash flow calculation. From the Numeric view of the Finance app, enter a value for $\mathrm{C} / \mathrm{YR}$. |
|  | Or, in a program, type: |
|  | $n$ - $\mathrm{CPY}^{\text {P }}$ |
|  | where $n>0$ |
| END | Determines whether interest is compounded at the beginning or end of the compounding period. From the Numeric view of the Finance app. Check or uncheck END. |
|  | Or, in a program, type: |
|  | 1DEND-for compounding at the end of the period (Default) |
|  | END-for compounding at the beginning of the period |
| FV | Future value. Sets the future value of an investment. From the Numeric view of the Finance app, enter a value for FV. |
|  | Or, in a program, type: |
|  | $n>\mathrm{FV}$ |
|  | Note: positive values represent return on an investment or loan. |
| IPYR | Interest per year. Sets the annual interest rate for a cash flow. From the Numeric view of the Finance app, enter a value for $I \% Y R$. |
|  | Or, in a program, type: |
|  | $n$-IPYR |
|  | where $n>0$ |
| NbPmt | Number of payments. Sets the number of payments for a cash flow. From the Numeric view of the Finance app, enter a value for N . |


|  | Or, in a program, type: |
| :---: | :---: |
|  | $n>$ NbPmt |
|  | where $n>0$ |
| PMT | Payment value. Sets the value of each payment in a cash flow. From the Numeric view of the Finance app, enter a value for Рмт. |
|  | Or, in a program, type: |
|  | $n-$ PMT |
|  | Note: payment values are negative if you are making the payment and positive if you are receiving the payment. |
| PPYR | Payments per year. Sets the number of payments made per year for a cash flow calculation. From the Numeric view of the Finance app, enter a value for $P / Y R$. |
|  | Or, in a program, type: |
|  | $n>P P Y R$ |
|  | where $n>0$ |
| PV | Present value. Sets the present value of an investment. From the Numeric view of the Finance app, enter a value for PV. |
|  | Or, in a program, type: |
|  | $n>P V$ |

Note: negative values represent an investment or loan.

```
GSize
Group size. Sets the size of each group for the amortization table. From the Numeric view of the Finance app, enter a value for Group Size.
Or, in a program, type:
\(n\)-GSize
```

Linear Solver app variables

LSystem

The following variables are used by the Linear Solver app. They correspond to the fields in the app's Numeric view.

Contains a $2 \times 3$ or $3 \times 4$ matrix which represents a $2 \times 2$ or $3 \times 3$ linear system. From the Numeric view of the Linear

Solver app, enter the coefficients and constants of the linear system.

Or, in a program, type:
matrix LSystem

Size
where matrix is either a matrix or the name of one of the matrix variables MO-M9.

Contains the size of the linear system. From the Numeric view of the Linear Solver app, press $2 \times 2$ or $3 \times 3$.

Or, from a program, type:
2-Size-for a $2 \times 2$ linear system
3-Size-for a $3 \times 3$ linear system

Triangle Solver app variables

SideA

SideB

SideC

The following variables are used by the Triangle Solver app. They correspond to the fields in the app's Numeric view.

The length of Side A. Sets the length of the side opposite the angle A. From the Triangle Solver Numeric view, enter a positive value for $A$.

Or, in a program, type:
$n$ - SideA
where $n>0$
The length of Side B. Sets the length of the side opposite the angle B. From the Triangle Solver Numeric view, enter a positive value for $B$.

Or, in a program, type:
$n$-SideB
where $n>0$
The length of Side C. Sets the length of the side opposite the angle C. From the Triangle Solver Numeric view, enter a positive value for C .

Or, in a program, type:
$n$-SideC
where $n>0$

AngleA

AngleB

Or, in a program, type:
$n$-AngleB
where $n>0$

## AngleC

RECT
The measure of angle $C$. Sets the measure of angle $C$. The value of this variable will be interpreted according to the angle mode setting (Degrees or Radians). From the Triangle Solver Numeric view, enter a positive value for C .

Or, in a program, type:
$n$-AngleC
where $n>0$
Corresponds to the status of RECT in the Numeric view of the Triangle Solver app. Determines whether a general triangle solver or a right triangle solver is used. From the Triangle Solver view, press RECT

Or, in a program, type:
0 RECT-for the general Triangle Solver
1-RECT——or the right Triangle Solver
Modes variables
These variables are found in the Symbolic setup of an app. They can be used to overwrite the value of the corresponding variable in Home Modes.

## ADigits

AFormat
Defines the number display format used for number display in the Home view and to label axes in the Plot view.

From the Modes view, choose Standard, Fixed, Scientific, or Engineering in the Number Format field.

Or, in a program, store the constant number (or its name) into the variable Format.

1 Standard
2 Fixed
3 Sci
4 Eng
Example:
Scientific AFormat
or
3 AFormat

| Results | These variables are found in various views. They capture <br> variables <br> the results of calculations such as those performed when <br> the STATS menu key is pressed in the Statistics 1Var <br> Numeric view. |
| :--- | :--- |
| The following results variables store calculations from the |  |
| Function app. They store results from the commands in |  |
| the Plot view FCN menu. |  |


| Q3 | Contains the value of the third quartile in the current 1 variable analysis (H1-H5). |
| :---: | :---: |
| Max | Contains the maximum value in the current 1 -variable analysis (H1-H5). |
| $\Sigma \mathbf{X}$ | Contains the sum of the data set in the current 1 -variable analysis (H1-H5). |
| $\Sigma X^{2}$ | Contains the sum of the squares of the data set in the current 1 -variable analysis ( $\mathrm{H} 1-\mathrm{H} 5$ ). |
| MeanX | Contains the mean of the data set in the current 1 -variable analysis (H1-H5). |
| sX | Contains the sample standard deviation of the data set in the current 1 -variable analysis ( $\mathrm{H} 1-\mathrm{H} 5$ ). |
| $\sigma X$ | Contains the population standard deviation of the data set in the current 1 -variable analysis ( $\mathrm{H} 1-\mathrm{H} 5$ ). |
| serrX | Contains the standard error of the data set in the current 1-variable analysis (H1-H5). |
|  | The following Results variables store calculations from the Statistics 2 Var app. These calculations are performed when STATS is pressed in the Numeric view or the Do2VarStats command is executed. |
| Corr | Contains the correlation coefficient from the latest calculation of summary statistics. This value is based on the linear fit only, regardless of the fit type chosen. |
| CoefDet | Contains the coefficient of determination from the latest calculation of summary statistics. This value is based on the fit type chosen. |
| sCOV | Contains the sample covariance of the current 2-variable statistical analysis (S1-S5). |
| $\sigma \mathrm{COV}$ | Contains the population covariance of the current 2variable statistical analysis ( $\mathrm{S} 1-\mathrm{S} 5$ ). |
| $\Sigma \mathbf{X Y}$ | Contains the sum of the $X \cdot Y$ products for the current 2 variable statistical analysis (S1-S5). |


| MeanX | Contains the mean of the independent values $(X)$ of the current 2 -variable statistical analysis (S1-S5). |
| :---: | :---: |
| $\Sigma \mathbf{X}$ | Contains the sum of the independent values $(\mathrm{X}$ ) of the current 2 -variable statistical analysis ( $\mathrm{S} 1-\mathrm{S} 5$ ). |
| $\Sigma X^{2}$ | Contains the sum of the squares of the independent values ( X ) of the current 2 -variable statistical analysis (S1-S5). |
| sX | Contains the sample standard deviation of the independent values $(\mathrm{X}$ ) of the current 2 -variable statistical analysis (S1-S5). |
| $\sigma X$ | Contains the population standard deviation of the independent values $(\mathrm{X}$ ) of the current 2 -variable statistical analysis (S1-S5). |
| serrX | Contains the standard error of the independent values ( X ) of the current 2 -variable statistical analysis ( $\mathrm{S} 1-\mathrm{S} 5$ ). |
| MeanY | Contains the mean of the dependent values $(\mathrm{Y})$ of the current 2 -variable statistical analysis ( $\mathrm{S} 1-\mathrm{S} 5$ ). |
| $\Sigma \mathrm{Y}$ | Contains the sum of the dependent values $(\mathrm{Y})$ of the current 2 -variable statistical analysis ( $\mathrm{S} 1-\mathrm{S} 5$ ). |
| $\Sigma Y^{2}$ | Contains the sum of the squares of the dependent values (Y) of the current 2 -variable statistical analysis ( $\mathrm{S} 1-\mathrm{S} 5$ ). |
| sY | Contains the sample standard deviation of the dependent values $(\mathrm{Y})$ of the current 2 -variable statistical analysis (S1-S5). |
| $\sigma \mathbf{Y}$ | Contains the population standard deviation of the dependent values $(Y)$ of the current 2 -variable statistical analysis (S1-S5). |
| serrY | Contains the standard error of the dependent values ( Y ) of the current 2 -variable statistical analysis (S1-S5). |
|  | The following Results variables store calculations from the Inference app. These calculations are performed when CALC is pressed in the Numeric view. |
| CritScore | Contains the value of the Z - or t -distribution associated with the input $\alpha$-value |


| CritVal1 | Contains the lower critical value of the experimental <br> variable associated with the negative TestScore value <br> which was calculated from the input $\alpha$-level. |
| :--- | :--- |
| CritVal2 | Contains the upper critical value of the experimental <br> variable associated with the positive TestScore value <br> which was calculated from the input $\alpha$-level. |
| DF Contains the degrees of freedom for the t-tests. |  |

## App Functions

App functions are used by several of the HP Apps to perform common calculations. For example, in the Function app, the Plot view FCN menu has a function called SLOPE that calculates the slope of a given function at a given point. The SLOPE function can be used, from the Home view or a program, etc. to give the same results as if you were in the Function app Plot view. App functions can be used to get the same results in a program or the Home view or anywhere else- just as if you were in the app. The App functions described in this section are grouped by app.

## Function app functions

The Function app functions provide the same functionality found in the Function app's Plot view under the FCN menu. All of these operations work on functions. The functions may be expressions in X or the names of the Function app variable FO through F9.

Area under a curve or between curves. Finds the signed area under a function or between two functions. Finds the area under the function Fn or below Fn and above the function Fm, from lower X-value to upper X-value.

AREA(Fn, [Fm,] lower, upper)
Example:
AREA(-X, $\left.X^{2}-2,-2,1\right)$ returns 4.5

## EXTREMUM

ISECT

ROOT

SLOPE

Solve app functions

Extremum of a function. Finds the extremum (if one exists) of the function Fn that is closest to the X -value guess.

EXTREMUM(Fn, guess)
Example:
EXTREMUM(X $\left.{ }^{2}-\mathrm{X}-2,0\right)$ returns 0.5
Intersection of two functions. Finds the intersection (if one exists) of the two functions Fn and Fm that is closest to the X -value guess.

ISECT(Fn, Fm, guess)
Example:
ISECT(X, 3-X,2) returns 1.5
Root of a function. Finds the root of the function Fn (if one exists) that is closest to the X -value guess.

ROOT(Fn, guess)
Example:
ROOT $\left(3-\mathrm{X}^{2}, 2\right)$ returns $1.732 \ldots$
Slope of a function. Returns the slope of the function Fn at the X -value (if value exists).

SLOPE(Fn, value)
Example:
$\operatorname{SLOPE}\left(3-\mathrm{X}^{2}, 2\right)$ returns -4

The Solve app has a single function that solves a given equation or expression for one of its variables. En may be an equation or expression, or it may be the name of one of the Solve Symbolic variables EO-E9.

SOLVE
Solve. Solves an equation for one of its variables. Solves the equation En for the variable var, using the value of guess as the initial value for the value of the variable var. If $E n$ is an expression, then the value of the variable var that makes the expression equal to zero is returned.

SOLVE(En, var, guess)
Example:
SOLVE ( $\mathrm{X}^{2}-\mathrm{X}-2, \mathrm{X}, 3$ ) returns 2
This function also returns an integer that is indicative of the type of solution found, as follows:

0 -an exact solution was found
1-an approximate solution was found
2-an extremum was found that is as close to a solution as possible

3 -neither a solution, an approximation, nor an extremum was found

See the Chapter Solve app for more details on the types of solutions returned by this function.

## Statistics IVar app functions

DolVStats

## SETFREQ

The Statistics 1Var app has a 3 functions designed to work together to calculate summary statistics based on one of the statistical analyses ( $\mathrm{H} 1-\mathrm{H} 5$ ) defined in the Symbolic view of the Statistics 1Var app.

Performs the same calculations as pressing STATS in the Statistics IVar app's Numeric view and stores the results in the appropriate Statistics 1Var app results variables. Hn must be one of the Statistics 1Var app Symbolic view variables $\mathrm{H} 1-\mathrm{H} 5$.

Do1VStats(Hn)
Set frequency. Sets the frequency for one of the statistical analyses ( $\mathrm{H} 1-\mathrm{H} 5$ ) defined in the Symbolic view of the Statistics 1 Var app. The frequency can be either one of the column variables D0-D9, or any positive integer. Hn must be one of the Statistics 1Var app Symbolic view variables H1-H5. If used, $D n$ must be one of the column variables DO-D9; otherwise, value must be a positive integer.
SETFREQ(Hn, Dn)
or
SETFREQ(Hn, value)

## Statistics 2Var app functions

Do2VStats

PredX

PredY

SetDepend

SetIndep

Inference app
functions

Set sample data. Sets the sample data for one of the statistical analyses (H1-H5) defined in the Symbolic view of the Statistics 1Var app. Sets the data column to one of the column variables D0-D9 for one of the statistical analyses H1-H5.

SETSAMPLE(Hn, Dn)

The Statistics 2 Var app has a number of functions. Some are designed to calculate summary statistics based on one of the statistical analyses (S1-S5) defined in the Symbolic view of the Statistics 2Var app. Others predict $X$ - and $Y$-values based on the fit specified in one of the analyses.

Performs the same calculations as pressing STATS in the Statistics 2Var app's Numeric view and stores the results in the appropriate Statistics 2 Var app results variables. Sn must be one of the Statistics 2Var app Symbolic view variables S1-S5.

Do2VStats(Sn)
Predict $X$. Uses the fit from the first active analysis (S1-S5) found to predict an $x$-value given the $y$-value value.

Predx(value)
Predict $Y$. Uses the fit from the first active analysis (S1S5) found to predict a $y$-value given the $x$-value value.

PredY(value)
Sets the dependent column for one of the statistical analyses $\mathrm{S} 1-\mathrm{S} 5$ to one of the column variables $\mathrm{C} 0-\mathrm{C} 9$.

SetDepend(Sn, Cn)
Sets the independent column for one of the statistical analyses S1-S5 to one of the column variables C0-C9.

SetIndep(Sn, Cn)

The Inference app has a single function that returns the same results as pressing CALC in the Inference app's Numeric view. The results depend on the contents of the Inference app variables Method, Type, and AltHyp.


Finance app functions

DoFinance

The Finance app has a single function that returns the same results as pressing SOLVE in the Finance app's Numeric view.

Calculate TVM results. Solves a TVM problem for the variable TVMVar. The variable must be one of the Finance app's Numeric view variables. Performs the same calculation as pressing SOLVE in the Finance app Numeric view with TVMVar highlighted.

DoFinance(TVMVar)
Example:
DoFinance(FV) returns the future value of an investment in the same way as pressing SOLVE in the Finance app Numeric view with FV highlighted.

## Linear Solver app functions

LinSolve

The Linear Solver app has a single function that solves a $2 \times 2$ or $3 \times 3$ linear system, based on a matrix of coefficients and constants.

Solve linear system. Solves the $2 \times 2$ or $3 \times 3$ linear system represented by matrix.

LinSolve(matrix)

Examples:
LinSolve([[A, B, C], [D, E, F]]) solves the linear system:

$$
\left\{\begin{array}{l}
a x+b y=c \\
d x+e y=f
\end{array}\right.
$$

Triangle Solver app functions

The Triangle Solver app has a group of functions which allow solving a complete triangle from the input of 3 consecutive parts of the triangle. The names of these commands use $A$ to signify an angle, and $S$ to signify a side length. To use these commands, enter 3 inputs in the specified order given by the command name.

AAS(angle, angle, side)
ASA(angle, side, angle)
SAS(side, angle, side)
SSA(side, side, angle)
sss(side, side, side)
Returns a list of three results that correspond to the opposite angle or side from the given input. If the input given was an angle, the item in same position in the results list will be the opposite side.

Example:
In Degree mode, $\operatorname{SAS}(2,90,2)$ returns $\{45,2.82 \ldots, 45\}$.

## Common app functions

In the indeterminate case AAS where two solutions may be possible, AAS may return a list of two such lists containing both results.

In addition to the app functions specific to each app, there are two functions common to the following apps:

- Function
- Solve
- Statistics IVar
- Statistics 2Var
- Parametric
- Polar
- Sequence


## CHECK

Checks the Symbolic view variable Symbn. Symbn can be any of the following:

- F0-F9-for the function app
- E0-E9-for the Solve app
- H1-H5-for the Statistics 1Var app
- S1-S5-for the Statistics 2Var app
- $\mathrm{x0} / \mathrm{Yo}-\mathrm{X9}$ /Y9-for the parametric app
- R0-R9-for the Polar app
- U0-U9-for the Sequence app

СНеск(Symbn)
Example:
CHECK(F1) checks the Function app Symbolic view variable F1. The result is that $\mathrm{Fl}(\mathrm{X})$ is drawn in the Plot view and has a column of function values in the Numeric view of the Function app.

Example:
UNCHECK(R1) unchecks the Polar app Symbolic view variable $R 1$. The result is that $R 1(\theta)$ is not drawn in the Plot view and does not appear in the Numeric view of the Polar app.

## Reference information

## Glossary

$\left.\begin{array}{ll}\text { app } & \begin{array}{l}\text { A small application, designed to } \\ \text { study one or more related topics or to } \\ \\ \text { solve problems of a particular type. }\end{array} \\ & \text { The built-in apps are Function, Solve, } \\ & \text { Statistics 1Var, Statistics 2Var, } \\ & \text { Inference, Parametric, Polar, } \\ & \text { Sequence, Finance, Linear Solver, } \\ & \text { Triangle Solver, Linear Explorer, } \\ & \text { Quadratic Explorer, and Trig } \\ & \text { Explorer. An app can be filled with } \\ \text { the data and solutions for a specific } \\ \text { problem. It is reusable (like a } \\ \text { program, but easier to use) and it } \\ \text { records all your settings and } \\ \text { definitions. }\end{array}\right\}$

| list | A set of values separated by commas <br> and enclosed in braces. Lists are <br> commonly used to enter statistical <br> data and to evaluate a function with |
| :--- | :--- |
| multiple values. Created and |  |
| manipulated by the List editor and |  |
| catalog. |  |

## Resetting the HP 39gll

If the calculator "locks up" and seems to be stuck, you must reset it. This is much like resetting a PC. It cancels certain operations, restores certain conditions, and clears temporary memory locations. However, it does not clear stored data (variables, app databases, programs) unless you use the procedure below, "To erase all memory and reset defaults".

To reset
Press and hold ${ }^{[\mathrm{ON} / \mathrm{C}}$ and ${ }^{\mathrm{F} 3}$ simultaneously, then release them.

## To erase all memory and reset defaults

If the calculator does not respond to the above resetting procedures, you might need to restart it by erasing all of memory. You will lose everything you have stored. All factory-default settings are restored.

1. Press and hold $\sigma \mathbb{O N / C}, F$, and $F 6$ simultaneously.
2. Release all keys in the reverse order.

## If the calculator does not turn on

If the HP 39gll does not turn on, follow the steps below until the calculator turns on. You may find that the calculator turns on before you have completed the procedure. If the calculator still does not turn on, please contact Customer Support for further information.

1. Press and hold ${ }^{\circ} \mathrm{ON/C}$ for 10 seconds, then release.
2. Press and hold ${ }^{\circ N / C}$ and simultaneously, then release $\mathrm{F3}$, then release $\frac{\mathrm{ON} / \mathrm{C}}{}$.
3. Press and hold $O N / \mathrm{F} / \mathrm{F}$, and Fb simultaneously. Release Fb , then release F , and then release ondc
4. Remove the batteries, press and hold $\mathrm{ON} / \mathrm{C}_{\mathrm{OF}}^{\mathrm{O}}$ for 10 seconds, then put the batteries back in and press
ON/C

## Batteries

## To install batteries



Warning: When the battery annunciator indicates that the batteries are low, you need to replace the batteries as soon as possible.
Please install the batteries according to the following procedure:

1. Turn off the calculator.
2. Slide up the battery compartment cover.
3. Insert 4 new AAA (LRO3) batteries into the compartment.
4. Make sure each battery is inserted in the indicated direction.
5. After installing the batteries, press calculator on.

Warning! There is danger of explosion if the battery is incorrectly replaced. Replace only with the same or equivalent type recommended by the manufacturer. Dispose of used batteries according to the manufacturer's instructions. Do not mutilate, puncture, or dispose of batteries in fire. The batteries can burst or explode, releasing hazardous chemicals.

## Operating details

Operating temperature: $0^{\circ}$ to $45^{\circ} \mathrm{C}\left(32^{\circ}\right.$ to $\left.113^{\circ} \mathrm{F}\right)$.
Storage temperature: $-20^{\circ}$ to $65^{\circ} \mathrm{C}\left(-4^{\circ}\right.$ to $\left.149^{\circ} \mathrm{F}\right)$.
Operating and storage humidity: $90 \%$ relative humidity at $40^{\circ} \mathrm{C}\left(104^{\circ} \mathrm{F}\right)$ maximum. Avoid getting the calculator wet.

Battery operates at $6.0 \mathrm{~V} \mathrm{dc}, 80 \mathrm{~mA}$ maximum.

## Variables

## Home variables

The Home variables are:

| Category | Available names |
| :--- | :--- |
| Complex | Z1...z9, zo |
| Graphic | G1...G9, G0 |
|  | Function <br> Solve <br> Statistics 1Var <br> Statistics 2Var <br> Inference <br> Parametric <br> Polar <br> Sequence <br> Finance <br> Linear Solver <br> Triangle Solver <br> User-named programs |
| List | L1...L9, L0 <br> M1...M9, M0 |


| Category | Available names (Continued) |
| :--- | :--- |
| Modes | Ans |
| HAngle |  |
| HDigits |  |
| HFormat |  |
| HComplex |  |
| Language |  |
| Program | Function |
|  | Solve |
|  | Statistics 1Var |
| Statistics 2Var |  |
| Inference |  |
| Parametric |  |
| Polar |  |
| Sequence |  |
| Real | Finance |
|  | Linear Solver |
|  | Triangle Solver |
|  | User-named programs |
|  | A...Z, $\theta$ |

## App variables

## Function app variables

The Function app variables are:

| Category | Available names |  |
| :---: | :---: | :---: |
| Results | Area | Root |
|  | Extremum | Slope |
|  | Isect |  |
| Symbolic | F1 | F6 |
|  | F2 | F7 |
|  | F3 | F8 |
|  | F4 | F9 |
|  | F5 | F0 |
| Plot | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Tracing | Yzoom |


| Category | Available names |  |
| :--- | :--- | :--- |
| (Continued) |  |  |
| Numeric | NumStart <br> NumStep | NumType <br> NumZoom |
|  | AAngle <br> AComplex | ADigits <br> AFormat |

## Solve app variables

The Solve app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Symbolic | E1 | E6 |
|  | E2 | E7 |
|  | E3 | E8 |
|  | E4 | E9 |
|  | E5 | E0 |
|  |  |  |
|  | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Recenter | Ytick |
|  | Tracing | Yzoom |
|  |  |  |
|  | AAngle | ADigits |
|  | AComplex | AFormat |

## Statistics 1Var app variables

The Statistics IVar app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Results | NbItem | $\sum \mathrm{X}$ |
|  | Min | $\sum \mathrm{X} 2$ |
|  | Q1 | MeanX |
|  | Med | SX |
|  | Q3 | X |
|  | Max | serrX |


| Category | Available names | (Continued) |
| :--- | :--- | :--- |
| Symbolic | H1 | H1Type |
|  | H2 | H2Type |
|  | H3 | H3Type |
|  | H4 | H4Type |
|  | H5 | H5Type |
|  |  |  |
|  | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Recenter | Ytick |
|  | Tracing | Yzoom |
|  |  |  |
|  | D1 | D6 |
|  | D2 | D7 |
|  | D3 | D8 |
|  | D4 | D9 |
|  | D5 | D0 |
|  |  |  |
|  | AAngle | ADigits |
|  | AComplex | AFormat |

## Statistics 2Var app variables

The Statistics 2 Var app variables are:

| Category | Available names |  |
| :---: | :---: | :---: |
| Results | NbItem | sX |
|  | Corr | $\sigma \mathrm{X}$ |
|  | CoefDet | serrX |
|  | sCov | MeanY |
|  | OCov | $\Sigma \mathrm{Y}$ |
|  | $\Sigma \mathrm{XY}$ | EY2 |
|  | MeanX | SY |
|  | $\Sigma \mathrm{X}$ | $\sigma Y$ |
|  | EX2 | serry |
| Symbolic | S1 | S1Type |
|  | S2 | S2Type |
|  | S3 | S3Type |
|  | S4 | S4Type |
|  | S5 | S5Type |


| Category | Available names | (Continued) |
| :---: | :---: | :---: |
| Plot | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Recenter | Ytick |
|  | Tracing | Yzoom |
| Numeric | C1 | C6 |
|  | C2 | C7 |
|  | C3 | C8 |
|  | C4 | C9 |
|  | C5 | C0 |
| Modes | AAngle | ADigits |
|  | AComplex | AFormat |

## Inference app variables

The Inference app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Results | Result | CritScore |
|  | TestScore | CritVal1 |
|  | TestValue | CritVal2 |
|  | Prob |  |
|  | DF |  |
| Symbolic | AltHyp | Type |
|  | Method |  |
|  |  |  |
|  | Alpha | Pooled |
|  | Conf | s1 |
|  | Mean1 | s2 |
|  | Mean2 | $\sigma 1$ |
|  | n1 | $\sigma 2$ |
|  | n2 | x1 |
|  | $\mu 0$ | x2 |
|  | $\pi 0$ |  |
|  | AAngle | ADigits |
|  | AComplex | AFormat |

## Parametric app variables

The Parametric app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Symbolic | X1 | X6 |
|  | Y1 | Y6 |
|  | X2 | X7 |
|  | Y2 | Y7 |
|  | X3 | X8 |
|  | Y3 | Y8 |
|  | X4 | X9 |
|  | Y4 | Y9 |
|  | X5 | X0 |
|  | Y5 | Y0 |
|  |  |  |
|  | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Recenter | Ytick |
|  | Tracing | Yzoom |
|  |  |  |
| Numeric | NumStart | NumType |
|  | NumStep | NumZoom |
|  |  |  |
|  | AAngle | ADigits |
|  | AComplex | AFormat |

## Polar app variables

The Polar app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Symbolic | R1 | R6 |
|  | R2 | R7 |
|  | R3 | R8 |
|  | R4 | R9 |
|  | R5 | R0 |


| Category | Available names |  |
| :--- | :--- | :--- |
| (Continued) |  |  |
| Plot | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Recenter | Ytick |
| Tracing | Yzoom |  |
|  | NumStart | NumType |
|  | Nodes | NumStep |
|  | AAngle | NumZoom |
|  | AComplex | ADigits |
|  |  | AFormat |

## Sequence app variables

The Sequence app variables are:

| Category | Available names |  |
| :---: | :---: | :---: |
| Symbolic | U1 | U6 |
|  | U2 | U7 |
|  | U3 | U8 |
|  | U4 | U9 |
|  | U5 | U0 |
| Plot | Axes | Xmax |
|  | Cursor | Xmin |
|  | GridDots | Xtick |
|  | GridLines | Xzoom |
|  | Labels | Ymax |
|  | Method | Ymin |
|  | Recenter Tracing | Ytick Yzoom |
|  |  |  |
| Functions | NumStart | NumType |
|  | NumStep | NumZoom |
| Modes | AAngle | ADigits |
|  | AComplex | AFormat |

## Finance app variables

The Finance app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Numeric | CPYR | NbPmt |
|  | END | PMT |
|  | FV | PPYR |
|  | GSize | PV |
|  | IPYR |  |

## Linear Solver app variables

The Linear solver app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Results | LSolution |  |
| Numeric | LSystem | Size |
| Modes | AAngle <br> AComplex | ADigits <br> AFormat |

## Triangle Solver app variables

The Triangle solver app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Numeric | AngleA | SideA |
|  | AngleB | SideB |
| AngleC | SideC |  |
| Modes | Rect |  |
|  | AAngle | ADigits |
|  | AComplex | AFormat |

## Linear Explorer app variables

The Linear Explorer app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Modes | AAngle <br> AComplex | ADigits <br> AFormat |

## Quadratic Explorer app variables

The Quadratic Explorer app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Modes | AAngle <br> AComplex | ADigits <br> AFormat |

## Trig Explorer app variables

The Trig Explorer app variables are:

| Category | Available names |  |
| :--- | :--- | :--- |
| Modes | AAngle <br> AComplex | ADigits <br> AFormat |

## Functions and Commands

## Math menu functions

The Math menu functions are:

| Category | Available functions |  |
| :---: | :---: | :---: |
| Calculus | $\begin{aligned} & \partial \\ & \int^{\partial} \text { (Where) } \end{aligned}$ |  |
| Complex | ARg CONJ | $\begin{aligned} & \text { IM } \\ & \text { RE } \end{aligned}$ |
| Constant |  | MAXREAL MINREAL $\pi$ |
| Distribution | normald <br> normald cdf <br> normald_icdf <br> binomial <br> binomial_cdf <br> binomial_icdf <br> chisquare <br> chisquare_cdf <br> chisquare_icdf | fisher <br> fisher cdf <br> fisher_icdf <br> poisson <br> poisson_cdf <br> poisson_icdf <br> student <br> student_cdf <br> student_icdf |
| Hyperbolic | ACOSH <br> ASINH <br> ATANH <br> COSH <br> SINH | TANH <br> ALOG <br> EXP <br> EXPM1 <br> LNP1 |
| Integer | ichinrem <br> idivis <br> iegcd <br> ifactor <br> ifactors <br> igcd <br> iquo <br> iquorem <br> irem | isprime ithprime nextprime powmod prevprime euler numer denom |
| List | CONCAT <br> $\Delta$ LIST <br> MAKELIST <br> $\pi$ LIST <br> POS | REVERSE <br> SIZE <br> ELIST <br> SORT |


| Category | Available functions (Continued) |
| :---: | :---: |
| Loop | ITERATE <br> $\Sigma$ |
| Matrix | COLNORM QR <br> COND RANK <br> CROSS ROWNORM <br> DET RREF <br> DOT SCHUR <br> EIGENVAL SIZE <br> EIGENVV SPECNORM <br> IDENMAT SPECRAD <br> INVERSE SVD <br> LQ SVL <br> LSQ TRACE <br> LU TRN <br> MAKEMAT  |
| Polynom. | POLYCOEF POLYROOT POLYEVAL |
| Prob. | COMB UTPC <br> $!$ UTPF <br> PERM UTPN <br> RANDOM UTPT |
| Real | CEILING MIN <br> DEG $\rightarrow$ RAD MOD <br> FLOOR $\%$ <br> FNROOT \%CHANGE <br> FRAC \%TOTAL <br> HMS $\rightarrow$ RAD <br> $\rightarrow$ DEG  <br> INT ROUND <br> MANT SIGN <br> MAX TRUNCATE <br>  XPON |
| Tests | $<$ AND <br> $\leq$ IFTE <br> $==$ NOT <br> $\neq$ OR <br> $>$ XOR <br> $\geq$  |


| Category | Available functions (Continued) |  |
| :--- | :--- | :--- |
| Trig | ACOT | COT |
|  | ACSC | CSC |
|  | ASEC | SEC |

## App functions

The app functions are:

| Category | Available functions |
| :---: | :---: |
| Function | $\begin{aligned} & \text { AREA (Fn, [Fm, ] lower, upper) } \\ & \text { EXTREMUM (Fn, guess) } \\ & \text { ISECT (Fn, Fm, guess) } \\ & \text { ROOT (Fn,guess) } \\ & \text { SLOPE (Fn, value) } \end{aligned}$ |
| Solve | SOLVE (En, var, guess) |
| Statistics 1Var | Do1VStats (Hn) <br> SETFREQ (Hn,Dn) or <br> SETFREQ (Hn, value) <br> SETSAMPLE (Hn, Dn) |
| Statistics <br> 2Var | Do2VStats (Sn) <br> PredX (value) <br> PredY (value) <br> SetDepend (Sn, Cn) <br> SetIndep ( $\mathrm{Sn}, \mathrm{Cn}$ ) |
| Inference | DoInference () |
| Sequence | RECURSE (Un, nthterm[, term1, term2]) |
| Finance | DoFinance ( TVMVar) |
| Linear Solver | LinSolve (matrix) |
| Triangle Solver | AAS (angle, angle, side) <br> ASA (angle, side, angle) <br> SAS (side, angle, side) <br> SSA (side, side, angle) <br> SSS (side, side, side) |

## Program commands

The Program commands are:

| Category | Available functions |  |
| :---: | :---: | :---: |
| App | CHECK <br> UNCHECK <br> STARTAPP | STARTVIEW VIEWS |
| Block | $\begin{aligned} & \text { BEGIN } \\ & \text { END } \end{aligned}$ | RETURN |
| Branch | IF <br> THEN <br> ELSE | END <br> CASE <br> IFERR |
| Drawing | PIXON <br> PIXON_P <br> PIXOF $\bar{F}$ <br> PIXOFF_P <br> GETPIX <br> GETPIX_P <br> RECT <br> RECT_P <br> INVE $\bar{R} T$ <br> INVERT_P <br> ARC <br> ARC_P <br> LINE <br> LINE_P | TEXTOUT <br> TEXTOUT_P <br> BLIT <br> BLIT_P <br> DIMG $\bar{R} O B$ <br> DIMGROB_P <br> SUBGRB <br> SUBGROB_P <br> FREEZE <br> GROBH <br> GROBH_P <br> GROBW <br> GROBW_P |
| 1/O | CHOOSE <br> EDITMAT <br> GETKEY <br> ISKEYDOWN <br> INPUT | MSGBOX <br> PRINT <br> WAIT <br> debug |
| Loop | $\begin{aligned} & \text { FOR } \\ & \text { FROM } \\ & \text { TO } \\ & \text { STEP } \\ & \text { END } \\ & \text { DO } \end{aligned}$ | UNTIL <br> WHILE <br> REPEAT <br> BREAK <br> CONTINUE |
| Matrix | ADDCOL <br> ADDROW <br> DELCOL <br> DELROW <br> EDITMAT <br> RANDMAT | REDIM <br> REPLACE <br> SCALE <br> SCALEADD <br> SUB <br> SWAPCOL <br> SWAPROW |
| Strings | asc <br> char <br> expr <br> string <br> inString | left <br> right <br> mid <br> rotate <br> dim |
| Variable | EXPORT | LOCAL |

## Constants

## Program constants

The Program constants are:


## Physical Constants

The Physical constants are:

| Category | Available names |
| :---: | :---: |
| Chemistry | ```Avogadro NA Boltmann, k molar volume, Vm universal gas, R standard temperature, StdT standard pressure, StdP``` |
| Phyics | ```Stefan-Boltzmann, \sigma speed of light, c permittivity, \Sigma ) permeability, 自 acceleration of gravity, g gravitation, G``` |
| Quantum | Planck, h <br> Dirac h <br> electronic charge, q <br> electron mass, me <br> q/me ratio, qme <br> proton mass, mp <br> $\mathrm{mp} / \mathrm{me}$ ratio, mpme <br> fine structure, $\alpha$ <br> magnetic flux, Фо) <br> Faraday, F <br> Rydberg, R $\infty$ <br> Bohr radius, $a_{0}$ <br> Bohr magneton, $\mu \mathrm{B}$ nuclear magneton, $\mu \mathrm{N}$ <br> photon wavelength, $\lambda_{0}$ <br> photon frequency, $f_{0}$ <br> Compton wavelength, $\lambda_{C}$ |

## Status messages

| Message | Meaning |
| :--- | :--- |
| Bad Argument | Incorrect input for this <br> operation. <br> Type |
| Bad Argument <br> Value | The value is out of range for this <br> operation. |

$\left.\left.\begin{array}{|l|l|}\hline \text { Message } & \text { Meaning (Continued) } \\ \hline \text { Infinity error } & \begin{array}{l}\text { Math exception, such as 1/0. } \\ \text { Yemicient } \\ \text { You must recover some memory } \\ \text { to continue operation. Delete } \\ \text { one or more matrices, lists, } \\ \text { notes, or programs (using } \\ \text { catalogs), or custom (not built- } \\ \text { in) apps (using shlit } \\ \text { MEMORY). }\end{array} \\ \text { Insufficient } & \begin{array}{l}\text { Not enough data points for the } \\ \text { calculation. For two-variable } \\ \text { statistics there must be two } \\ \text { columns of data, and each } \\ \text { column must have at least four } \\ \text { numbers. }\end{array} \\ \text { Invalid Dimension } & \begin{array}{l}\text { Array argument had wrong } \\ \text { dimensions. }\end{array} \\ \text { Invalid Statistics } & \begin{array}{l}\text { Need two columns with equal } \\ \text { numbers of data values. }\end{array} \\ \text { Invalid Syntax } & \begin{array}{l}\text { The function or command you } \\ \text { entered does not include the } \\ \text { proper arguments or order of } \\ \text { arguments. The delimiters } \\ \text { (parentheses, commas, } \\ \text { periods, and semi-colons) must } \\ \text { also be correct. Look up the } \\ \text { function name in the index to }\end{array} \\ \text { find its proper syntax. }\end{array}\right\} \begin{array}{l}\text { The / (where) function } \\ \text { attempted to assign a value to } \\ \text { the variable of integration or } \\ \text { summation index. } \\ \text { You must enter and check an } \\ \text { equation in the Symbolic view } \\ \text { before entering the Plot view. } \\ \text { Function value, root, extremum, } \\ \text { or intersection is not visible in } \\ \text { the current screen. }\end{array}\right\}$

| Message | Meaning (Continued) |
| :--- | :--- |
| Receive Error | Problem with data reception <br> from another calculator. Re- <br> send the data. |
| Arguments | The command requires more <br> arguments than you supplied. |
| Undefined Name | The global variable named <br> does not exist. |
| Out of Memory | The calculation has a <br> mathematically undefined result <br> (such as 0/O). <br> You must recover a lot of <br> memory to continue operation. <br> Delete one or more matrices, <br> lists, notes, or programs (using <br> catalogs), or custom (not built- <br> in) apps (using sylliz mEMORY). |

## Appendix: Product Regulatory Information

## Federal Communications Commission Notice

This equipment has been tested and found to comply with the limits for a Class B digital device, pursuant to Part 15 of the FCC Rules. These limits are designed to provide reasonable protection against harmful interference in a residential installation. This equipment generates, uses, and can radiate radio frequency energy and, if not installed and used in accordance with the instructions, may cause harmful interference to radio communications. However, there is no guarantee that interference will not occur in a particular installation. If this equipment does cause harmful interference to radio or television reception, which can be determined by turning the equipment off and on, the user is encouraged to try to correct the interference by one or more of the following measures:

- Reorient or relocate the receiving antenna.
- Increase the separation between the equipment and the receiver.
- Connect the equipment into an outlet on a circuit different from that to which the receiver is connected.
- Consult the dealer or an experienced radio or television technician for help.


## Modifications

The FCC requires the user to be notified that any changes or modifications made to this device that are not expressly approved by Hewlett-Packard Company may void the user's authority to operate the equipment.

## Cables

Connections to this device must be made with shielded cables with metallic RFI/EMI connector hoods to maintain compliance with FCC rules and regulations. Applicable only for products with connectivity to $\mathrm{PC} /$ laptop.
Declaration of Conformity for products Marked with FCC
Logo, United States Only

This device complies with Part 15 of the FCC Rules. Operation is subject to the following two conditions: (1) this device may not cause harmful interference, and (2) this device must accept any interference received, including interference that may cause undesired operation.

If you have questions about the product that are not related to this declaration, write to:
Hewlett-Packard Company
P.O. Box 692000, Mail Stop 530113

Houston, TX 77269-2000

For questions regarding this FCC declaration, write to: Hewlett-Packard Company P.O. Box 692000, Mail Stop 510101 Houston, TX 77269 2000 or call HP at 281-514-3333

To identify your product, refer to the part, series, or model number located on the product.

## Canadian Notice

This Class B digital apparatus meets all requirements of the Canadian Interference-Causing Equipment Regulations.

## Avis Canadien

Cet appareil numérique de la classe $B$ respecte toutes les exigences du Règlement sur le matériel brouilleur du Canada.

## European Union Regulatory Notice

Products bearing the CE marking comply with the following EU Directives:

- Low Voltage Directive 2006/95/EC
- EMC Directive 2004/108/EC
- Ecodesign Directive 2009/125/EC, where applicable

CE compliance of this product is valid if powered with the correct CE -marked AC adapter provided by HP.

Compliance with these directives implies conformity to applicable harmonized European standards (European Norms) that are listed in the EU Declaration of Conformity issued by HP for this product or product family and available (in English only) either within the product documentation or at the following web site: www.hp.ev/certificates (type the product number in the search field).

The compliance is indicated by one of the following conformity markings placed on the product:
C $\epsilon$
For non-telecommunications products and for EU harmonized telecommunications products, such as Bluetooth ${ }^{\circledR}$ within power class below 10 mW .

## $C \in(1)$

For EU non-harmonized telecommunications products (If applicable, a 4-digit notified body number is inserted between CE and !).

Please refer to the regulatory label provided on the product.
The point of contact for regulatory matters is: Hewlett-Packard GmbH, Dept./MS: HQ-TRE, Herrenberger Strasse 140, 71034 Boeblingen, GERMANY.

## Japanese Notice

この装置は，クラスB情報技術装置です。この装置は，家庭環境で使用 することを目的としていますが，この装置がラジオやテレビジョン受信機に近接して使用されると，受信障害を引き起こすことがあります。
取扱説明書に従って正しい取り扱いをして下さい。 VCCI－B

## Korean Class Notice

$B$ 급 기기
（가정용 뱡송통신기기）

이 기기는 가정용 $(\mathrm{B}$ 급 $)$ 으로 젼자파적합등록을 한 기기로서 주 로 가정예서 사용하는 것을 목적으로 하며，모든 지역예서 사 용할 수 있습니다．

## Disposal of Waste

 Equipment by Users in Private Household in the European Union

This symbol on the product or on its packaging indicates that this product must not be disposed of with your other household waste．Instead，it is your responsibility to dispose of your waste equipment by handing it over to a designated collection point for the recycling of waste electrical and electronic equipment．The separate collection and recycling of your waste equipment at the time of disposal will help to conserve natural resources and ensure that it is recycled in a manner that protects human health and the environment．For more information about where you can drop off your waste equipment for recycling，please contact your local city office，your household waste disposal service or the shop where you purchased the product．

Chemical Substances HP is committed to providing our customers with information about the chemical substances in our products as needed to comply with legal requirements such as REACH (Regulation EC No 1907/2006 of the European Parliament and the Council). A chemical information report for this product can be found at:

## http://www.hp.com/go/reach

Perchlorate Material - special handling may apply This calculator's Memory Backup battery may contain perchlorate and may require special handling when recycled or disposed in California.


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